February 2018

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Assignment Project Fxam Help

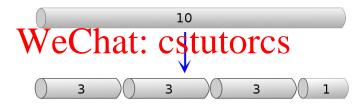
WeChat: CStutorcs

Back To Solving Problems

The Rod Cutting Problem

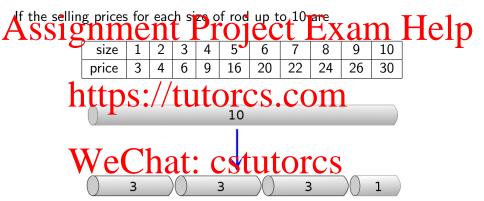
Assignment of roject left am Help They will cut the rods into smaller pieces to sell on

- Each rod size has a different market value
- What the grain ynt ever of the length N?



Is
$$p(3) + p(3) + p(3) + p(1) > p(4) + p(4) + p(2)$$
?

Instance of The Problem



Then the answer for N=10 is 32 $(1 \times 6 + 4 \times 1, \text{ or } 2 \times 5)$

Rod Cutting

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	size	1	2	3	4	5	6	7	8	9	10
1.	price	3	4/	6	9	16	20	22	24	26	30
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Question

Given an array of prices $P = [P_1, ..., P_k]$ and an integer N between 1 and k, how call N be defined as N between 1 and N become N between 1 and N become N between 1 and N become N between 1 and N betwee

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Possible httreps://tutorcs.com

- Choose some sizes $s = \langle s_1, \dots, s_i \rangle$ that sum to N
- (Values can repeat in s)
- Com We Chat: estutores
- For all possible s
- Update current best R(N) as you go

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size	1	2	3	4	5	6	7	8	9	10
price	3	4	6	9	16	20	22	24	26	30

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Question

How do you generate (only) sequences s that sum to N?

At this point it will be useful to trink about reducing the problem to solving one or more smaller subproblems.

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Choosing sizes:

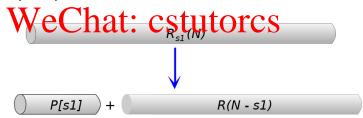
- Pick https://tutorcs.com
- Then s is s_1 followed by $\langle s_2, \dots \rangle$ that sum to $N-s_1$

Can now whe tructure of the problem: CStutorcs

- For each possible s_1
- Find all solutions for $N-s_1$, and combine with s_1
- Base case: only sequence that sums to 0 is ()



- Pick an s₁
- · Maxhtetpsing / tutores.com
- $R(N-s_1)$ is overall solution for rod length $(N-s_1)$
- One option per value for s_1



A Simple Recursive Solution

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return 0

elshttps://tutorcs.com

choices[i] = P[i] + SimpleRodCut(N-i, P) return max(choices)

• choices collects total for each s₁

- max finds the maximum of the choices

How does this run?

Simple Rod Cut — Reflection

WOW that was sloooooowww.

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Question

Solving R(0) takes $\Theta(1)$ time. What about R(N)?

Time for Simple Solution

The time taken by SimpleRodCut is

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$$T(0) = \Theta(1)$$

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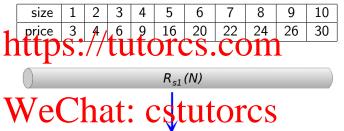
or

so
$$T(N) = \Theta(2^N)$$
.

- The running time grows exponentially.
- This is not a practical solution.

Divide & Conquer?

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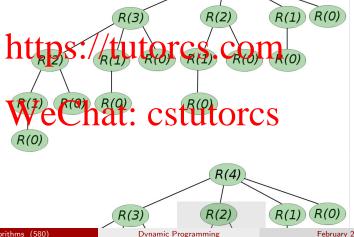


$$P[s1]$$
 + $R(N-s1)$

New Strategy

What is there that we can take advantage of?

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Dynamic Programming

Assignment Programming makes a space-time tradeoff Assignment Programming makes a space-time tradeoff the space of the spa

- Compute it once and save the answer in a table
- Check the table before computing each subproblem

This is called memorsation (we are making a note for later)

```
MemoisedRodCut(Input: N, P = [P_1, ..., P_k])

for the contact cstutorcs

return MemoiseAux(N, P, R)
```

R is the table to be filled in

Memoisation

```
MemoiseAux(Input: N, P = [P<sub>1</sub>,...,P<sub>k</sub>], R = [R<sub>0</sub>,...,R<sub>N'</sub>])

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return 0

if R[N] > 0

return R[N]./tutorcs.com

choices[i] = P[i] + MemoiseAux(N-i, P, R)

R[N] = max(choices)

return R[N] Chat: cstutorcs
```

- If R[N] was already computed (R[N] > 0) it is returned immediately
- Otherwise we compute it, save it, and then return it
- Also called Top Down (set out to solve the biggest problem)

The 'Bottom Up' Method

We know which problems depend on which others

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```
BottomUpRodCut(Input: N, P = [P<sub>1</sub>,...,P<sub>k</sub>])

R[1] LUDS: //tutorcs.com

for i = 1 to N

choices = [0,...,0]

two jet 1 jat categories

choices[j] Lyches Com

R[i] = max(choices)

return R[N]
```

• What is the running time?

Dynamic Programming

Project Exam Help • The problem has optimal substructure

- The problem has overlapping subproblems

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- the problem can be decomposed into subproblems
- an optimal solution uses optimal solutions to the subproblems

In rod cutting the Coth astiutic Stuttorics

•
$$P[i] + R[N - i]$$
, where $1 \le i < N$

and each R[N-i] was an optimal solution for N-i.

Optimal Substructure

Problems may appear to have potimal substructure when they depot expenses the problem (Problem (Problem (Problem (Problem (Parket)))) and the problem (Problem (Problem (Parket))) and the problem (Problem (Problem (Parket))).

Input: graph G = (V, E).

Input tertices · u// futorcs.com
Output: the simple path from u to v containing the fewest edges

Problem (by reighted Longest Path) Input: graph G = (1, E) CStutores

Input: vertices $u, v \in V$.

Output: the simple path from u to v containing the most edges

Optimal Substructure

A shortest path is composed of optimal solutions to subproblems

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The shortest path from 1 to 2 (via x) is

- shortest path from 1 to x
- plus the shortest path from x to 2

Optimal Substructure

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- Independent subproblem solutions do not make an optimal solution
- In an optimal solution the subproblems will interfere

Overlapping Subproblems

The second property we need when applying dynamic programming is

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- The same problems are generated over and over
- The subproblems must still be independent
- The set of all subproblems is the subproblem space
- The smaller the subproblem space the quicker the (dynamic) algorithm