

程序代写代做 CS编程辅导

CMT1@@ual Computing

VII.2 Freeform Surfaces WeChat: cstutorcs

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Overview

- ➤ Surface representations cs编程辅导
- > Parametric surfaces
- Piecewise po al al surfaces
 - Tensor produles and es
- > Subdivision swe@cescutores
 - Loop subdivisionignment Project Exam Help
 - Doo-Sabin subdivisioners@163.com
 - Catmull-Clark subdivision 6

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Surfaces

- ➤ We require general surface shapes (something better than polygonal meshes)
 - Exact bounda essentation for some objects
 - Create, edit a yse shapes



Explicit Surfaces

➤ A surface is a set o程post頂 is of aspoint of the bound with two



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- > Explicit and implicit representation similar to curve
 - Explicit: z = f(x, y) for $(x, y) \in \mathbb{R}^2$

Implicit Surfaces

- - $\lim_{z \to z} \frac{f(z)}{y} y, z) = 0$
 - Usually one equal 3D
- Example: linear ec

$$\overrightarrow{ax} + \overrightarrow{by} + cz + d = 0$$

• Using vectors: WeChat: cstutorcs



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Implicit Quadrics

Duadrics (quadrati在病代码的)做 CS编程辅导

$$ax^{2} + by^{2} + cz^{2} + c$$

$$\mathbf{v}^{\mathsf{T}} \mathbf{x} + \mathbf{s} = \mathbf{0}$$

- •Sphere / Ellipsoid $extit{WeChat: cstutozes}$ $\frac{1}{Assignment} + \frac{1}{Project Exam Help}$
- Cylinder (elliptic mail: tutorcs@163.com $QQ_{1}\sqrt{49389476}=0$
- Cone (elliptic): $\frac{\text{https://tutorcs.com}}{\frac{x^2}{r^2} + \frac{y^2}{r^2} z^2} = 0$

Properties of Implicit Surfaces



Mathematical Functions / Sets

Blobby Models

Parametric Surfaces

Describe points on surface by parametric functions

$$\begin{array}{c}
\mathbf{x}(\mathbf{u}, \mathbf{v}) \\
\mathbf{y}(\mathbf{u}, \mathbf{v}) \\
\mathbf{z}(\mathbf{u}, \mathbf{v})
\end{array}$$

• Maps 2D (u,v) parameter domain to 3D (x,y,z) model space WeChat: cstutorcs

Example: ellipsøidignment Project Exam Help

•
$$x(u, v) = r_x \cos u \cos v \cos u \cos 0.63.com$$

 $y(u, v) = r_y \cos u \sin v$
 $z(u, v) = r_z \sin u$
 $z(u, v) \in [-\pi/2, \pi/2]^{\text{tutores.20m}}$

H&B Figure 10.10

Properties of Parametric Surfaces

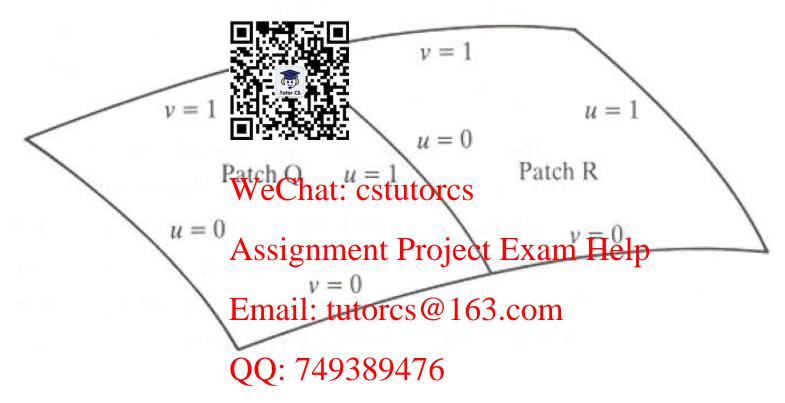
- > Properties similagto pasametric编程编导
 - Simple to render naints
 - Hard to test if positive surface, compute intersections, etc.
- Hard to represent whole surface by single polynomial weChat: cstutorcs
 function

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- Use piecewise polynomial surfaces
- Surface is cut into patches
- Smoothness / continuity problem when joining patches https://tutorcs.com

Piecewise Polynomial Surface

> Spline surface: piecewise polynamia surface patches



- > Use spline curve approach with two degrees of freedom
 - Each patch is defined by a set of control points

Tensor Product

Intuitively, a surface is a curve which moves through space while it changes its shape

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Mathematically this is the tensor product of two curves

Tensor Product Surfaces

- Surface patch as accurregne wingsthrough space
 - Assume this curve any time $v \in [0, 1]$ a Bézier curve $c^{\nu}(u) = C^{\nu}(u)$
 - The control points $P_{\text{hat:}}$ clie on curves as well, assume these are also Bézier curves Assignment Project Exam Help

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Combing both gives the formula for a *Bézier surface patch*https://tutorcg.com

$$Q(\mathfrak{u},\mathfrak{v}) = \sum_{l=0} \sum_{k=0} P_{l,k} B_l^{\alpha}(\mathfrak{u}) B_k^{\beta}(\mathfrak{v})$$

Bézier Surface Patches

Point Q(u, v) on the patch is the tensor product of Bézier curves defined by the control points $P_{l,k}$



• Order of surface is given by order of curves α , β (e.g. bicubic: $\alpha = \beta = 3$)

Properties of Bézier Patches

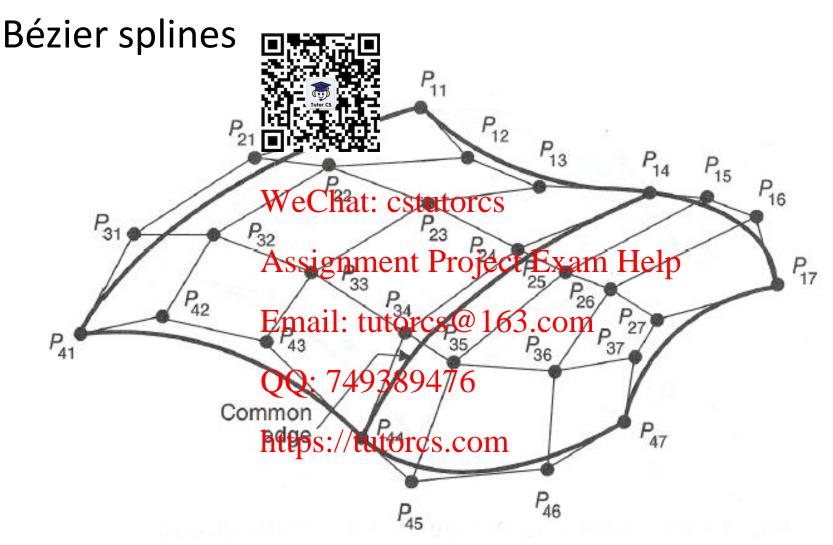
- > Interpolates four gotnertwots编脚编ipts
- ➤ Lies inside *converse* of control points

Changing contributes has only local effect (local control)



Smooth Bézier Surfaces

> Continuity / smeothness cons 編 整 imilar to



C⁰ and C¹ Bézier Surfaces

► C⁰ requires aligning boundary curves 辅导



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C¹ requires aligning boundary curves and derivatives

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C¹ continuity

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Drawing Bézier Surfaces

➤ Simple approach程序代写代做 CS编程辅导

loop through uniformial spaced increments of u and v

```
for (int l = 0; l < l_m
   double u = u_{\min}
   for (int k = 0; k \leftarrow k that: cstutores
    double v = v_{\min} + k * v_{\text{step}};
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DrawQuadrilateral (...);
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                          QQ: 749389476
```

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• Note, Bézier surfaces always have quadrilateral structure

Drawing Bézier Surfaces

➤ Better approach: 程序代写代做 CS编程辅导 use adaptive subdivision DrawSurface (surfact) if flat(surface, eps DrawQuadrilateral (surface); WeChat: cstutorcs Uniform subdivision } else { SubdivideSurface (surfacent) Project Exam Help DrawSurface (surfaceLL); DrawSurface (suffmailRtutorcs@163.com DrawSurface (surfaceRL): 389476 DrawSurface (surfaceRR): https://tutorcs.com Adaptive subdivision

Drawing Bézier Surfaces

> Problem of adaptive subdivising 辅导

• Cracks at boundaries between patches at different subdivision leve

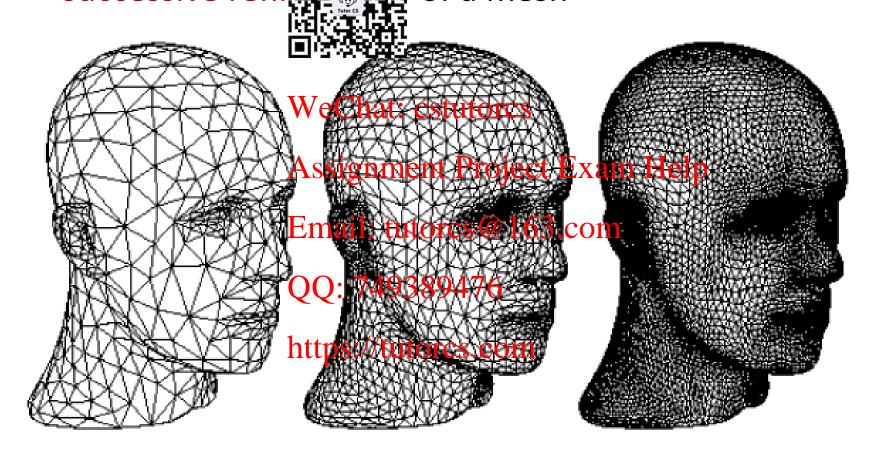
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• Avoid cracks by had aling textro wertices and triangulating quadrilaterals with neighbours at finer level

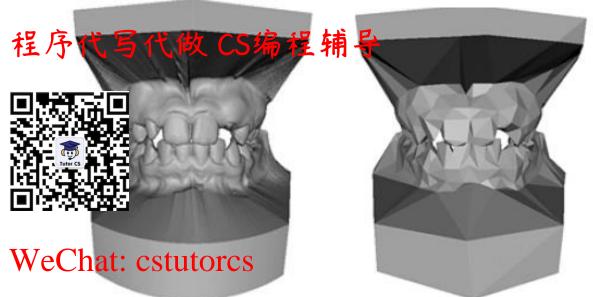
Subdivision Surfaces

- ▶Idea of subdivisi程序系以重写€酸 CS编程辅导
 - Define a smooth surface as the limit of a sequence of successive refires of a mesh



Why Subdivision?

- Level of Detail
- Compression
- Smoothing





Cutting Corners – Curves



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Surface Subdivision

- > Start with a contr程序彩写代做 CS编程辅导
- > Per iteration construct refined mesh by inserting vertices
- Mesh sequence s nverge to a limit surface
- > Subdivision scher
 - Generate topology of the new mesh
 - Compute vertex locations in new mesh Help
 - Vertex point: new location of old vertex Email: tutorcs@163.com
 - Edge point: location of new vertex on old edge OO: 749389476
 - Face point: location of new vertex on old face https://tutorcs.com

Loop Subdivision

- ➤ Loop subdivisio程系he实现 cs编程辅导
 - Refine each triangle into 4 triangles by splitting each edge and connected ew vertices



Loop Subdivision

- > Computing locations pfingwygrtic编程辅导
 - Weighted average of original vertices in neighbourhood



$$\beta = \frac{1}{n} \left(\frac{5}{8} - \left(\frac{3}{8} \frac{QQ}{8} ; 749389 \right) \right)^{2}$$
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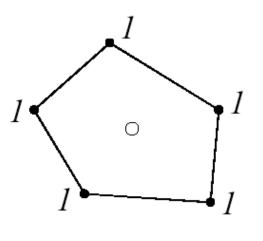
No face points

- > Mesh is the control mesh @fcg编程解ipe surface
 - Refined mesh is sontrol mesh of a B-Spline Surface
- > Incremental cor
 - Calculate face pwirthat: cstutorcs
 - Calculate edge points Help
 - Calculate vertex points using face and edge points
 - Connect vertices QQ: 749389476

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Step 1

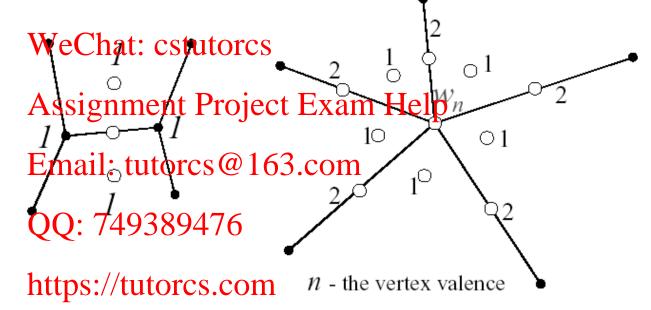
First, all the face points are calculated



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Last, the vertex points are calculated using the values of the face and edge points and the original vertex



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- ➤ Connecting new Price K 做 CS编程辅导
 - Connect each new face point to edge points of the edges defining ace
 - Connect each received ex point to new edge points of all old edges incident on the old vertex point



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Face Point

$$f = \frac{1}{m} \sum_{i=1}^{m} p_i$$

Edge Point

$$\mathring{e} = \frac{p_1 + p_2 + f_1 + f_2}{4}$$
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Vertex Point

$$v = \frac{Q}{n} + \frac{2R}{n} + \frac{p}{n}$$
 (nEmail: tutorcs@163.com

n n QQ: 749389476

$$\mathbf{v} = \frac{1}{n^2} \sum_{i=1}^{n} \mathbf{f}_i + \frac{1}{n^2} \sum_{i=1}^{n} \mathbf{p}_i \mathbf{tps:} \frac{n-2}{n}$$

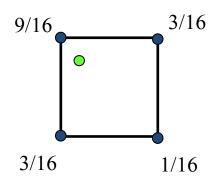
☐ Q – Average of face points

By: Ofir Weber

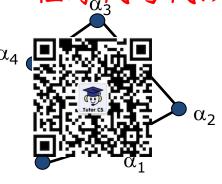
- \square R Average of midpoints
- \Box p old vertex

Doo-Sabin Subdivision

Masks:



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$$\alpha_{i} = \frac{\delta_{i,0}}{4} + \frac{3 + 2\cos(2i\pi i n)}{4n} \text{utorcs@163.com}$$

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$$\stackrel{\circ}{p} = \sum_{i=0}^{n-1} \alpha_i \stackrel{\bullet}{p_i}$$
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Properties of Subdivision Surfaces

- > Advantages 程序代写代做 CS编程辅导
 - Simple methods for describing complex surfaces
 - Multi-resolutio tion and manipulation
 - Arbitrary topol ontrol mesh (not only quadrilateral)
 - Limit surface is Whobath cstutorcs
- Disadvantages Assignment Project Exam Help
 - No obvious Email: httprcs@163.com parametrisation 749389476
 - Hard to find intersections





Summary

- ➤ What are paramet程序軟傷侵級 Wh编辑 heir advantages and disadvantage and disadvantage
- What are spline supplies What are their advantages and disadvantages? While have major problem when defining surfaces "piecewise"?
- ➤ What is the principle of a tensor product surface? What are Bézier surfaces? What coppditions don't help ontrol points of C⁰/C¹ continuous Bézier surfaces have to fulfil? Email: tutorcs@163.com

 ➤ What is the principle of subdivision surfaces? What are
- What is the principle of subdivision surfaces? What are their advantages / Wisadvantages?
- > How do Loop, Catmull-Glarke Degn Sabin subdivision schemes work?