

1 Variable partition

Since we adopt outbound approach, for a line of input like “1 4 5”, we calculate the contribution from 1 to node 4 and 5 respectively and then aggregate the results.

Concretely, we use **localPageRankValues** to record the increment of pagerank value within each chunk and if the chunk has dangling node we use **danglingContrib** to store the dangling node contribution. Then, we aggregate the value from **localPageRankValues** to **globalPageRankValue** and dangling node contribution to **tempRecv**. For example, given the input as follows, we have two partitions. For the first partition, we use outbound algorithm to calculate the incremental value for 4 and 5, recorded in **localPageRankValues** of this partition; for the second partition, we store the incremental value separately in **localPageRankValues** of partition2. Let’s say we only have two partitions, then we can aggregate two **localPageRankValue** data structures and update the **globalPageRankValue** in process with rank 0.

Nodes ID	Ajacent nodes	
1	4 5	<partition1>
2	4	
3	4	
4	5	<partition2>
5	4	

Once we’ve updated the **globalPageRankValue**, we can use Eq. 1. And then we broadcast it to all the processes.

$$PR(u) = \frac{1-d}{N} + d * globalValue \quad (1)$$

To sum up the difference between sequential version and parallel version in terms of data flow, we list two versions as follows.

Sequential PageRank	Parallel Pagerank
Read the file and initialize adjMatrix	Read the file and initialize adjMatrix
Initialize the PageRankValue Hashmap	Initialize PageRankValue; partition variables
For each iteration:	For each iteration:
Initialize temprankValues with PageRankValue	MPI: Initialize chunkPageRankValueIncrem
For each line of input:	MPI:For each line within that partition/chunk:
Calculate the incremental value	Calculate the incremental value
Update the PageRankValue with the equation	MPI: Aggregate results into globalPageRankValue
Write the output file.	Calculate PageRankValue with the equation

2 How to Run and Results.

To execute the code, type following commands.

```
mpjrun.sh -np 4 MPIPageRank input.txt output.txt 10 .85
```

The result which looks like following is saved in a file with the name of arg2.

```

0 :- 0.01634534321875001
1 :- 0.38543613337511734
2 :- 0.3308768754288676
3 :- 0.030798070455108458
4 :- 0.09720673122275134
5 :- 0.030798070455108458
6 :- 0.021707755168859418
7 :- 0.021707755168859418
8 :- 0.021707755168859418
9 :- 0.021707755168859418
10 :- 0.021707755168859418

```

3 Data Structures and Data Flow.

We use two hash maps to store the adjacent nodes, i.e. `adjMatrix`. The “adjMatrix” hash map is pretty dummy as it basically copies the data from the input file. For example, for the input data,

Nodes ID	Adjacent nodes
0	
1	2
2	1
3	0 1
4	1 3 5
5	1 4
6	1 4
7	1 4
8	1 4
9	4
10	4

With these hash maps, interpreting the algorithm is be quite straightforward. For each of the popular nodes, we sum the value over all its contributors, as illustrated by the Eq. 2.

$$PR(u) = \frac{1-d}{N} + d * \sum_{v \in Set} \frac{PR(v)}{L(v)} \quad (2)$$

```

for (int i = 0; i < iterations; i++) {
    for (int j = 0; j < numofLine; j++)
        localPageRankValues[j] = 0.0;
    double danglingContrib = 0.0;
    Iterator it = adjMatrix.entrySet().iterator();
    while (it.hasNext()) {
        Map.Entry<Integer, List> pair = (Map.Entry) it.next();

        //If it is a dangling node,
        if (pair.getValue() == null)
            danglingContrib += globalPageRankValue[pair.getKey()]/numofLine;
        else{
            int current_size = pair.getValue().size();
            Iterator iter = pair.getValue().iterator();

```

```
        // For each outbound link for a node
        while (iter.hasNext()) {
            int node = Integer.parseInt(iter.next().toString());
            double temp = localPageRankValues[node];
            temp += globalPageRankValue[pair.getKey()] / current_size;
            localPageRankValues[node] = temp;
        }}
        double tempSend[] = new double[1];
        double tempRecv[] = new double[1];
        tempSend[0] = danglingContrib;
        MPI.COMM_WORLD.Allreduce(tempSend,0,tempRecv,0,1,MPI.DOUBLE,MPI.SUM);
        MPI.COMM_WORLD.Allreduce(localPageRankValues,0,globalPageRankValue,0,numofLine,MPI.DOUBLE);
        if(rank==0){
            for(int k=0;k<numofLine;k++) {
                globalPageRankValue[k] += tempRecv[0];
                globalPageRankValue[k] = df * globalPageRankValue[k] + (1 - df) * (1.0 / (double)
            }
        }
        MPI.COMM_WORLD.Bcast(globalPageRankValue, 0, numofLine, MPI.DOUBLE, 0);
    }
```

Acknowledgement