

程序代写代做 CS编程辅导



# CMT10 Qual Computing

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## Corner Detection

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# Overview

- Feature Extraction

- Characteristics of good features
- Applications

- Corner Detection

- Basic idea
- Mathematics

- Harris Detector

- Invariance and Covariance

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# Feature Extraction: Corners

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# Why Extract Features

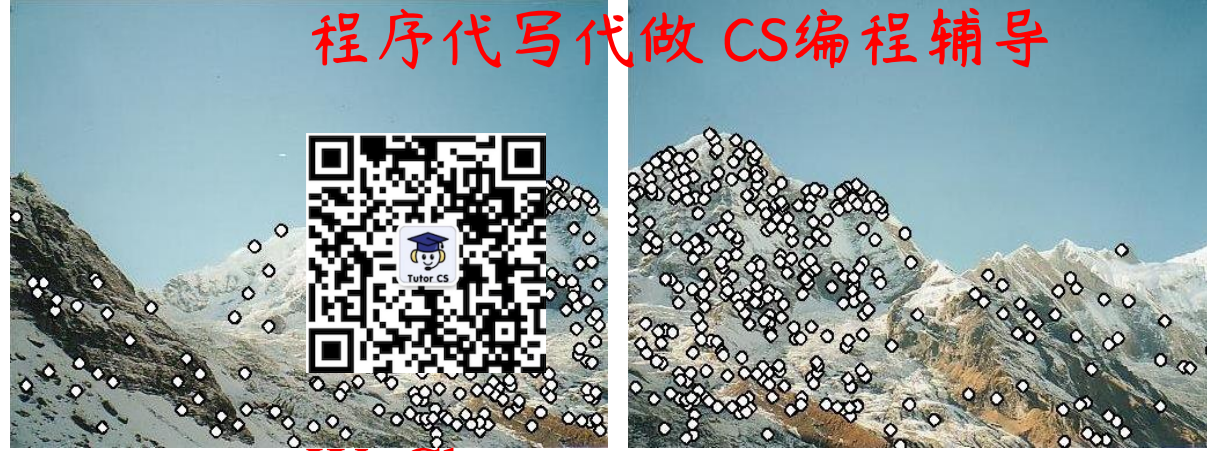
- Motivation: panorama stitching
- We have two images – how do we combine them?



- Step 1: extract features
- Step 2: match features
- Step 3: align images



# Characteristics of Good Features



- Repeatability

- The same feature can be found in several images despite geometric and photometric transformations

- Saliency

- Each feature is distinctive

- Compactness and efficiency

- Many fewer features than image pixels

- Locality

- A feature occupies a relatively small area of the image; robust to clutter and occlusion

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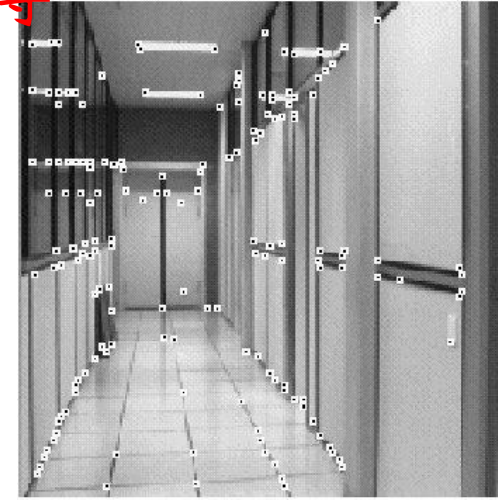
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# Applications

- Feature points are used for 程序代写代做 CS编程辅导
  - Image alignment
  - 3D reconstruction
  - Motion tracking
  - Robot navigation
  - Indexing and database retrieval
  - Object recognition



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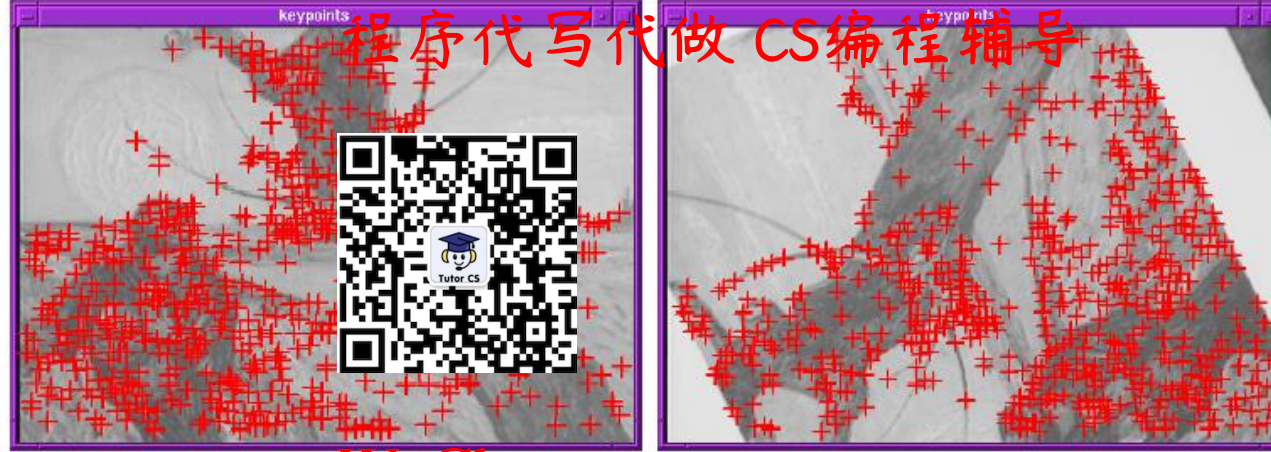
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# Finding Corners



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- Key properties: In the region around a corner, image gradient has two or more dominant directions
- Corners are repeatable and distinctive

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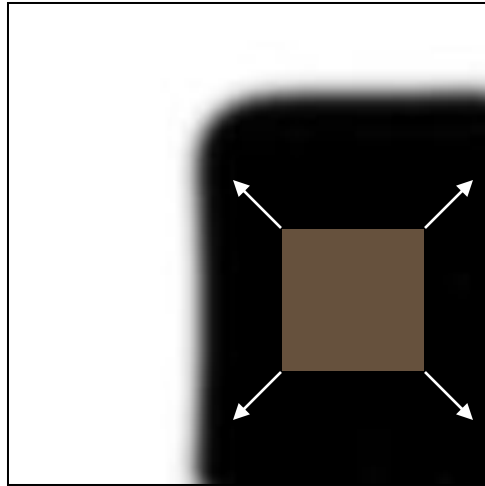
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C.Harris and M.Stephens. "[A Combined Corner and Edge Detector.](#)" *Proceedings of the 4th Alvey Vision Conference, 1988*: pages 147--151.

# Corner Detection: Basic Idea

- We can easily recognise the point by looking through a small window
- Shifting a window in any direction should give a large change in intensity



“flat” region:  
no change in  
all directions



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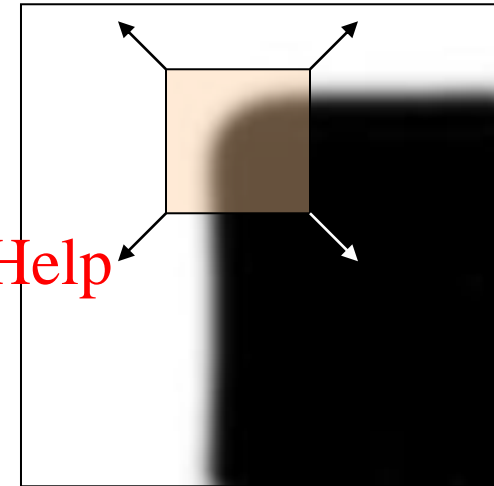
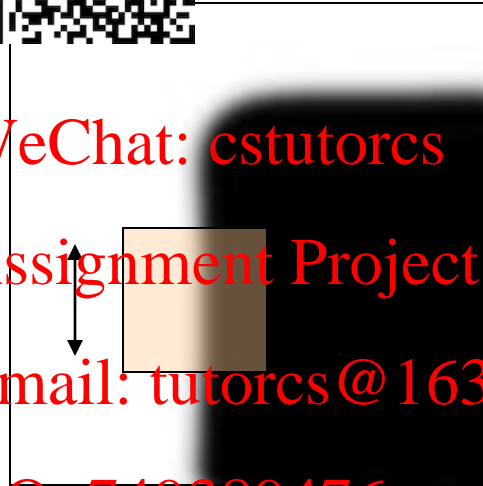
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no change along  
the edge direction



“corner”:  
significant change  
in all directions



# Corner Detection: Mathematics

- Change of intensity for the shift  $[u, v]$

$$E(u, v) = \sum_{x, y} w(x, y) [I(x + u, y + v) - I(x, y)]^2$$



$I(x, y)$

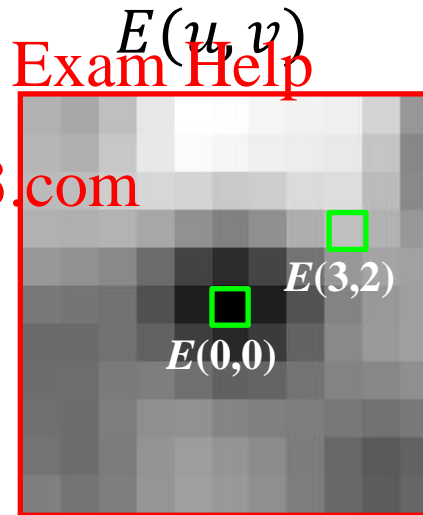
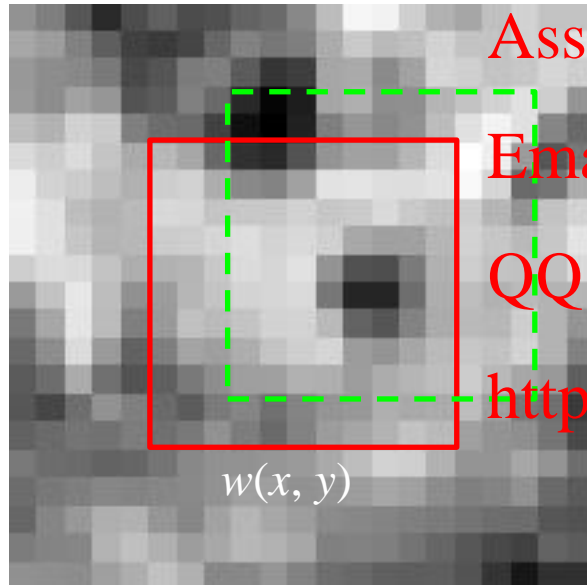
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# Corner Detection: Mathematics

- Change of intensity for the shift  $[u, v]$

$$E(u, v) = \sum_{x, y} w(x, y) [I(x+u, y+v) - I(x, y)]^2$$

Window  
function

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Intensity

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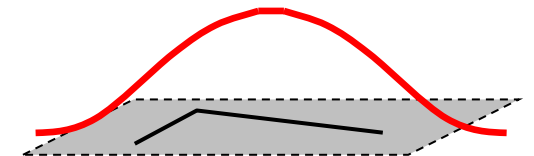
- Window function  $w(x, y) =$

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1 in window, 0 outside

or



Gaussian

# Corner Detection: Mathematics

- Change of intensity for the shift  $[u, v]$

$$E(u, v) = \sum_{x, y} w(x, y) [I(x + u, y + v) - I(x, y)]^2$$

- We want to find out how this function behaves for small shifts

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 $E(u, v)$

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# Corner Detection: Mathematics

- Change of intensity for the shift  $[u, v]$

$$E(u, v) = \sum_{x, y} w(x, y) [I(x + u, y + v) - I(x, y)]^2$$

- We want to find out how this function behaves for small shifts
- Using *first-order Taylor approximation*:

$$I(x + u, y + v) \approx I(x, y) + uI_x(x, y) + vI_y(x, y), \text{ Then:}$$

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$$\begin{aligned} E(u, v) &\approx \sum_{x, y} w(x, y) [I(x, y) + uI_x(x, y) + vI_y(x, y) - I(x, y)]^2 \\ &= \sum_{x, y} w(x, y) [uI_x(x, y) + vI_y(x, y)]^2 = \dots \end{aligned}$$



# Corner Detection: Mathematics

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$$\dots = \sum_{x,y} w(x,y) [u^2 I_x^2 + v^2 I_y^2 + 2uv I_x I_y]$$



$$= \sum_{x,y} w(x,y) [u \ v] \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix}$$

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$$= [u \ v] \left( \sum_{x,y} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} \right) \begin{bmatrix} u \\ v \end{bmatrix}$$

$M$

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# Corner Detection: Mathematics

- The approximation simplifies to 程序代写代做 CS编程辅导


$$E(I_x^2 + I_y^2) [u \ v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

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- where  $M$  is a second moment matrix computed from image derivatives: Assignment Project Exam Help

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$$M = \sum_{x,y} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

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# Interpreting the Second Moment Matrix

- The surface  $E(u, v)$  is locally approximated by a quadratic form. Let's try to understand its shape.



$$E(u, v) \approx [u \ v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

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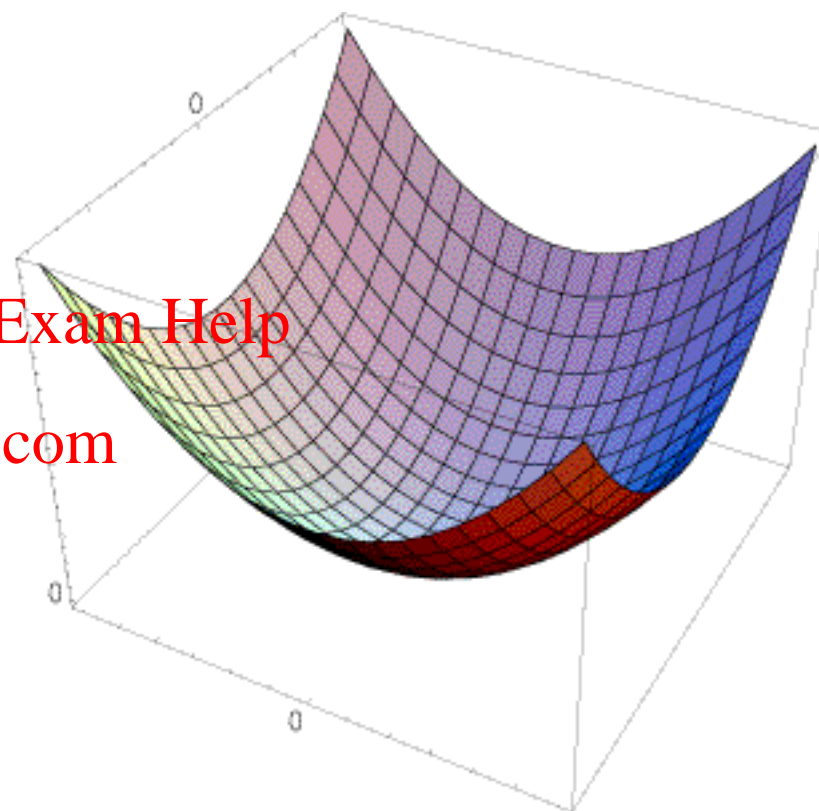
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$$M = \sum_{x,y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$



# Interpreting the Second Moment Matrix

- Consider a horizontal slice of  $E(u, v)$ :  $[u \ v] M \begin{bmatrix} u \\ v \end{bmatrix} = \text{const}$
- This is an equation of an ellipse



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# Interpreting the Second Moment Matrix

- Consider a horizontal slice of  $E(u, v)$ :  $[u \ v] M \begin{bmatrix} u \\ v \end{bmatrix} = \text{const}$

- This is an equation of an ellipse

- Diagonalization of  $M$ :  $M = \begin{bmatrix} 0 & 0 \\ 0 & \lambda_2 \end{bmatrix} R$

- The axis lengths are determined by the eigenvalues:  $\lambda_1$  and  $\lambda_2$ , and the orientation is determined by  $R$

- If either  $\lambda$  is close to 0, then this is not a corner, so look for positions where both are large.

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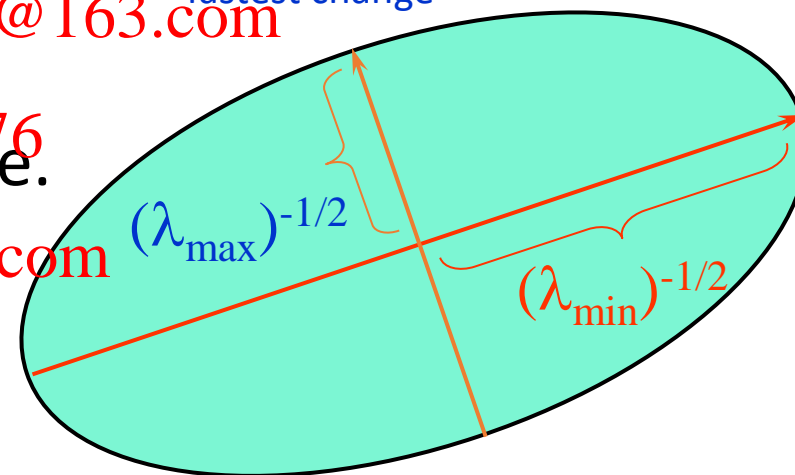
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direction of the  
fastest change



direction of the  
slowest change

# Visualization of Second Moment Matrices

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# Visualization of Second Moment Matrices

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# Interpreting the Eigen Values

- Classification of image points using eigenvalues of  $M$ .



“Edge”

$$\lambda_2 \gg \lambda_1$$

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“Corner”

$\lambda_1$  and  $\lambda_2$  are large,

$$\lambda_1 \sim \lambda_2;$$

$E$  increases in all directions

$\lambda_1$  and  $\lambda_2$  are small;  
 $E$  is almost constant  
in all directions

“Flat”  
region

“Edge”

$$\lambda_1 \gg \lambda_2$$

$\lambda_1$



# Corner Response function

- $R = \lambda_1 \lambda_2 - \alpha(\lambda_1 + \lambda_2)^2 = \det(M) - \alpha \text{trace}(M)^2$

$\alpha$ : constant (0.04 to 0.1)



“Edge”

$R < 0$

“Corner”

WeChat: cstutorcs  $R > 0$

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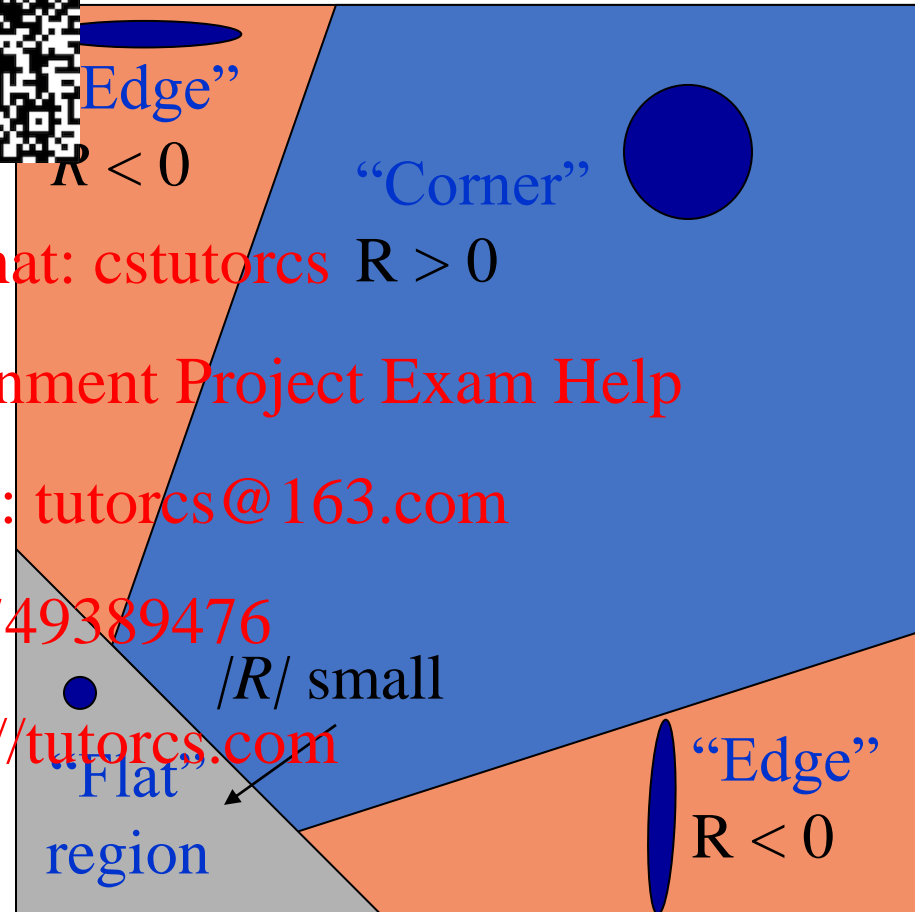
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$|R|$  small

“Flat”  
region

“Edge”

$R < 0$



# Harris Detector: Steps

- Compute Gaussian derivatives at each pixel
- Compute second moment matrix  $M$  in a Gaussian window around each pixel
- Computer corner response  $R$
- Threshold  $R$
- Find local maxima of response function (nonmaximum suppression)



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C.Harris and M.Stephens. [“A Combined Corner and Edge Detector.”](#)  
*Proceedings of the 4th Alvey Vision Conference*: pages 147—151, 1988.

# Harris Detector: Steps

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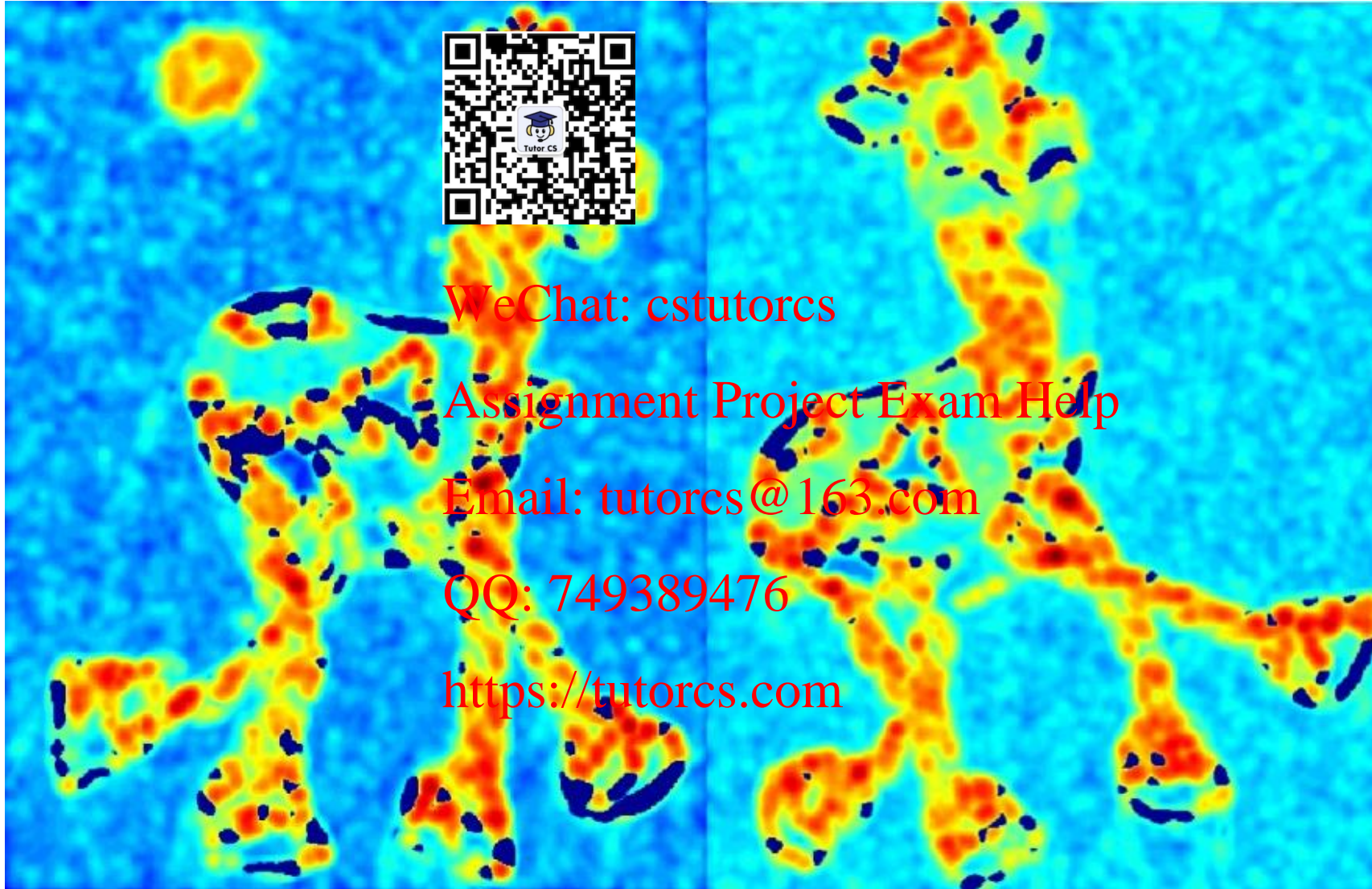
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# Harris Detector: Steps

- Compute corner response  $R$  程序代写代做 CS编程辅导





# Harris Detector: Steps

- Find points with larger corner response:  $R > threshold$



# Harris Detector: Steps

- Take the points of local maxima of  $R$



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# Harris Detector: Steps

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# Harris Detector: Steps

- We want corner locations to be *invariant* to photometric transformations, and *covariant* to geometric transformations.
  - **Invariance**: image is transformed, corner locations do not change
  - **Covariance**: if we have two tilted versions of the same image, features should be detected in corresponding locations.

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# Affine Intensity Change

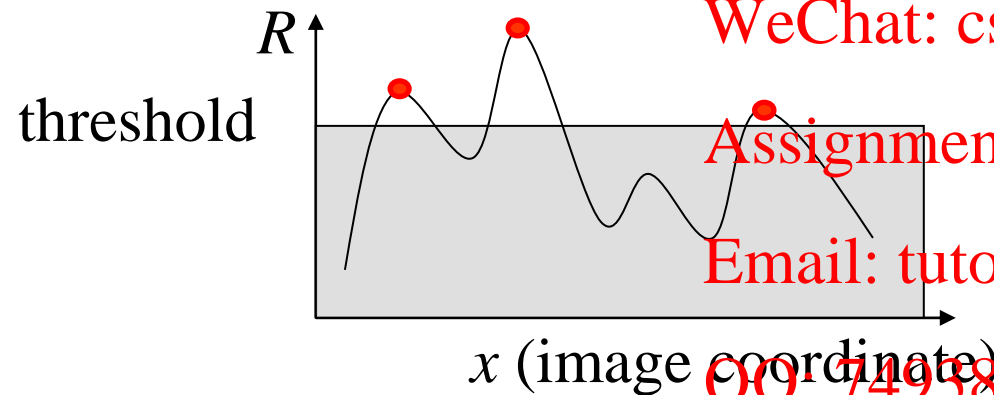
- $I \rightarrow aI + b$



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- Only derivatives are used  $\Rightarrow$  Invariant to intensity shift  $I \rightarrow I + b$

- Intensity scaling:  $I \rightarrow aI$

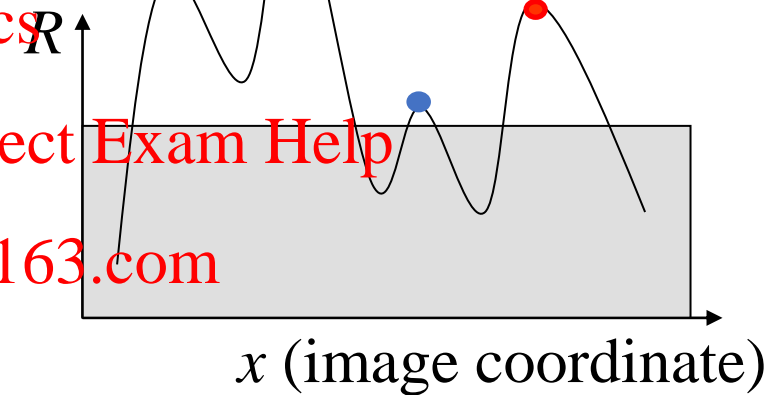


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*Partially invariant to affine intensity change*



# Image Translation



- Derivatives and window function are shift-invariant

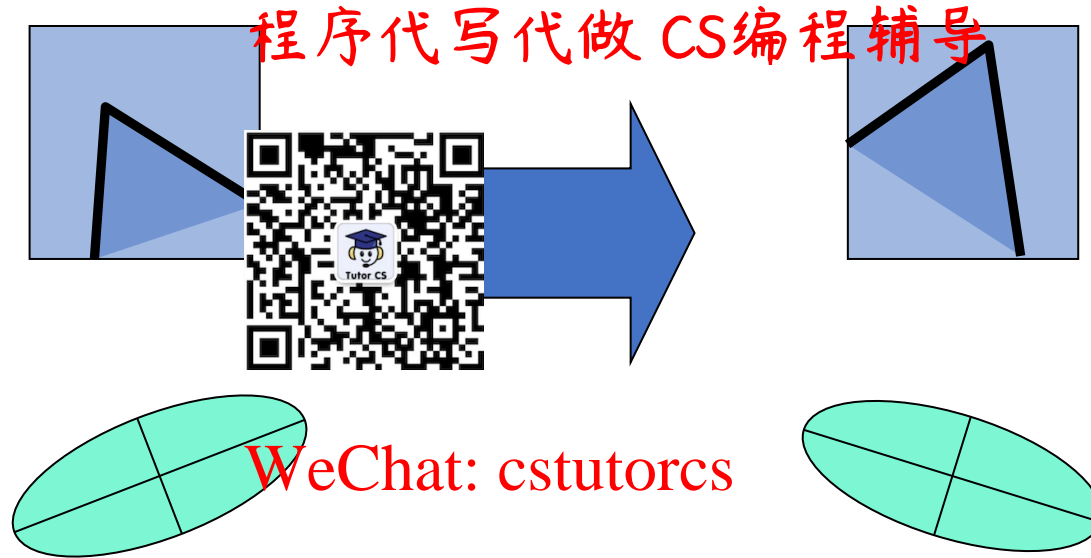
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Corner location is covariant w.r.t. translation

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# Image Rotation



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- Second moment ellipse rotates, but its shape (i.e., eigenvalues) remains the same

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Corner location is covariant w.r.t. rotation

# Scaling

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Corner

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All points will be classified as edges

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Corner location is not covariant to scaling!

# Summary

- Why we need feature extraction? What are the applications of feature extraction?
- What are the characteristics of good features?
- Describe the basic idea of corner detection
- How to decide whether a point is in a flat region, on an edge, or a corner according to the two eigenvalues of the second moment matrix?
- Describe the steps of Harris detector
- What is Invariance and Covariance?
- Is affine intensity change invariant? Is image translation, rotation, scaling covariant?



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