

#### 程序代写代做 CS编程辅导

# CMT1@ ual Computing

II.1 Transformations
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Assignment Project Exam Help

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#### Overview

- ➤ Model transformations cs编程辅导
  - 2D/3D linear transformations
  - 2D/3D affin prmations
- ➤ Homogeneo **<b>日 基基**dinates
  - Homogeneous affine transformations
- > Coordinate transformations Exam Help
  - Reference frames tutorcs@163.com
  - Object vs. Frame Transformations
  - Camera Transformation https://tutorcs.com
- OpenGL transformations

#### **Model Transformations**

> Transforming an object: transforming all its points



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> Transforming a polygoihalutarde ! fransforming its vertices



#### **Basic 2D Transformations**

#### > Scale:

$$x' = x \cdot s_x$$
$$y' = y \cdot s_y$$

(mirror:  $s_x$  and/or間

> Rotate:

$$x' = x \cdot \cos \phi - y \cdot \text{Mine}\phi$$
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$$y' = x \cdot \sin \phi + y \cdot$$

> Shear:

$$x' = x + h_x \cdot y$$

$$y' = y + h_y \cdot x$$

> Translate:

$$x' = x + t_x$$

$$y' = y + t_y$$





 $y' = x \cdot \sin \phi + y \cdot \cos \phi$  Help

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x"https://tutorcy.com  $y'''' = y'' + h_v x'' + t_v$ 

### **Matrix Representations**

Matrices are *convenient* to represent linear transformations:  $\begin{cases} x' = s_x \cdot x & (x') \\ y' = s_y \end{cases} = \begin{pmatrix} s_x & 0 \\ 0 & s_y \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$ 

• Rotate: 
$$\begin{cases} x' = \cos \phi \cdot y & (x') \\ y' = \sin \phi \cdot x + \cos \phi \cdot y & (y') \\ \text{WeChat: cstutores} \end{cases} = \begin{pmatrix} \cos \phi & -\sin \phi \\ \sin \phi & \cos \phi \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

• Shear:  $\begin{cases} x' = x + Assignment \\ y' = y + h \cdot x, \\ y' = y + h \cdot$ 

> Efficient due to hardware matrix multiplication

#### **Linear Transformations**

- ➤ Linear transformations are combinations of 程序代写代做 CS编程辅导 scaling, mirroring, rotation, shearing
- - Satisfies  $\mathbf{T}(s_1\mathbf{v}_1) = s_1\mathbf{T}(\mathbf{v}_1) + s_2\mathbf{T}(\mathbf{v}_2), s_1, s_2 \in R$
  - Origin maps to
  - Lines map to lines Chat: cstutorcs
  - Parallel lines remain parallel
  - Ratios are preservee Project Exam Help
  - Closed under composition of two or more linear transformations is a linear transformation)

$$T_0(T_1(T_2(v))) \equiv (T_0 \circ T_1 \circ T_2)(v) = T(v)$$

Translation is not linear transformation

#### **Affine Transformations**

- ➤ Affine transformations are combinations of 程序代与代数 CS编程辅导 Linear transformations (matrices)

  - •Translations (vec



$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} x \\ y \end{pmatrix} + \begin{pmatrix} t_x \\ t_y \end{pmatrix}$$

- General representation  $\begin{pmatrix} x' \\ stutor \begin{pmatrix} a \\ c \end{pmatrix} \begin{pmatrix} x \\ v \end{pmatrix} + \begin{pmatrix} t_x \\ t_y \end{pmatrix}$
- > Properties of affine transformations. Exam Help
  - Origin does not Becekswichten to be boomigin
  - Lines map to lines 0: 749389476
  - Parallel lines remain parallel
  - Ratios are preserved //tutorcs.com
  - Closed under composition

### **Homogeneous Coordinates**

- $\blacktriangleright$  Homogeneous coordinates in 2D 程序代写代做 CS编程辅导 (x, y, w) represents a point at position (x/w, y/w)
  - •(x, y, 0) represer
  - •(0, 0, 0) is not al
- > We need a 3rd co file for 2D points to represent translations solely, with matrices
- $\triangleright$  2D translation can be represented by a 3  $\times$  3 matrix: Assignment Project Exam Help

$$\begin{pmatrix} x' \\ \text{Email: tutorcs} \\ y' = 0 & 1 & t_y \\ 0 & 1 & t_y \\ 749389476_w \end{pmatrix} 3.\text{com}$$

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### **Homogeneous 2D Transformations**

Basic 2D homogeneous transformation matrices 程序代写代做 CS编程辅导

$$\begin{pmatrix} x' \\ y' \\ w' \end{pmatrix} = \begin{pmatrix} s_x & 0 & 0 \\ \vdots & \vdots & \vdots \\ s_x & 0 & 0 \\ \vdots & \vdots & \vdots \\ w \end{pmatrix} \begin{pmatrix} x \\ y \\ w \end{pmatrix}$$

• Shear:

$$\begin{pmatrix} x' \\ y' \\ w' \end{pmatrix} = \begin{cases} Assignment 1 toject Example 1 & h_x & 0 \\ 1 & h_x & 0 \\ Emaili & tutorcs @ 163.com \\ QQ: 749389476 \end{cases}$$

$$\begin{pmatrix} x' \\ y' \\ w' \end{pmatrix} = \begin{pmatrix} 1 & 0 & t_{x} \\ \text{https://tutorcs} \\ 0 & 1 & t_{y} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ w \end{pmatrix} com$$

### **3D Transformations**

- Same idea as 2D transformations

  - Affine transform  $\mathbf{p}' = \mathbf{T}\mathbf{p} + \mathbf{t}$
- Common 3D trans
  Common 3D trans

$$\begin{pmatrix}
s_x & 0 & 0 \\
0 & s_y & 0 \\
0 & 0 & s_z
\end{pmatrix}$$
We Chat: 
$$\begin{pmatrix}
\cos \phi & -\sin \phi & 0 \\
\sin \phi & \cos \phi & 0 \\
\text{stutorcs} \\
0 & 0 & 1
\end{pmatrix}$$

Assignment Project Exam Help Scale/mirror Rotate around Z axis

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Rotate around Y axis Rotate around X axis

### **Homogeneous 3D Transformations**

- Homogeneous coordinates in 3D:

   (x, y, z, w) represents 3D position (x/w, y/w, z/w)
  - (x, y, z, 0) repre
  - (0, 0, 0, 0) is not (0, 0, 0, 0)
- > Affine transforma resented by matrices

Identity

QQ: 749389476 Scale Mirror over *x* axis

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### Homogeneous 3D Rotations

Rotate around z axis Rotate around y axis

$$\begin{pmatrix} 1 & 0 & 0 & A_{ss}^{0} & \text{ignment Project Exam}^{t} & \text{Help} \\ 0 & \cos \phi & -\sin \phi & 0 & 0 & 1 & 0 & t_{y} \\ 0 & \sin \phi & \cos \phi & \text{Email: tutorcs@} & 163 & \text{com} & t_{z} \\ 0 & 0 & 0 & QQ. & 7493894760 & 0 & 0 & 1 \end{pmatrix}$$

Rotate around x https://tutorcs.comanslation

### **Matrix Composition**

- ➤ Transformations can be combined by matrix multiplication

  ➤ Using homogeneous coordinates all affine transformations
- - Matrix multiplicative:

$$\mathbf{p}' = (\mathbf{T}_0 \cdot (\mathbf{T}_1 \cdot (\mathbf{T}_2(\mathbf{p})) + (\mathbf{T}_1 \cdot \mathbf{T}_1) \cdot \mathbf{T}_1) \cdot \mathbf{T}_2)(\mathbf{p}) = (\mathbf{T}_0 \cdot \mathbf{T}_1 \cdot \mathbf{T}_2)(\mathbf{p})$$

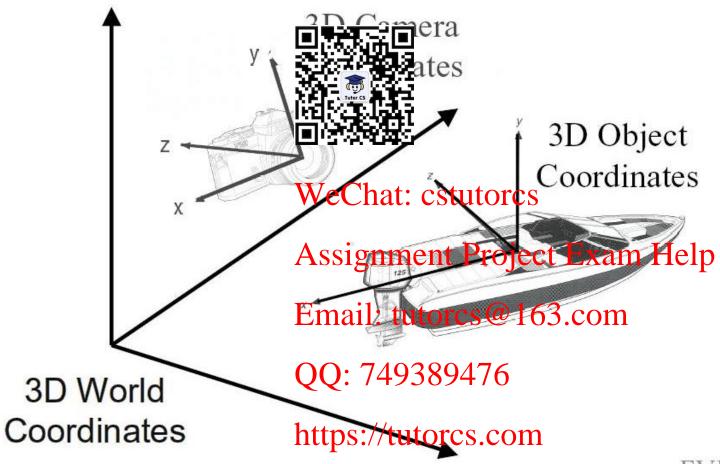
- Simple way to compline: transformations
- Only one matrix multiplication to transform vertices
- > Beware: order of transformations matters
  - Matrix multiplication is hot commutative:

$$(\mathbf{T}_1 \cdot \mathbf{T}_2) (\mathbf{p}) \neq (\mathbf{T}_2 \cdot \mathbf{T}_1) (\mathbf{p})$$

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### Reference Frames

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FVFHP Figure 6.1

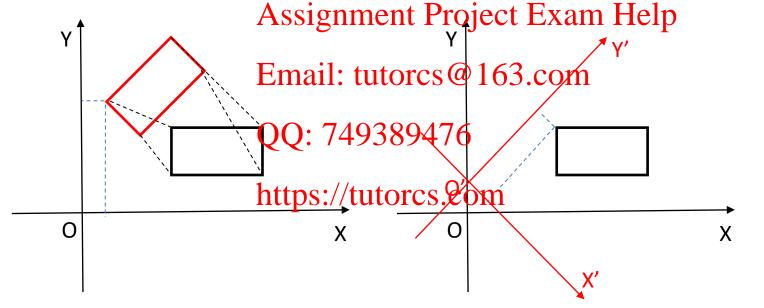
#### **Coordinate Transformations**

- ➤ Scenes are defined in a world-coordinate system
  ➤ Objects in a scene are represented in a local object
- Objects in a scene are represented in a local object coordinate system
  - Transform local ates into other local coordinates
- A camera is represented in a camera coordinate system
   A scene is viewed by a camera from an arbitrary
  - A scene is viewed by a camera from an arbitrary position and orientaltionorcs@163.com
  - Transform world-6091dinates into camera coordinates
- Transformation from object coordinate system to camera coordinate system can be represented by a signal matrix called model-view matrix in OpenGL.

## **Object vs. Coordinate Transformations**

- ➤ Object transformations transfer a object in a fixed coordinate system 程序代写代做 CS编程辅导
- Coordinate transferm an object's coordinates from the reduced relative to another, while keep the object. So original position.

The coordinates of a object transformation can be obtained equivalently by a coordinate transformation



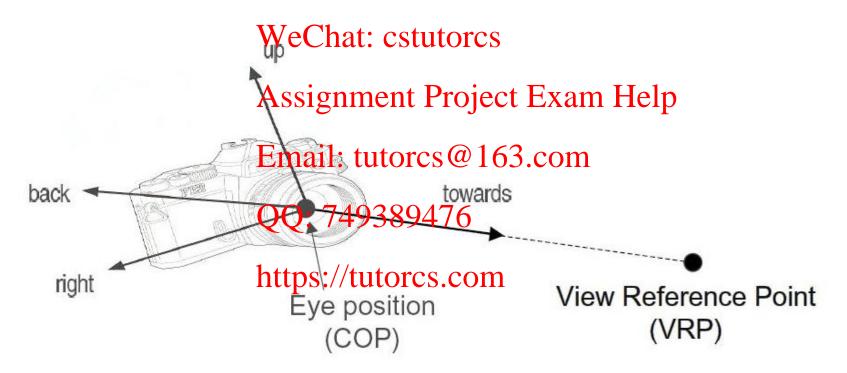
## **Object vs. Coordinate Transformations**

- Translate an object by (t, t, t) is equivalent to translate the reference frame by  $(-t_x, -t_y, -t_z)$
- $\blacktriangleright$  Rotate an object  $\blacksquare$  an axis by angle  $\alpha$  is equivalent to rotate the reference  $\blacksquare$  me around the same axis by angle  $-\alpha$ .
- Scale an object in direction by value s is equivalent to scale the reference frame in the same direction by value Assignment Project Exam Help



### Camera Analogy

- ➤ Define a *synthetic camera* to determine view of a scene 程序代写代做 CS编程辅导
  ➤ Camera parameters:
- - View direction ( vector, up vector)
  - Field of view (xfc)



#### **Camera Coordinates**

- ➤ Mapping from world to camera coordinates (*normalisation*)

   Origin moves to eye position

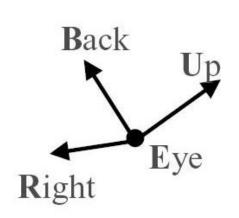
  - Up vector maps 

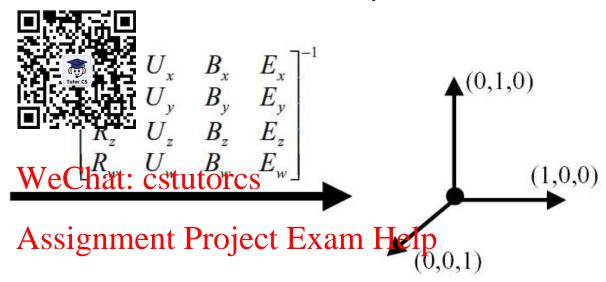
    | The properties of the content of the content
  - Canonical coordimites tem for camera coordinates
  - Convention is right
  - New versions of OpenGL adopts left-handed Frame WeChat: cstutorcs



#### **Camera Transformation**

➤ Transformation matrix maps camera basis vectors to canonical vectors in camera coordinate system





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world coordinates: 
$$(x_w, y_w, z_w, w_w)^{t}$$
  $M \rightarrow (x_c, y_c, z_c, w_c)^{t}$  https://tutorcs.com

#### **Derivation of Camera Transformation**

Let the camera transformation matrix be **M**, then because **R**, **U**, **B**, and **E** are transformed to [1 0 0 0]<sup>T</sup>,  $[0\ 1\ 0\ 0]^{\mathsf{T}}$ ,  $[0\ 0\ 1\ 0]^{\mathsf{T}}$ ,  $[0\ 0\ 1\ 0]^{\mathsf{T}}$ , respectively, we have

$$\begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} = M \begin{pmatrix} R_x \\ R_y \\ R_z \\ R_w \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} = M \begin{pmatrix} B_x \\ B_y \\ B_z \\ R_w \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} = M \begin{pmatrix} E_x \\ E_y \\ E_z \\ E_w \end{pmatrix}$$

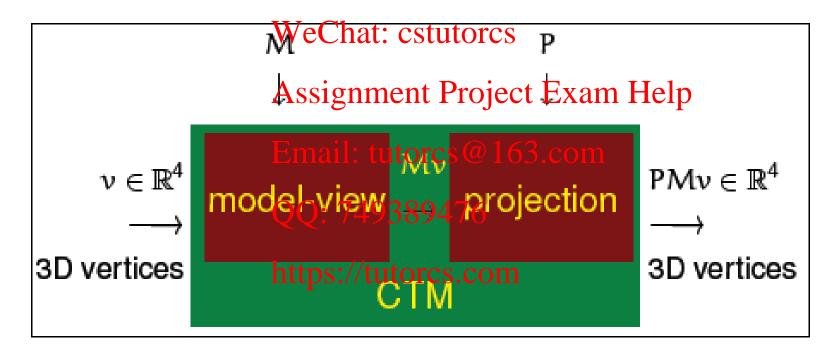
$$\Rightarrow \text{ Combine them together form the matrix equation}$$

- $\triangleright$  Note that **R**, **U**, and **B**'represent direction, so  $R_w = U_w = B_w = 0$
- $\triangleright$  **E** represents a point, so here  $E_w = 1$

#### **Current Transformation Matrix**

- ➤ Conceptually two 4×4 matrices:

   a model-view and a projection matrix in pipeline
  - Both matrices 但認識。current transformation matrix (CTM)
  - All vertices are med by the CTM



### **OpenGL Transformations**

- Early versions of OpenGL use some functions to represent transformations (matrix computations)
- > Current OpenGL w. ers needs the programmers to write their own transaction code

  Maths libraries for computations are available
- - vecmath from jaya package jayax.vecmath
- > An example simple matrix computation package is provided in the labs of this modified Exam Help
  - > Vec3.java, Vec4Ejava; Matesjava, 3Transform.java

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## Matrix Representation in OpenGL

- ➤ OpenGL uses 4x4 matrices to represent transformations ➤ A matrix is stored in a vector in the program
- ➤ Two orders to stor □ □ ix in a vector
  - Row major (in it ow order)
  - column major ( n by column order)
- > We use row major order in the package provided
- > Shaders use column major order to represent matrices
- > Post-multiplying with column Project Exam Helpproduces the same result as mainultiply in powith row-major matrices.

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#### **Transform Class**

- ➤ In Transfrom.java, a class Transform is defined. T is the transformation matrix
- Constructor Transpire or function initialize() will assign T as an identity metable
- Functions scale(), rotateX(), rotateY(), rotateY(), rotateZ() perform as their names defined
- rotateA() performs rotation around an arbitrary axis
- reverseZ() is to convert right-frame to left-hand frame Email: tutorcs@163.com
- > lookAt() is to locate the samera in the scene
  - Transform the model coordinates into camera frame
- > ortho(), frustum(), and perspective() perform projection transformation (discuss later)

### Function scale()

- ➤ Pre-multiply the current matrix T by a scaling transformation matrix

  \*\*Total Company of the current matrix T by a scaling transformation matrix T by a sca
- For scale(sx, sy, sz

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Current matrix is modified as:

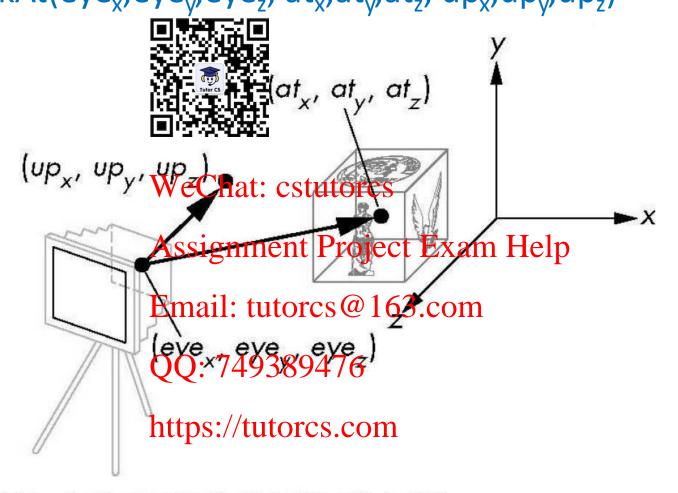
### Function scale()

Implementation of function scale(sx, sy, sz): 程序代写代做 CS编程辅导

```
public void scale sx, float sy, float sz) {
  for(int i=0;i<
                 [0][1]*sx;
        T.M[2][i] = T.M[2][i]*sz;
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               Assignment Project Exam Help
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               https://tutorcs.com
```

### lookAt()

Simulate gluLookAt() function in early versions of OpenGL void lookAt(eye<sub>x</sub>, eye<sub>y</sub>, eye<sub>z</sub>, at<sub>x</sub>, at<sub>y</sub>, at<sub>z</sub>, up<sub>x</sub>, up<sub>y</sub>, up<sub>z</sub>)



Angel: Interactive Computer Graphics 3E © Addison-Wesley 2002

#### **Use Transform class**

```
// Define a Transform程序代写优数 CS编程辅导
// Transformation matrix is initialised as Identity;
Transform T = new Tra:
// In display(), load
                           matrix
T.initialize();
//Do transformations
T.scale(scale, scale, Wellat: cstutorcs
T.rotateX(rx);
T.translate(tx, ty, 0); Assignment Project Exam Help
T.lookAt(0, 0, 0, 0, -100, 0, 1, 0); //default parameters
                   OO: 749389476
// Send model view matrix to shader. Here true for transpose
//means converting the row-major matrix to column major one
gl.glUniformMatrix4fv( ModelView, 1, true, T.getTransformv(), 0);
```

### Summary

- ➤ What is a reference frame? How can points in space be represented?
- ➤ What are linear ar 및 透透 transformations?
- What are homoge coordinates? For what are they used?
- List some common/basic linear and affine 2D/3D transformations and their representation for Cartesian and homogeneous coordinates: Ject Exam Help
- What is object transformation and what is frame transformation? What's their relation?
- How can one build more complex affine transformations from the basic transformations?