# **Chapter 3: Computer Arithmetic**

- Not implement ALU
  - Domain knowledge
- Do think about
  - Representing numbers (and ALU)
  - ISA from data perspective
- (optional) subword parallelism

## **Big Picture**

- ☐ Part 1: what is computer, CSE, computer architecture?
  - Fundamental concepts and principles
- ☐ Part 2: ISA (externals)
  - Ch. 1: performance
    - Exe. time, benchmark, model, RISC, power, multicore
  - Ch. 2: language of computer; ISA
    - What is a good ISA? Today's RISC-style ISA (MIPS)
  - Ch. 3: computer arithmetic (key internal building block)
    - Data representation and ALU, ISA data perspective
- ☐ Part 3: implementation of ISA (internals)
  - Ch. 4: processor
  - Ch. 5: memory system

#### **Numbers**

- □ Data types (INT and FP)
  - Numbers
  - Text, audio, image, video, and so on
- Representing numbers and ALU
  - Positive and negative integers
    - Numbers are finite (overflow)
  - Scientific numbers (too big or too small)
- ☐ ISA from data perspective

#### **Possible Representations**

Sign Magnitude: One's Complement Two's Complement

000 = +0	000 = +0	000 = +0
001 = +1	001 = +1	001 = +1
010 = +2	010 = +2	010 = +2
011 = +3	011 = +3	011 = +3
100 = -0	100 = -3	100 = -4
101 = -1	101 = -2	101 = -3
110 = -2	110 = -1	110 = -2
111 = -3	111 = -0	111 = -1

- ☐ Issues: balance, number of zeros, ease of operations
- ☐ Which one is best? Why?

#### **Possible Representations**

Biased Notation: Unsigned:

000 = -3
001 = -2
010 = -1
011 = 0
100 = +1
101 = +2
110 = +3
111 = +4
(Bias 3)

$$000 = -4$$
  $000 = +0$   
 $001 = -3$   $001 = +1$   
 $010 = -2$   $010 = +2$   
 $011 = -1$   $011 = +3$   
 $100 = 0$   $100 = +4$   
 $101 = +1$   $101 = +5$   
 $110 = +2$   $110 = +6$   
 $111 = +3$  (Bias 4)

#### MIPS (반복)

#### ☐ 32 bit signed numbers:

```
0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ _{two} = 0_{ten}
0000 0000 0000 0000 0000 0000 0001<sub>two</sub> = + 1_{ten}
0000 0000 0000 0000 0000 0000 0000 0010_{two} = + 2_{ten}
1000 0000 0000 0000 0000 0000 0000 _{\text{two}} = -2,147,483,648_{\text{ten}}  minint
1000 0000 0000 0000 0000 0000 0001 _{\text{two}} = -2,147,483,647_{\text{ten}}
1000 0000 0000 0000 0000 0000 0000 0010_{two} = -2,147,483,646_{ten}
1111 1111 1111 1111 1111 1111 1111 1101_{two} = -3_{ten}
1111 1111 1111 1111 1111 1111 1111 1110_{two} = -2_{ten}
1111 1111 1111 1111 1111 1111 1111 1111_{two} = -1_{ten}
```

## Two's Complement Operations (반복)

- □ Negating two's complement number: invert all bits and add 1
  - Remember: "negate" and "invert" are quite different!
- □ Signed and unsigned numbers
  - Memory address: start at 0 and end at the largest (e.g., FFFF)
  - Negative address make no sense
  - Some programming languages make this distinction
    - ⇒ C: int versus unsigned int
  - MIPS comparison instructions
    - ⇒ signed: slt, slti
    - ⇒ unsigned: sltu, sltiu

## Signed and unsigned loads (반복)

- ☐ Singed load: copy sign repeatedly to fill rest of register
  - e.g., two's complement numbers
- ☐ Unsigned load: fill with 0s to left of data
  - When bit pattern is unsigned
- MIPS instructions
  - Ib versus Ibu
  - Ih versus Ihu
  - lw
  - † No concern to store

#### **Addition & Subtraction**

☐ Just like in grade school (carry/borrow 1s)

```
0111 0110
+ 0110 - 0110 - 0101
```

- □ Two's complement operations easy
  - subtraction using addition of negative numbers

```
0111
+ 1010
```

- ☐ Arithmetic overflow (result too large for finite word):
  - e.g., adding two n-bit numbers not yield an n-bit number

```
0111
+ 0001
1000
```

#### **Two's Complement Arithmetic Overflow**

- No overflow when adding a positive and a negative number
- ☐ Overflow occurs when the value affects the sign:
  - overflow when adding two positives yields a negative
  - or, adding two negatives gives a positive
- $\Box$  Consider the operations A + B, and A B
  - Can overflow occur if B is 0?
  - Can overflow occur if A is 0?
- Overflow detection using a single exclusive-or gate

70	0110 0110	-70 1011 1010
+ 80	0101 0000	-80 1011 0000
150	1001 0110	-150 0110 1010

#### **Effects of Overflow**

- An exception (interrupt) occurs
  - Control jumps to predefined address for exception
  - Interrupted address is saved for possible resumption
- Given overflow, what does OS do?
- □ Arithmetic overflow: program bug
  - What do programmers should do?
    - Flight control vs. homework assignment
- What about unsigned integers?
  - Commonly used for memory addresses (by compiler)
  - 2's complement arithmetic overflows are ignored
- MIPS solution: provide two kinds of arithmetic instructions add, addi, sub addu, addiu, subu

// do not detect over

#### MIPS Assembly Language: add, subtract

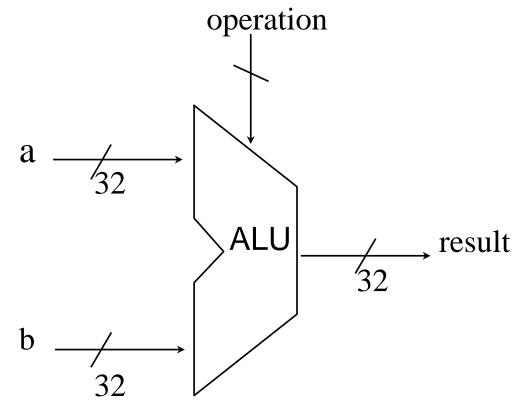
MIPS assembly language				
Category	Instruction	Example	Meaning	Comments
	add	add \$s1,\$s2,\$s3	\$s1 = \$s2 + \$s3	Three operands; overflow detected
	subtract	sub \$s1,\$s2,\$s3	\$s1 = \$s2 - \$s3	Three operands; overflow detected
	add immediate	addi \$s1,\$s2,100	\$s1 = \$s2 + 100	+ constant; overflow detected
	add unsigned	addu \$s1,\$s2,\$s3	\$s1 = \$s2 + \$s3	Three operands; overflow undetected
Arithmetic	subtract unsigned	subu \$s1,\$s2,\$s3	\$s1 = \$s2 - \$s3	Three operands; overflow undetected
	add immediate unsigned	addiu \$s1,\$s2,100	\$s1 = \$s2 + 100	+ constant; overflow undetected
	move from coprocessor register	mfc0 \$s1,\$epc	\$s1 = \$epc	Used to copy Exception PC plus other special registers

#### **Build ALU**

(Topic 1 에서 abstraction 이라는 개념을 설명하며 어느 정도 다룬 내용임)

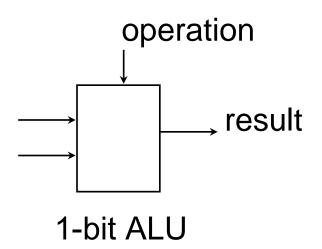
#### 32-bit ALU Design

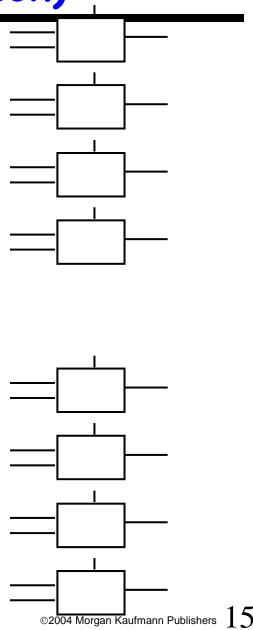
- Operations
  - Arithmetic: add, subtract, multiply, divide
  - · Logical: bitwise AND, OR, NOT



## 32-bit ALU Design (Abstraction)

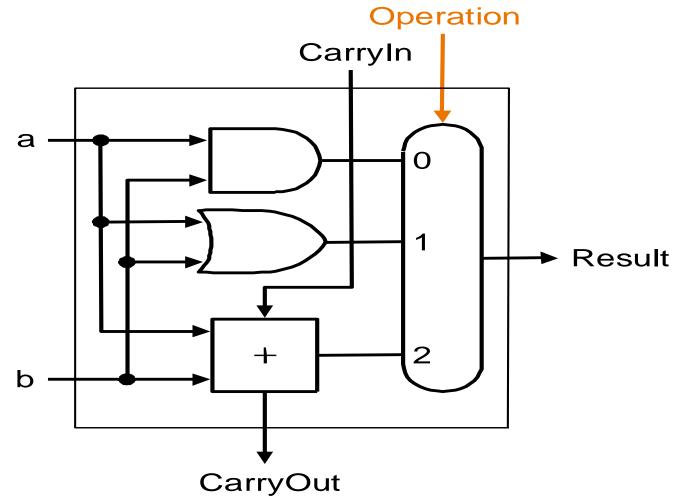
- ☐ Build 1-bit ALU
  - Use 32 of them in parallel





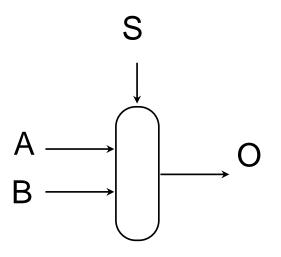
## 1-bit ALU Design (디지털논리설계; Abstraction)

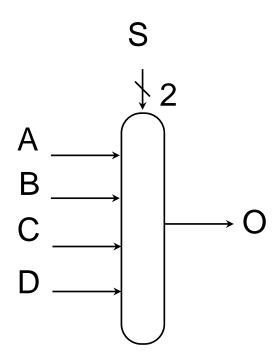
☐ 1-bit ADD, AND, OR



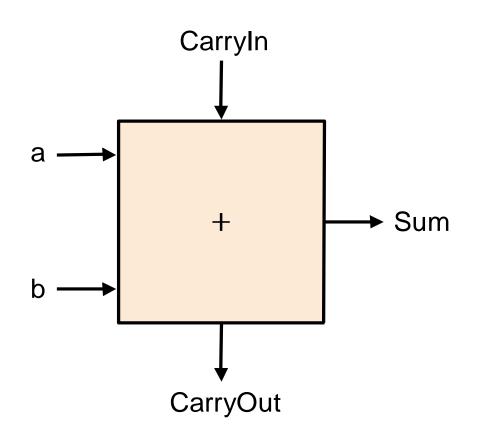
#### Multiplexor (Data Selector; Abstraction)

□ 2-to-1 MUX, 4-to-1 MUX (c.f., Demultiplexer)





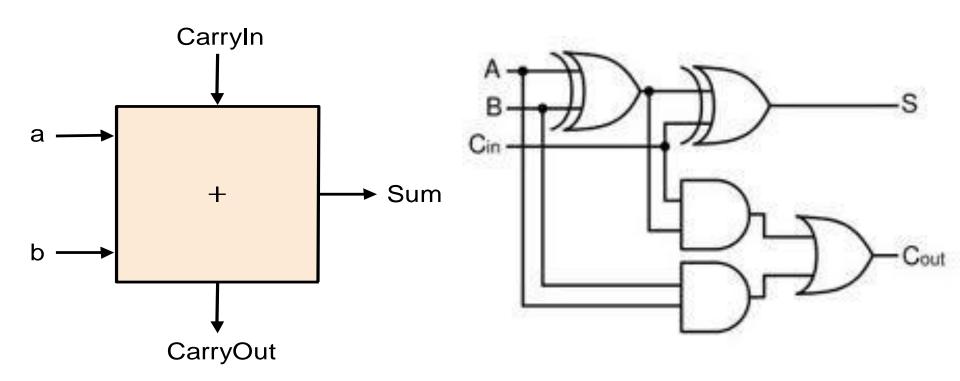
## 1-bit Full Adder Design (디지털논리설계)



A	В	C <sub>in</sub>	S	C <sub>out</sub>
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

$$c_{out} = a \cdot b + a \cdot c_{in} + b \cdot c_{in}$$
  
 $sum = a xor b xor c_{in}$ 

## 1-bit Full Adder Design (Abstraction)



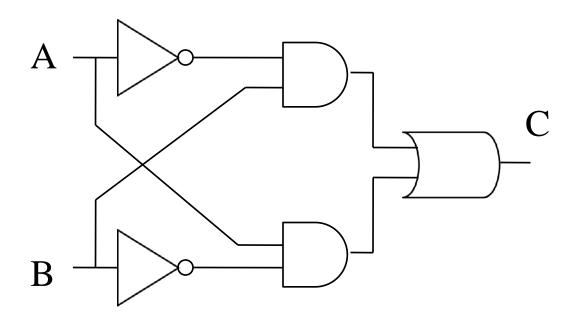
$$c_{out} = a \cdot b + a \cdot c_{in} + b \cdot c_{in}$$
  
 $sum = a xor b xor c_{in}$ 

## XOR (Exclusive-OR) Gate (Abstraction)

$$\Box$$
  $C = A XOR B = A \oplus B$ 

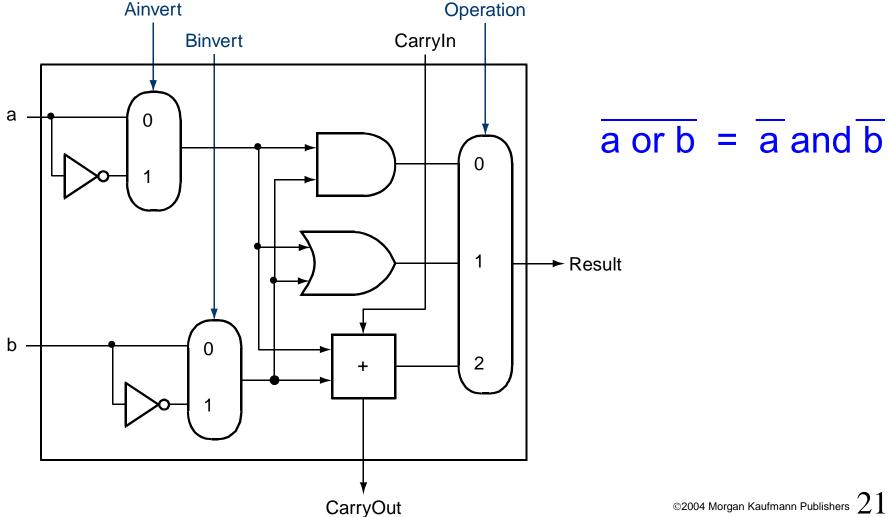
p	q	p⊕q
1	1	0
1	0	1
0	1	1
0	0	0

$$C = A \cdot B + A \cdot B$$



#### Adding a NOR function

☐ Can also choose to invert **a**. How do we get "**a** NOR **b**"?



#### Add Binary Numbers

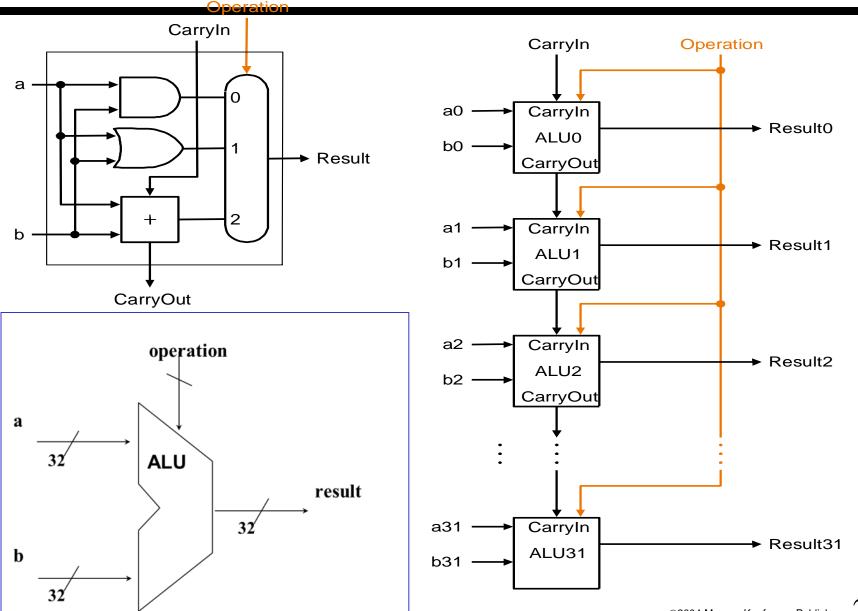
☐ Same with decimal add

Carry out Carry in

$$1000$$
 Carry

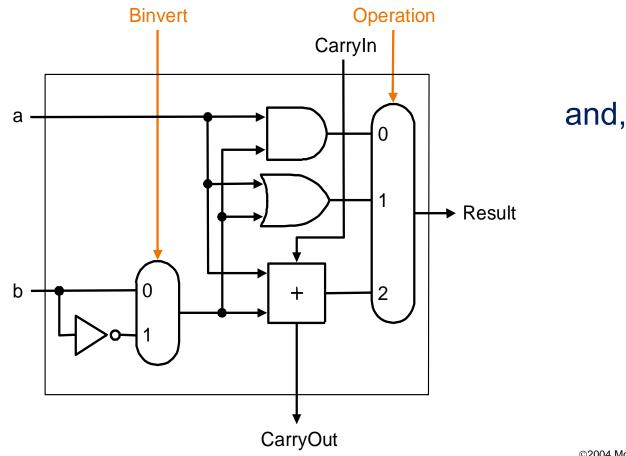
 $9_{10} = 1001$ 
 $12_{10} = 1100$ 
 $10101 = 21_{10}$ 

## 32-bit ALU Design (Abstraction)



#### What about subtraction (a - b)?

- ☐ Two's complement approach: negate b and add
  - Negate: bitwise NOT, then add 1

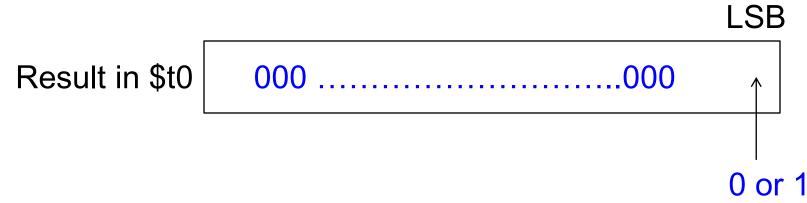


and, or, +, -

#### Tailoring the ALU to the MIPS

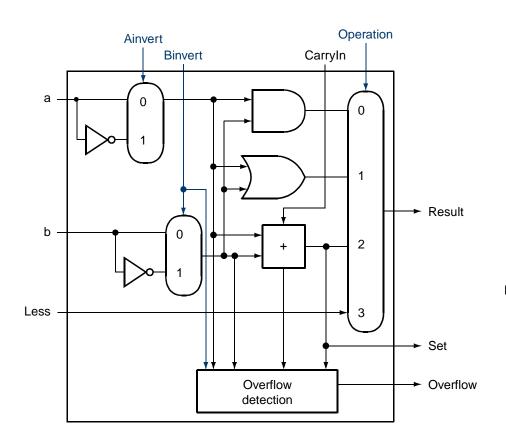
- ☐ Need to support the set-on-less-than instruction (slt)
  - Remember: slt is an arithmetic instruction
  - Produces a 1 if rs < rt and 0 otherwise</li>
  - Use subtraction: (a-b) < 0 implies a < b</li>

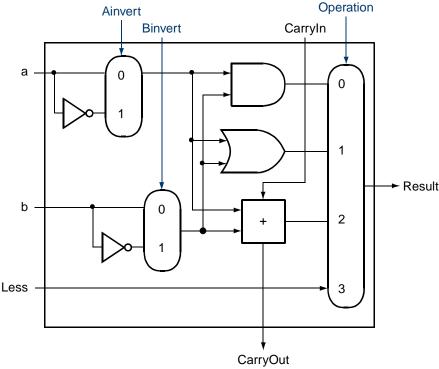
slt \$t0, \$t1, \$t2



#### **Supporting slt**

☐ Can we figure out the idea?

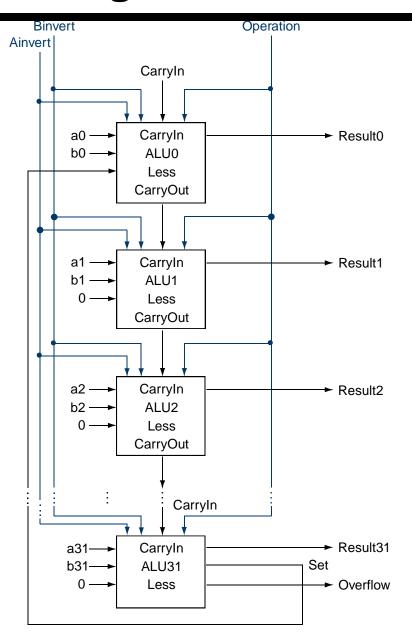




Adding all other bits

Adding most significant bits

#### **Supporting slt**



#### slt:

- 1) MUX는 less 선택
- 2) Bits 1-31: always 0
- 3) Bit 0: 0 or 1 (크기비교 결과)

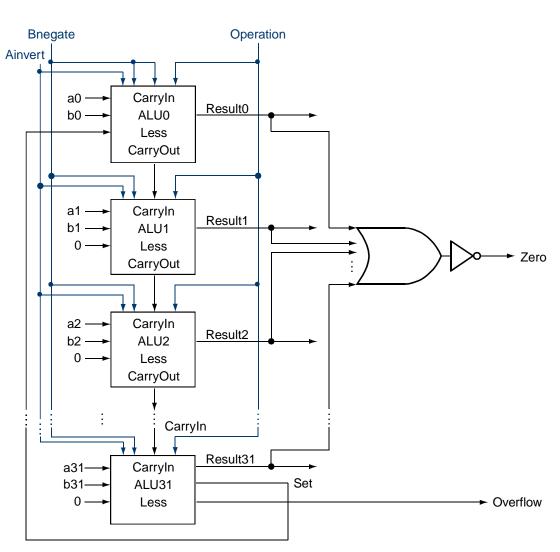
#### Tailoring the ALU to the MIPS

- ☐ Need to support test for equality (beq \$t5, \$t6, \$t7)
  - use subtraction: (a-b) = 0 implies a = b

#### **Test for equality**

■ Notice control lines:

† Note: zero is a 1 when the result is zero!



#### Conclusion

- □ We can build an ALU to support the MIPS instruction set
  - Key idea: use multiplexor to select the output we want
  - Can efficiently perform subtraction using 2's complement
  - Can replicate a 1-bit ALU to produce a 32-bit ALU
- ☐ Our primary focus: comprehension, however,
  - Clever changes to organization can improve performance (similar to using better algorithms in software)
  - Will see this in multiplication, let's look at addition now

#### Problem: ripple carry adder is slow

- □ Is a 32-bit ALU as fast as a 1-bit ALU?
- ☐ Is there more than one way to do addition?
  - Two extremes: ripple carry and sum-of-products
- † Can you see the ripple? How could you get rid of it?

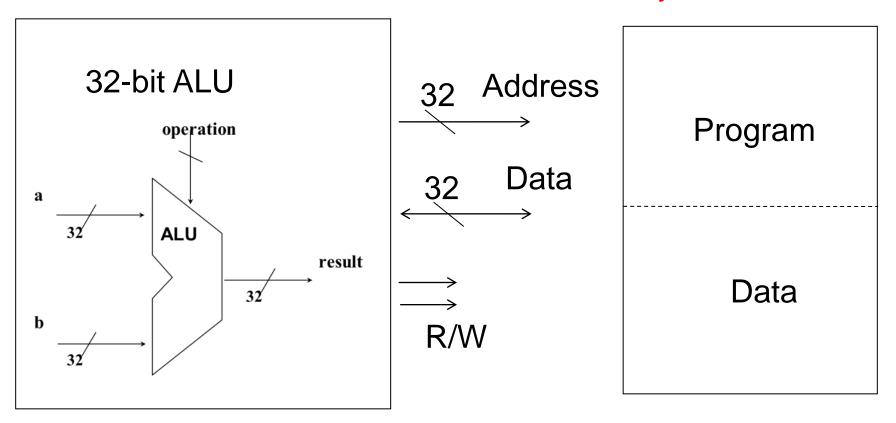
$$c_1 = b_0c_0 + a_0c_0 + a_0b_0$$
  
 $c_2 = b_1c_1 + a_1c_1 + a_1b_1$   $c_2 =$   
 $c_3 = b_2c_2 + a_2c_2 + a_2b_2$   $c_3 =$   
 $c_4 = b_3c_3 + a_3c_3 + a_3b_3$   $c_4 =$ 

Not feasible! Why?

## 32-bit Computer

**CPU** 

Memory: 32-bit wide



I/O: Monitor/keyboard, LAN-Internet, ...

# Computer Arithmetic and ALU

- ☐ Can you imagine
  - Many algorithms for addition,
    - Multiplication, division, FP operations as well
- □ Focus of building computer in 1945
  - Faster ALU
    - How to represent numbers
- □ Computer arithmetic
  - Matured in 1950s and 1960s
- □ Today, can buy ALU as IP (Intellectual Property)

#### **Arithmetic for Multimedia**

- ☐ Graphics and media processing operates on vectors of 8-bit and 16-bit data
  - Use 64-bit adder, with partitioned carry chain
    - Operate on 8×8-bit, 4×16-bit, or 2×32-bit vectors
  - SIMD (single-instruction, multiple-data), SSE
    - Subword parallelism
- □ Saturating operations
  - On overflow, result is largest representable value
    - c.f. 2s-complement modulo arithmetic
  - e.g., clipping in audio, saturation in video

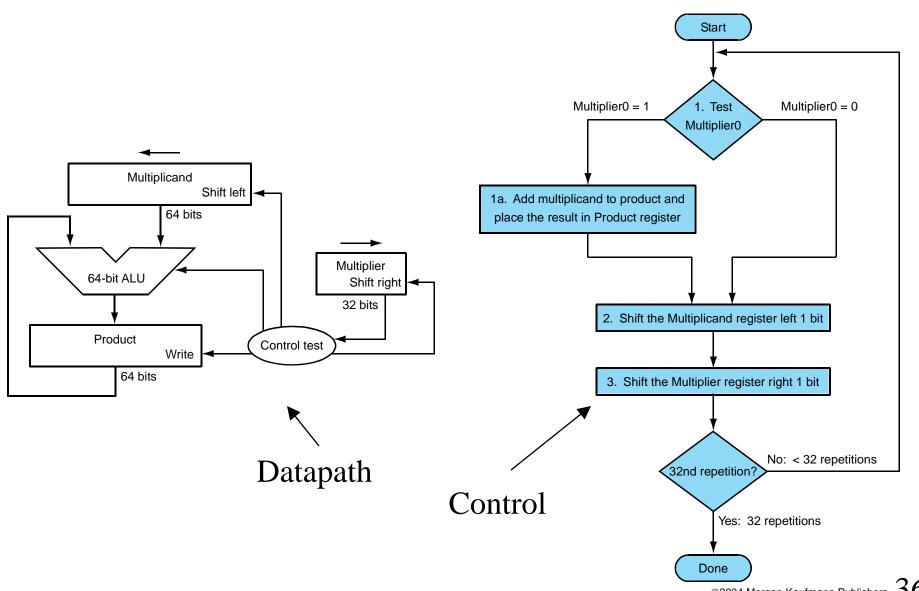
#### Multiplication

- More complicated than addition
  - Accomplished via shifting and addition
- More time and more area
- ☐ Let's look at 3 versions based on a gradeschool algorithm

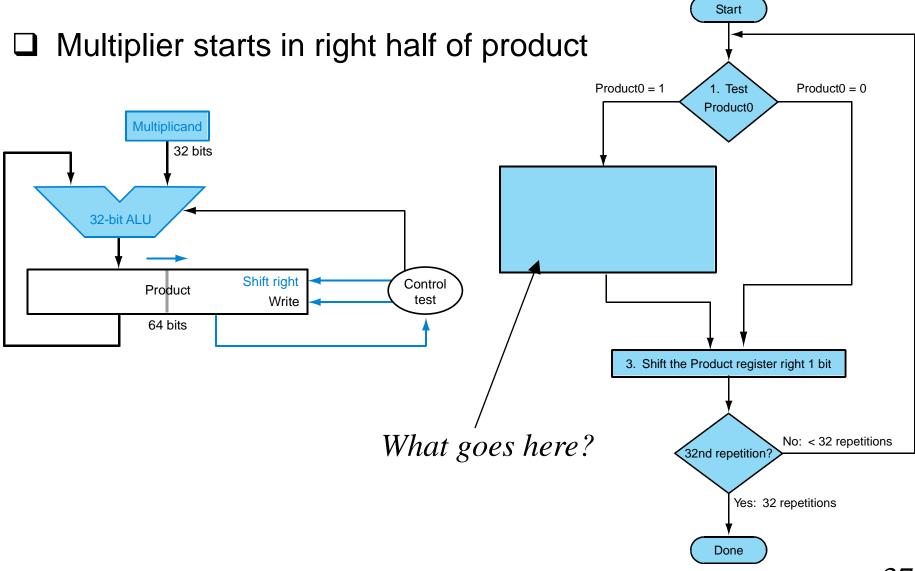
```
0010 (multiplicand)
<a href="mailto:x">x</a> 1011 (multiplier)
```

- Negative numbers: convert and multiply
  - There are better techniques, we won't look at them

#### Multiplication: Implementation



#### **Final Version**



# MIPS Assembly Language: multiply, divide

Category	Instruction	Example		Meaning	Comments
	add	add	\$s1,\$s2,\$s3	\$s1 = \$s2 + \$s3	Three operands; overflow detected
	subtract	sub	\$s1,\$s2,\$s3	\$s1 = \$s2 - \$s3	Three operands; overflow detected
	add immediate	addi	\$s1,\$s2,100	\$s1 = \$s2 + <b>100</b>	+ constant; overflow detected
	add unsigned	addu	\$s1,\$s2,\$s3	\$s1 = \$s2 + \$s3	Three operands; overflow undetected
	subtract unsigned	subu	\$s1,\$s2,\$s3	\$s1 = \$s2 - \$s3	Three operands; overflow undetected
	add immediate unsigned	addiu	\$s1,\$s2,100	\$s1 = \$s2 + 100	+ constant; overflow undetected
	move from coprocessor register	mfc0	\$s1,\$epc	\$s1 = \$epc	Copy Exception PC + special regs
Arithmetic	multiply	mult	\$s2,\$s3	Hi, Lo = \$s2 × \$s3	64-bit signed product in Hi, Lo
	multiply unsigned	multu	\$s2,\$s3	Hi, Lo = \$s2 × \$s3	64-bit unsigned product in Hi, Lo
	divide	div	\$s2 <b>,</b> \$s3	Lo = \$s2 / \$s3, Hi = \$s2 mod \$s3	Lo = quotient, Hi = remainder
	divide unsigned	divu	\$s2,\$s3	Lo = \$s2 / \$s3, Hi = \$s2 mod \$s3	Unsigned quotient and remainder
	move from Hi	mfhi	\$s1	\$s1 = Hi	Used to get copy of Hi
	move from Lo	mflo	\$s1	\$s1 = Lo	Used to get copy of Lo

# Floating-Point Numbers

(Why the name? Fixed-point numbers?)

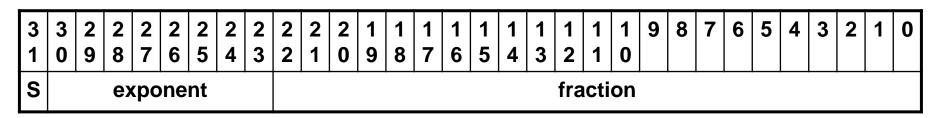
# Floating Point (a brief look)

- ☐ We need a way to represent
  - numbers with fractions, e.g., 3.1416
  - very small numbers, e.g.,  $0.71 \times 10^{-78}$
  - very large numbers, e.g.,  $3.15576 \times 10^{69}$
- ☐ Representation:
  - sign, exponent, significand: (-1)<sup>sign</sup> · significand · 2<sup>exponent</sup>
  - more bits for significand gives more accuracy
  - more bits for exponent increases range
- ☐ IEEE 754 floating point standard:
  - single precision: 8 bit exponent, 23 bit significand
  - double precision: 11 bit exponent, 52 bit significand Publishers 2

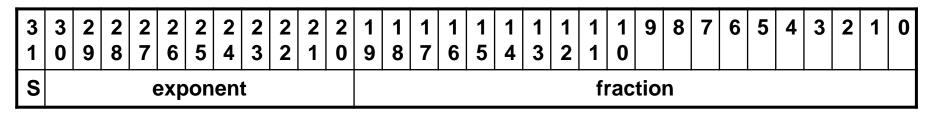
# **IEEE 754 floating-point standard**

- ☐ Leading "1" bit of significand is implicit
- Exponent is "biased" to make sorting easier
  - all 0s is smallest exponent all 1s is largest
    - bias of 127 for single precision and 1023 for double precision
  - summary: (-1)<sup>sign</sup> · (1+significand) · 2<sup>exponent bias</sup>
- Example:
  - decimal:  $-.75 = -(\frac{1}{2} + \frac{1}{4})$
  - binary:  $-.11 = -1.1 \times 2^{-1}$
  - floating point: exponent = 126 = 011111110
  - IEEE single precision:

### **IEEE 754 floating-point standard**



1 bit 8 bits 23 bits



1 bit 11 bits 20 bits

fraction (continued)

32 bits

# **Single-Precision Range**

- Exponents 00000000 and 11111111 reserved
- ☐ Smallest value
  - Exponent: 00000001
     ⇒ actual exponent = 1 127 = -126
  - Fraction:  $000...00 \Rightarrow significand = 1.0$
  - $\pm 1.0 \times 2^{-126} \approx \pm 1.2 \times 10^{-38}$
- ☐ Largest value
  - exponent: 111111110
     ⇒ actual exponent = 254 127 = +127
  - Fraction: 111...11 ⇒ significand ≈ 2.0
  - $\pm 2.0 \times 2^{+127} \approx \pm 3.4 \times 10^{+38}$

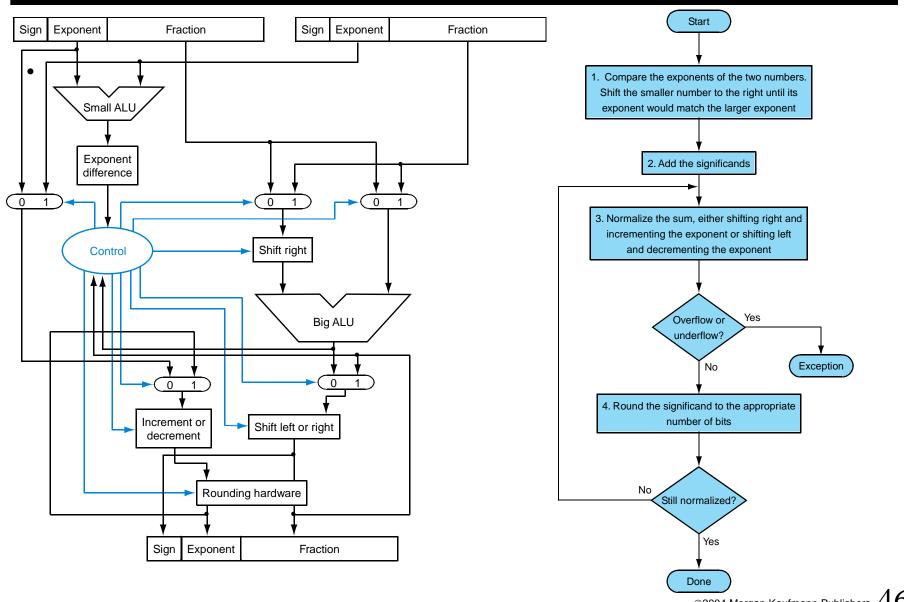
#### **Double-Precision Range**

- ☐ Exponents 0000...00 and 1111...11 reserved
- Smallest value
  - Exponent: 0000000001
    - $\Rightarrow$  actual exponent = 1 1023 = –1022
  - Fraction:  $000...00 \Rightarrow \text{significand} = 1.0$
  - $\pm 1.0 \times 2^{-1022} \approx \pm 2.2 \times 10^{-308}$
- □ Largest value
  - Exponent: 1111111110
    - $\Rightarrow$  actual exponent = 2046 1023 = +1023
  - Fraction: 111...11 ⇒ significand ≈ 2.0
  - $\pm 2.0 \times 2^{+1023} \approx \pm 1.8 \times 10^{+308}$

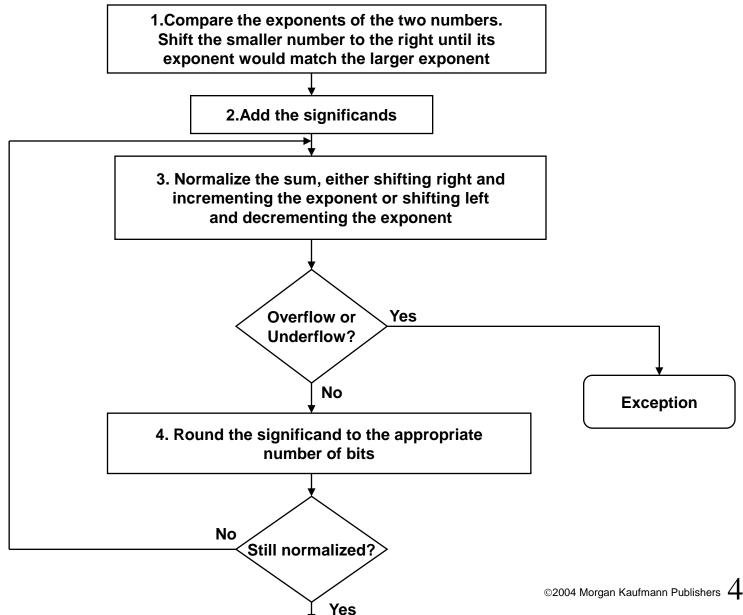
# **IEEE 754 floating point standard**

- Why do we use floating point representation?
  - Very large numbers, very small numbers
- What do we lose?
  - Accuracy, intervals not uniform
- ☐ Think about overflow, underflow
- ☐ In 32-bit standard, how many bits for significand?
  - Range vs. accuracy trade-off
- ☐ How do we represent 0, infinity?
  - Exp = 255, sig != 0  $\rightarrow$  NaN
  - Exp = 255, sig = 0  $\rightarrow$  +, infinity
  - Exp = 0, sig =  $0 \rightarrow 0$
  - Exp =0, sig != 0  $\rightarrow$  even smaller numbers 45

# Floating point addition



# Floating point addition

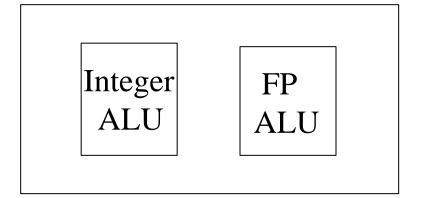


#### **FP Adder Hardware**

- ☐ Much more complex than integer adder
- Doing it in one clock cycle would take too long
  - Much longer than integer operations
  - Slower clock would penalize all instructions
- ☐ FP adder usually takes several cycles
  - Can be pipelined

# Integer and FP ALUs (반복)

☐ Processor for general-purpose computers:



Pentium

☐ Processors for embedded systems:

Integer ALU

Smaller Cheaper Low-power

# MIPS Assembly Language: floating-point

#### MIPS floating-point operands

Name	Example	Comments
32 floating- point registers	\$f0, \$f1, \$f2, , \$f31	MIPS floating-point registers are used in pairs for double precision numbers.
2 <sup>30</sup> memory words	Memory[0], Memory[4], , Memory[4294967292]	Accessed only by data transfer instructions. MIPS uses byte addresses, so sequential word addresses differ by 4. Memory holds data structures, such as arrays, and spilled registers, such as those saved on procedure calls.

#### MIPS floating-point assembly language

Category	Instruction	Example	Meaning	Comments
handwidth b	FP add single	add.s \$f2,\$f4,\$f6	\$f2 = \$f4 + \$f6	FP add (single precision)
	FP subtract single	sub.s \$f2,\$f4,\$f6	\$f2 = \$f4 - \$f6	FP sub (single precision)
	FP multiply single	mul.s \$f2,\$f4,\$f6	\$f2 = \$f4 × \$f6	FP multiply (single precision)
Arithmetic	FP divide single	div.s \$f2,\$f4,\$f6	\$f2 = \$f4 / \$f6	FP divide (single precision)
Arithmetic	FP add double	add.d \$f2,\$f4,\$f6	\$f2 = \$f4 + \$f6	FP add (double precision)
	FP subtract double	sub.d \$f2,\$f4,\$f6	\$f2 = \$f4 - \$f6	FP sub (double precision)
	FP multiply double	mul.d \$f2,\$f4,\$f6	$$f2 = $f4 \times $f6$	FP multiply (double precision)
	FP divide double	div.d \$f2,\$f4,\$f6	\$f2 = \$f4 / \$f6	FP divide (double precision)
Data	load word copr. 1	1wc1 \$f1,100(\$s2)	\$f1 = Memory[\$s2 + 100]	32-bit data to FP register
transfer	store word copr. 1	swc1 \$f1,100(\$s2)	Memory[ $$s2 + 100$ ] = $$f1$	32-bit data to memory (101)
	branch on FP true	bclt 25	if (cond == 1) go to PC + 4 + 100	PC-relative branch if FP cond.
Condi-	branch on FP false	bc1f 25	if (cond == 0) go to PC + 4 + 100	PC-relative branch if not cond.
tional branch	FP compare single (eq,ne,lt,le,gt,ge)	c.lt.s \$f2,\$f4	if (\$f2 < \$f4) cond = 1; else cond = 0	FP compare less than single precision
	FP compare double (eq,ne,lt,le,gt,ge)	c.lt.d \$f2,\$f4	if (\$f2 < \$f4) cond = 1; else cond = 0	FP compare less than double precision

### MIPS Assembly Language: floating-point

	AND REPORT OF THE PARTY OF THE	MARKEN SER		ating-point <b>m</b> a		FSVIII (SSVIII) (SSSIII)	MATERIAL TRANSPORTER		
Name	Format		Example					Comments	
add.s	R	17	16	6	4	2	0	add.s \$f2,\$f4,\$f6	
sub.s	R	17	16	6	4	2	1	sub.s \$f2,\$f4,\$f6	
mul.s	R	17	16	6	4	2	2	mul.s \$f2,\$f4,\$f6	
div.s	R	17	16	6	4	2	. 3	div.s \$f2,\$f4,\$f6	
add.d	R	17	17	6	4	2	0	add.d \$f2,\$f4,\$f6	
sub.d	R	17	17	6	4	2	1	sub.d \$f2,\$f4,\$f6	
mul.d	R	17	17	6	4	2	2	mul.d \$f2,\$f4,\$f6	
div.d	R	17	17	6	4	2	3	div.d \$f2,\$f4,\$f6	
lwc1		49	20	2	D to Wass	100	gelen.	lwc1 \$f2,100(\$s4)	
swc1	CLIFF	57	20	2	LUT BORRES	100	y d	swc1 \$f2,100(\$s4)	
bc1t	110 <sup>1</sup> 8 and	17	8	100_0	atic noi 300	25	n wen ni b	bc1t 25	
bc1f slamaza no?	ed elstwhere.	17	8 - 65	DHU 011000	its 31-26) is	25	alue of the	bc1f 25 document	
c.lt.s	R	17.50	16	he bg 4 gd end	2 1101	d or O it he	60	c.1t.s \$f2,\$f4	
c.lt.d	R	17	17	4	2	0	60	c.1t.d \$f2,\$f4	
Field size	(z = 0 = a) ele	6 bits	5 bits	5 bits	5 bits	5 bits	6 bits	All MIPS instructions 32 bit	

#### To Think about

- When you do C, Java programming
  - When do you use float?
  - When do you use double?
  - Do you ever think about long integer or arithmetic overflow?
- FP numbers and FP ALU
  - 계산을 위한 인공적인 고안의 결과
  - No beauty of integers
    - Not accurate from mathematics perspective

# **Associativity**

- □ Parallel programs may interleave operations in unexpected orders
  - Assumptions of associativity may fail

		(x+y)+z	x+(y+z)
X	-1.50E+38		-1.50E+38
У	1.50E+38	0.00E+00	
Z	1.0	1.0	1.50E+38
		1.00E+00	0.00E+00

- Need to validate parallel programs under varying degrees of parallelism – numerical analysis
- FP numbers only approximations of real numbers

# Who Cares About FP Accuracy?

- ☐ Important for scientific code
  - But for everyday consumer use?
    - "My bank balance is out by 0.0002¢!" ☺
- ☐ The Intel Pentium FDIV bug
  - The market expects accuracy
  - See Colwell, The Pentium Chronicles



The Hardware/Software Interface



# **Sections 3.6**

# Parallelism and Computer Arithmetic: Subword Parallelism



The Hardware/Software Interface



# **Sections 3.7**

Real stuff: streaming SIMD extensions and advanced vector extensions in x86



The Hardware/Software Interface



# **Sections 3.8**

# Going faster: subword parallelism and matrix multiply



The Hardware/Software Interface



# **Sections 3.10**

### **Concluding Remarks**

(가볍게 읽어 보실 것)

# **Concluding Remarks**

- Bits have no inherent meaning
  - Interpretation depends on the instructions applied
- Computer representations of numbers
  - Finite range and precision
  - Need to account for this in programs

# **Concluding Remarks**

- ISAs support arithmetic
  - Signed and unsigned integers
  - Floating-point approximation to reals
- Bounded range and precision
  - Operations can overflow and underflow
- MIPS ISA
  - Core instructions: 54 most frequently used
    - 100% of SPECINT, 97% of SPECFP
  - Other instructions: less frequent

# MIPS Core, MIPS-32, Pseudo MIPS

MIPS core instructions	Name	Format	MIPS arithmetic core	Name	Format
add	add	R	multiply	mult	R
add immediate	addi	1	multiply unsigned	multu	R
add unsigned	addu	R	divide	div	R
add immediate unsigned	addiu	1	divide unsigned	divu	R
subtract	sub	R	move from Hi	mfhi	R
subtract unsigned	subu	R	move from Lo	mflo	R
AND	AND	R	move from system control (EPC)	mfc0	R
AND immediate	ANDi	1	floating-point add single	add.s	R
OR	OR	R	floating-point add double	add.d	R
OR immediate	ORi	1	floating-point subtract single	sub.s	R
NOR	NOR	R	floating-point subtract double	sub.d	R
shift left logical	s11	R	R floating-point multiply single		R
shift right logical	srl	R	floating-point multiply double	mul.d	R
load upper immediate	er immediate lui l floating-point divide single		div.s	R	
load word	1w	1	floating-point divide double	div.d	R
store word	SW	1	load word to floating-point single	lwc1	Î
load halfword unsigned	1hu	1	store word to floating-point single	swc1	1
store halfword	sh	1	load word to floating-point double	1dc1	Ĭ
load byte unsigned	1bu	(1)	store word to floating-point double	sdcl	1
store byte	sb	1	branch on floating-point true	bc1t	1
load linked (atomic update)	11	1	branch on floating-point false	bc1f	1
store cond. (atomic update)	SC	1	floating-point compare single	c.x.s	R
branch on equal	beq	1	(x = eq, neq, lt, le, gt, ge)		
branch on not equal	bne	1	floating-point compare double	c.x.d	R
jump	j	J	(x = eq, neq, lt, le, gt, ge)		
jump and link	jal	J	2		
jump register	jr	R	A.		
set less than	slt	R		,	
	4		<b>-</b>		

slti

sltu

sltiu

R

set less than unsigned
set less than immediate unsigned

set less than immediate

Figure 3.26



Remaining MIPS-32	Name	Format	Pseudo MIPS	
exclusive or (rs ⊕ rt)	xor	R	absolute value	
exclusive or immediate	xori	1	negate (signed or <u>u</u> nsigned)	
shift right arithmetic	sra	R	rotate left	
shift left logical variable	sllv	R	rotate right	
shift right logical variable	srlv	R	multiply and don't check oflw (signed or uns.)	
shift right arithmetic variable	srav	R	multiply and check oflw (signed or uns.)	
move to Hi	mthi	R	divide and check overflow	
move to Lo	mtlo	R	divide and don't check overflow	
load halfword	1h	1	remainder (signed or unsigned)	
load byte	16	1	load immediate	
load word left (unaligned)	1w1	1	load address	
load word right (unaligned)	1wr	1	load double	
store word left (unaligned)	swl	1	store double	
store word right (unaligned)	swr	- 1	unaligned load word	
load linked (atomic update)	11	1	unaligned store word	
store cond. (atomic update)	SC	1	unaligned load halfword (signed or uns.)	
move if zero	movz	R	unaligned store halfword	
move if not zero	movn	R	branch	
multiply and add (S or <u>u</u> ns.)	madds	R	branch on equal zero	
multiply and subtract (S or uns.)	msubs	1	branch on compare (signed or unsigned)	
branch on ≥ zero and link	bgeza1	1	(x = 1t, 1e, gt, ge)	
branch on < zero and link	bltzal	1	set equal	
jump and link register	jalr	R	set not equal	
branch compare to zero	bxz	1	set on compare (signed or unsigned)	
branch compare to zero likely	bxz1	1	(x = 1t, 1e, gt, ge)	
(x = 1t, Te, gt, ge)			load to floating point (s or d)	
branch compare reg likely	bx1	1	store from floating point (s or d)	
trap if compare reg	tx	R	0 0000 0000 11-40	
trap if compare immediate	txi	1		
(x = eq, neq, lt, le, gt, ge)				
return from exception	rfe	R	1	
system call	syscall	113	1	
break (cause exception)	break	- 1	1	
move from FP to integer	mfc1	R	1	
move to FP from integer	mtc1	R	1	
FP move (s or d)	mov.f	R	1	
FP move if zero (s or d)	movz.f	R	†	
FP move if not zero (s or d)	movn.f	R	1	
FP square root (s or d)	sart.f	R	1	
FP absolute value (s or d)	abs.f	R	+	
		R	<del></del>	
FP negate (s or d)	neg.f	R D	Figu	

cvt.f.f

C.XN.

R



Name

abs

negs

rol

ror

muls.

mulos.

div

divu

rems

11

1a

1d

sd

ulw

USW

ulhs

ush

begz

bxs

seq

sne

SXS

1.1

5.1

b

**Format** 

rd,rs

rd,rs

rd,rs,rt

rd,rs,rt

rd,rs,rt

rd,rs,rt

rd,rs,rt

rd,rs,rt

rd,rs,rt

rd,imm

rd,addr

rd,addr

rd,addr

rd,addr

rd,addr

rd,addr

rd,addr

Label

rs,L

rs,rt,L

rd,rs,rt

rd,rs,rt

rd,rs,rt

rd,addr

rd,addr

Figure 3.27



FP convert (w, s, or d)

FP compare un (s or d)

# MIPS Core, MIPS-32, Pseudo MIPS

Frequency of use in SPEC CPU2006 benchmark

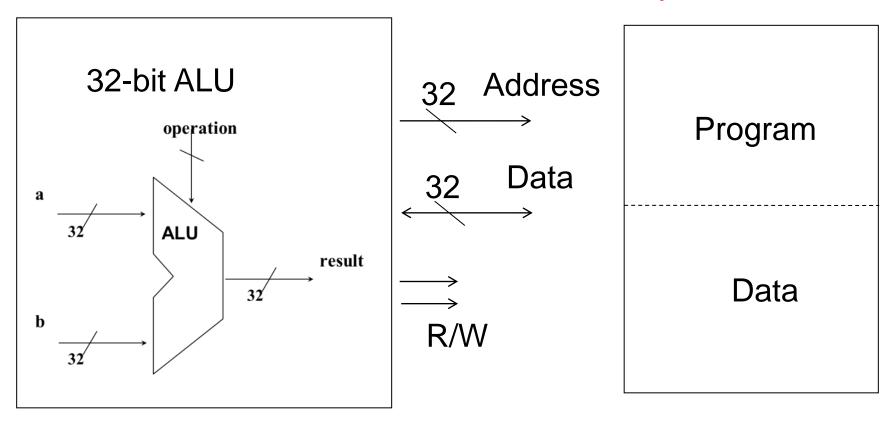
Instruction subset	Integer	Fl. pt.	
MIPS core	98%	31%	
MIPS arithmetic core	2%	66%	
Remaining MIPS-32	0%	3%	

- For the rest of book, focus on MIPS core (integer instruction set excluding multiply and divide)
  - To make the explanation of computer design easier

# 32-bit Computer

**CPU** 

Memory: 32-bit wide



I/O: Monitor/keyboard, LAN-Internet, ...