

COMP 440 Homework 5

Tony Chen(xc12) and Adam Wang(sw33)

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1 Bayesian networks for astronomy

- Based on the above information, it can be seen that M_1 and N , M_2 and N , F_1 and N , F_2 and N are pairs that conditionally dependent on each other. So the first network is incorrect since F_1 and N , F_2 and N would become conditionally independent in that case. The second and the third network are correct.
- The second network is the best.
Because it represents a more realistic conditional dependency: each measurement depends on both the true number of stars and whether the focus is bad. Consequently, the second network is also simpler than the third network.

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$$\begin{aligned} P(M_1|N) &= P(M_1|N, F_1)P(F_1|N) + P(M_1|N, \neg F_1)P(\neg F_1|N) \\ &= P(M_1|N, F_1)P(F_1) + P(M_1|N, \neg F_1)P(\neg F_1) \end{aligned}$$

	$N = 1$	$N = 2$	$N = 3$
$M_1 = 0$	$f + e(1 - f)$	f	f
$M_1 = 1$	$(1 - 2e)(1 - f)$	$e(1 - f)$	0
$M_1 = 2$	$e(1 - f)$	$(1 - 2e)(1 - f)$	$e(1 - f)$
$M_1 = 3$	0	$e(1 - f)$	$(1 - 2e)(1 - f)$
$M_1 = 4$	0	0	$e(1 - f)$

- If we only consider the result $M_1 = 1$, then the possible numbers of N are $\{0, 1, 2, \geq 4\}$.
If we only consider the result $M_2 = 3$, then the possible numbers of N are $\{2, 3, 4, \geq 6\}$.
So the possible number of N is 2 or 4 or any integer greater than or equal to 6.
- We need to know that the event of a telescope having one-off measurement mistake is independent of that same telescope having a bad focus, and also that the two telescopes are independent of each other. The following analysis is made based on this independence assumption.
The only combination of events that can let $N = 2$ is when both telescopes had good focuses and M_1 counted one down while M_2 counted one up. So the probability of this happening is $(1 - f)^2 e^2$.
The only combination of events that can let $N = 4$ is when M_1 had a bad focus and M_2 had a good

focus but got the one-off mistake. So the probability of this happening is $f(1 - f)e$.

When $N \geq 4$, both telescopes had bad focuses. So the probability of this happening is f^2 .

Given the statement that e is small and f is much smaller, it is safe to assume that $0.5 > e \gg f$.

So $(1 - f)^2 e^2$ is the largest probability, which makes the most likely number of stars 2.

2 Gibbs Sampling

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3 Tracking cars by particle filtering

4 Bayesian networks for predicting the 2016 presidential elections