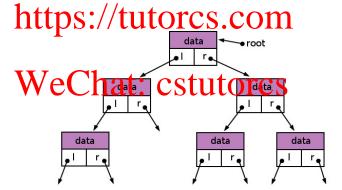
Dynamic Data Structures

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January 2018



Dynamic Data Structures

Assignmentur Projectudes salaton help The problems seen so far involved fixed length lists

- In most languages we have a simple way to implement this efficiently
 - https://tutorcs.com
- Our algorithms assumed some sort of array type was available

Other problems require dynamic data structures such as

- Lists, Water and Quates CStutorcs
- Sets and Dictionaries

These are designed to hold variable, essentially unlimited amounts of data.

Ordered Data Structures

A *list* is an ordered collection of {nodes, items, elements}.

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A list might support operations such as

push adds an element to the end of the list top removes the fact element of the list unshift adds an element to the front of the list insert adds an element at a given position vove removes the element at a given position iterate returns the items in order

- Plus sorting, searching, copying, joining, splitting ...
- The most appropriate implementation depends on which operations are needed.

Stacks

A *stack* is a last-in first-out (LIFO) list.

Assignment Project Exam Help pop for removing elements

• Stacks are usually pictured as a vertical (stacked!) structure https://tutorcs.com



• Stacks support recursive algorithms including fundamental operations such as calling subprocedures and evaluating arithmetic expressions

Stacks

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Question

How would tot in plement that the orcs. com

- Must be able to add "unlimited" objects
- Push and Pormist implement LIFO behaviour WECNAL CSTUTOICS

Performance of Push

Question

Aignsisochemient of opensyle of the work asmine Help complexity of push?

- Assume: time to insert (copy, add) one object to array is c
- · Assumet trips capacitus torcs.com

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Performance of Push

Revised Question Air Salganne mt : Ptroject tire x nam of the lp

- Assume: initial capacity is 4
- Assume; time to insert (copy, add) one object to array is ϵ **nttps:**//tutorcs.com

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Amortisation

Abstime for Whather the Project Exam Help A single push is effectively a constant time operation

- More correctly: push is amortised $\Theta(1)$
- No htetps://tutorcs.com

Amortisation

- Related to accountancy method used to defer large costs
- · Amortised Columbia atider C Setupt Of the Stions
- Cost of individual ops is "amortised" across the sequence
- Unlike accountancy, must never be in debt

Amortised Analysis

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- Pick a representative subsequence
- Subsequence is some "cycle" that repeats
 Pickandar outsed cost tartoperaces. COM
- Show that paying amortised cost covers all costs (never in debt)

Exercise WeChat: cstutorcs

Find a representative cycle (subsequence) of pushes into the stack and show that the amortised cost of 3c covers all costs.

Amortised Analysis

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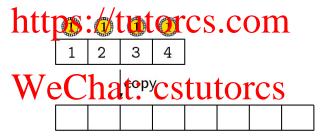
End cycle when ...

Amortised Analysis

Argument only works because array is initially empty and size is doubled

Assignment copy we always push of more Exam Help

This is how cost is covered



Multiplying by any factor will do - will affect amortisation constant

Queues

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- The earliest one added (FIFO Queue)
- The one with highest priority (Priority Queue) https://tutorcs.com

Questions

- How could you implement a priority queue (PQ)?
- Giver A collowing your design that contains V objects, what would be the worst case time to add a new object? (Each object has a key attribute that determines its priority.)

Priority Queue Design

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Heap: a Tree in an Array

We want to know where the "end" of the tree is:

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- Track end using "stack pointer"
- Navigate by indices
- Leaving [0] Chark means: CStutorcs

 - children of a[n] are a[2*n] and a[2*n+1]

Exercise

How should a new object be added to a max binary heap? (i.e. the greatest key should be at the root).

Heap: a Tree in an Array

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- Trackend pring: stack pointer CS. COM
- Leaving a[0] blank means:

 - parent of a full is a [n/2]
 White of a n ada [20] Stutton ICS

Exercise

How should the object with the greatest key be removed from a max binary heap?

Binary Heap Performance

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Question

Given a heap containing N objects, what is the time complexity for adding or removing one object?

Heapsort

Heaps also provide us with the Heapsort algorithm (JWJ Williams, 1964) ASSIGNMENT Project Exam Help

- Create an empty heap H
- Rempye each element of Land add it to H
- Remove each element of H and add it to L
- HALT
- What Cueles in Part: CStutorcs
- Performance is again $\Theta(Nlog_2N)$
- Can also be implemented in place by setting up list and heap partitions within a single array

Design

Sets

Assignment of the form of the large of the l

- Should have "unlimited" capacity
- Want to put and get, by key
- A kentupsany/tytutorices.crom

Questions

- How Yould you implement a set? tutores
 Given a set following your design that contains N objects, what would be the worst case time to get the object with key k?

A Search Tree?

A tree will divide the data but need a different ordering

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- Start at the root (it's a tree)
- Go right: find/add larger keys
- Go left: find/add smaller keys

Binary Search Tree

A selimary Search Tree Project Exam Help

• Go left: find/add smaller keys

Exercise https://tutorcs.com

• Draw the (integer) binary search tree implied by the following code:

```
bst = new BST

Wse [5,3,2)1,60,81,410TCS

for i = 0 to 8

bst.put(keys[i])
```

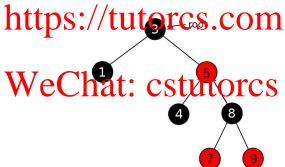
• What is the worst case time complexity of the put procedure?

Red-Black Trees

Red-Black Trees are binary search trees that maintain balance

As δ is an interpretable purchasing a BST takes O(N) time in the worst case

• The branches of a balanced tree remain as short as possible



Red-Black Tree Properties

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A binary search tree T is a red-black tree iff T satisfies the following five properties:

- All nattosting tultorics ecom
- 2 The root node is black
- Every leaf (all null) is black
- Both Mider of hatiode Gratuatores
- All paths from a node to a descendant leaf contain the same number of black nodes

A node is inserted using the ordinary BST procedure

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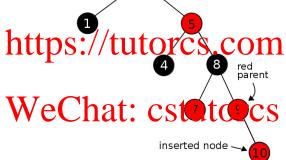
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• A new node is always colored red

inserted node ~

The insertion may result in a violation of the red-black tree properties

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- The root might be coloured red
- A red node might have a red child

Either recolour $\Theta(1)$ nodes

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- There is still a red node with a red parent
- The problem has moved closer to the root (continue)

Or perform a rotation of $\Theta(1)$ nodes and Stop

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- Reduces height of the tree
- Preserves key ordering

The properties are restored Assignment Project Exam Help https://tatorcsecom WeChat: estutores

Performance

Assignment Project Exam Help By maintaining the red-black tree properties, we have $h \leq 2\log_2(N+1)$

- Get procedure is the same as for BST
- · Heighten Shit / the treat of the Com

For Put, only the last part is different

- The extra work is still localised to one branch
 So, Put also uns in a Loga Cost mutorcs