



Australian  
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程序代写代做 CS编程辅导



## Functional Dependencies – Part 3

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### Finding Keys

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## A Bunch of Keys



- We will need keys for the normal forms later on.
  - A subset of the attributes of a relation schema  $R$  is a **superkey** if it uniquely determines all the attributes of  $R$ .
  - A superkey  $K$  is called a **candidate key** if no proper subset of  $K$  is a superkey.
    - That is, if you take any of the attributes out of  $K$ , then there is not enough to uniquely identify tuples.
  - **Candidate keys** are also called **keys**, and the **primary key** is chosen from them.

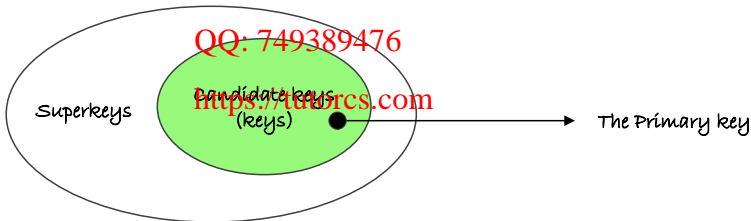
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## Finding Keys



- Given a set  $\Sigma$  of FDs on a relation  $R$ , the question is:

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**How can we find all the (candidate) keys of  $R$ ?**

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## 程序代写代做 CS编程辅导 Implied Functional Dependencies



- To design a good database, we need to consider **all possible FDs**.
- If each student works on one project and each project has one supervisor, does each student have one project supervisor?

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$\{\{\text{StudentID}\} \rightarrow \{\text{ProjectNo}\},$   
 $\{\text{ProjectNo}\} \rightarrow \{\text{Supervisor}\}\}$

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- We use the notation  $\Sigma \models X \rightarrow Y$  to denote that  $X \rightarrow Y$  is **implied** by the set  $\Sigma$  of FDs.

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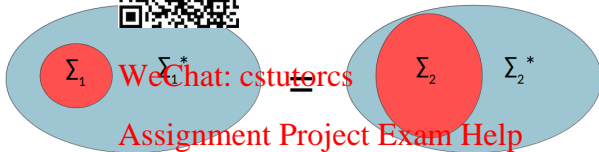
- We write  $\Sigma^*$  for all possible FDs **implied** by  $\Sigma$ .



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## Equivalence of Functional Dependencies

- $\Sigma_1$  and  $\Sigma_2$  are **equiv**  $\Sigma_2^*$ .



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- Example:** Let  $\Sigma_1 = \{X \rightarrow Y, Y \rightarrow Z\}$  and  $\Sigma_2 = \{X \rightarrow Y, Y \rightarrow Z, X \rightarrow Z\}$ . We have  $\Sigma_1 \neq \Sigma_2$  but  $\Sigma_1^* = \Sigma_2^* = \{X \rightarrow Y, Y \rightarrow Z, X \rightarrow Z\}$ . Hence,  $\Sigma_1$  and  $\Sigma_2$  are equivalent.

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- Questions:**

- Is it possible that  $\Sigma_1^* = \Sigma_2^*$  but  $\Sigma_1 \neq \Sigma_2$ ? **Yes**
- Is it possible that  $\Sigma_1^* \neq \Sigma_2^*$  but  $\Sigma_1 = \Sigma_2$ ? **No**



## 程序代写代做 CS编程辅导 Implied Functional Dependencies



- Let  $\Sigma$  be a set of FD. Whether or not  $\Sigma \models X \rightarrow W$  holds?  
We need to

- 1 Compute **the set of attributes** that are dependent on  $X$ , which is called the **closure** of  $X$  under  $\Sigma$  and is denoted by  $X^+$ .

- 2  $\Sigma \models X \rightarrow W$  holds iff  $W \subseteq X^+$

### Algorithm<sup>1</sup>

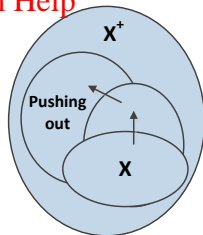
- $X^+ := X$ ;
- repeat until no more change on  $X^+$ 
  - for each  $Y \rightarrow Z \in \Sigma$  with  $Y \subseteq X^+$ ,  
add all the attributes in  $Z$  to  $X^+$ , i.e.,  
replace  $X^+$  by  $X^+ \cup Z$ .

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<sup>1</sup> See Algorithm 15.1 on Page 538 in [Elmasri & Navathe, 7th edition] or Algorithm 1 on Page 555 in [Elmasri & Navathe, 6th edition]



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## Implied Functional Dependencies – Example



- Consider a relation schema  $R = \{A, B, C, D, E, F\}$ , a set of FDs  $\Sigma = \{AC \rightarrow B, B \rightarrow C, AF \rightarrow B\}$  on  $R$ .
- Decide whether or not  $\Sigma \models AC \rightarrow ED$  holds.

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- We first build the closure of  $AC$ .

$(AC)^+ \supseteq AC$                       initialisation  
 $\supseteq ACB$                       using  $AC \rightarrow B$   
 $\supseteq ACBD$                       using  $B \rightarrow C$   
 $\supseteq ACBDE$                       using  $C \rightarrow E$   
 $= ACBDE$

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- Then we check that  $ED \subseteq (AC)^+$ . Hence  $\Sigma \models AC \rightarrow ED$ .

- Can you quickly tell whether or not  $\Sigma \models AC \rightarrow EF$  holds?



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## Finding Keys



- **Fact:** A key  $K$  of  $R$  defines a FD  $K \rightarrow R$ .

- **Algorithm**<sup>2</sup>:

**Input:** a set  $\Sigma$  of FDs on  $R$ . WeChat: cstutorcs

**Output:** the set of all keys of  $R$ .

- for every subset  $X$  of the relation  $R$ , compute its closure  $X^+$
- if  $X^+ = R$ , then  $X$  is a key. Email: supatkeys@163.com
- if no proper subset  $Y$  of  $X$  with  $Y^+ = R$ , then  $X$  is a key. QQ: 749389476

- A **prime attribute** is an attribute occurring in a key, and a **non-prime attribute** is an attribute that is not a prime attribute. <https://tutorcs.com>

<sup>2</sup> It extends Algorithm 15.2(a) in [Elmasri & Navathe, 7th edition, pp. 542], or Algorithm 2(a) or in Algorithm 2(a) in [Elmasri & Navathe, 6th edition pp. 558] to finding all keys of  $R$





## 程序代写代做 CS编程辅导 Exercise – Finding Keys



- Consider a relation  $R$  with attributes  $\{A, B, C, D\}$  and a set of functional dependencies  $\Sigma = \{A \rightarrow B, B \rightarrow C, C \rightarrow D\}$ .

- List all the keys of  $R$ .
- Find all the prime attributes of  $R$ .

### Solution:

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- We compute the closures for all possible combinations of the attributes in  $R$ :

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- $(A)^+ = A, (B)^+ = B, (C)^+ = C, (D)^+ = D;$
- $(AB)^+ = ABCD, (AC)^+ = ACD, (AD)^+ = AD, (BC)^+ = BC, (BD)^+ = BD, (CD)^+ = CD;$
- $(ABC)^+ = ABCD, (ABD)^+ = ABCD, (ACD)^+ = ACD, (BCD)^+ = BCD;$

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- Hence, we have
  - $AB$  is the only key of  $R$ .
  - $AB, ABC, ABD$  and  $ABCD$  are the superkeys of  $R$ .
  - $A$  and  $B$  are the prime attributes of  $R$ .



## 程序代写代做 CS编程辅导 Exercise – Finding Keys



- Checking all possible combinations of the attributes is too tedious!

**Example:** Still consider a relation schema  $R = \{A, B, C, D\}$  and  $\Sigma = \{AB \rightarrow C, AC \rightarrow D\}$ . List all the keys of  $R$ .

- **Some tricks:**
  - If an attribute *never* appears in the dependent of any FD, this attribute must **be part of each key**.
  - If an attribute *never* appears in the determinant of any FD but appears in the dependent of any FD, this attribute must **not be part of each key**.
  - If a proper subset of  $X$  is a key, then  $X$  must **not be a key**.

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## 程序代写代做 CS编程辅导 Finding Keys - Example



- Consider ENROLMENT following FDs:

- $\{ \text{StudentID} \} \rightarrow \{ \text{ConfirmedBy} \}$
- $\{ \text{StudentID}, \text{CourseNo}, \text{Semester} \} \rightarrow \{ \text{ConfirmedBy}, \text{Office} \};$
- $\{ \text{ConfirmedBy} \} \rightarrow \{ \text{Office} \}.$

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| ENROLMENT |           |          |          |             |        |
|-----------|-----------|----------|----------|-------------|--------|
| Name      | StudentID | CourseNo | Semester | ConfirmedBy | Office |
| Tom       | 123456    | COMP2400 | 2010 S2  | Jane        | R301   |
| Mike      | 123458    | COMP2400 | 2008 S2  | Linda       | R203   |
| Mike      | 123458    | COMP2600 | 2008 S2  | Linda       | R203   |

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- What are the keys, superkeys and prime attributes of ENROLMENT?

- $\{ \text{StudentID}, \text{CourseNo}, \text{Semester} \}$  is the only key.
- Every set that has  $\{ \text{StudentID}, \text{CourseNo}, \text{Semester} \}$  as its subset is a superkey.
- StudentID, CourseNo and Semester are the prime attributes.

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