



Operations Management I

Material Requirement Planning

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Material Requirement Planning

Introduction ←

Inputs, Outputs, and Procedure

Further Considerations

- Developer and Extensions
- Key Insight
- Prerequisites
- Basic MRP Procedure

- Special Topics
- Problems

Hopp and Spearman, 2008, **Factory Physics**, McGraw Hill. (Section 3.1)

Krajewski and Ritzman, 2005, **Operations Management**, Prentice Hall. (Chapter 16)

MRP

◆ Introduction

Developer and Extensions

- Developer

- ✓ Josef Orlicky (IBM, early 1960s)

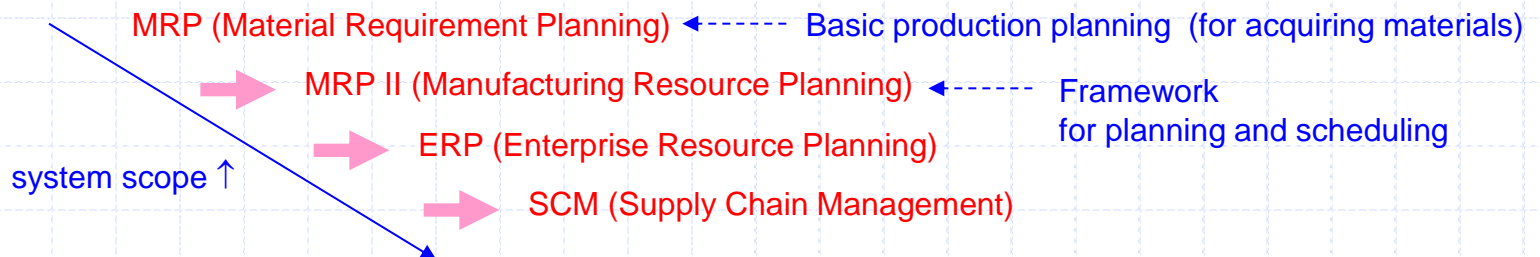
- Use of computer in production control

- Tremendous boost in 1970s (MRP crusade)

- ✓ APICS (American Production and Inventory Control Society)

- ✓ Principal production control paradigm in the United States

- Extensions



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Introduction

Key Insight (1)

- Dependent demand inventory

Raw materials, components, and subassemblies that are used in the production of the parent or the final products

- ✓ Prediction ← Concept of requirement (소요)
(Material requirement planning: MRP)

e.g. demand of keyboards depends on the demand for computers

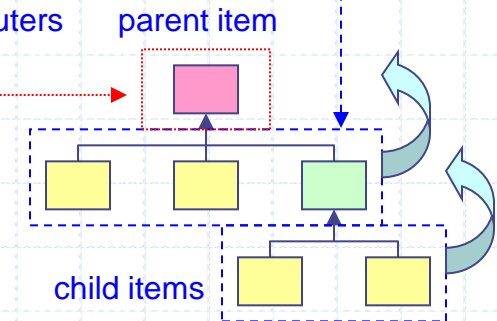
- Independent demand inventory

Finished products, service parts, and other items whose demand arises more directly from uncertain market environment

- ✓ Forecasting ← Concept of replenishment (보충)
(general inventory models)

e.g. computers as final product

	Independent demand	Dependent demand
Demand	Uncertain	Certain (relatively)
Estimation	Forecasting	Compute from independent demand
Methods	Inventory models	MRP

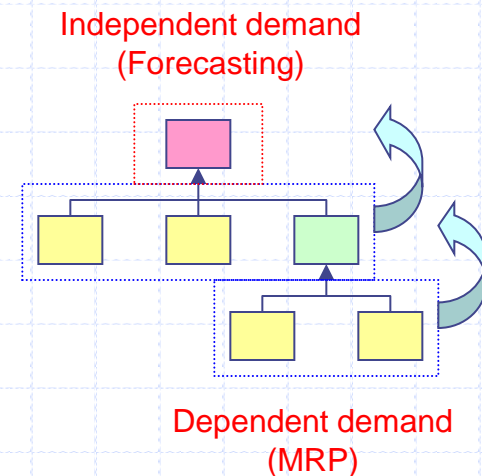


MRP

◆ Introduction

Key Insight (2)

- Dependent and independent demands
 - ✓ MRP (Material Requirement Planning) ← push system
 - Add the link between independent and dependent demand
 - MRP is used to coordinate orders from within the plant and from outside.
- ← Two basic dimensions
- Timing
 - Quantity



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Introduction

Prerequisites (1)

- **Bucket** ←----- period in the planning horizon

Interval used to break time and demand into discrete chunks

e.g. bucket length = 1 week (5 days)

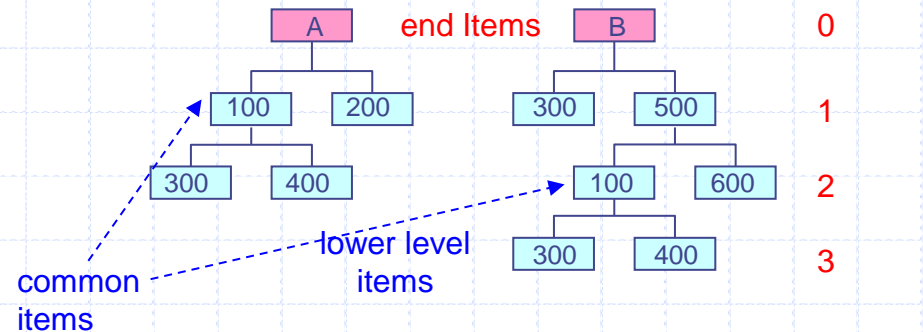
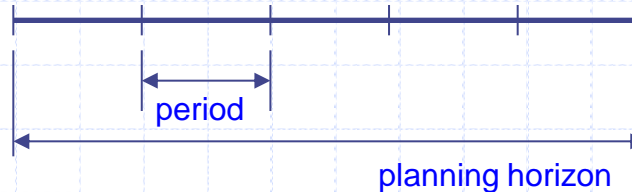
demand

Mon	Tue	Wed	Thu	Fri
250	300	200	100	150

demand of this bucket = 1000

- **Bill of Material (BOM)**
Relationship between end items and lower level items
- **Master Production Schedule (MPS)**
Information concerning independent demand (end-items)

Planning horizon and discrete time periods

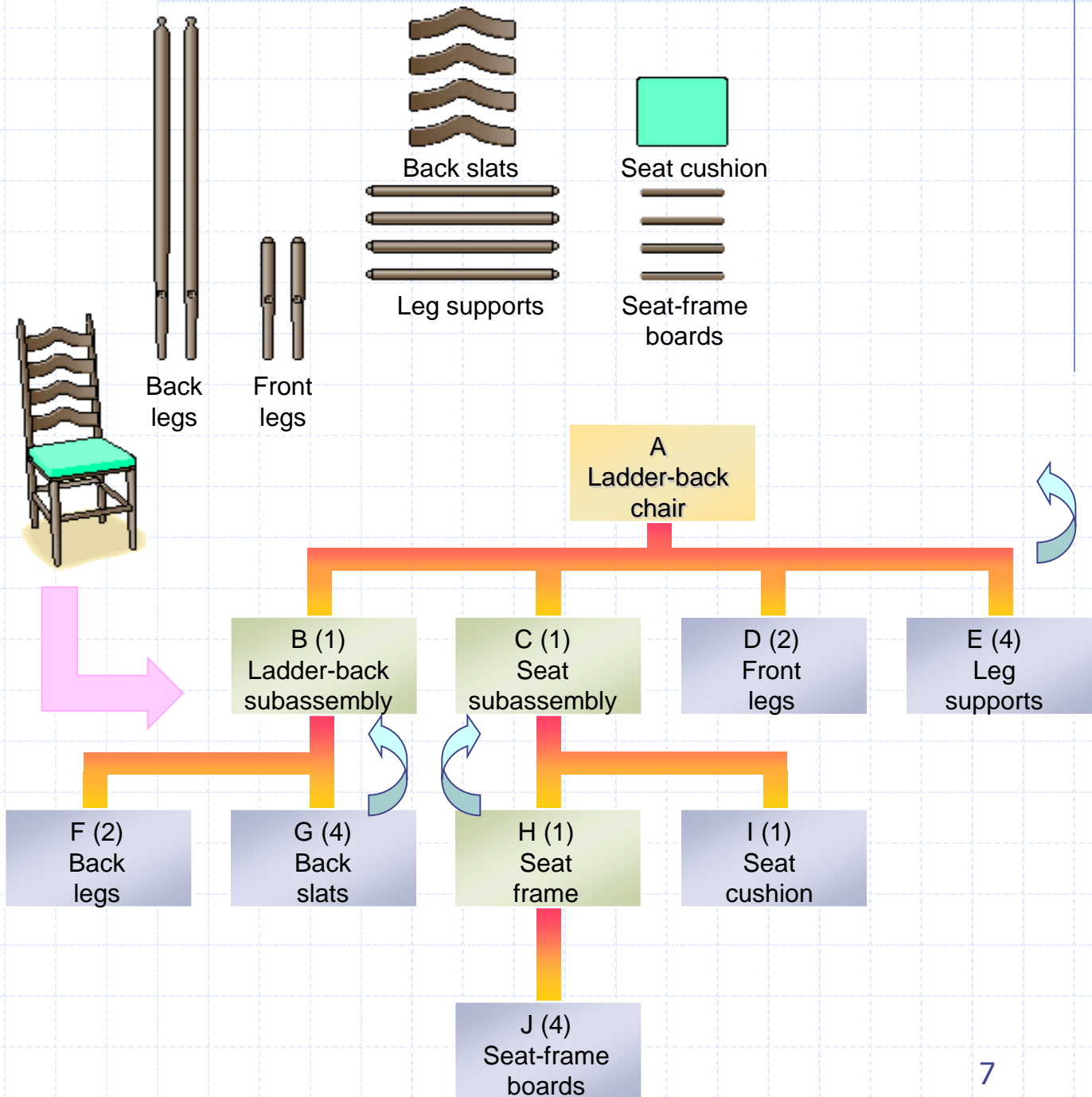


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Introduction

Prerequisites (2)

- Bill of Material (BOM)
- Example



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◆ Introduction

Prerequisites (3)

- Master Production Schedule (MPS) – Example

	April				May			
	1	2	3	4	5	6	7	8
Ladder-back chair	150					150		
Kitchen chair				120			120	
Desk chair		200	200		200			200
Aggregate production plan for chair family	670				670			

MRP

◆ Introduction

Basic Procedure (1)

- Overview

For each level in the BOM, beginning with end items, MRP does the following for each part

→ 1) Netting

↓ Determine the net requirement

2) Lot sizing

↓ Divide the netted demand into appropriate lot sizes to form jobs

3) Time Phasing

↓ Offset the due dates of the jobs with lead times to determine the start times

→ 4) BOM explosion

Generate **gross requirements** of any required components at the next level

- End-items ← MPS
- Lower level items ← previous MRP operations

net requirement = {0, gross requirement} - on-hand inventory - scheduled receipts

- Wagner-Whitin algorithm
- Lot-for-lot
- Fixed order quantity (EOQ)
- Fixed order period
- Part-period balancing, etc.

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Introduction

Basic Procedure (2)

- Example

- ✓ Netting

Determine the net requirement (Initial on-hand inventory = 30 units)

Item A	1	2	3	4	5	6	7	8
Gross requirements	15	20	50	10	30	30	30	30
Projected on-hand	15	-5						
Net requirement	0	5	50	10	30	30	30	30

Projected on-hand
 = on-hand inventory + scheduled receipts – gross requirement
 = 30 + 0 – 15 = 15

Net requirement
 = max { 0, gross requirement – on-hand inventory – scheduled receipts }
 = max { 0, 15 – 30 – 0 } = 0

- ✓ Data

➤ Demand (planning horizon = 8 weeks) ←---- master production schedule (MPS)

Item A	1	2	3	4	5	6	7	8
Gross requirements	15	20	50	10	30	30	30	30

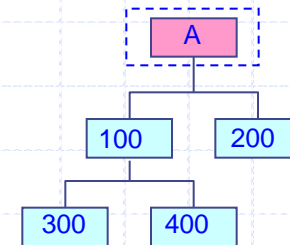
➤ Initial on-hand inventory = 30 units

➤ No scheduled receipts

➤ Lot size = 75 units

➤ Lead time = 1 week

- Bill of material (BOM)



MRP

Introduction

Basic Procedure (3)

- Example

- Lot sizing (lot size = 75 units)

✓ Data

➤ Demand (planning horizon = 8 weeks) ←---- master production schedule (MPS)

Item A	1	2	3	4	5	6	7	8
Gross requirements	15	20	50	10	30	30	30	30

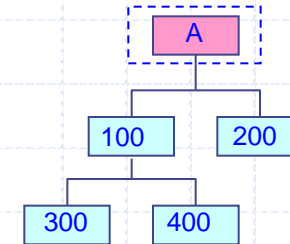
➤ Initial on-hand inventory = 30 units

➤ No scheduled receipts

➤ Lot size = 75 units

➤ Lead time = 1 week

- Bill of material (BOM)



Item A	1	2	3	4	5	6	7	8
Gross Requirements	15	20	50	10	30	30	30	30
Projected on-hand	15	-5						
Net requirements	0	5	50	10	30	30	30	30
Planned order receipts		75			75		75	

75 = 5 + 50 + 10 + 10
20 units remain in period 5.

75 = 20 + 30 + 25
5 units remain in period 7.

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Introduction

Basic Procedure (4)

• Example

✓ Time Phasing

Item A	1	2	3	4	5	6	7	8
Gross Requirements	15	20	50	10	30	30	30	30
Projected on-hand	15	-5						
Net requirements	0	5	50	10	30	30	30	30
Planned order receipts		75			75		75	
Planned order releases	75			75		75		

lead time = 1 week

✓ BOM explosion

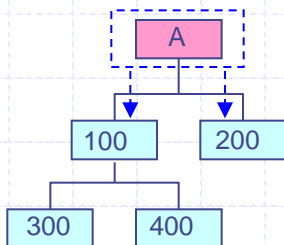
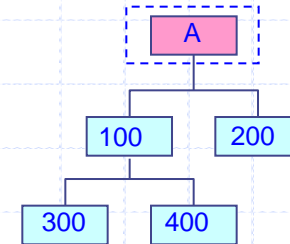
Generate gross requirements of items 100 and 200
(Items 300 and 400)

✓ Data
➤ Demand (planning horizon = 8 weeks) ←---- master production schedule (MPS)

Item A	1	2	3	4	5	6	7	8
Gross requirements	15	20	50	10	30	30	30	30

- Initial on-hand inventory = 30 units
- No scheduled receipts
- Lot size = 75 units
- Lead time = 1 week

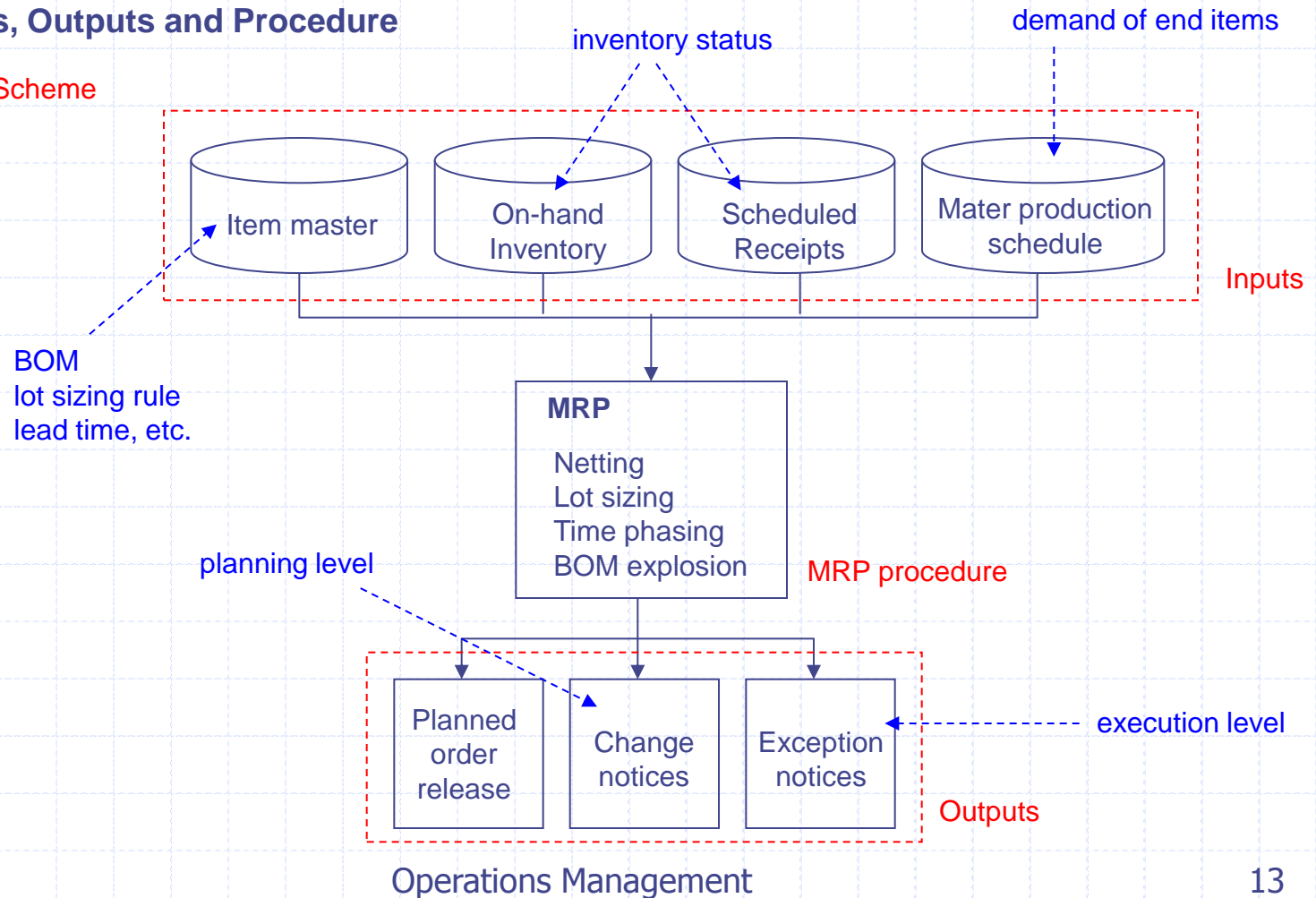
• Bill of material (BOM)



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◆ Inputs, Outputs and Procedure

Basic Scheme



MRP

Inputs, Outputs and Procedure

Inputs (1)

- Item Master File
 - ✓ Description of part/product
 - ✓ Bill of material (BOM) data

MRP accumulates all the demand of a part before it processes that part

- ✓ Lot sizing rule (LSR)

How the job will be sized?

balance the competing desires of reducing inventory (by using smaller lots) and increasing capacity (by using larger lots to avoid frequent setups)

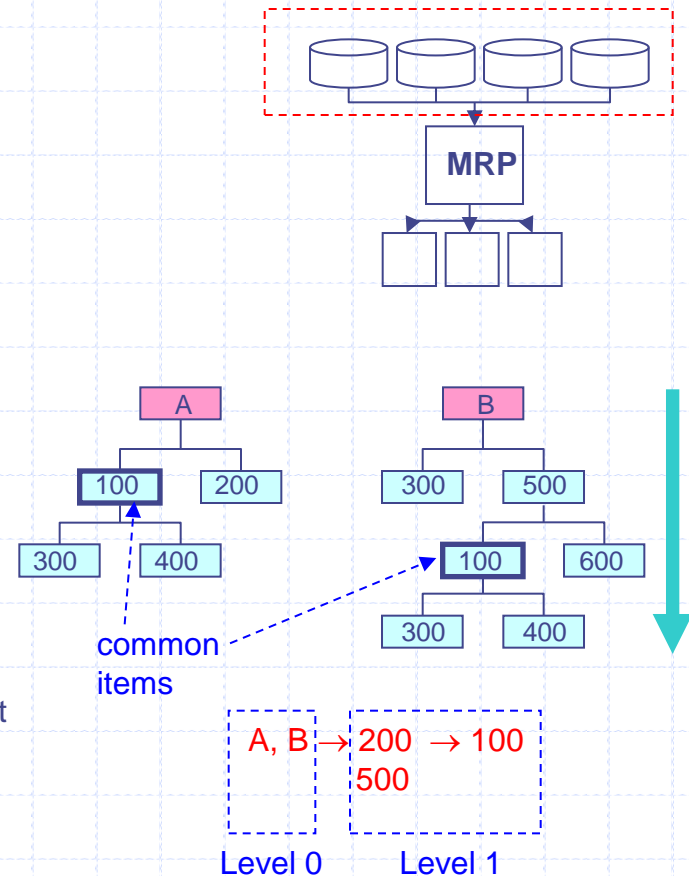
e.g, EOQ, Wagner-Whitin, etc.

- ✓ Planning lead time (PLT)

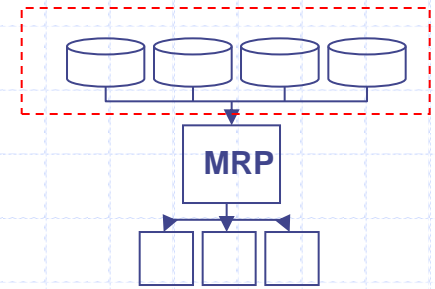
PLT is used to determine job start times

MRP – fixed (deterministic)

Actual lead times vary and are never known in advance. (→ safety lead time)



MRP



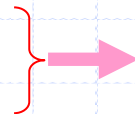
◆ Inputs, Outputs and Procedure

Inputs (2)

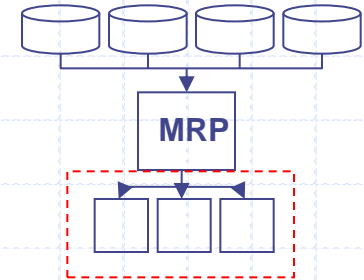
- **Master Production Schedule (MPS)**
 - ✓ Quantity and due dates of all parts that have independent demand (demand for all end items and external demand for lower-level parts)
 - ✓ Information
 - Part number
 - Needed quantity
 - Due date for each purchase order
- **Inventory Status File**
 - ✓ **On-hand inventory**

Information describing the part, where it is located, and how many are currently on hand
 - ✓ **Scheduled receipts**

Planned order release that has actually been released (Identifier, due date, release date, quantity needed, and current quantity, etc.)



gross requirements that initiate the MRP procedure



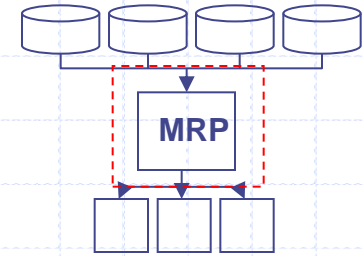
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◆ Inputs, Outputs and Procedure

Outputs

- Basic
 - ✓ Planned Order Release (POR)
 - Basic MRP output representing production or purchase orders
 - Information (material requirements)
 - Part ID
 - Number of units required
 - Due date of the job
- Additional
 - ✓ Change Notices ←----- planning level
 - Modification of existing job
(e.g. changes in due dates or priorities) ←-----
 - ✓ Exception Reports ←----- execution level
 - Notify the users that there are discrepancies
between what is expected and what is done

- Expediting: making due date earlier
- Deferring: making due date later



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◆ Inputs, Outputs and Procedure

Procedure (1)

- Overview

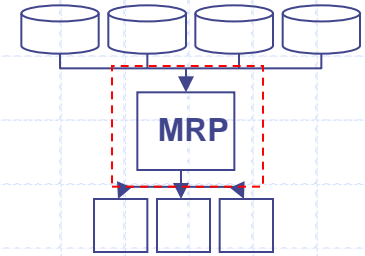
- (1) Netting ←----- net requirements (adjust scheduled receipts)
 (2) Lot sizing ←----- planned order receipts
 (3) Time Phasing ←----- planned order release
 (4) BOM explosion

Notation

- D_t gross requirement (demand) for period t
 S_t scheduled receipt in period t
 I_t projected on-hand inventory at the end of period t
 (I_0 is the initial on-hand inventory)
 N_t net requirement for period t

Projected on-hand
 = on-hand inventory + scheduled receipts – gross requirement

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Inputs, Outputs and Procedure

Procedure (2)

• Netting

Step 1. (Adjusting the scheduled receipts)

- (1) Find the period when the first scheduled receipts should arrive and adjust scheduled receipts (expediting or deferring). ←----- change notice

adjusted
scheduled receipt

$$I_t = I_{t-1} - D_t \quad \text{Increment } t \text{ and continue to compute } I_t \text{ until it becomes less than zero}$$

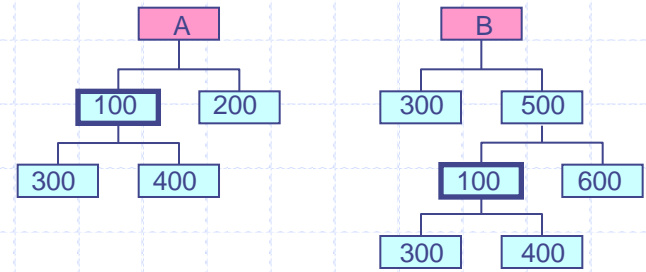
- $$I_t = I_{t-1} + S_t - D_t \quad \text{-----} \rightarrow (2) \text{ Modify the current on-hand inventory using the adjusted scheduled receipts. From the period obtained in Step (1), do Step (1) repeatedly until either we exhaust scheduled receipts or we have reached the end of the time horizon.}$$

- #### Step 2. (Calculating the net requirements) ←----- The net requirements are used in the lot-sizing procedure.

$$N_t = \begin{cases} 0 & \text{for } t < t^* \\ -I_t & \text{for } t = t^* \\ D_t & \text{for } t > t^* \end{cases}$$

t^* the first period with a negative projected on-hand inventory after all scheduled receipts have been properly adjusted.

MRP



Inputs, Outputs and Procedure

Procedure (3)

- Netting

✓ Example

$$I_3 = I_2 - D_3 = 5 - 50 = -45 < 0$$

→ Adjust S_3 (expediting)

$$I_3 = S_3 + I_2 - D_3 = 100 + 5 - 50 = 55$$

Initial on-hand inventory (I_0)

Item A	1	2	3	4	5	6	7	8
Gross requirements (D_t)	15	20	50	10	30	30	30	30
Scheduled receipts (S_t)	10	10		100				
Adjusted SR		20	100					
Projected on-hand (I_t)	20	5	55	45	15	-15		
Net requirements (N_t)						15	30	30
Planned order receipts								
Planned order releases								

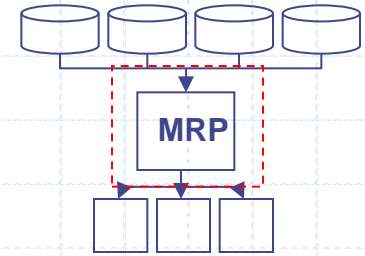
$$I_1 = I_0 - D_1 = 20 - 15 = 5$$

$$I_2 = I_1 - D_2 = 5 - 20 = -15 < 0$$

→ Adjust S_2 (deferring)

$$I_2 = S_2 + I_1 - D_2 = 20 + 5 - 20 = 5$$

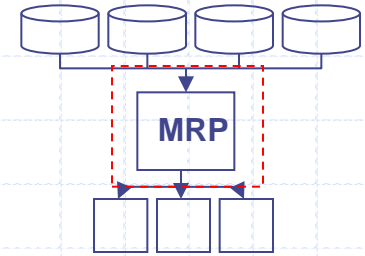
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◆ Inputs, Outputs and Procedure

Procedure (4)

- Lot sizing
 - ✓ Role
 - Net requirements (N_t) → planned order receipts (dynamic lot sizing problem)
 - ✓ Methods
 - Lot-for-lot
 - Fixed order quantity
 - Fixed order period
 - Part-period balancing, etc.



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◆ Inputs, Outputs and Procedure

Procedure (5)

- Lot sizing
 - ✓ Lot-for-lot (L4L)
 - Lot sizes (planned order receipts)

Amount to be produced in a period is equal to that period's net requirement

$$POR_t = N_t, t = 1, 2, \dots, T$$

➤ Practical reasons

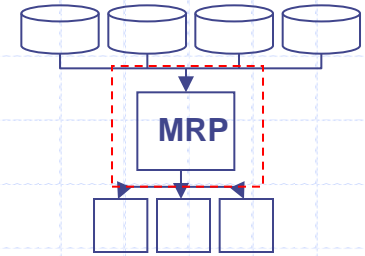
- Simple
- Production smoothing

←----- Not good for high setup costs

Example

Net requirement						15	30	30
Planned order receipts						15	30	30

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◆ Inputs, Outputs and Procedure

Procedure (6)

- Lot sizing
 - ✓ Fixed order quantity (FOQ)
 - Lot sizes (planned order receipts)

Fixed amount to be produced in each period

$$POR_t = \text{constant, for some } t$$

➤ Methods

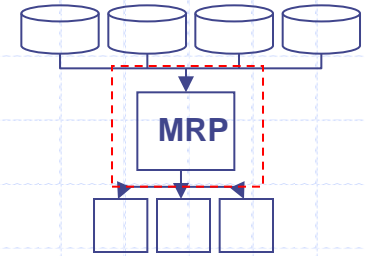
- Lot size = production capacity
- Economic order quantity (EOQ) based method

←---- Modification

Lot size = exact demand of one or more periods
(choose the number of periods closest to the desired fixed lot size)

Example (Q = 50)

Net requirement	15	15	60	65	55	15	20	10
Planned order receipts	30		60	65	55	45		



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◆ Inputs, Outputs and Procedure

Procedure (7)

- Lot sizing
 - ✓ Fixed order period (FOP)
 - Lot sizes (planned order receipts)

Amount to be produced in a period is the sum of the net requirements of P periods

$$POR_t = \text{demand for } t, t+1, \dots, t+P-1$$

P periods (fix)

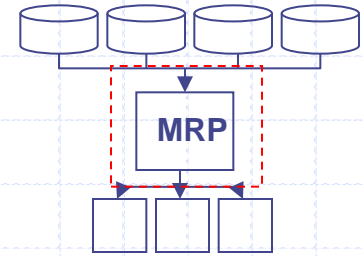
←---- lot-for-lot when P = 1

- How to select P?

e.g., using the EOQ formula

Example (P = 3)

Net requirement		15	45			25	15	20	15
Planned order receipts		60				60			15



MRP

◆ Inputs, Outputs and Procedure

Procedure (8)

- Lot sizing
 - ✓ Part-period balancing

➤ Basic idea

Balance the inventory carrying cost and setup cost while satisfying the Wagner-Whitin property

←----- EOQ: average inventory carrying cost = setup cost

➤ Computation of inventory cost (using part-period)

inventory cost = number of part-periods × inventory cost

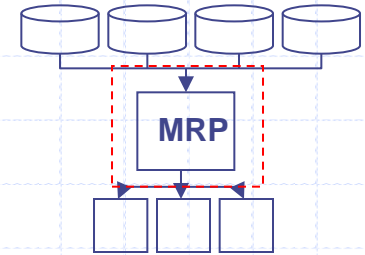
▪ Part-period

Number of parts in a lot × number of periods they are carried in inventory

e.g., 1 part carried for 10 period = 5 parts carried for 2 periods

————→ 10 part-period (same inventory carrying cost)

MRP



Inputs, Outputs and Procedure

Procedure (9)

- Lot sizing
- ✓ Part-period balancing

Example: $A = 150$, $h = 2$

Net requirement		15	45			25	15	20	15
Planned order receipts		60				60			15

period	1	2	3	4	5	6	7	8	9
Net requirement		15	45			25	15	20	15

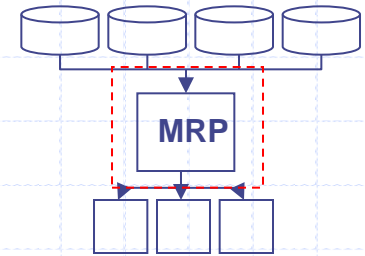
Period 2

Lot size	Setup cost	Part-period	Inventory cost
15	150	0	0
60	150	45	90 (45 × 2)
85	150	145	290 (145 × 2)

Period 6

Lot size	Setup cost	Part-period	Inventory cost
25	150	0	0
40	150	15	30
60	150	55	110
75	150	100	200

25



MRP

◆ Inputs, Outputs and Procedure

Procedure (10)

- Time Phasing (offsetting)

Consideration of lead times (constant)

Examples

Lead time = 1 period

Planned order receipts						45		30
Planned order releases					45		30	

Lead time = 2 periods

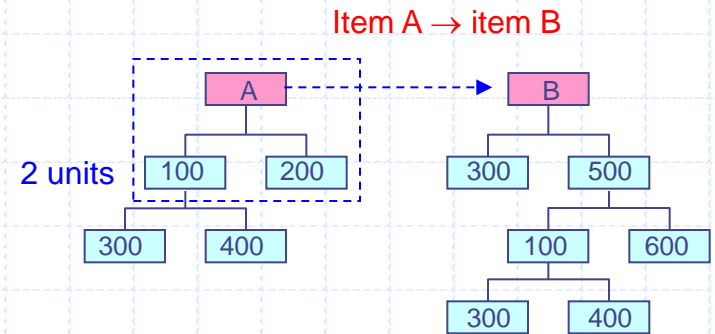
Planned order receipts						45		30
Planned order releases				45		30		

MRP

Inputs, Outputs and Procedure

Procedure (11)

- BOM Explosion – Example



Item A (lot sizing: fixed order period $P = 2$, lead time = 2 periods)

Initial inventory = 20

Item A	1	2	3	4	5	6	7	8
Gross requirements	15	20	50	10	30	30	30	30
Scheduled receipts (SR)	10	10		100				
Adjusted SR		20	100					
Projected on-hand	5	5	55	45	15	-15	-	-
Net requirements						15	30	30
Planned order receipts					45	30		
Planned order releases				45	30			

Planned order release generated for item A creates gross requirements for items 100 and 200.

Item 100

Gross requirements

Item 200

Gross requirements

2 units of part 100 for Part A

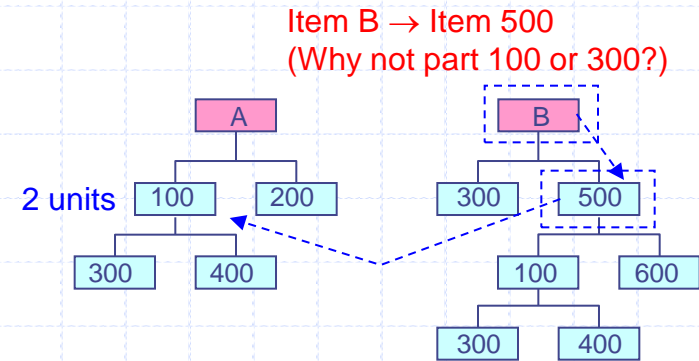
1 unit of part 200 for Part A

MRP

Inputs, Outputs and Procedure

Procedure (12)

- BOM Explosion – Example



Item B (lot sizing: fixed order period ($P = 2$), lead time = 2 periods)

No scheduled receipts
Initial inventory = 40

Item B	1	2	3	4	5	6	7	8
Gross requirements	10	15	10	20	20	15	15	15
Scheduled receipts (SR)								
Adjusted SR								
Projected on-hand	40	30	15	5	-15	-	-	-
Net requirements				15	20	15	15	15
Planned order receipts				35		30		15
Planned order releases		35		30		15		

Item 500 (lot sizing: lot-for-lot, lead time = 4 periods)

No scheduled receipts
Initial inventory = 40

Item 500	1	2	3	4	5	6	7	8
Gross requirements		35		30		15		
Scheduled receipts (SR)								
Adjusted SR								
Projected on-hand	40	5	5	-25	-	-	-	-
Net requirements				25		15		
Planned order receipts				25		15		
Planned order releases	25	15						

Late start

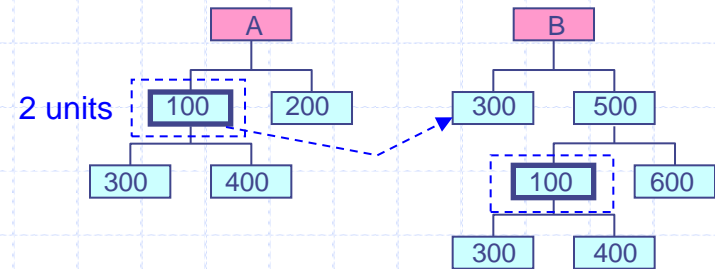
MRP

Inputs, Outputs and Procedure

Procedure (13)

- BOM Explosion – Example

Item 100 (lot sizing: lot-for-lot, lead time = 2 periods)



Item 100 → Item 300

Planned order releases (A)				45		30		
Planned order releases (500)	25	15						
Item 100	1	2	3	4	5	6	7	8
Gross requirements	25	15		90		60		
Scheduled receipts (SR)								
Adjusted SR								
Projected on-hand	15	0	0	-90	-	-	-	-
Net requirements				90		60		
Planned order receipts				90		60		
Planned order releases		90		60				

No scheduled receipts

Initial inventory = 40

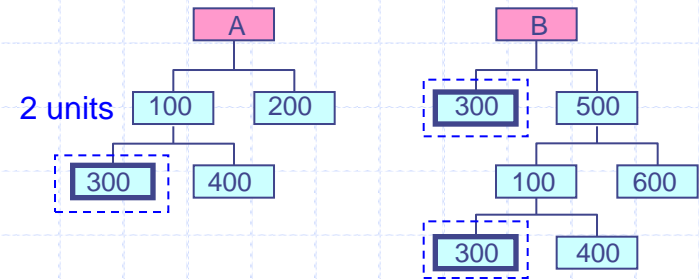
MRP

Inputs, Outputs and Procedure

Procedure (14)

- BOM Explosion – Example

Item 300 (lot sizing: lot-for-lot, lead time = 1 period)



Planned order releases (B)		35		30		15		
Planned order releases (100)		90		60				
Item 300	1	2	3	4	5	6	7	8
Gross requirements		125		90		15		
Scheduled receipts (SR)		100						
Adjusted-SR		100						
Projected on-hand	50	25	25	-65	-	-15	-	-
Net requirements				65		15		
Planned order receipts				65		15		
Planned order releases			65		15			

Initial inventory = 50

scheduled receipts (100 in period 2)

MRP

◆ Inputs, Outputs and Procedure

Procedure (15)

- BOM Explosion – Example
- ✓ Summary of MRP output

Transaction	Item Number	Old Due date Release Date	New Due Date	Quantity	Notice
Change notice	A	1 -----> 2	2	10	Defer
Change notice	A	4 -----> 3	3	100	Expedite
Planned order release	A	4	6	45	OK
Planned order release	A	6	8	30	OK
Planned order release	B	2	4	35	OK
Planned order release	B	4	6	30	OK
Planned order release	B	6	8	15	OK
Planned order release	100	2	4	90	OK
Planned order release	100	4	6	60	OK
Planned order release	300	3	4	65	OK
Planned order release	300	5	6	15	OK
Planned order release	500	1	4	25	Late
Planned order release	500	2	6	15	OK

MRP

◆ Further Considerations

Special Topics (1) ←----- Improving the performance of MRP

- Updating frequency

- ✓ Frequent update

Shop can be inundated with exception reports and constantly changing planned order release.

- ✓ Infrequent update

We can end up with old plans that are often out of date

←----- Balancing (trade-off)

- Firm Planned Order

- ✓ Planned order release that **held fixed**
(release regardless of changes in the system)

←----- The MRP procedure consider it as scheduled receipts.

- ✓ Why

Minimize schedule disruptions due to changes
(useful for reducing system nervousness)

MRP

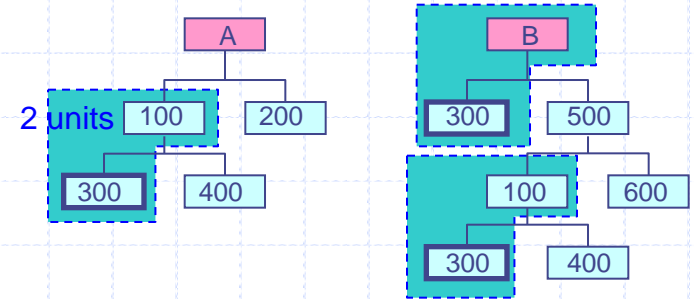
◆ Further Considerations

Special Topics (2)

- Troubleshooting
- ✓ Pegging

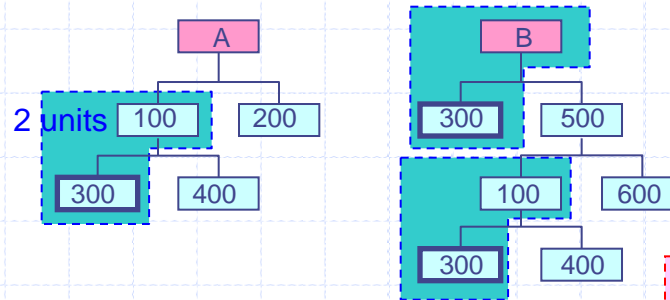
Allows the planner to see the source of demand that results in a given planned order release

Example



Planned order releases (B)		35		30		15		
Planned order releases (100)		90		60				
Item 300	1	2	3	4	5	6	7	8
Gross requirements		125		90		15		
...								
Planned order receipts				65		15		
Planned order releases			65		15			

MRP



See if we can deliver 25 units of A when requested, the remaining quantity later

Further Considerations

Special Topics (3)

- Troubleshooting
- ✓ Bottom-up replanning (based on pegging)

Example

Planned order releases (A)				45	25	30		
Planned order releases (500)	25	15						
Item 100	1	2	3	4	5	6	7	8
Gross requirements	25	15		90		60		
...								
Planned order receipts				90		60		
Planned order releases		90	50	60				

satisfy requirements of item B or 100?
- if we select to satisfy item 100 (50)

Planned order releases (B)		35		30		15		
Planned order releases (100)		90	50	60				
Item 300	1	2	3	4	5	6	7	8
Gross requirements		125		90		15		
Scheduled receipts (SR)		100						
Adjusted SR								
Projected on-hand	50	50						

schedules receipts cannot arrive on-time.

Call vendor, place the order immediately, etc.
→ Bottom-up replanning (if they are impossible)

MRP

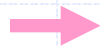
◆ Further Considerations

Problems (1)

- **Capacity Infeasibility** ←----- capacity = maximum output of a production (service) system (measures by units or time)
 - ✓ MRP assumes infinite capacity
 - ✓ Problems when production levels are at or near capacity.
 - > Development of MRP II (manufacturing resource planning)
 - Rough-cut capacity planning (RCCP) for master production schedule
 - Capacity requirement planning (CRP) for detailed capacity assessment

- **Long Planned Lead Times**

MRP uses the constant and long lead time (pessimistic).



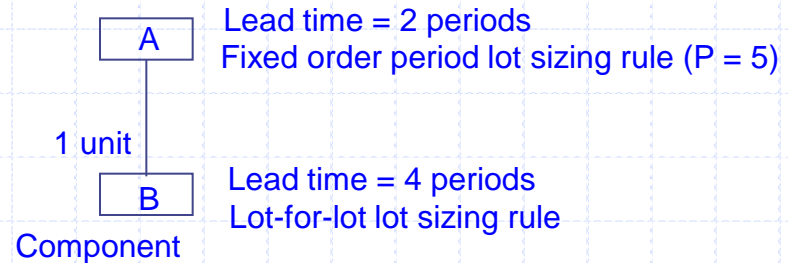
Large inventories
Low customer service level



Uncertainties in production systems

- 1) Demand (quantity and timing)
- 2) Processing time
- 3) Machine breakdowns
- 4) Quality problems, etc.

MRP



Further Considerations

Problems (2)

- System Nervousness

A small change in the master production schedule results in a large change in planned order releases.

Example

MRP calculations for Item A (before change in demand)

No scheduled receipts

Item A	1	2	3	4	5	6	7	8
Gross requirements	2	24	3	5	1	3	4	50
Projected on-hand	28	26	2	-1	-	-	-	-
Net requirements			1	5	1	3	4	50
Planned order receipts			14					50
Planned order releases	14					50		

MRP calculations for item B (before change in demand)

Item B	1	2	3	4	5	6	7	8
Gross requirements	14					50		
Scheduled receipts (SR)	14							
Adjusted SR	14							
Projected on-hand	2	2	2	2	2	-48	-	-
Net requirements						48		
Planned order receipts						48		
Planned order releases		48						

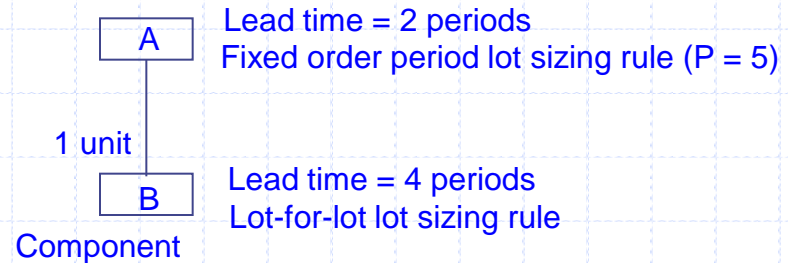
MRP

◆ Further Considerations

Problems (3)

- System Nervousness

Example



MRP calculations for Item A (after change in demand) demand change: 24 → 23

Item A	1	2	3	4	5	6	7	8
Gross requirements	2	23	3	5	1	3	4	50
Projected on-hand 28	26	3	0		-	-	-	-
Net requirements				5	1	3	4	50
Planned order receipts				63				
Planned order releases		63						

MRP calculations for item B (before change in demand)

Item B	1	2	3	4	5	6	7	8
Gross requirements		63						
Scheduled receipts (SR)	14							
Adjusted SR		14						
Projected on-hand 2	2	-47	-	-	-	-	-	-
Net requirements		47						
Planned order receipts		47						
Planned order releases	47							

Late start (almost impossible)

MRP

◆ Further Considerations

Problems (3)

- System Nervousness
- ✓ Methods to reduce system nervousness
 - Proper use of lot sizing rule

Lot-for-lot reduces nervousness, but results in too many setups

- Frozen zone (\equiv time fence) ←----- before MRP calculations

Initial number of periods in the MPS in which changes are not permitted

e.g.,

Item A	1	2	3	4	5	6	7	8
Gross requirements	2	24	3	5	1	3	4	50
Scheduled receipts (SR)								

frozen zone

- Firm planned order ←----- after MRP calculations

Planned order release that **held fixed**
(release regardless of changes in the system)