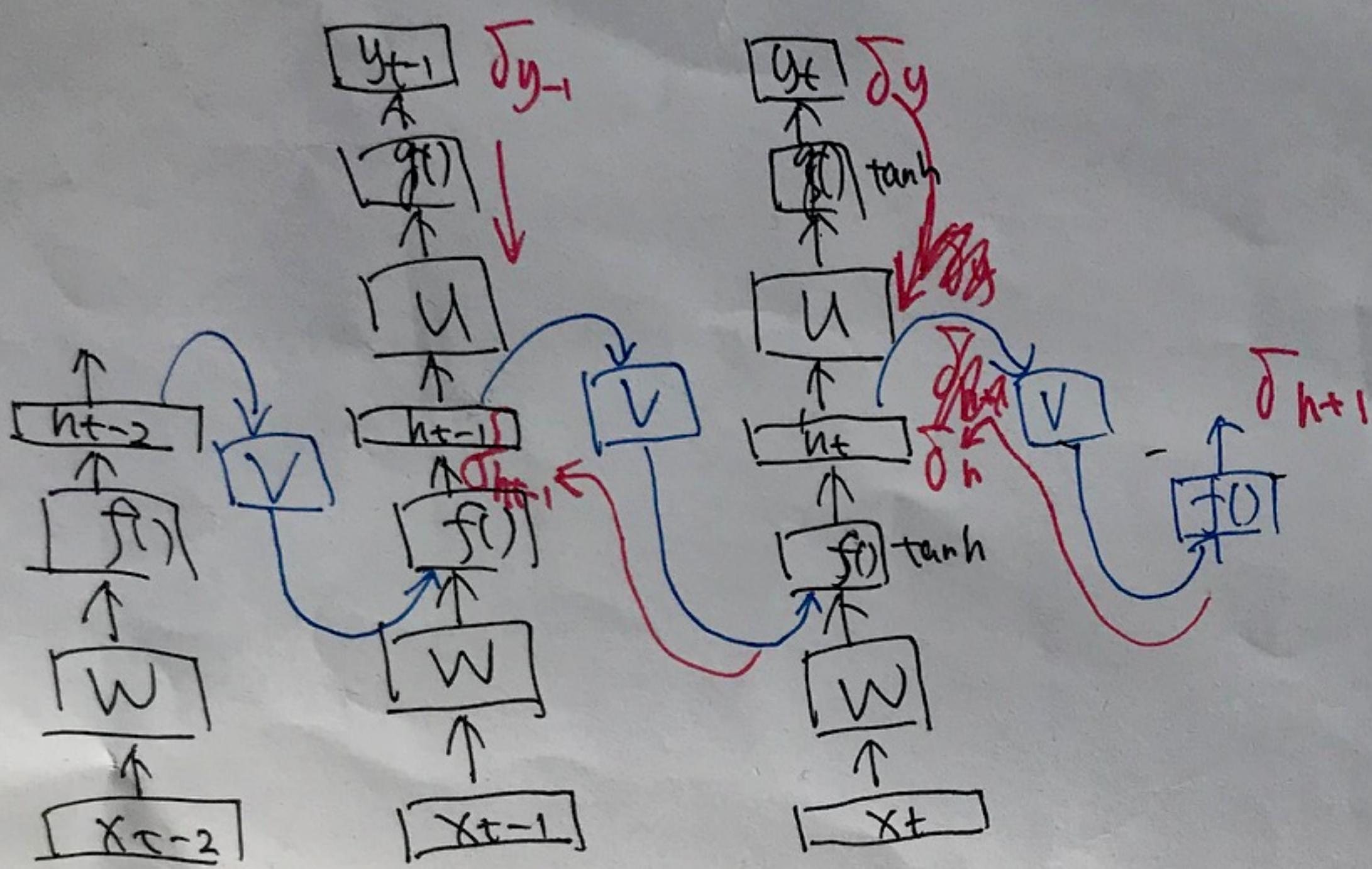


# RNN



$$h_t = f(Wx_t + Vh_{t-1} + b_h)$$

$$y_t = g(Uh_t + b_y)$$

$$\frac{\partial L}{\partial U} = \underbrace{\frac{\partial L}{\partial a_y} \cdot \frac{\partial a_y}{\partial z_y}}_{\text{error term}} \cdot \frac{\partial z_y}{\partial u} = \underbrace{L' g' h_t}_{\delta_y} \quad \begin{aligned} z_y &= Uh_t + b_y \\ a_y &= g(z) \end{aligned}$$

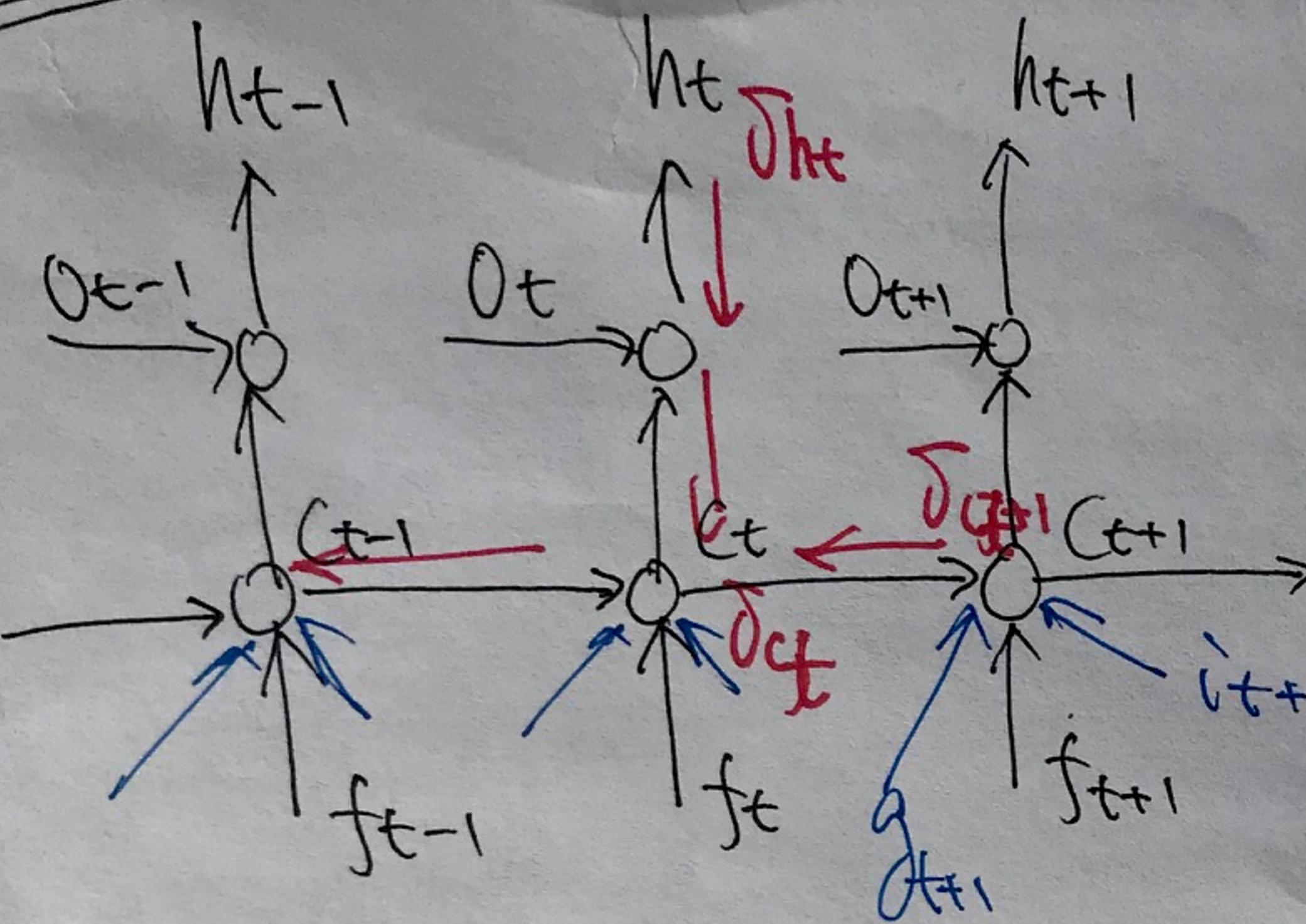
(same as FFNN)

$$\frac{\partial L}{\partial W} = \underbrace{\frac{\partial L}{\partial a_h} \cdot \frac{\partial a_h}{\partial z_h}}_{\text{error term}} \cdot \frac{\partial z_h}{\partial W} = \delta_h x_t \quad \begin{aligned} z_h &= Wx_t + Vh_{t-1} + b_h \\ a_h &= f(z) \end{aligned}$$

$$\frac{\partial L}{\partial V} = \underbrace{\frac{\partial L}{\partial a_h} \cdot \frac{\partial a_h}{\partial z_h}}_{\text{error term}} \cdot \frac{\partial z_h}{\partial V} = \delta_h h_{t-1}$$

$$\delta_h = g' u \delta_y + f' V \delta_{h+1}$$

# LSTM



$$\delta_{c_t} = \delta_{h_t} \odot \tanh'(c_t) \odot o_t + \delta_{c_{t+1}} \odot f_{t+1}$$

The gating mechanisms allow for gradient related to the memory cell  $c_t$  to stay high across long time ranges.