

程序代写代做 CS编程辅导

CMT1@ ual Computing

I.3 Vectors and Matrices WeChat: cstutorcs

Assignment Project Exam Help

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Overview

- 程序代写代做 CS编程辅导 > Vectors
 - Vector Opera<u>+</u>
 - Vector Geom
 - Vector Projed
- > 3D Vectors
 - Cross Product
 3D Vector Geometry
- ► Matrices Assignment Project Exam Help
 - Special Matricesail: tutorcs@163.com
 - Matrix Operations
 - Determinant QQ: 749389476

Vectors

- ➤ A vector is a directed line segment, characterised by: 程序代写代做 CS编程辅导
 - Length
 - Direction
 - But NOT Position



- Zero vectors doesn't have direction.
- > A vector with length Weshalit vector.cs
- > A vector u with the same length b Propposite direction of vector \mathbf{v} is the negative vector of \mathbf{v} , denoted by $\mathbf{u} = -\mathbf{v}$.
- > Two vectors are equal iff they have the same length and the same direction: 749389476
 - Two zero vectors and plantage equations are undefined.

Vector Operations

- A vector \mathbf{u} multiplied by a scalar α denoted by $\alpha \mathbf{u}$ has the same direction of \mathbf{u} if $\alpha > 0$ and the opposite direction if $\alpha < 0$. The length of \mathbf{u} times of the length of \mathbf{u} .
- The sum w of two \ and v:

u v

follows the head-to-tail rule. That is,

- if the head of **u** is connected to the tail of **v**, then **w** is the directed line segment Project Exam Help directed of **v**.
- The subtraction of vectorive from vector we and vector -v

$$u = w - \sqrt{2} \sqrt{423} 89476$$

Vector Operations

► A nD vector is represented by:
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> The sum and subtrate two vectors are:

$$\mathbf{u} + \mathbf{v} = \begin{bmatrix} u_1 + v_1 u_2 + v_2 \cdots u_n + v_n \end{bmatrix}^T$$

$$\mathbf{w} = \begin{bmatrix} u_1 - v_1 u_2 - v_2 \cdots u_n - v_n \end{bmatrix}^T$$

> The multiplication of a vector v by a scalar λ is defined by

$$\lambda \mathbf{v} = [\lambda \mathbf{E} \mathbf{r} \mathbf{v} \mathbf{a} \mathbf{i} \mathbf{l} : \lambda \mathbf{v} \mathbf{t} \mathbf{d}^T \mathbf{c} \mathbf{s} @ 163.\mathbf{com}]$$

The inner product (dot product scalar product) of two vectors is:

$$\mathbf{u} \cdot \mathbf{v} = \mathbf{u}^T \mathbf{v} \stackrel{\text{https://tutores.com}}{=} \frac{1}{u_1 v_1} \frac{1}{v_1 v_2} \frac{1}{v_2 v_2} \frac$$

Vector Geometry

- ➤ A vector has direction and length. 在序代与代做 CS编程辅导
 - The length is defined by

$$|\mathbf{v}| = \sqrt{\mathbf{v}_1^2 + \cdots + \mathbf{v}_n^2}$$

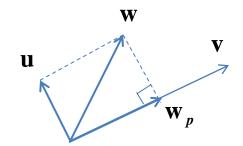
- The direction is partial to the direction from the origin to the point (v_1, v_2, \dots, v_m) Euclidean space.
- The angle θ between two vectors **u** and **v** is calculated by WeChar: estutores
- > Normalisation of a vector and represent Punit vector of Helpch has length 1: Email:/tutorcs@163.com
- are perpendicular to each other, and the angle between these two https://tutorcs.com vectors are 90°.

Vector Projection

➤ The vector projection w, of a vector w on a nonzero vector v is a vector parallel to v, d籍格的 代做 CS编程辅导

where α is a scalar α





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The vector \mathbf{w} then can be represented by the sum of \mathbf{w}_p and vector \mathbf{u} , which is perpendical sign mental \mathbf{w}_p is \mathbf{Exam} Help

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 $\mathbf{u} \cdot \mathbf{v} = 0$ $\mathbf{u} \cdot \mathbf{w} = 0$ $\mathbf{Q} \cdot 749389476$

Cross Product

Denote two 3D vectors \mathbf{V}_1 and \mathbf{V}_2 by $\mathbf{v}_1 = [x_1, y_1, z_2]^T$, the vector product (also called closs product, outerplace) of \mathbf{V}_1 and \mathbf{V}_2 is defined by

 $\mathbf{v}_{1} \times \mathbf{v} = \begin{bmatrix} \mathbf{v}_{1} \mathbf{y}_{2} \\ \mathbf{v}_{1} \mathbf{z}_{2} \\ \mathbf{v}_{2} \mathbf{z}_{3} \\ \mathbf{v}_{3} \mathbf{z}_{4} \mathbf{z}_{2} \end{bmatrix}$

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 \triangleright If θ is the angle between \mathbf{v}_1 and \mathbf{v}_2 , then the length is:

Assignment Project Exam Help $|\mathbf{v}_1 \times \mathbf{v}_2| = |\mathbf{v}_1| |\mathbf{v}_2| \sin \theta$ a×b Email: tutorcs@163.com

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 The direction satisfies right-hand rule a
 - $\mathbf{v}_1 \times \mathbf{v}_2$ is perpendicular to 19689476

 \mathbf{v}_1 and \mathbf{v}_2 .



3D Vector Geometry

- \blacktriangleright A point in 3D space can be represented by a 3D vector: $p = [x \ yz]^T$
- A directed line sequence om p_1 to p_2 can be represented by vector:
- Let v_1 and v_2 are two directed line segments on a plane, then the normal direction is determined by the cross product of v_1 and v_2 .

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Matrices

- > A matrix is a rectangular array of scalars, arranged in rows and columns. The individual 和新教育。 entries. The number num and column dimensic
- \triangleright The following matrix $\mathbf{H}_{\mathbf{r}}$ w dimension \mathbf{m} and column dimension n, or simply, $m \times n$ di ਸਿਣਿਆ a_{ii} is an element of the matrix

$$\mathbf{A} = \begin{bmatrix} a_{11} & a_{12} & \mathbf{WeChat} : \mathbf{cstutorcs} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \mathbf{Assignment Project} & \mathbf{Exam Help:} \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{bmatrix}$$

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$$\mathbf{A}^\mathsf{T} = \begin{bmatrix} a_{11} & a_{21} & \cdots & a_{m1} \\ a_{12} & a_{22} & \cdots & a_{m2} \\ a_{1n} & a_{2n} & \cdots & a_{mn} \end{bmatrix}$$

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$$\mathbf{A}^\mathsf{T} = \begin{bmatrix} a_{11} & a_{21} & \cdots & a_{m1} \\ a_{12} & a_{22} & \cdots & a_{m2} \\ a_{1n} & a_{2n} & \cdots & a_{mn} \end{bmatrix}$$

$$\mathbf{Email: tutorcs@163.com}$$

$$\mathbf{A}^\mathsf{T} = \begin{bmatrix} a_{11} & a_{21} & \cdots & a_{m1} \\ a_{12} & a_{22} & \cdots & a_{m2} \\ a_{1n} & a_{2n} & \cdots & a_{mn} \end{bmatrix}$$

- matrix obtained by intechanging the rows and columns of A.
- To save the space, the matrix is often written as $A = [a_{ij}]_{m \times n}$, or simply, $A = [a_{ij}]$, if the dimension of the matrix is implicitly known.

Special Matrices

- ➤ A square matrix is a matrix which has the same row and column dimension. 程序代写代做 CS编程辅导
- A symmetric matrix in a matrix that is equal to its transpose. Let $A = [a_{ij}]$ be a symmetric matrix, then $A = A^T$. Its elements satisfy
- A diagonal matrix is a first \overline{A} tusually square matrix) in which the elements outside the main diagonal are all zero, i.e., $\mathbf{A} = [a_{ij}]$,

$$a_{ij} = 0$$
 if $i \neq j$ Project Exam Help

An identity matrix, denoted by I, is a square diagonal matrix with 1's on the diagonal and 0's elsewhere

$$I = [a_{ij}]$$
, $Q = \begin{cases} 1496389476 \\ 0 \text{ otherwise.} \end{cases}$
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Special Matrices

➤ A row matrix is a matrix of dimension 1 x n. It is also called a row vector.

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 $[\quad a_n]$

A column matrix is a column vector. dimension $m \times 1$, also called a column vector.

 $\mathbf{a} = \begin{bmatrix} a_2 \\ \mathbf{w} \\ \mathbf{e} \\ \mathbf{c} \\ \mathbf{e} \\$

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Matrix Operations

- ➤ Scalar-Matrix multiplication is defined by multiplying each element to the scalar 程序代写代做 CS编程辅导 by the scalar
 - $\alpha \mathbf{A} = [\alpha a_{ii}]$
- Matrix-Matrix Addit matrices of the same dimension is defined by adding cc ing elements of the two matrices
 - $\mathbf{C} = \mathbf{A} + \mathbf{B} = [\mathbf{a}_{ij} + \mathbf{b}_{ij}]$
- \triangleright Matrix-Matrix Multiplication of an $m \times l$ dimensional matrix A and an l x n dimensional matrix Brisnd finect by Exam Help

 - $C = AB = [c_{ij}]$ Email: tutorcs@163.com Where $c_{ij} = \sum_{k=1}^{l} a_{ik} b_{kj}$ QQ: 749389476
- \triangleright Inverse of a Square Matrix **A** is a square matrix **B**, such that https://tutorcs.com AB = I
 - Denote by $\mathbf{B} = \mathbf{A}^{-1}$

Orthogonal Matrix

An orthogonal matrix is a square matrix with real entries whose columns and rows are of thogonal thick the square matrix with real entries whose vectors).

Equivalently, a matrix hogonal if its transpose is equal to its inverse:

which entails

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$$QQ^T = Q^TQ = I$$

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Determinant

> The determinant is a value associated with a square matrix, denoted by det(A), det A, 你有你能够。



- where A_{ij} is the (integral matrix of A, which is obtained by deleting the *i*th region A).
- > The determinant of a matrix is calculated by

$$|\mathbf{A}_{\overline{s}}|_{a_{21}}^{a_{11}} = \mathbf{a}_{12}$$

> The determinant of F3723 intaters & alegiated by

$$|\mathbf{A}| = \begin{vmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{vmatrix} = a_{11} \begin{vmatrix} \mathbf{A}_{11} | -a_{12} | \mathbf{A}_{12} | + a_{13} | \mathbf{A}_{13} | = a_{11} \\ \mathbf{A}_{12} | -a_{12} | \mathbf{A}_{13} | = a_{11} \begin{vmatrix} a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{vmatrix} - a_{12} \begin{vmatrix} a_{21} & a_{23} \\ a_{31} & a_{33} \end{vmatrix} + a_{13} \begin{vmatrix} a_{21} & a_{22} \\ a_{31} & a_{32} \end{vmatrix}$$
$$= a_{11} a_{22} a_{33} + a_{12} a_{23} a_{31} + a_{13} a_{21} a_{32} - a_{11} a_{23} a_{32} - a_{12} a_{21} a_{33} - a_{13} a_{22} a_{31}$$

Cross Product Using Determinant

➤ The cross product of two 3D vectors can be calculated using determinant as follows: 序代写代做 CS编程辅导

$$\mathbf{v}_{1} \times \mathbf{v}_{2} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{j} & \mathbf{k} & \mathbf{j} \\ \mathbf{x}_{1} & \mathbf{y}_{1} & \mathbf{k} & \mathbf{j} \\ \mathbf{x}_{2} & \mathbf{y}_{2} & \mathbf{k} & \mathbf{j} \\ \mathbf{x}_{2} & \mathbf{y}_{2} & \mathbf{j} & \mathbf{k} & \mathbf{j} \\ \mathbf{x}_{1} & \mathbf{j} & \mathbf{j} & \mathbf{k} & \mathbf{j} \\ \mathbf{x}_{2} & \mathbf{j} & \mathbf{j} & \mathbf{k} & \mathbf{j} \\ \mathbf{x}_{2} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{k} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j} & \mathbf{j} & \mathbf{j} & \mathbf{j} \\ \mathbf{k} & \mathbf{j$$

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Summary

- ➤ What are the characteristics cof 编程编ter?
- What operations are defined for vectors.
- ➤ How to calculate ector projection onto another vectors.
- > How to calculate cross product? What is the geometric meaning of cross product?
- > How to do matrix operations?

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- What is a orthogonal matrix?
- > How to calculate determinant? 3.com

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