# Notes for Lecture 23 (Fall 2022 week 11, part 1): Modes in Prolog

Jana Dunfield

November 21, 2022

The code for this lecture is in lec23.pl.

These notes introduce one new topic, modes, and one specific feature of Prolog, printing.

### 1 Modes

By itself, Prolog code doesn't do anything. For something to happen, we have to run queries.

In Haskell, like most languages, a function is a machine that takes input (one or more arguments) and returns output. Functions cannot be run backwards; if you want the inverse of the function

```
add1 :: Assignment Project Exam Help

you need to write another function:
subtract1 x = x https://tutorcs.com
```

As we'll see later, not all arithmetic functions have inverses, and the inverse *map* is not always easy to define, so let's that a somewhat easier situation: a function whose input and output are elements of a Haskell data type. The control of t

```
data Colour = Orange
            Rose
            | Violet
            | White
            | Grey
            | Black
            deriving (Show, Eq)
cycle :: Colour -> Colour
cycle Orange = Rose
cycle Rose = Violet
cycle Violet = Orange
cycle _
           = Grey
We might try to translate this into Prolog as:
cycle(orange, rose).
cycle(rose,
              violet).
cycle(violet, orange).
cycle(_,
              grey).
```

This behaves the same as the Haskell function for *some* queries, but not all. If all our queries look like

```
?- cycle( some-colour, Result).
```

where some-colour is a specific colour like orange or black, and if we stop at the first solution (by typing a period), we get the same answers we would get in Haskell:

In the first query, cycle(rose, Result), Prolog waited for us to tell it whether to look for more solutions: it had already noticed that the last clause cycle(\_, grey) matched.

In the second query, cycle(grey, Result), Prolog finished by itself because only one clause matched (the last one: cycle(\_, grey)).

If we type a semicolon instead, we get two results, and the second is he consistent with the Haskell code (eyele Rose returns violet, not crey):

```
?- cycle(rose, Result).

Result = violet https://turtorcs.com

Result = grev.
```

We have two approaches to solving this problem.

The first approach the first property of the Haskell values. Since the wildcard clause in the Haskell version of cycle comes after the Orange, Rose, and Violet patterns, the Haskell clause will match White, Grey, and Black. That leads to the Prolog code

```
cycle(orange, rose).
cycle(rose, violet).
cycle(violet, orange).
cycle(white, grey).
cycle(grey, grey).
cycle(black, grey).
```

Now, Prolog will give only one answer—the same one Haskell would have given—for queries like cycle(rose, Result).

The second approach is to use cuts, which we will not discuss until Week 12.

For queries like ?- cycle(X, grey). Prolog will give three solutions, corresponding to the three possible inputs to the Haskell function that return Grey. Technically, the Haskell function cycle does not have an inverse function because there is no unique x such that cycle x == Grey, but it has an inverse map that "returns" any of White, Grey, Black.

If we give the Prolog query

```
?- cycle(X, grey).
```

and ask for multiple solutions, we get the three solutions

```
X = white % type ;
X = grey % type ;
X = black.
```

#### 1.1 Input and output modes

Queries involving the predicate cycle work regardless of which arguments to cycle are "concrete" (Prolog terms like orange and grey), and which arguments are "unknown" (Prolog variables like X):

```
?- cycle(orange, rose).
                          % Both arguments concrete; in Haskell:
                                                     cycle Orange ==
                                                                     Rose
true.
?- cycle(orange, grey).
                          % Both arguments concrete; in Haskell:
                                                     cycle Orange
                                                                       Grey
?- cycle(orange, Z).
                          % Second argument unknown; in Haskell:
                                                     cycle Orange
                https://tutorcs.com
Z = rose.
?- cycle(X, orange).
                          % First argument unknown; Haskell can't do this
X = violet.
                          % First argument unknown; Haskell can't do this
X = white
X = grey
X = black.
?- cycle(X, Y).
                          % Both arguments unknown; Haskell can't do this
X = orange,
Y = rose
X = rose,
Y = violet
X = violet,
Y = orange
X = white,
Y = grey
X = Y, Y = grey
X = black,
Y = grey.
?-
```

When an argument is concrete, it is in *input mode*. When an argument is unknown (a variable), it is in *output mode*. Queries like

```
?- cycle(orange, Z).
Z = rose.
```

are the only kind that Haskell can handle directly, because the first argument orange is an input, and the second argument Z is an output. That is what the Haskell function does.

All argument "modings" (a moding is a sequence of modes, like "first argument input, second argument output") work for cycle, but that does not hold for all Prolog predicates.

For example, our factorial function only works when the first argument is input.

```
/*
 Factorial function
 ?- fact(5, R).
 R = 120
 false.
           ssignment Project Exam Help
fact(N, R) := N >
           NMin attps://tutorcs.com
           fact(NMinus1, Result).
           R is N * Result.
                WeChat: cstutorcs
 ERROR: Arguments are not sufficiently instantiated
 ERROR: In:
 ERROR:
          [9] _2864>0
 ERROR:
          [8] fact(_2890,120) at ...
          [7] <user>
 ERROR:
*/
```

On the other hand, the built-in append predicate works for all modings, though it isn't particularly useful when all three arguments are outputs.

## 2 Printing

In Prolog, unlike Haskell, it is pretty easy to print messages while queries are being run.

The most versatile way to print is the built-in predicate format, which is basically similar to printf in C, and to the % operator in Python.

Here is an example from lec24.pl:

```
get2( Xs, (Y1, Y2)) :-
   print("a string~n"),
   print(Xs),
```

```
member(Y1, Xs),
format("called member, Y1 = ~p...~n", Y1),
member(Y2, Xs),
format("called member again, Y1 = ~p, Y2 = ~p...~n", [Y1, Y2]).
```

In general, format takes two arguments.

The first argument to format is a string, with ~p denoting things we want to print (similar to \%s in some languages) and ~n denoting a line break.

The second argument to format is a list of the things we want to print. (If there is only one thing to print, then we can give that thing, as above where we passed Y1 as the second argument.)

(The print predicate also prints, but it can only print one thing, either a fixed string like "a string"n" or a Prolog thing like Xs.)

#### 3 Arithmetic

It makes sense that the factorial predicate fails for "interesting" modes. A query like

?- fact(X, Y).

Assignment Project Exam Help
says "come up with some X and Y such that fact(X) = Y." Prolog does not have types, so we
have to look at how fact is defined. But fact is defined using arithmetic operations that only work

"forwards": if X is known, we can compute Y, but not backwards.

Some functions do not law Siverses. Use which halve that divides by 2 (rounding down) does not have an inverse:

```
halve :: Integer That: cstutorcs

double :: Integer -> Integer

double x = x * 2
```

The function double is not an inverse. If we have a function f and its inverse  $f^{-1}$ , then for all x, we should have  $f^{-1}(f(x)) = x$ . The function halve 21 returns 10, but double 10 returns 20.

```
f 	 (f 	 (x)) = x
double(halve(21)) = 20
```

If we want to "run halve backwards" on 10, we should really get both 20 and 21. That would require running arithmetic operations backwards, and in general, doing algebra to solve equations. This is more than Prolog can handle (which seems fair, it's not Matlab or Mathematica).

Thus, when we translate Haskell functions involving arithmetic, our translations will pretty much always work only in one mode.

# 4 On a quiz

When asking you to write a Prolog predicate from an English specification, I try to be clear about which modes the Prolog predicate needs to handle.

If the Prolog predicate needs to do arithmetic, there will usually just be one "moding", like "first argument input, second argument input, third argument output".

When translating a Haskell function to a Prolog predicate, you *never* need to handle modes that are "more unknown" than what the Haskell function can handle.

# Assignment Project Exam Help

https://tutorcs.com

WeChat: cstutorcs