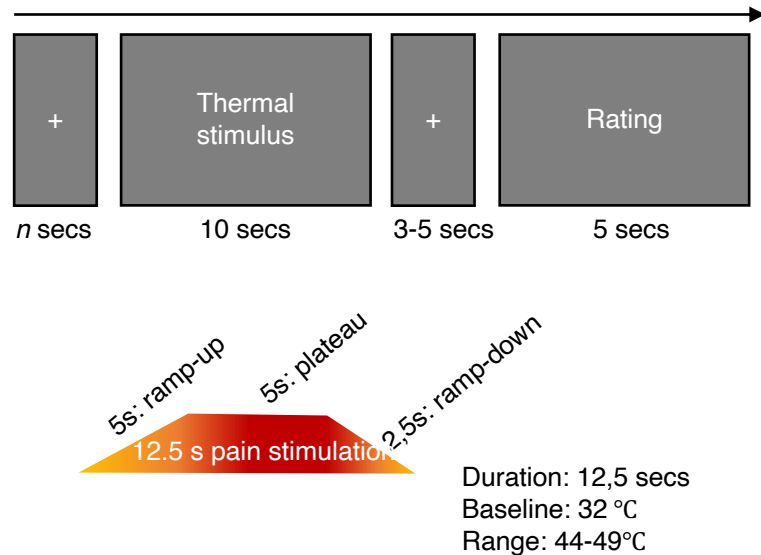


Multilevel model: tutorial

- Let's try to perform multilevel model using SEMIC pain calibration data (`glmfit_multilevel` in CanlabTools)
 - It is exactly same as I described previously (Two-stage model)
- The goal of this analysis is to estimate the temperature effects on pain ratings, considering between-participant variance



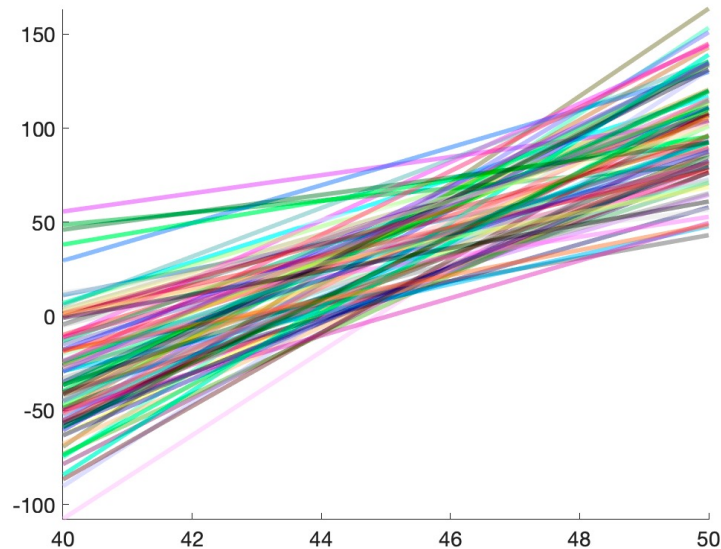
Tasks

- Participants: $N = 84$
- There were 12 trials per each
- We have information about pain ratings and temperature
- First-level: individual level (12 trials per individual)
- Second-level: group level (84 participants)



Multilevel model: tutorial

- Let's fit each first-level regression model
- Although all slopes show similar patterns, but there are not exactly same
→ between-subject variability



```
%% SET PATH
% calibration datasets
basedir = '/Users/suhwan/Dropbox/Projects/SEMIC/data_NAS/behavioral/raw'
datdir = fullfile(basedir, 'CALI_SEMIC_data'); % sein
matlist = filenames(fullfile(datdir, '*.mat'));

%% LOAD DATA
cal_dat = [];
for i = 1:length(matlist)
    cal_dat{i} = load(fullfile(matlist{i}, 'reg'));
end

%% Comparison between single-level linear regression and first-level regression
% 1. Estimating each participant's first-level regression model
create_figure;
set(gca, 'Ylim', [0 100], 'Xlim', [40 50]);
clear hline;
col = colorcube(length(cal_dat));
col = col(shuffles(1:length(cal_dat)), :);

for i = 1:length(cal_dat)
    % reffline function is to represent regression line on a plot
    slope = cal_dat{i}.reg.total_fit.Coefficients.Estimate(2);
    intercept = cal_dat{i}.reg.total_fit.Coefficients.Estimate(1); %intercept
    hline(i) = reffline([slope intercept]);
    hline(i).LineWidth = 3;
    hline(i).Color = [col(i, :) 0.2];

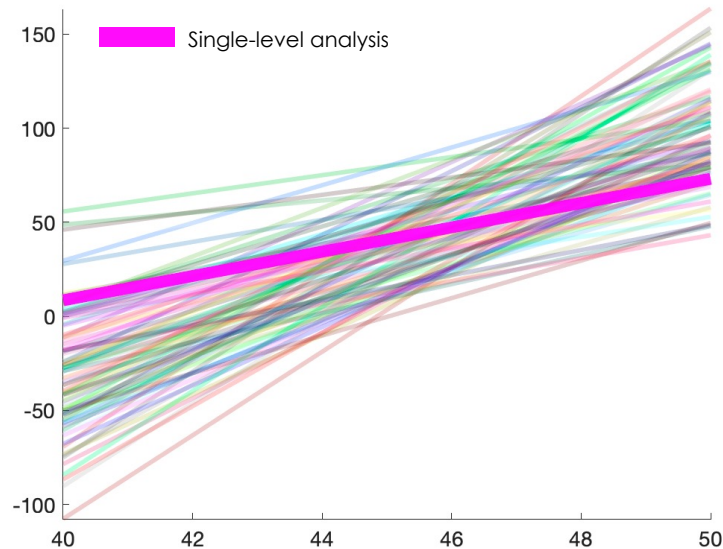
    hold on;
end

hold off;
```



Multilevel model: tutorial

- Let's compare between single-level analysis results and the trends of first-level analysis results
- In this case, all data were aggregated without considering the participants
- The estimated regression line quite differ compared to trends of the first-level analysis results



```
% 2. single-level regression model
rating = [];
degree = [];
% aggregate all variables
for i = 1:length(cal_dat)
    degree = [degree cal_dat{i}.reg.stim_degree];

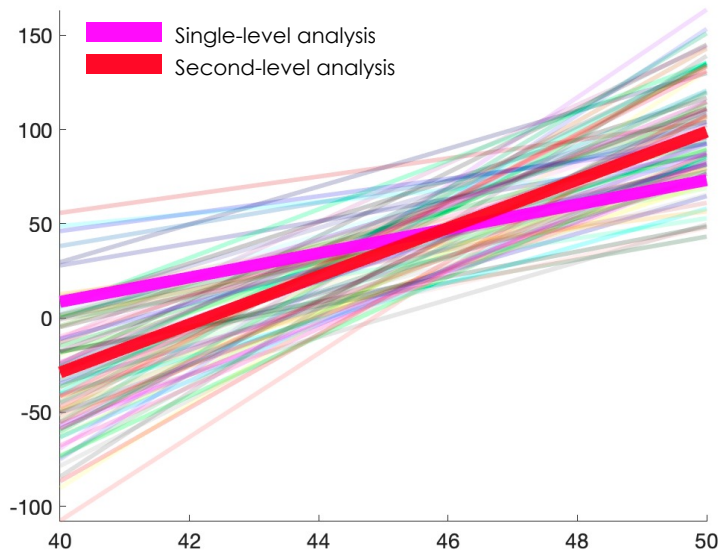
    rating = [rating cal_dat{i}.reg.stim_rating];
end
res_lm = fitlm(degree, rating); % fit linear model

clear h2line
slope = res_lm.Coefficients.Estimate(2);
intercep = res_lm.Coefficients.Estimate(1); %intercept
h2line = reffline([slope intercep]);
h2line.Color = [1 0 1 0.9];
h2line.LineWidth = 8;
```



Multilevel model: tutorial

- The next is to consider hierarchical data structures
- Using `glmfit_multilevel` in CanlabCORE, we can estimate the second-level analysis
 - **help glmfit_multilevel**



```
%  
stats = glmfit_multilevel(y,x1,[],'names',{'intercept','temperature'},'verbose');  
%%
```

```
%% Multilevel linear regression  
x1 = [];  
y = [];  
% making data structure depends on participants  
for i = 1:length(cal_dat)  
    x1{i} = cal_dat{i}.reg.stim_degree';  
    y{i} = cal_dat{i}.reg.stim_rating';  
end  
%  
stats = glmfit_multilevel(y,x1,[],'names',{'intercept','temperature'},'verbose');  
%%  
clear h3line  
h2line = refline([stats.beta(2) stats.beta(1)]);  
h2line.Color = [1 0 0.1 0.9];  
h2line.LineWidth= 8;
```

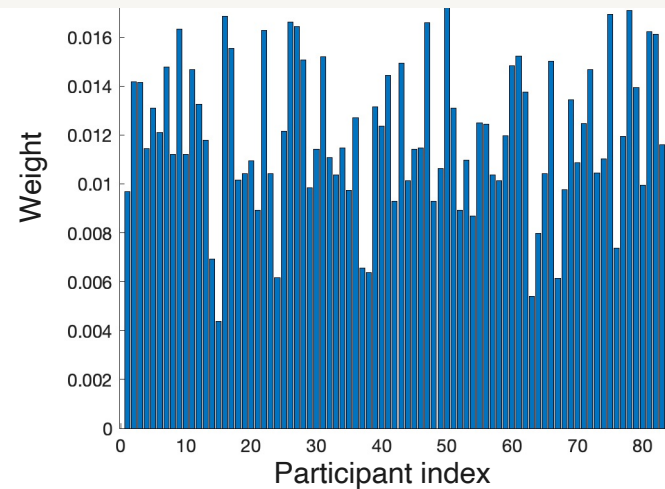
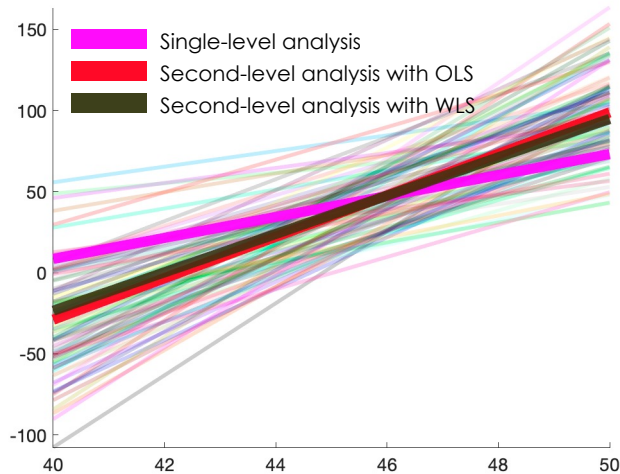
Second Level of Multilevel Model		
Outcome variables:		
	intercept	temperature
Adj. mean	-539.95	12.77
2nd-level B01		
	intercept	temperature
Coeff	-539.95	12.77
STE	23.88	0.52
t	-22.61	24.56
Z	-8.21	8.21
p	0.00000	0.00000



Multilevel model: tutorial

- Finally, there are several useful options to estimate multilevel regression models in `glmfit_multilevel`
 - 'weighted'**: Using empirical Bayesian estimation, each first-level results will be reweighted. In other words, if the first-level results is unstable, their weight is down-weighted when a second-level beta estimated
 - 'boot'**: One of the non-parametric significance inference options with random sampling

```
stats2 = glmfit_multilevel(y, x1, [], ...  
                          'names', {'intercep', 'temp'}, 'verbose', 'boot', 'nresample', 10000, 'weighted');
```



Bootstrapped statistics. **Bootstrap** inference

Outcome variables:

	intercep	temp
Adj. mean	-496.60	11.83
2nd-level B01		
Coeff	-496.42	11.82
STE	16.60	0.35
t	-20.98	23.05
Z	-3.72	3.81
p	0.00020	0.00014



Multilevel model: Additional issues

- To estimate more accurately, usually the multilevel analysis is useful methods because of decomposition of variance
- In our examples, or tutorial, the OLS (or WLS) was used to estimate the beta
- However, the other packages such as **LME4 packages** in R language employ maximum likelihood estimation or restricted maximum likelihood to estimate beta coefficients

<https://cran.r-project.org/web/packages/lme4/vignettes/lmer.pdf>



- In psychology, there are consensus the multilevel approach can be helpful to make inference population level results
 - Because it can decompose between-each level variance by building each level regression models
- However, someone raise a question of this approach. So, if you have interest, I will recommend you the article (Yarkoni 2021)

The generalizability crisis

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Yarkoni, T. (2020). The generalizability crisis. Behavioral and Brain Sciences, 1-37. doi:10.1017/S0140525X20001685

