

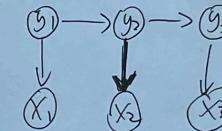
$y = \text{PRP } \text{NNS } \text{NNS } \text{NNS } \text{DT}$
 $x = \text{I } \text{love } \text{cats } \text{and } \text{dogs}$

$$\begin{aligned} \text{score}_4(\text{VB}) &= \max_{y_3} \left\{ \begin{array}{l} P(y_3 | y_3) P(x_4 | y_3) \\ P(\text{VB} | \text{DT}) P(\text{VB} | \text{NNS}) \cdot \text{score}_3(\text{VB}) \\ P(\text{VB} | \text{IN}) \cdot \text{score}_3(\text{IN}) \\ P(\text{PRP} | \text{NNS}) P(\text{PRP} | \text{IN}) \cdot \text{score}_3(\text{PRP}) \end{array} \right. \\ &\quad \left. \begin{array}{l} \text{and VB} \\ \text{and IN} \\ \text{and PRP} \end{array} \right\} \end{aligned}$$

HMM

$n=3$

x_1	x_2	x_3
I	love	cats
y_1	y_2	y_3



edges convey conditional independence
i.e. x_2 is conditionally independent of everything else given y_2

$x_2 \perp\!\!\!\perp y_1, x_1 | y_2$

$$\begin{aligned} P(x, y) &= P(x_1, x_2, x_3, y_1, y_2, y_3) = \frac{P(y_1 | x_1) P(y_2 | y_1, x_2) P(y_3 | y_2, x_3)}{P(x_1 | y_1) P(x_2 | y_1, x_1) P(x_3 | y_2, x_2)} \\ &= \frac{P(y_1) \cdot P(x_1 | y_1) \cdot P(y_2 | y_1, x_1) \cdot \overbrace{P(x_2 | y_1, x_1, y_2)}^{\perp\!\!\!\perp} \cdot \overbrace{P(y_3 | y_1, x_1, y_2, x_2)}^{\perp\!\!\!\perp}}{P(x_3 | y_1, x_1, y_2, x_2, y_3)} \cdot P(y_3 | y_2) \\ &\quad \swarrow P(x_3 | y_3) \end{aligned}$$

Dependency Grammars.

Syntactic structure = lexical items linked by binary asymmetrical relations called dependency

dependency type
 Head
 Dependent
 (modifier/object/complement)

Dynamic Programming

1, 1, 2, 3, 5, 8, 13, ...

Fibonacci Numbers: $F_1 = F_2 = 1; F_n = F_{n-1} + F_{n-2}$

• naive algorithm

$\text{fib}(n)$:

if $n \leq 2$, return 1
else return $\text{fib}(n-1) + \text{fib}(n-2)$.

$$\Rightarrow T(0) = T(1) = 1 \quad \text{constant}$$

$$T(n) = T(n-1) + T(n-2) + O(1) \approx c$$

$$\geq 2T(n-2) + O(1) \approx c$$

$$\geq 2(2T(n-4) + c) + c = 4T(n-4) + 3c$$

:

$$\geq 2^k T(n-2^k) + (2^k - 1)c$$

$$\text{when } n-2^k = 0 \Rightarrow k = n/2$$

$$T(n) \sim 2^{n/2} \cdot T(0)$$

• dynamic programming

Memo = {}

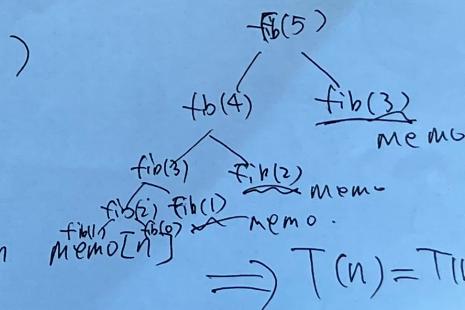
$\text{fib}(n)$:

if n in memo, return memo[n]
else: if $n \leq 2$: $f = 1$

else: $f = \text{fib}(n-1) + \text{fib}(n-2)$

memo[n] = f

return f.



$\overbrace{\text{memo}}^{\text{free lookup.}}$