CIT 596 Spring 2023

Module 5-6

Name: NAME HERE Collaborator: COLLABORATOR NAME HERE

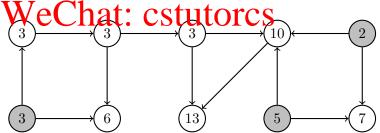
Answers that describe an algorithm should always include a proof of correctness and running time analysis. Algorithms may be described in English or in clear pseudocode with explanatory comments.

- 1. You are given an integer $r \in [1..n]$ and a sequence $\sigma = s_1, s_2, \ldots, s_n$ of n distinct elements in which elements are presented one at a time. When element s_i is presented, you can no longer access any of s_1, \ldots, s_{i-1} unless your algorithm has stored them. You are asked to output the r^{th} smallest element in σ . Design an algorithm that can accomplish this using O(r) space and O(n) expected time. (25 points)
- 2. You are given the adjacency-list representation of a directed acyclic graph G = (V, E) with n vertices and m edges. Furthermore, for every vertex $v \in V$ with in-degree zero, you are given $value(v) = \sum_{(u,v)\in E} value(u),$

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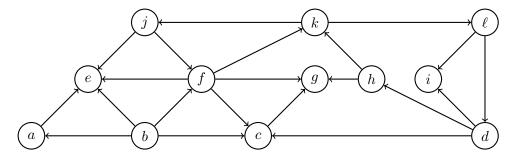
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For example, in the graph below, the gray vertices have in-degree zero, so their values determine the values of all other vertices in the graph.



Design a O(n+m)-time algorithm to compute value(v) for all vertices $v \in V$. (25 points)

3. You are given the adjacency list representation of a directed graph G = (V, E) with n vertices and m edges. We define the set $S = \{v \in V : \text{ some cycle in } G \text{ is reachable from } v\}$. For example, in the graph below, $S = \{b, d, f, h, j, k, \ell\}$.



Design an O(n+m) time algorithm to find the set S.

(25 points)

4. Let G(V, E) be an undirected graph with n vertices and m edges such that G has two vertices s and t where the shortest path from s to t has length strictly more than n/2. Then, prove that there must be a vertex $w \in V \setminus \{s, t\}$ such that every path from s to t must pass through w. Furthermore, assuming that G is given to you in the adjacency-list representation along with vertices s and t, design an O(n+m) time algorithm to output such a vertex w. (25 points)

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