Week 1 part 2: Stepping; Haskell intro

Jana Dunfield

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References to "Thompson" are to Haskell: The Craft of Functional Programming, 3rd ed.

1 Functional programming in industry

- http://cufp.org/2015/fighting-spam-with-haskell-at-facebook.html (Haskell at Facebook)
- http://cufp.org/2016/yaron-minsky-keynote.html (OCaml at Jane Street, a financial services firm)
- http://cufp.org/2017/using-functional-programming-to-accelerate-translational-research-at-pfizer.html (functional programming for pharmaceuticals)

An (argually Silgon program in Planguage Cutt, Esscalish stantage of Firefox—for both reliability and performance reasons (functional programs are often easier to parallelize).

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2 Stepping

The behaviour of Haskell *expressions*, such as 2 + 2 and $(\x -> x + 1)$ 3, can be predicted by a process of stepping. Thompson calls stepping "calculation"; another name is "tracing".

For very simple examples, stepping is hard to distinguish from equality in algebra:

(Thompson uses a squiggly arrow \rightsquigarrow instead of \Rightarrow .) If you are taking notes on a laptop, I suggest typing ==> to avoid confusion with =>, which is part of Haskell's type syntax.

For slightly larger examples, however, stepping distinguishes itself from equality—we do only *one* operation per step:

$$(2+2)+(3+4) \qquad \qquad (2+2)+(3+4) \\ = 11 \qquad \qquad \Rightarrow \ 4+(3+4) \qquad \text{by arithmetic} \\ \Rightarrow \ 4+7 \qquad \qquad \text{by arithmetic} \\ \Rightarrow \ 11 \qquad \qquad \text{by arithmetic}$$

And wherea Analysing a quality have parented a result. The Haskell expression 11 will not step "backwards" to 4+7.

Adding integers may seem simple but it is not always clear how stepping should work. How should 1 / 3 step? In a previous iteration of 360, 4 received four suggestions:

1.
$$\Rightarrow We Charitmetic stutores$$

- 2. (1 / 3)
- 3. (1 / 3)
 - \Rightarrow 1 by arithmetic
- 4. (1 / 3) $\Rightarrow \frac{1}{3}$ by arithmetic

All of these are reasonable choices, and at least three of them are found in actual programming languages; the operator / exists in most languages, but they don't agree on its meaning (its *semantics*).

- Suggestion 1 interprets / as integer division, rounding down. C, Java and Python interpret / this way.
 - (In algorithms textbooks, this would be written $\lfloor 1/3 \rfloor$: mathematicians usually assume / means division on real numbers, so they have to "floor" or "truncate" the result $\frac{1}{3}$ by applying the operation $|\dots|$.)
- Suggestion 2 interprets / as real (floating-point) division. Haskell interprets / this way.

- Suggestion 3 interprets / as integer division, rounding up (like \[\frac{1}{3} \]). I don't know of any language that does this, but there probably are some.
- Suggestion 4 interprets / as exact division or rational division (1/3 being the ratio of two integers). The Racket language interprets / this way (though in Racket, you write (/ 1 3) rather than 1 / 3). A student said that Matlab does this, and I expect that Maple and Mathematica do as well.

Aside:

Assignment Project Exam Help Using GHCi read-eval-print loop

We interact with GHCi through its "read-eval-print loop" (which some people call a REPL, pronounced "repple"). Real evil print loops at a large of many languages, including Python, but not others (including Java, C and C++).

The read-eval-print loop is:

- 1. read input WeChat: cstutorcs
- 2. **evaluate** input
- 3. **print** result
- 4. loop back to 1

When you enter an expression such as 2 + 2 into GHCi, the loop **reads** the expression, **evaluates** it to a result (namely 4), **prints** the result, and then waits to read more input.

(If you are familiar with command-line shells such as bash, they are generally not "read-eval-print", but "read-run": by default, they don't print the exit status. If you are not familiar with command-line shells, don't worry about this.)

Typing large expressions is tedious and unreliable, however, so most of the time we will enter Haskell code in files (with the extension .hs), load them into GHCi (as described below), and then evaluate some expressions. For example, if we define a function triple in a .hs file, we can type

triple 10

and (hopefully) get the result 30.

3.1 Loading files

To load filename.hs into GHCi, enter a load command:

```
:load filename.hs
or
:load filename
or
:l filename
```

Once the file is loaded, the prompt "Prelude>" becomes "*Main>". (If the file contains a module, then the module's name will be printed instead of "Main".)

A load command is *not* a Haskell expression: When you enter a line beginning with: into GHCi, it interprets the line as a command. Commands ask GHCi to take some action that is not "evaluate a Haskell expression". You can see a list of GHCi commands by entering: ? or:help, though I find this more useful for reminding myself of commands' spelling than for learning how they work.

The :reload command, which can be abbreviated :r, reloads the previously loaded file. So if you change filename.hs and want to use the updated version, enter :r.

3.2 Seein Athesting of an expression roject Exam Help

Like Java, but unlike Python, Haskell is a "statically typed" language. You can ask GHCi for the type of an expression by entering the command

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Haskell's type system prioritizes power (being good at catching subtle bugs) over ease of learning, so this can give surprising results:

```
*Main> :type 3 WeChat: cstutorcs
```

I won't explain this in full detail now, but roughly, this is Haskell "hedging its bets": the expression 3 can have a variety of numeric types (including integers and floating-point numbers, which behave differently), so Haskell refuses to choose just one. Instead, it says 3 has type 'a', where all we know is that a is some numeric type ('Num a')".

If we tell Haskell that we want a specific numeric type, say Int, it accepts our request and says the expression (3 :: Int) has type Int.

```
*Main> :type (3 :: Int) (3 :: Int) :: Int
```

If 3 is an Int, then Haskell decides (reasonably) that adding 4 to it gives an Int, even though we wrote 4 and not (4 :: Int):

```
*Main> :type (3 :: Int) + 4
(3 :: Int) + 4 :: Int
```

This is all somewhat confusing, but Haskell is more decisive when you ask it about definitions in loaded files: if you put

```
x = 3
```

in a file a.hs, load a.hs, and then ask for the type of x, you get a clearer answer. Try it!

4 Functions

An anonymous function, called a *lambda* (λ), is written in Haskell by writing a backslash (which sort of resembles λ), followed by the name of the argument (called the *bound variable*), followed by ->, followed by the function body:

We can call this function by writing it, then giving an argument:

$$(\x -> x + 1) 6$$

This is a small expression: try it in the GHCi read-eval-print loop. How does this step? Since GHCi prints 7 at the end, there must be a sequence of steps

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:

> 6 + 1

In fact, there are just two steps: the second is arithmetic, the first is a function application (another name for a function call).

by arithmetic

If we can step from $(\x -> x + 1)$ 6 to 6 + 1 there must be a stepping rule that explains how to do this.

4.1 Stepping rule for function application

If f is a function, and the bound variable of f is x, and the body of f is body, then

f arg \Rightarrow body with arg substituted for x

Read the last line as:

f applied to argument arg steps to body with arg substituted for x

Exercise 1. Using the stepping rule for function application, then the stepping rule for arithmetic, fill in the following:

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$$ht \stackrel{\text{($f \rightarrow f - f)}}{\rightleftharpoons} \text{s://tutorcs.com}^{\text{by arithmetic}}$$

(There is only one correct result, zero, but several reasonable sequences of steps. Only one sequence of steps corresponds to what Haskell actually does!)

5 Optional readings for this lecture

- Thompson, chapter 1
 - Section 1.10, "Calculation and evaluation", is another presentation of *stepping*.

6 Other remarks

Remark 1. In Thompson's discussion of fixed-size integers, the bound 2147483647—which is $2^{31} - 1$ —is almost certainly out of date. To see the value on your system, enter (in GHCi)

If you enter maxBound without the ":: Int", you won't get anything useful. (GHCi won't even give you an error message, though Hugs will.) GHC has different maximum values for different types; when you enter maxBound by itself, it doesn't know what type you want.

(It's usually better to use Integer instead of Int anyway, because Integer avoids the possibility of overflow.)