### **Electrical Engineering**

### HW 3 - Chapter 4

#### <1>

**4.2** For each case shown below, derive the expression for the current through a 200- $\mu$ F capacitor.  $v_C(t)$  is the voltage across the capacitor.

a. 
$$v_C(t) = 22\cos(20t - \frac{\pi}{3}) V$$

b. 
$$v_C(t) = -40\cos(90t + \frac{\pi}{2}) \text{ V}$$

c. 
$$v_C(t) = 28\cos(15t + \frac{\pi}{8}) \text{ V}$$

d. 
$$v_C(t) = 45\cos(120t + \frac{\pi}{4}) V$$

# <2>

**4.4** In the circuit shown in Figure P4.4, assume  $R = 1 \Omega$  and L = 2 H. Also, let:

$$i(t) = \begin{cases} 0 & -\infty < t < 0 \\ t & 0 \le t < 10 \text{ s} \\ 10 & 10 \text{ s} \le t < \infty \end{cases}$$

Find the energy stored in the inductor for all time.

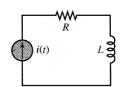


Figure P4.4

## <3>

**4.14** The current through a 16- $\mu$ H inductor is zero at t = 0, and the voltage across the inductor (shown in Figure P4.14) is:

$$v(t) = \begin{cases} 0 & t \le 0\\ 3t^2 & 0 \le t \le 20 \,\mu\text{s} \\ 1.2 \,\text{nV} & t \ge 20 \,\mu\text{s} \end{cases}$$

Determine the current through the inductor at  $t = 30 \,\mu\text{s}$ .

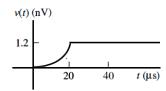


Figure P4.14

#### <4>

**4.35** Assume steady-state conditions and find the energy stored in each capacitor and inductor shown in Figure P4.35.

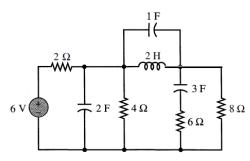


Figure P4.35

<5>

**4.37** Find the phasor form of the following functions:

a. 
$$v(t) = 155 \cos (377t - 25^{\circ}) \text{ V}$$

b. 
$$v(t) = 5 \sin(1,000t - 40^{\circ}) \text{ V}$$

c. 
$$i(t) = 10 \cos (10t + 63^\circ) + 15 \cos (10t - 42^\circ) A$$

d. 
$$i(t) = 460 \cos (500\pi t - 25^{\circ})$$
  
-  $220 \sin (500\pi t + 15^{\circ}) A$ 

### <6>

**4.47** Determine the equivalent impedance seen by the source  $v_S$  in Figure P4.47 when:

$$v_S(t) = 10\cos(4,000t + 60^\circ) \text{ V}$$
  
 $R_1 = 800 \text{ mH}, \Omega$   $R_2 = 500 \text{ nF } \Omega$   
 $L = 200 \text{ mH}$   $C = 70 \text{ nF}$ 

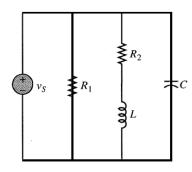


Figure P4.47

**4.51** Determine the voltage  $v_2(t)$  across  $R_2$  in the circuit of Figure P4.51.

$$i(t) = 20\cos(533.33t) \text{ A}$$
  
 $R_1 = 8 \Omega$   $R_2 = 16 \Omega$   
 $L = 15 \text{ mH}$   $C = 117 \mu\text{F}$ 

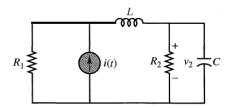


Figure P4.51

<8>

**4.70** Determine the Thévenin equivalent network seen by the load  $R_o$  in Figure P4.70. Assume:

$$R_S = R_o = 500 \,\Omega$$
  $L = 10 \,\mathrm{mH}$   $R = 1 \,\mathrm{k}\Omega$  and:

a. 
$$v_S(t) = 10\cos(1,000t)$$

b. 
$$v_S(t) = 10\cos(1,000,000t)$$

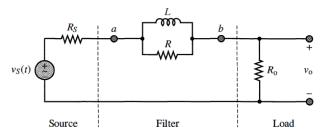


Figure P4.70

**4.74** Use nodal analysis to determine the node voltages  $v_a(t)$  and  $v_b(t)$  shown in Figure P4.74. Assume:

$$i(t) = 2\cos(300t) \text{ A}$$
  
 $v(t) = 7\cos(300t + \pi/4) \text{ V}$   
 $R_1 = 4 \Omega$   $R_2 = 3 \Omega$   $R_3 = 5 \Omega$   
 $L = 300 \text{ mH}$   $C = 300 \mu\text{F}$ 

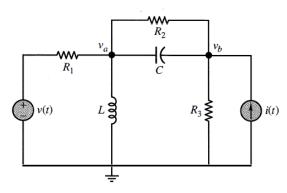


Figure P4.74