

Imperial College London – Department of Computing

MSc in Computing Science

580: Algorithms  
Tutorial: Dynamic Programming

1. The array  $A = [A_1, \dots, A_N]$  contains  $N$  integers.
  - (a) A *prefix subarray* of  $A$  is any continuous subarray that starts with  $A[1]$ . Write a  $\Theta(N)$ -time algorithm to find the greatest sum of any prefix subarray of  $A$ .
  - (b) The greatest sum of *any* continuous subarray of  $A$  can be found as follows. For each position  $i$  in the array, find  $s_i$ , the maximum sum of any continuous subarray starting at  $i$ . The solution is then the maximum of those  $s_i$  values. There are  $N$  such values, so this method will take  $\Theta(N^2)$  time using your answer for (1a). This is referred to as a *naïve* solution.

By considering the structure of the naive solution, design a  $\Theta(N)$ -time solution to the problem.

WeChat: cstutorcs