Introduction to Al

Assignment Project Exam Help

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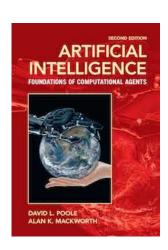
Outline

- Solving problems by search
- Basic search algorithms (uninformed blind search)
- Heuristic-based search algorithms (informed search) https://tutorcs.com
- Search for games (adversarial search)

Recommended reading: (most of) Chapters 3, 5



Additional reading:
Chapter 3
Section 11.2.2



Solving problems by search

- Problem solution can be abstracted as **path** from some (**start**) nodestone (**start**)
- Search algorithms to find (optimal) paths WeChat: cstutores

Route finding example

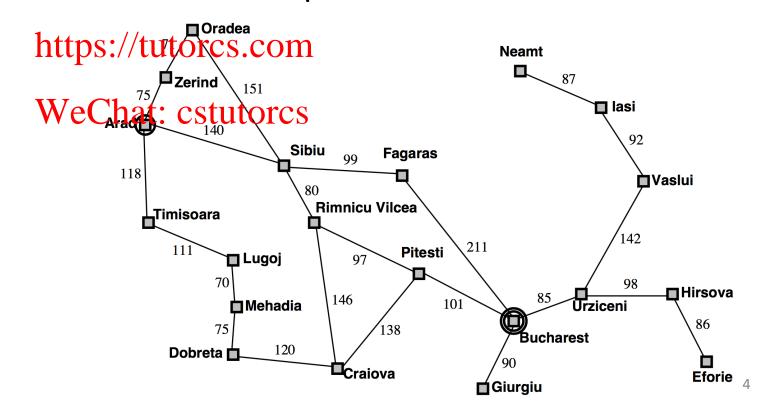
On holiday in Romania; today in Arad; flight leaves tomorrow from Bucharest

Start: Arad

Goal: Bucharest

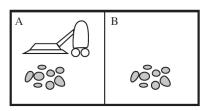
- Optimal path
 - shortest, or
 - quickest, or
 - cheapest

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Vacuum world example

The vacuum cleaner needs to remove all dirt from the room



• Start: A

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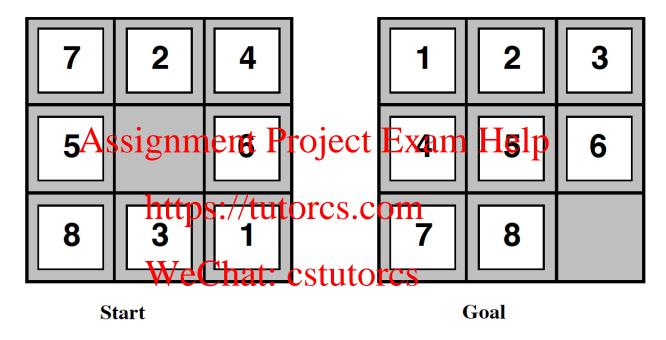
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• Goal: no dirt anywhere Hittps: Btutorcs.com

Optimal path

- shortest, or
- quickest, or
- cheapest

8-puzzle example



- Optimal path?
- Graph?

Which problems can be solved by (classical) search?

Environment is

- Observable Assignment Project Exam Help
 - Current state known
- Discrete

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- From each state finitelymany next states (by executing actions)
- Deterministic
 - Each action has exactly one outcome (next state)
- Known
 - Possible actions and next states for each state

Search problems – formally

- Initial state (start) e.g. In(Arad)
- Transition model between states (graph)

possibly given by successor function RESULT: States \times Actions \rightarrow States

Assignment Project Arady, Golfzerind) = In(Zerind)

- Goal test (set of goal states)://tutorcs.com
 - explicit

• implicit

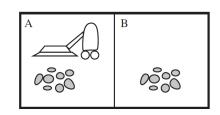
e.g. In(Bucharest), or WeChat: cstutorcs e.g. $\forall x \neg Dirt(x)$

• Path cost (additive = sum of positive step costs)

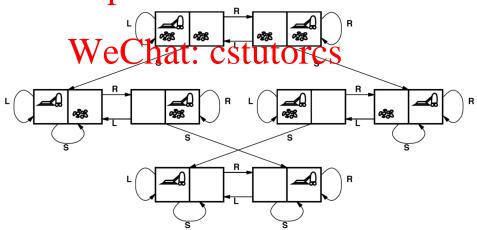
e.g. sum of distances, number of actions

Solution=path (sequence of actions) from the initial state to a goal state **Optimal solution**= solution with lowest path cost

Vacuum world example – formally

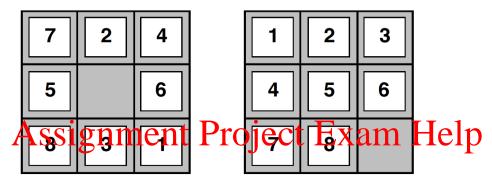


- Initial state= $In(A) \land Dirt(A) \land Dirt(B)$
- Goal test= $\{\neg Dirt(A) \land_{As}Digit(B)\}$ Project Exam Help
- RESULT $(In(A) \land Dirt(A) \land Dirt(B), S) = In(A) \land \neg Dirt(A) \land Dirt(B), etc$



Step cost=1, path cost=number of actions

8-puzzle example – formally



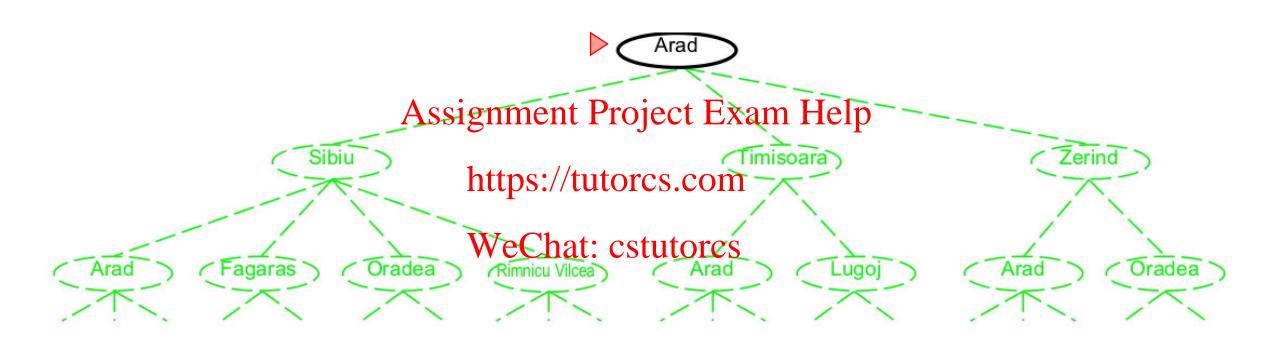
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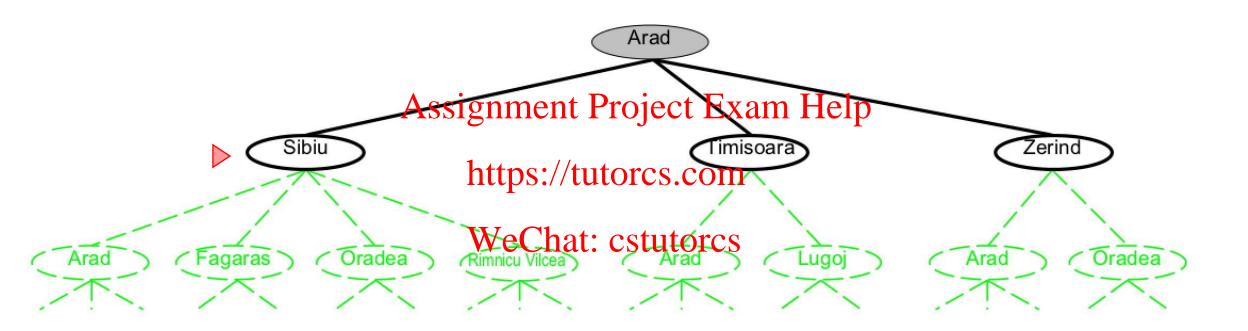
- Initial state = Start e.g. represented by integer locations of tiles
- Transition model between states?
 (successor function RESULT: States × Actions → States ?)
- Goal test ={Goal} e.g. represented by integer locations of tiles
- *Path cost=* number of actions

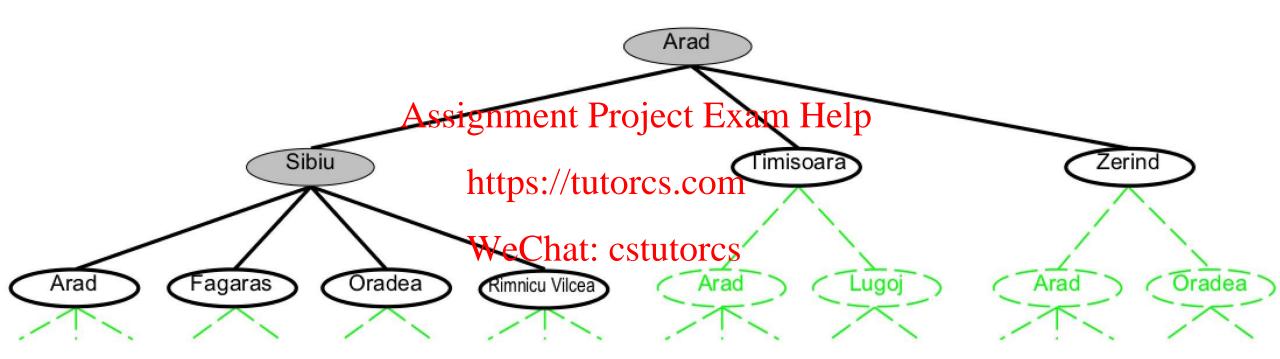
Search algorithms — basic idea

Generate a (search) tree:

- 1. Initialise the tree with the initial state as ropt (frontier)
- 2. Repeat
 - i. if the frontier of the tree is empty then return fail
 - ii. choose and remove weathodeck from the frontier
 - iii. if L is a goal state (in the goal test) then return corresponding solution
 - iv. expand L, adding the resulting nodes to the frontier







Search algorithms – basic idea with loop checking

Generate a (search) tree:

- 1. Initialise the tree with the initial state as rootelp
- 2. Repeat
 - https://tutorcs.com i. if the frontier of the tree is empty then return fail
 - ii. choose and remove weathande ufrem the frontier
 - iii. if <u>L is a goal state</u> (in the goal test) then return corresponding solution*add L to the "explored set"
 - iv. <u>expand L</u>, adding the resulting nodes to the frontier*only if not in the frontier or the "explored set" already

^{*} Additions to avoid loops

Search algorithms - concretely

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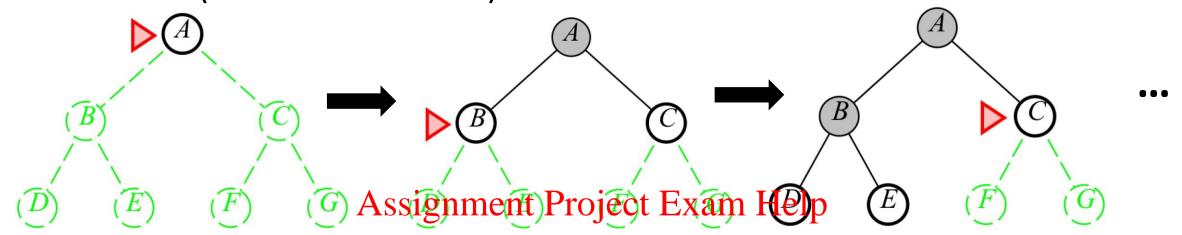
Definite choose

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Uninformed/blind search

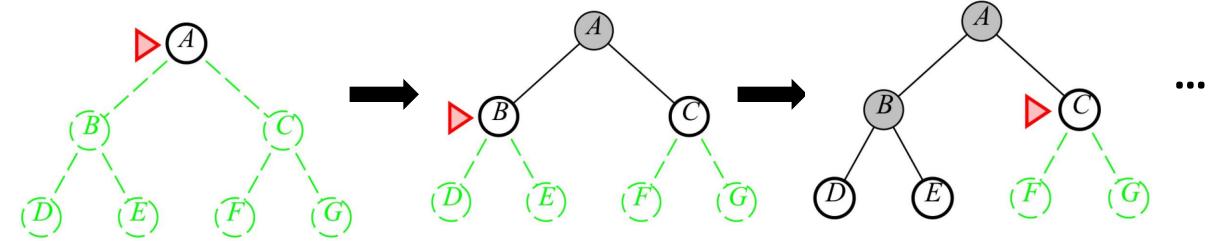
- Breadth-first search
- choose (a) shallowest (closest to root) unexpanded node
 Uniform-cost search ssignment Project Exam Help
 - choose unexpanded node with the west path fost
- Depth-first search
 - choose deepest (farthest from the state Punexpanded node.
- Depth-limited search
 - depth-first search with given depth limit ℓ (nodes of depth ℓ have no children)
- Iterative deepening search
 - depth-limited search of increasing ℓ

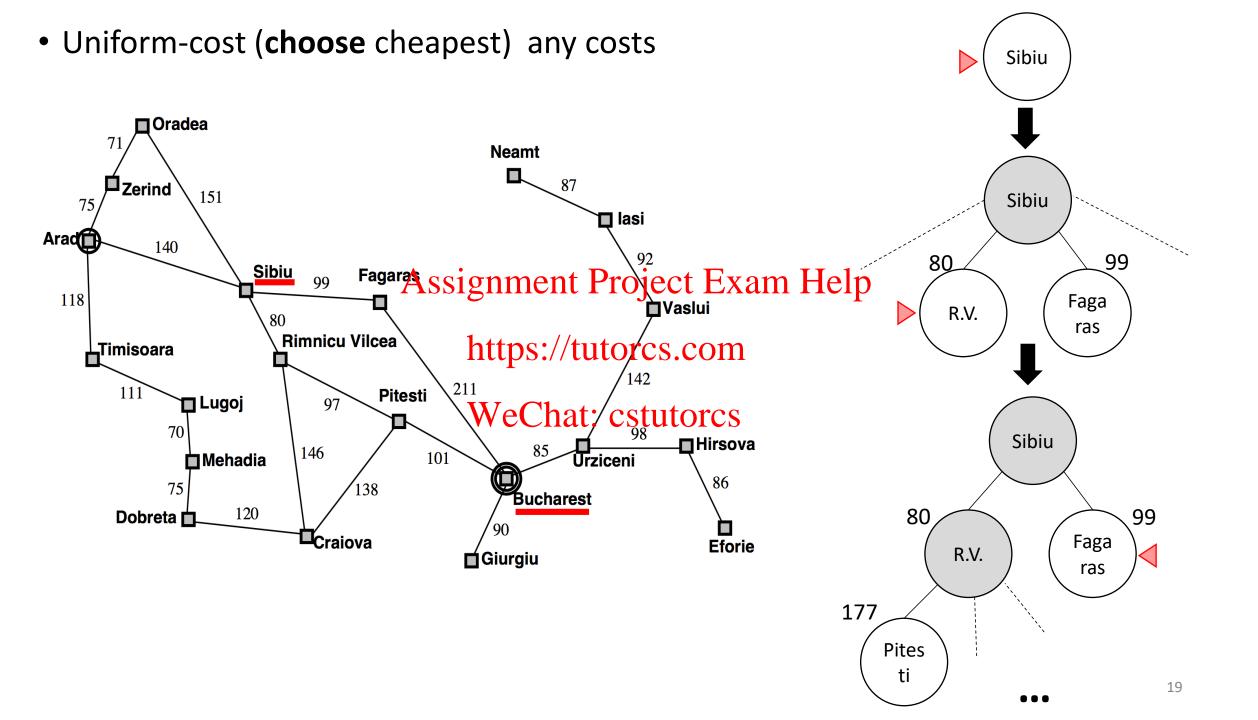
• Breadth-first (choose shallowest)



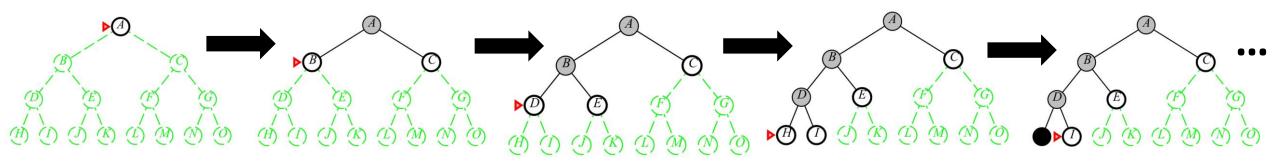
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• Uniform-cost (choose cheape) elleasts equales Breadth-first

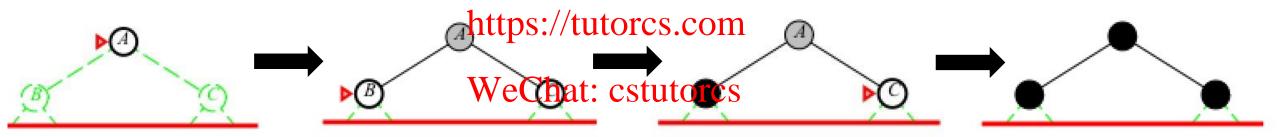




• Depth-first (choose deepest)



Depth-limited (½=1) Assignment Project Exam Help



Iterative deepening

Depth-limited ($\ell=0$) \longrightarrow Depth-limited ($\ell=1$) \longrightarrow Depth-limited ($\ell=2$) •••

Uninformed search - Variants

- Backtracking search variant of depth-first search

 - Only one (successor) node generated when expanded.
 Each (partially expanded) successor node remembers which node to generate next

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- Bi-directional search WeChat: cstutorcs
 - Two simultaneous searches (from start to goal and from goal to start)
 - Succeeds when (if) the frontiers of the two searches intersect

Properties

- completeness—does the algorithm always find a solution if one exists?
 solution if one exists?
- time complexity—number of nodes generated/expanded futures://tutorcs.com
- space complexity—Maximum from the memory
- optimality—does the algorithm always find an optimal (least-cost) solution?

Properties of uninformed search (with loop-checking)

Criterion	Breadth-first	Uniform-cost	Depth-first	Backtracking	Depth-limited	Iterative deepening	Bidirectional (breadth-first)
Complete?	Yes*	Yes*o Assi	gynnent P	r oje ct Exa	n Help	Yes*	Yes*
Time	O(b ^d)	O(b ^{d+1}) ●	https://tut	orcs.com	s(l)	O(b ^d)	O(b ^{d/2})
Space	O(b ^d)	O(b ^{d+1}) ●	O(bm)	O(m)	O(bl)	O(bd)	O(b ^{d/2})
Optimal?	Yes●	Yes	WeChat:	estutores	No	Yes●	Yes●

- * **b** is finite
- step cost is constant
- o step cost is >0
- † s is finite

b—maximum branching factor of the search tree (may be ∞)

d–depth of the optimal (least-cost) solution

m–maximum depth of the state space (may be ∞)

s–overall size of the state space

s(\ell) –size of the state space till depth ℓ

Properties of uninformed search (without loop-checking)

Criterion	Breadth-first	Uniform-cost	Depth-first	Backtracking	Depth-limited	Iterative deepening	Bi-directional (breadth-first)
Complete?	Yes*	Yes*o Assi	grament P	rwject Exa	n Help	Yes*	Yes*
Time	O(b ^d)	O(b ^{d+1}) ●	https://tut	O(b ^m) Orcs.com	O(b ^ℓ)	O(b ^d)	O(b ^{d/2})
Space	O(b ^d)	O(b ^{d+1}) ●	O(bm)	O(m)	O(bl)	O(bd)	O(b ^{d/2})
Optimal?	Yes●	Yes	WeChat:	estutores	No	Yes●	Yes●

- * **b** is finite
- step cost is constant
- o step cost is >0

b—maximum branching factor of the search tree (may be ∞)

d—depth of the optimal (least-cost) solution

m–maximum depth of the state space (may be ∞)

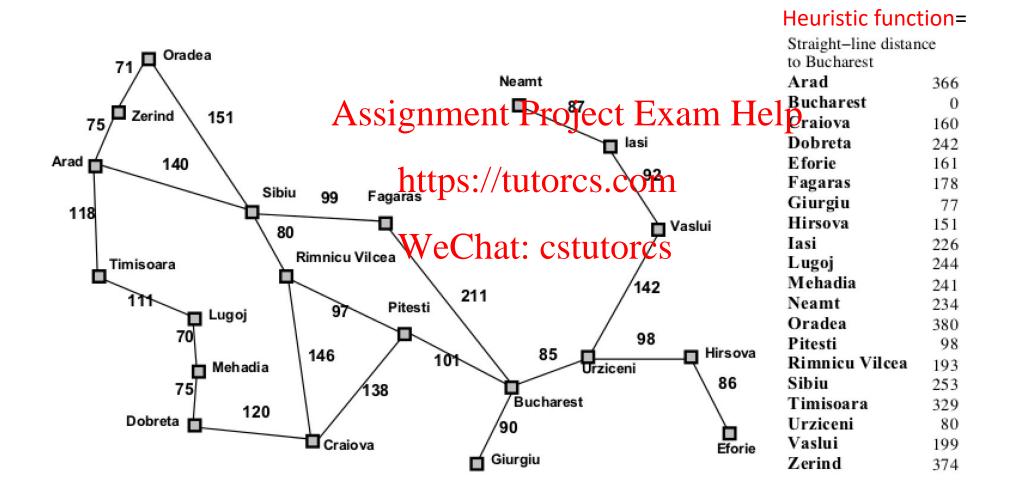
Informed (heuristic-based) search

Use a cost estimate (of optimal path to goal) to choose node with the least restimate depath costelp

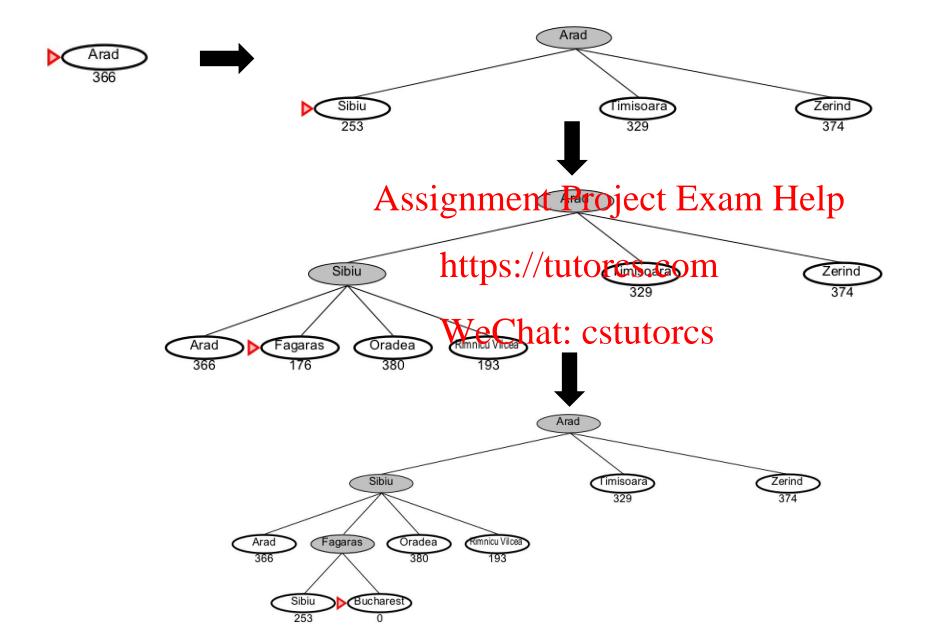
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- Greedy-best-first search WeChat: cstutorcs
 - cost estimate=heuristic function(node to goal)
- A* search
 - cost estimate=actual cost(to node)+heuristic function(node-to-goal)

Heuristic function: route finding example



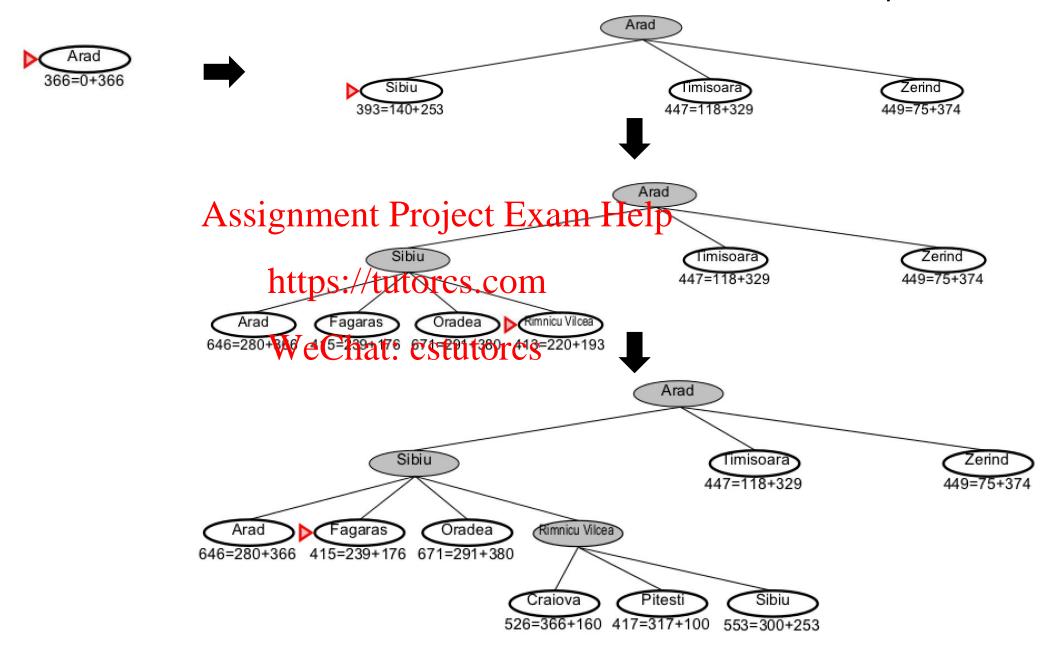
• Greedy-best-first (choose node with lowest value of heuristic function)

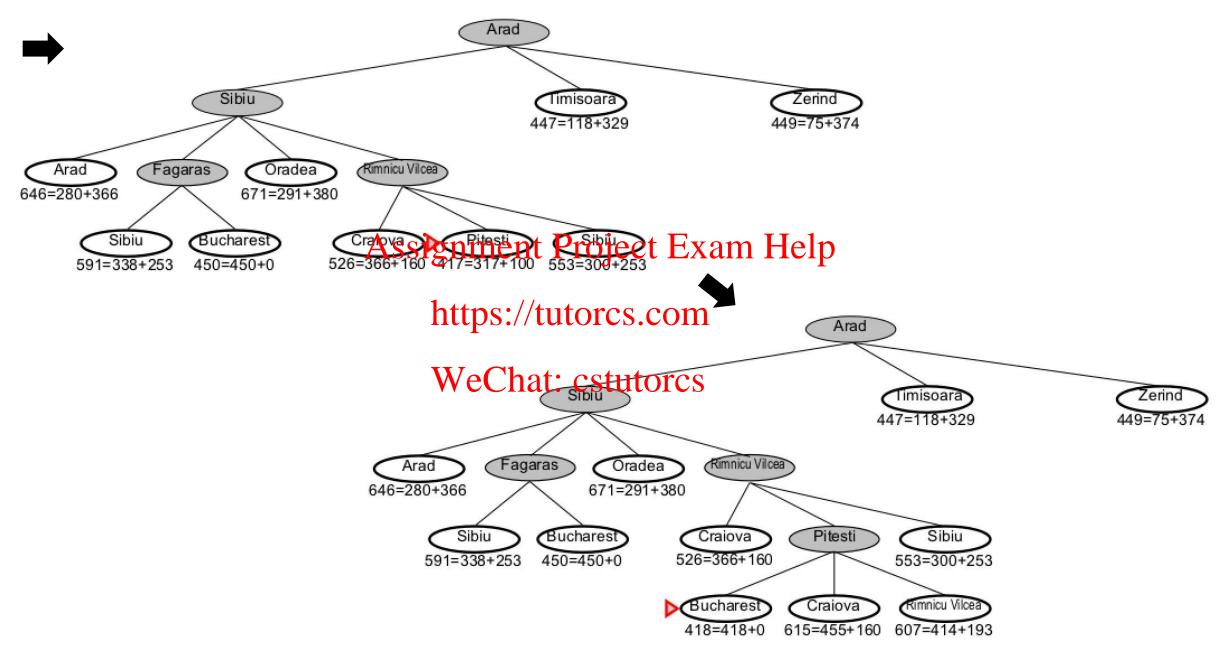


Straight-line distan	ce
to Bucharest	
Arad	366
Bucharest	0
Craiova	160
Dobreta	242
Eforie	161
Fagaras	178
Giurgiu	77
Hirsova	151
Iasi	226
Lugoj	244
Mehadia	241
Neamt	234
Oradea	380
Pitesti	98
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374

Straight line dictance

• A* (choose node with lowest value of actual cost+heuristic function)





Properties of heuristic functions

For n any node, let

g(n,m) be the actual cost of reaching node m from n

h(n) be the heuristic function applied to n (assume $h(n) \ge 0$ -- so that h(goal) = 0)

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Admissible: it never overestimates the actual cost (to goal) - e.g. straight-line distance

- Admissible: it never overestimates the actual cost (to goal) e.g. straight-line distance $h(n) \leq g(n, mgoal)$ for m_g at the m distance m depends a goal reachable from m
- Consistent/Monotonic: it never overestimates the actual cost to any successor node+the heuristic function applied to that node e.g. straight-line distance

 $h(n) \le g(n, n') + h(n')$ for n' any successor of n

Consistent/Monotonic → Admissible

Properties of informed search (with or without loop-checking)

Criterion	Greedy (with)	Greedy (without)	A* (with)	A* (without)		
Complete?	Yes† Assignmen	No nt Project Exam	Yes*o Heln	Yes*o		
Optimal?	No	No	Yes ◊	Yes ‡		
https://tutorcs.com						

† **s** is finite

* **b** is finite

o step cost is >0

♦ h consistent/monotonic

‡ **h** admissible

WeChat: cstudyoralsize of the state space

b-maximum branching factor of the search tree (may be ∞)

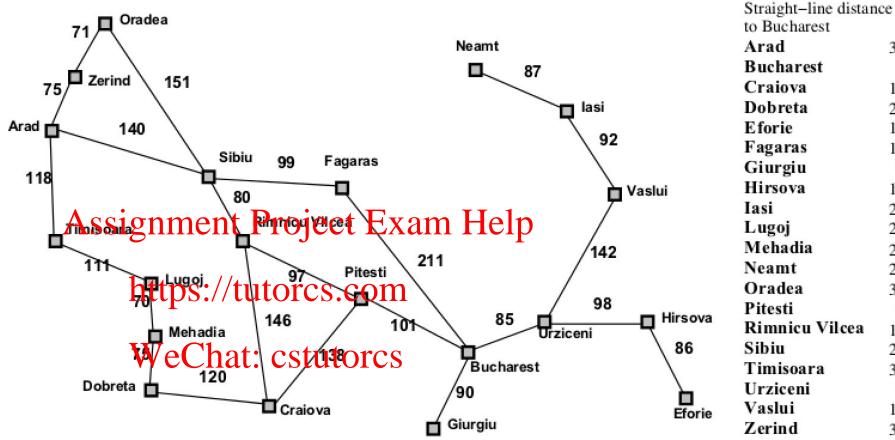
m–maximum depth of the state space (may be ∞)

h–heuristic function

A* is **optimally efficient** (no other optimal search algorithm is guaranteed to expand fewer nodes) but it often runs out of **space**

 Greedy best-first search not optimal:

Path via Sibiu-Fagaras is (32 km) longer than path through RV-Pitesti



to Bucharest Arad 366 Bucharest Craiova 160 Dobreta 242 E forie 161 Fagaras 178 Giurgiu 77 Hirsova 151 Iasi 226 Lugoj 244 Mehadia 241 Neamt 234 Oradea 380 Pitesti 98 Rimnicu Vilcea 193 Sibiu 253 Timisoara 329 Urziceni 80 Vaslui 199 Zerind 374

Greedy best-first search without loop checking is not complete: $lasi \rightarrow Neamt \rightarrow lasi \rightarrow Neamt \rightarrow ...$

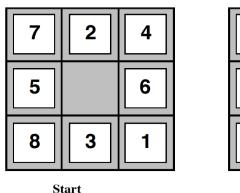
How to identify admissible/consistent heuristics?

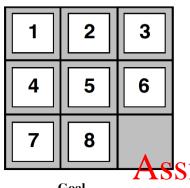
• Identify a relaxed version of the search problem (with a larger graph – with more edges).com

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 Use cost of optimal solutions for the relaxed problem as (admissible/consistent) heuristics for the original search problem

8-puzzle example – relaxed problems





A tile can move from square A to square B if

- A is horizontally/vertically adjacent to B, and
- B is blank

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Relaxed problems:

- https://tutorcs.com

 A tile can move from A to B if A is horizontally/vertically adjacent to B
- A tile can move from A to B Meichlankcstutorcs
- A tile can move from (any) A to (any) B

Heuristics:

- h(n)=Manhattan distance (sum of the distances of tiles as in n from their goal positions)
- h(n)= number of switches (blank-non-blank tile) to obtain goal from n
- h(n) = number of misplaced tiles in n wrt the goal

Heuristic search – today (example-non-examinable)



Artificial Intelligence
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Artificial Intelligence

In Predations ententions comnote to users

WeChat: cstutorcs Star-Topology Decoupled State Space Search



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https://doi.org/10.1016/j.artint.2017.12.004

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Omitted

- Local search
 - Genetic algorithms
 Simulated annealing

 Assignment Project Exam Help
- Non-deterministic, partially observable mor unknown environments

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Adversarial search

- Competitive environment
 - opponents with sconflicting goals am Help
- "Unpredictable" apponentes.com
 - solution is a strategy (=specifying a move for every possible opponent's move/sequence of moves)
- Hard to solve, time limits
 - must approximate

Types of games

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perfect information

imperfect information

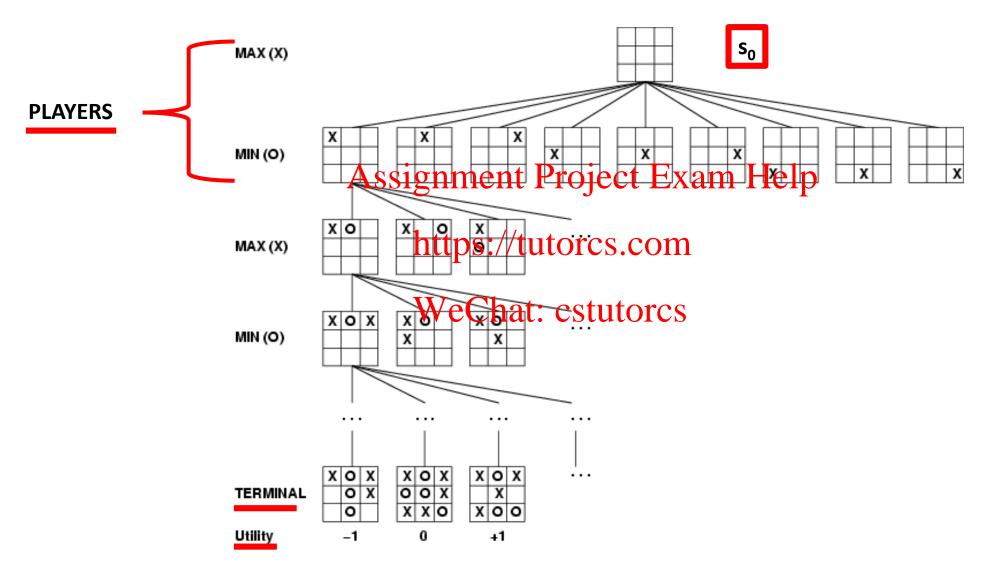
https://tutorcs.com go. othello WeChat: cstutorcs	backgammon monopoly
battleships,	bridge, poker, scrabble
blind tictactoe	nuclear war

Adversarial search problems – formally

Two-player, zero-sum (constant-sum) games

- s₀: initial state Assignment Project Exam Help
- PLAYER(s): determines which player (of two) moves in a state https://tutorcs.com
- ACTIONS(s): returns the set of legal moves in a state
- RESULT(s,a): returns the state resulting from a move in a state
- TERMINAL(s): is true if the game has ended, false otherwise.
- UTILITY(s,p): returns 1 (win), -1 (lose), 0(draw)
 or 1 (win), 0 (lose), 1/2 (draw)

Example of two-player, zero-sum game: tic-tac-toe



Perfect play for deterministic, perfect-info games

- Minimax strategy
- •α-β pruning Assignment Project Exam Help

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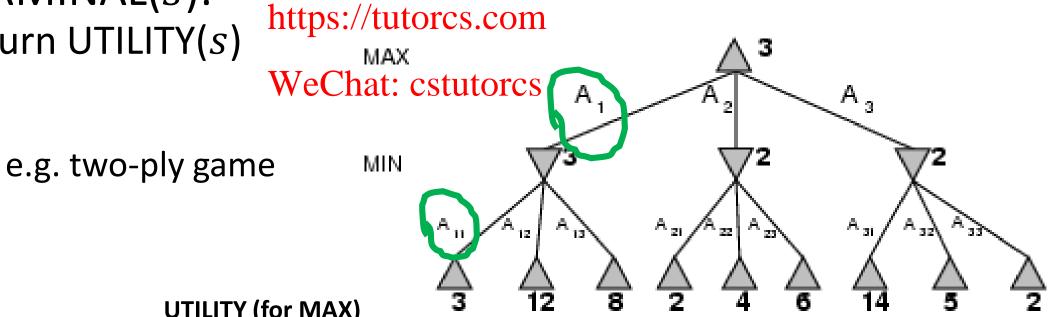
MINIMAX(s) – best payoff against best play

for $\neg TERMINAL(s)$:

- if PLAYER(s)=MAX: return max_{actions a} MINIMAX(RESULT(s,a))
- if PLAYER(s) = MAN: return minertides am Hall MAX(RESULT(s,a))

for TERMINAL(s):

return UTILITY(s)



UTILITY (for MAX)

Properties of minimax



* If search tree finite

b—maximum branching factor of the search tree (may be ∞) **m**—maximum depth of the state space (may be ∞)

For chess, b ≈ 35, m ≈100 for "reasonable" games: not feasible

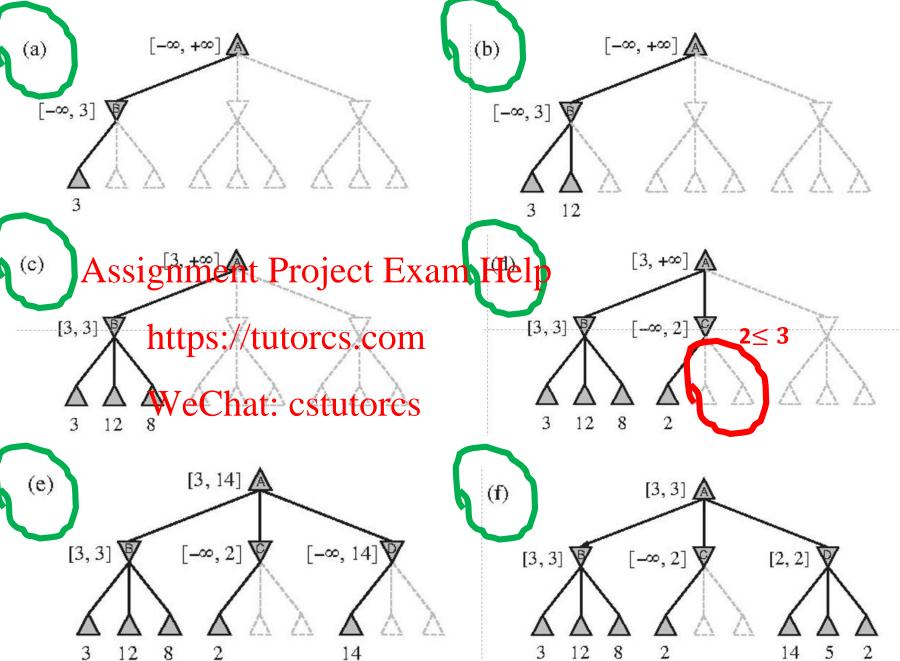
α-β pruning

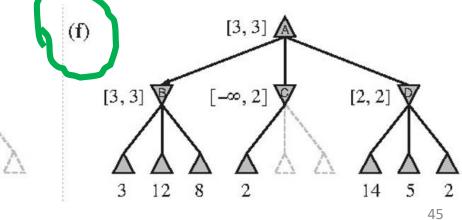
- α minimum value that MAX is guaranteed to achieve so far (in some state)
- β maximum value that MAX is guaranteed to achieve so far (in some state)

```
Determine for initial state size of the state of the stat
                                                                                                                                                                                            https://tutorcs.comin-value(s,\alpha,\beta):
    max-value(s,\alpha,\beta):
• if TERMINAL(s) then
                                                                                                                                                                                            WeChat: cstutorsin-value
              return UTILITY(s)
           else, starting from v = -\infty,
            for each action a:
                                       let v=\max(v,\min-value(RESULT(s,a),\alpha,\beta))
                                                                                                                                                                                                                                                                                                ...min(v,max-value(RESULT(s,a),\alpha,\beta))
                                                                                                                                                                                                                                                                                                If(v≤α then return v
                                   If v \ge \beta) then return v
                                    else let \alpha=\max(\alpha,v)
                                                                                                                                                                                                                                                                                                else let \beta = \min(\beta, v)
              return v
```

α - β pruning

 $[\alpha,\beta]$





Properties of α - β pruning



* If search tree finite

□ if successors are examined best-first

b—maximum branching factor of the search tree (may be ∞) **m**—maximum depth of the state space (may be ∞)

For chess, b ≈ 35, m ≈100 for "reasonable" games: still slow

Omitted

Resource limits:

- Cutoff-Test instead of TERMINAL
- Evaluation instead of Project Exam Help
 - for chess weighted sum of features (e.g. number of white queens-number of black queens....)

Other types of games WeChat: cstutorcs

	deterministic	chance
perfect information	chess, checkers, go, othello	backgammon monopoly
imperfect information	battleships, blind tictactoe	bridge, poker, scrabble nuclear war

Search&Games – today (example – non-examinable)



Article

https://tutorcs.com

Mastering the game of Go without human weChat: cstutorcs knowledge

David Silver , Julian Schrittwieser, Karen Simonyan, Ioannis Antonoglou, Aja Huang, Arthur Guez, Thomas Hubert, Lucas Baker, Matthew Lai, Adrian Bolton, Yutian Chen, Timothy Lillicrap, Fan Hui, Laurent Sifre, George van den Driessche, Thore Graepel & Demis Hassabis

Nature 550, 354-359 (19 October 2017)

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Search - summary

- Formulation of search problems
- Uninformed search algorithms: preadth-first, uniform-cost, depth-first, limited-depth, iterative deepening, backtracking, bidirectional
- Informed (heuristic-based) search algorithms: greedy-best-first, A*, admissible and consistent/monotonic heuristic functions
- Adversarial search: minimax, α - β pruning
- Properties of search algorithms: completeness, optimality, time and space complexity