Assignment Project Exam Help Dr Timothy Kimber

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Introduction

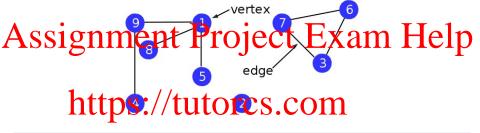
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- We have already seen how trees are used as data structures
- All sorts of problems can be modelled using graphs
- Networks, images, programs, anything involving related objects

Graph Terminology

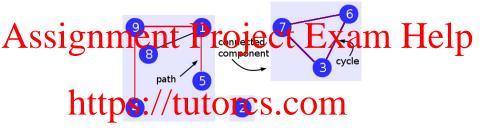


Definition

A graph C sapar C where C is a finite set (of objects) and E is a binary relation on C. Elements of C are called vertices and elements of E are called edges.

- E is a set of pairs of vertices: $\{u, v\}$ such that there is an edge between u and v
- Vertices u and v are adjacent if there is an edge $\{u, v\}$

Graph Terminology

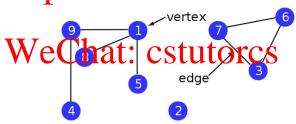


- A path from v_1 to v_n , written $v_1 \leadsto v_n$, is a sequence $\langle v_1, v_2, \ldots, v_n \rangle$ such there is a left $\{v_1, v_2, \ldots, v_n\}$
- A cycle exists if there is a path from v to v, containing at least 4 vertices, for some vertex v
- Vertex v is reachable from vertex u if u = v, or if there is a path $u \rightsquigarrow v$
- A connected component (also just called a component) is a set of vertices all reachable from each other

Graph Representation

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- A graph vertex is connected to 0-to-many other vertices
- Going to assume that |V| is fixed | TUTOTCS.COM



Graph Representation

Two common ways:

• Adjacency Matrix: $adj_{uv} = 1$ if there is an edge $\{u, v\}$, else 0

Adjacency lists good for sparse graphs https://tutorcs.com

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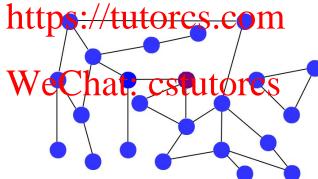
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Graph Search

Question

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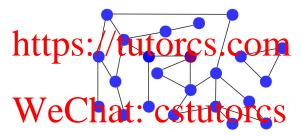
- Searching a graph is like iterating through an ordered structure
- Want to use data in the graph for some computation



Graph Search Actions

Searching a graph has two actions:

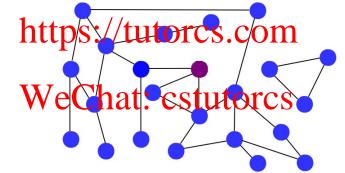
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- Visiting means using the vertex: includes finding further vertices
- Vertices are visited in the order they are first found
- Vertices are coloured when they are first found/visited

Breadth-First Search

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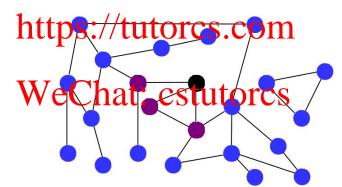
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Breadth-First Search

In breadth-first search

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• Result: search proceeds gradually down every path at the same rate



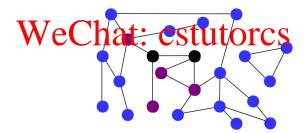
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BFS Procedure

Question

As significant and vertex of the Exam Help

- g.adj[u] returns list of vertices
- g.vertices is number/of vertices
- Objective: find all reachable vertices (will add actions later)



Breadth-First Search

```
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   q = new Queue(s)
                        // FIFO queue
   while q is not empty
       tps. ditutores.com
      if not found[v]
                        // avoid loops
       found[y] = true
```

- The use of a (FIFO) queue is characteristic of BFS
- By convention only search from given s

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Shortest Paths

BFS searches all paths at the same rate, so ...

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How would you modify the BFS procedure to find the length (number of edges) of the shortest path from s to every other vertex?

```
BFS (Input: graph g: //tutorcs.com
     found = new boolean[g.vertices]
     q = new Queue(s) // FIFO queue while not mett: CStutorcs
       u = q.remove()
       for v in g.adj[u]
         if not found[v]
                                  // avoid loops
           found[v] = true
           q.add(v)
```

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Shortest Paths

```
BFS (Input: graph g, vertex s)
 ssignment Project Exam Help
   dist.fill(-1)
   dist[s] = 0
   while the continuous com
    for v in g.adj[u]
      if dist[v] == −1
                       // not found
       VEC'hat." cstutorcs
```

- The distance is recorded when a vertex is (first) found
- Arrays of size |V| like dist are also common in graph search
- Unreachable vertices have dist[v] = -1

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Time

gament Project Exam Help take?

```
BFS (Inphterps: //tutorcs.com
    found = new boolean[g.vertices]
    q = new Queue(s)
    while a is not empty
           eChat: cstutorcs
      for v in g.adj[u]
       if not found[v]
         found[v] = true
         q.add(v)
```

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BFS Time Complexity

Each vertex is added and removed from the queue exactly once

Assignmentus Project Exam Help • Each edge contributes exactly two vertices to the adjacency lists

• Time depends on both variables: O(V + E)

```
found = new boolean[g.vertices]

q = new Quexe(s)

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u = q.remove()

for v in g.adj[u]

if not found[v]

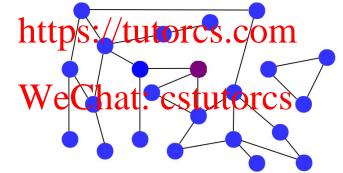
found[v] = true

q.add(v)
```

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Depth-First Search

Question Assignment Project Exam Help



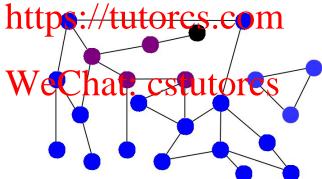
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Depth-First Search

In depth-first search

Assignment broken to the content of the content of

 Result: search follows a single path as far as possible and then backtracks to the last alternative path



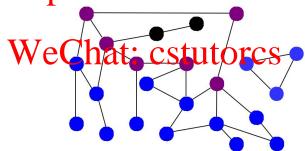
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DFS Procedure

Question

How would you implement Project Exam Help

- Assume g.adj[u] returns list of vertices
- · Objective find all hereignstores.com



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Depth-First Search

```
DepthFirstSearch (Input: graph g)
 ssignment Project Exam Help
     if not found[v]
      DFS(g, v, found)
      https://tutorcs.com
DFS (Input: graph g, vertex s, array found)
    found[s] = true
    for Wie Caplet: cstutorcs
       DFS(g, v, found)
```

- DFS can use call stack instead of explicit queue
- Restart until whole graph searched (or not)

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An Application

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Depth-First Search

```
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 if parent[v] == -1
                      // not found
   parent[v] = u
   ittbs:adyctictores.com
 else if parent[u] != v
                      // cycle detected
  return false
***WeChat: cstutorcs
```

- A cycle exists if v was already found, unless it is u's parent
- Since u was just found, and not from v, the edge $\{u,v\}$ completes an alternative path to u from the source

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For a connected graph with V vertices and E edges, how long does DFS take?

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```
DFS (Input: graph g, vertex s, array found)
```

found[s] = true

```
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```

DFS(g, v, found)

DFS Time Complexity

Assissamenton Project Exam Help • Each adjacency list is used exactly once

- Each edge contributes exactly two vertices to the adjacency lists
- Timhteps: Htutores.com

```
DFS (Input: graph g, vertex s, array found)
    for wing and salt: CStutorcs
      if not found[v] runs 2E times
        DFS(g, v, found)
```

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