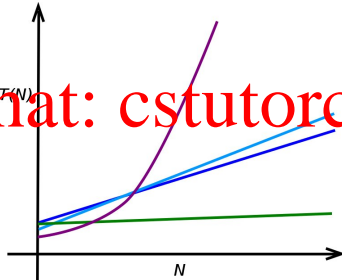


# Assignment Project Exam Help

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January 2018  
<https://tutorcs.com>

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# Course Outline

## The lecturer

- PhD in Computational Logic (Imperial)
- 5 years as Teaching Fellow/Senior Teaching Fellow
- Also teach Prolog to the MAC and Specialism classes

## The structure

- 28 hours of interactive lectures (weeks 2–9)
- Sessions include unassessed group and individual exercises
- Two assessed exercises (one in Java) (10%)
- A 2-hour written examination *next term* (90%)

## Books

- *Introduction to Algorithms*, Cormen et al., 3rd edn, 2009.
- *Algorithms*, Sedgewick & Wayne 4th edn, 2011.

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# Intended Learning Outcomes

At the end of this module YOU will be better able to ...

- 1 Communicate with other engineers about how to solve a computational problem\*.
- 2 Organise and manage computational resources.
- 3 Deploy known solutions to common problems.
- 4 Create original solutions to problems using sound general approaches.
- 5 Design appropriate data structures.
- 6 Explain properties of a solution, existing or original, to customers.
- 7 Analyse performance of code using established engineering techniques and terminology.

\*e.g. at an interview

## Course Summary

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This course: [How To Write Good Programs](#)

A [good](#) program...

- Always gives some output (terminates)
- Always gives a correct output (sound)
- Gives an output for every possible input (complete)
- Uses as few [resources](#) as possible

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## Aims

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This course is concerned with the resources consumed by your programs, principally **space** and **time**.

Questions To Answer

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- How much time/space does a program use?
- What kind of program uses least time/space?

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These questions are a bit harder to answer for time, but that is what we are usually most interested in, so that is where we will start.

# An Algorithm

Example (Sequence Search)

Input: a sequence  $L = \langle a_1, \dots, a_N \rangle$  of  $N$  integers, and an integer  $k$

Output: *True* if  $k$  is in  $L$ , *False* otherwise

Simplification: assume  $L$  is ordered

Procedure: SimpleSearch (Input: seq  $L$ , int  $k$ )

```
1 for each  $e$  in  $L$ 
2   if  $e == k$ 
3     return True
4 return False
```

## Input Cases

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When analysing an algorithm's performance it is essential to be clear what input cases are being considered. Most often this will be one of

- Best case (least possible time/space consumed)
- Worst case (greatest possible time/space consumed)
- Average case (see later)

Later, you will see how to combine these analyses to describe performance for any input.

## Formal Analysis (Worst Case)

- The input has  $N$  elements
- The cost (time taken) for line  $i$  is represented by  $c_i$ .
- We know exactly how many times each instruction happens (only worst case considered).

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Simple Search (Input: seq  $L$  and int  $k$ )

	Cost	Times
1 for each $e$ in $L$	$c_1$	$N+1$
2     if $e == k$	$c_2$	$N$
3         return True	$c_3$	0
4 return False	$c_4$	1



## Simple Search (Worst Case)

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- So the running time, or **time complexity** for a worst case input of size  $N$  is

$$T(N) = c_1 + Nc_1 + Nc_2 + c_4$$

- so, <https://tutorcs.com>

$$T(N) = (c_1 + c_4) + (c_1 + c_2)N$$

- so,

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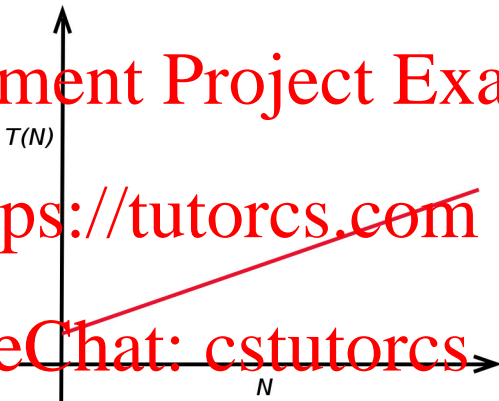
- There is a chunk of time  $a$  that is used for each element of  $L$
- There is a chunk of time  $b$  that is used just once

## Simple Search (Worst Case) Time Complexity

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- Longer sequences take more time
- The increase is linear
- $a$  and  $b$  will differ with language, hardware, load etc.

# Comparing Algorithms

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Given an input of size  $N$ , the worst-case time complexity for a range of algorithms that all solve Problem X is

- (A)  $T(N) = a_1 N + a_2$
- (B)  $T(N) = b_1 N$
- (C)  $T(N) = c_1 N^2 + c_2 N + c_3$
- (D)  $T(N) = d_1 N^3 + d_2$

where  $a_1, b_1, c_1$  and  $d_1$  are positive constants in terms of time, which is:

- the **best** algorithm? (why?)
- the **worst** algorithm? (why?)

# Highest Order Terms

For large  $N$  functions are dominated by their highest order  $N$  term

- Polylogarithmic functions include a term of the form  $(\log_b N)$
- Any degree  $d$  positive polynomial grows faster than any polynomial of degree less than  $d$ , and any polylogarithm

Definition (Polynomial) <https://tutorcs.com>

A polynomial of degree  $d$  (for  $d \geq 1$ ) is a function  $p(N)$  of the form

$$p(N) = a_0 + a_1 N + a_2 N^2 + \dots + a_d N^d$$

in which  $a_d \neq 0$ . The polynomial is asymptotically positive iff  $a_d > 0$ .

Exponential functions include a term of the form  $a^N$

- If  $a > 1$  then the function grows faster than any polynomial

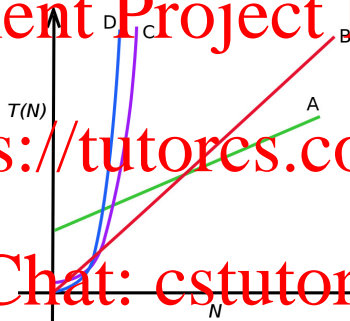
## Comparing Algorithms

Depending on the constants, the time complexities might look like this ...

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- Regardless of constant factors, D will take longest for large  $N$
- “Large  $N$ ” is usually small enough that we don’t want C or D

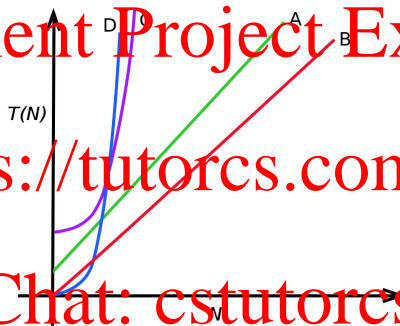
# Comparing Algorithms

Or like this ...

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- A and B are, in a sense, indistinguishable (constant factors)
- The value of large  $N$ , and if it exists, for A and B needs to be considered

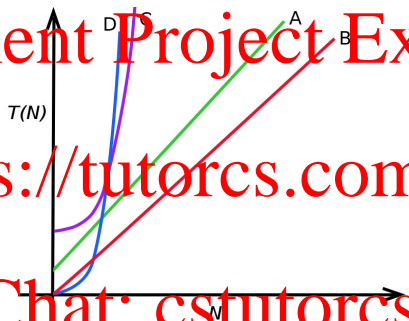
## Comparing Algorithms

So, we have clear(ish) goals

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- Any “ $N^3$  algorithm” is worse than any “ $N^2$  algorithm”
- Any “ $N^2$  algorithm” is worse than any “ $N$  algorithm”
- Unless we have big constants\*, or small  $N$
- \*Normally, we don't