

$$J_{MSE}(\theta) = \frac{1}{2n} \sum_{i=1}^n \left(y^{(i)} - \left(\sum_{k=1}^n w_{z,k} \cdot \sigma(w_{x,k} \cdot x^{(i)} + b_{x,k}) + b_z \right) \right)^2$$

$$\frac{\partial}{\partial w_{x,k}} = \frac{1}{n} \sum_{i=1}^n \left(y^{(i)} - \left(\sum_{k=1}^n w_{z,k} \cdot z + b_z \right) \cdot z \cdot (1-z) \cdot x^{(i)} \cdot w_{x,k} \right),$$

$$z = \sigma(w_{x,k} \cdot x^{(i)} + b_{x,k})$$

$$\frac{\partial}{\partial w_{z,k}} = \frac{1}{n} \sum_{i=1}^n \left(y^{(i)} - \left(\sum_{k=1}^n w_{z,k} \cdot z + b_z \right) \cdot z \right),$$

$$z = \sigma(w_{x,k} \cdot x^{(i)} + b_{x,k})$$

$$\frac{\partial}{\partial b_{x,k}} = \frac{1}{n} \sum_{i=1}^n \left(y^{(i)} - \left(\sum_{k=1}^n w_{z,k} \cdot z + b_z \right) \cdot z \cdot (1-z) \right),$$

$$z = \sigma(w_{x,k} \cdot x^{(i)} + b_{x,k})$$

$$\frac{\partial}{\partial b_z} = \frac{1}{n} \sum_{i=1}^n \left(y^{(i)} - \left(\sum_{k=1}^n w_{z,k} \cdot z + b_z \right) \cdot 1 \right),$$

$$z = \sigma(w_{x,k} \cdot x^{(i)} + b_{x,k})$$