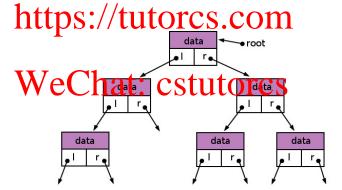
#### Dynamic Data Structures

## Assignment Project Exam Help

January 2018



#### Dynamic Data Structures

## Assignmentur Projectudes salaton help The problems seen so far involved fixed length lists

- In most languages we have a simple way to implement this efficiently
  - https://tutorcs.com
- Our algorithms assumed some sort of array type was available

Other problems require dynamic data structures such as

- Lists, Water and Quates CStutorcs
- Sets and Dictionaries

These are designed to hold variable, essentially unlimited amounts of data.

#### Ordered Data Structures

A *list* is an ordered collection of {nodes, items, elements}.

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A list might support operations such as

push adds an element to the end of the list top removes the fact element of the list unshift adds an element to the front of the list insert adds an element at a given position vove removes the element at a given position iterate returns the items in order

- Plus sorting, searching, copying, joining, splitting ...
- The most appropriate implementation depends on which operations are needed.

#### **Stacks**

A *stack* is a last-in first-out (LIFO) list.

## Assignment Project Exam Help pop for removing elements

• Stacks are usually pictured as a vertical (stacked!) structure https://tutorcs.com



 Stacks support recursive algorithms including fundamental operations such as calling subprocedures and evaluating arithmetic expressions

#### **Stacks**

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#### Question

How would tot in plement that the orcs. com

- Must be able to add "unlimited" objects
- Push and Pormist implement LIFO behaviour WECNAL CSTUTOICS

#### Stack Implementation

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- Array has fixed capacity
- Linked list has higher overheads https://tutorcs.com
- Can make array dynamic (variable size)
- Integer sp points to the top of the stack
- Update sp within Push and Pop

#### Dynamic Array-Based Stack

## Assignment Project Exam Help

```
if s.sp == k // array
s' = new stack of size 2k

fittpsto/k tutorcs.com
s'[i] = s[i]
s = s'
s[s.sp] = x
s.sp = x hat: cstutorcs
```

• push increases the capacity of the stack if it is full

#### Dynamic Array-Based Stack

```
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if s.sp < k/2  // array is less than half full

s' = new stack of size k/2

for it = 0 to k/2 - 1

for it = 0 to k/2 - 1

s = s'

s.sp = s.sp - 1

returns sphat: cstutorcs
```

- pop decreases the capacity if it is too big
- a full implementation should have a minimum size

#### Performance of Push

#### Question

## Aigraisachennieint of peropette for asmine Help complexity of push?

- Assume: time to insert (copy, add) one object to array is c
- Assumet tripias capacituis tores.com

The time taken for pushing objects is:

• "WeChat: cstutorcs

- So:
  - Worst time to push a single object is Nc
  - So T(N) = O(N)
  - Want to reflect fact that most pushes are not O(N)

#### Performance of Push

### Assignment Project Exam Help Given an Empty stack, what is the worst case time to push N objects?

- Assume: initial capacity is 4
- Assumet tipeso in set (140) at the She con 110 array is c

The time taken for the each push is still:

- c, c, we chart: cstutorcs
   For N pushes the worst single push is NC
- $T(N) = O(N^2)$

However, this is a big overestimate

#### Performance of Push

## Abstright Project Exam Help $T(N) = Nc + (4c + 8c + \cdots + (N/2)c + Nc)$

#### where https://tutorcs.com

- the first No is the cost of writing N elements
- the rest is for copying to new arrays

- $T(N) \le 3Nc 4c$
- T(N) = O(N)

#### Amortisation

## Abstime for Whather the Project Exam Help A single push is effectively a constant time operation

- More correctly: push is amortised  $\Theta(1)$
- No htetps://tutorcs.com

#### **Amortisation**

- Related to accountancy method used to defer large costs
- · Amortised Columbia atider C Setupt Of the Stions
- Cost of individual ops is "amortised" across the sequence
- Unlike accountancy, must never be in debt

#### Amortised Analysis

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- Pick a representative subsequence
- Subsequence is some "cycle" that repeats
  Pickandar outsed cost tartoperaces. COM
- Show that paying amortised cost covers all costs (never in debt)

#### Exercise WeChat: cstutorcs

Find a representative cycle (subsequence) of pushes into the stack and show that the amortised cost of 3c covers all costs.

#### **Amortised Analysis**

• Start after any expensive push

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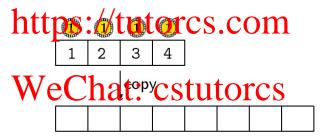
- Cheap pushes each put 2c in the bank
- Have enough to cover extra costs when next expensive push occurs
- (If you started with a copy you are immediately over budget)

#### **Amortised Analysis**

Argument only works because array is initially empty and size is doubled

### Assignment copy we always push of more Exam Help

This is how cost is covered



Multiplying by any factor will do - will affect amortisation constant

#### Queues

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- The earliest one added (FIFO Queue)
- The one with highest priority (Priority Queue) https://tutorcs.com

#### Questions

- How could you implement a priority queue (PQ)?
- Giver A Per ollowing your design true to objects, what would be the worst case time to add a new object? (Each object has a key attribute that determines its priority.)

#### Priority Queue Design

If we maintain a total ordering of the queue:

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- Can search a sorted array quickly but have to shift existing objects
- Prinding position in a linked list is O(N)https://tutorcs.com

  9, 8, 7, 6, 3

  Max Priority Queue

  remove items

  Wechat: cstutorcs

Do not actually need total ordering.

- Queue does not support indexed access
- Just want to find object with highest priority

#### Priority Queue Design

Solution is to divide and conquer the data

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- Key Property: Maintain order within each branch
- Highest (or lowest) key will be at the root
- Behaves like lots of mini queues

#### Priority Queue Design

Solution is to divide and conquer the data

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### We@hat.4cstutorcs

#### Question

A new object could go in any branch. (Do you agree?) So, where should it go? Why?

#### Heap: a Tree in an Array

We want to know where the "end" of the tree is:

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- Track end using "stack pointer"
- Navigate by indices
- Leaving [0] Chark means: CStutorcs

  - children of a[n] are a[2\*n] and a[2\*n+1]

#### Exercise

How should a new object be added to a max binary heap? (i.e. the greatest key should be at the root).

Adding an object to the heap Assignment Project Exam Help https://tutorcs.c We hat 4 cst utorcs

- Restore the "shape"
- Then restore the order

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- Restore the "shape"
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- Restore the "shape"
- Then restore the order

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- Restore the "shape"
- Then restore the order

#### Heap: a Tree in an Array

## Assignment Project Exam Help

- Trackend pring: stack pointer CS. COM
- Leaving a[0] blank means:

  - parent of a full is a [n/2]
     White of a n ada [20] Stutton ICS

#### Exercise

How should the object with the greatest key be removed from a max binary heap?

To remove the object at the root

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- Restore the "shape"
- Then restore the order

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- Restore the "shape"
- Then restore the order

To remove the object at the root

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- Restore the "shape"
- Then restore the order

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- Restore the "shape"
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- Restore the "shape"
- Then restore the order

#### Binary Heap Performance

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#### Question

Given a heap containing N objects, what is the time complexity for adding or removing one object?

#### Binary Heap Performance

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Both operations are  $O(\log_2 N)$ 

- Height of the heap is  $\Theta(\log_2 N)$
- Each operation confined to one branch

#### Heapsort

## Heaps also provide us with the Heapsort algorithm (JWJ Williams, 1964) Assignment Project Exam Help

- Create an empty heap H
- Rempye each element of Land add it to H
- Remove each element of H and add it to L
- HALT
- What Cueles in Part: CStutorcs
- Performance is again  $\Theta(Nlog_2N)$
- Can also be implemented in place by setting up list and heap partitions within a single array