程序代写代做 CS编程辅导

Comp3620/Comp6320 Artificial Intelligence

ations, Strategies, and Algorithms Tutorial 1: 14 - 20,2023

Exercise 1 (proble

For each of the following problem, explain how states and actions can be represented, and give the initial state, goal test, successor function, and a plausible step cost function. Remember from the lectures that these elements constitutes a search problem formulation.

1. Color a planar map using a minimum of colors in such a way that no two adjacent regions have the same color.

We are given the number n of regions and an adjacency matrix $A[i,j], i,j \in 1,\ldots,n$, where A[i,j] is true iff region i is adjacent to region j. A state is a vector C, where $C[i], i \in 1, ..., n$ is the color of

region i or is NONE, and satisfies $A[i,j] \rightarrow C[i] \neq C[j]$ or C[i] is NONE). In the initial state C[i] and satisfies $A[i,j] \rightarrow C[i] \neq C[j]$ or C[i] is NONE).

The successor function maps a state to a set of pairs, each consisting of an action applicable and a successor state. Formally, this is written as follows:

 $C[j] \neq C$ for all j such that A[i,j] and C'[i] = c and C'[j] = C[j] for $j \neq i$

The step-cost function adds a cost of one for the use of a new color, and uses a small positive cost otherwise: g(C, color(t, t)) = 1/if(t) + 1/if(t) = 1/if(t) + 1/if(t) = 1/if(t) =

The goal test is goal(C) iff $C[i] \neq NONE$ for all i.

Alternative Solution

For those who don't like formal notations, a less formal, but still acceptable definition of the successor function would be as follows. The actions are color(i, c) for coloring a yet uncolored region i with color c. For such an action to be applicable in state C:

- region i must be yet uncollored: C[i] = NONE
- color c must not have been used to color an adjacent region: $\forall j$ such that $A[i,j], C[j] \neq c$

The resulting state C' is such that:

• C' is the same as C except that i has been colored with color c: C'[i] = c and $C'[j] = C[j] \forall j \neq i$

2. Using a water tap and three jugs of possibly different capacities (e.g., 12, 5, and 8 litres), collect a given around of water tag of light) in one of the jugs of fact as possible. The available operations are: filling up a jug completely with the water tap, pouring the contents of one jug into another until one of them is full or empty, or completely emptying the contents of one jug onto the ground. Assume that moving 1 liter takes 1 unit of time.

Solution

A state is a vector addition, we know jugs.

enting the current amount of liquid in the respective jugs. In \blacksquare ies M[i], $i = 1 \dots 3$ and the amount x to collect in one of the

The successor fun

```
\mathbf{F}'[i] = 0 \text{ and } S'[j] = S[j] \text{ for } j \neq i, i = 1 \dots 3 \} \cup
                                 \langle \mathrm{fill}(i), S' \rangle \mid S'[i] = \mathrm{M}[i] \text{ and } S'[j] = S[j] \text{ for } j \neq i, i = 1 \dots 3 \} \cup S'[i]
successorFn(S) =
                                \{\langle pour(i,j), S' \rangle \mid S'[j] = min(M[j], S[j] + S[i]), S'[i] = S[i] - S'[j] + S[j],
                                                          and S'[k] = S[k] for k \neq i and k \neq j, i, j = 1 \dots 3, i \neq j
```

The goal test is $goal(S) \equiv \exists i \in 1...3 \text{ s.t. } S[i] = x$

The step-cost function can be equal to the amount of water moved at the rate of 1l per second:

- $\begin{array}{l} \bullet \ \operatorname{step-cost}(\mathit{S}, \operatorname{ext}(\mathit{S}, \operatorname{ext}(\mathsf{S}, \operatorname{ext}(\mathsf{S},$
- step-cost(S, pour(i, j), S') = S[i] S'[i].

tutores (a) 63 compensative Solution

Again, a less formal definition of the successor function, e.g. for the poor actioon, would be as follows. The actions are:

- (a) pour (i, j) for pour in the forcett of S_i into jut j, with $i \neq j, i, j = 1 \dots 3$. This action is always applicable in any state S_i although if i is empty or j is full, it doesn't have much effect. The resulting state is S' such that:
 - jug j now additionally contains the full contents of jug i if that doesn't lead to exceed j's capacity, or else is completely full of [i] - Smin(M[j], [i]) + S[i])• jug i is left with whatever could not fit in j: S'[i] = S[i] - S'[j] + S[j]

 - any other jugs k is unchanged: $S'[j] = S[j], \forall k \neq i \text{ and } k \neq j$
- (b) $empty(i) \dots$
- (c) $fill(i) \dots$

Side Remark

As an aside: For the example with 12, 8, 5 liter jugs, we can get 9 liters in 30 secs as follows: fill 12 liter jugg, pour 12 liter jug into 8 liter jug, fill 5 liter jug, pour 5 liter jug into in 12 liter jug. A more time consuming solution would be to fill the 8 liter jug, fill the 5 liter jug, poor the 8 liter jug into the 12 liter jug, pour the 5 liter jug into the 12 liter jug, empty the 12 liter jug, fill in the 8 liter jug, poor the 5 liter jug into the 12 liter jug, poor the 8 liter jug into the 12 liter jug.

3. Three superheroes and three supervillains are on the side of a river, along with a boat which can hold me of two people. Find a try of getting them all the other side, without ever leaving superheroes outnumbered by supervillains at any place. Naturally, the boat cannot move across the river by itself, and none of our super-humans can fly!

Solution

The state S repre plus the position

erheroes $(h(S) \in \mathbb{N})$ and supervillains $(v(S) \in \mathbb{N})$ on the left,

The initial state

river they're being successor function

 $\mathbf{I}(I) = 3 \text{ and } p(I) = 1.$ Actions move the (boat capacity co

rom one side to another, subject to the numbering constraints ple can be moved on the boat than exist on the side of the Lero left outnumbered on either side of the river). Hence the

 $\{\langle \text{move-right}(v',h'),S'\rangle \mid h(S') = h(S) - h', v(S') = v(S) - v', p(S) = l, p(S') = r \}$ $1 \le v' + h' \le 2, v' \le v(S), h' \le h(S),$

 $\{v(S') \to h(S') = 0, v(S') < h(S') \to h(S') = 3\} \cup \{v(S') \to h(S') = 0, v(S') < h(S') \to h(S') = 3\} \cup \{v(S') \to h(S') = 0, v(S') < h(S') \to h(S') = 3\} \cup \{v(S') \to h(S') \to h(S') = 1\}$ $1 \le v' + h' \le 2, v' \le 3 - v(S), h' \le 3 - h(S),$ $h(S') < v(S') \to h(S') = 0, v(S') < h(S') \to h(S') = 3$

ignment Project Exam Help The goal is to have no one

The step-cost: 1 per action.

Alternative Solution

the successor lunction world 60 A less formal definition of

(a) The actions that can be applied in a state S = (h, v, 1) are move-right (v', h') to move v' supervillains and h' superheroes to the right hand side of the border.

For such an acting to be applicable, 3, 8 or must 6

- satisfy the fact that you can't put more people on the boat than you have on the left hand side of the river $v' \leq v$ and $h' \leq h$
- satisfy the boat capacity constraints: $1 \le v' + h' \le 2$
- leave no superher Suthymberel of the 1st lands de of the river: if $h h' \leq v v'$ then h - h' = 0
- leave no superhero outnumbered on the right hand side of the river: if $3 h + h' \le 3 v + v'$ then 3 - h + h' = 0

The action leads to the state S' with

- h h' super-heroes on the left hand side
- v v' super-villains on the left hand side
- boat position p = r
- (b) actions that can be applied in a state S = (h, v, r) are similar.

As an aside, here i羟utionsequence写代做 CS编程辅

state(v,h,p)	action	comment
(3, 3, 1)	$\underline{\text{move-right}(2,0)}$	move 2 supervillains
$(1, \square \square$	0)	move 1 supervillain back
$(2, \blacksquare \blacksquare$		move 2 supervillains
$(0, \bullet, \bullet)$		move 1 supervillain back
$(1, \blacksquare, \blacksquare, \blacksquare)$	(2)	move 2 superheroes
$(1, \bullet, \bullet)$	(i)	move 1 supervillain & 1 superhero back
(2,1)	1 , 2)	move 2 superheroes
(2,15)		move 1 supervillain back
$(3, \blacksquare)$	(2,0)	move 2 supervillains
(1, 0, r)	move-left(1,0)	move 1 supervillain back
(2,0,1)	move-right(2,0)	move 2 supervillains
(0, 0, r)	goal!	
TTT	\frown 1	4 4

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Exercise 2 (properties of search strategies)

True or False?

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True False: Depth-first graph search is guaranteed to return a shortest solution.

False: Depth-first provides no optimality guarantee at all. (It is only complete in finite search spaces).

True False: Breadth-first graph search is guaranteen to return a shortest solution.

True. This is because front is addes are tanked by increasing odd ref lightly The strategy expands all nodes whose depth is less than the depth of the shallowest goal node).

True False: Uniform-cost graph search is guaranteed to return an optimal solution.

True: This is because frontier nodes are ranked by increasing order of g(n). (The strategy expands all nodes such that $g(n) \leq C^*$ and some nodes such that $g(n) \neq C^*$ including one single goal node.)

True False: Greedy graph search is guaranteed to return an optimal solution.

False: This is because it completely ignores the cost to reach frontier nodes from the initial state, and only looks into the future estimated cost to the goal.

True False: Breadth-first graph starrit is a special easy of uniform-cost search.

True: This is because breadth-first search behaves like uniform-cost search when all step costs are iden-

True False: A* graph search with an admissible heuristic is guaranteed to return an optimal solution.

True: Note that this is only true of the version with node re-expansion. (Consistency is a stronger property than admissibility which does not require node re-expansion.)

True False: A* graph search is guaranteed to expand no more nodes than depth-first graph search.

False: In dense solution spaces, depth-first could find a solution much faster than A*.

True False: A* graph search with a consistent heuristic is guaranteed to expand no more nodes than uniform-cost graph search.

True: this is because uniform-cost amounts to A^* with h=0 which is the most uninformed heuristic. Uniform cost completely ignores the future cost to reach a goal. An alternative way to see this is to observe that uniform cost expand all nodes such that $q < C^*$ whilst A* only expand all nodes such that $q < C^* - h$ (with $h \geq 0$).

Exercise 3 (search strategies at work)

Consider the search space below, where S is the initial state and G1 and G2 both satisfy the goal test. Arcs are labelled with the cost of traversing them and the estimated cost to a goal is reported inside nodes.

For each of the founiform cost, greedy list, in order, all the from the frontier. Enalphabetical order. a node is dequeued newly generated nod on the frontier.

egies: breadth-first, depth-first, iterative deepening, dicate the path found (if any) by graph-search and recall that a state is expanded when it is removed equal, nodes should be removed from the frontier in ess of the strategy, the goal-test is performed when or breadth-first and depth-first search, assume that the frontier if they have already been explored or are



Breadth-first: finds $S \to C \to G2$. Expanded nodes: S(0), A(1), C(1), B(2), D(2), E(2), G(2)

Depth-first: finds S — TITES D//FUITOFFC Sode OTTA(1), B(2), D(3), G2(4)

Iterative deepending: finds $S \to C \to G2$. Expanded nodes: S(0), S(0), A(1), C(1), S(0), A(1), B(2), E(2), C(1), D(2), G(2)

Uniform cost: finds $S \to C \to D \to G2$. Expanded nodes: S(0), A(2), C(2), B(3), D(3), G(6)

Greedy: finds $S \to A \to B \to G1$. Expanded nodes: S(5), A(2), B(1), G1(0)

A*: finds $S \to C \to D \to G2$. Expanded nodes: S(0+5=5), A(2+2=4), B(3+1=4), D(4+1=5), C(2+4=6) D(3+1=4) G2(6+0=6)

Exercise 4 (Graph Search algorithm)

List all the issues in the following implementation of Graph Search, and explain their impact on completeness and optimality of the various strategies. Assume the EXPAND function is correct and as given in the lectures.

```
function Graph-S
                                               returns a solution, or failure
   explored \leftarrow an empty
   frontier \leftarrow Insert
                                              \texttt{STATE}[problem]), frontier)
   loop do
       if frontier is
       node \leftarrow Remo
                                                then return node
                                             -bde, problem), frontier)
function InsertNodes (nodes, frontier) returns updated frontier
   for each n in nodes do
       add n to fronti
     if \exists m \text{ in } explored \cup frontier s.t.}
       PATH-Cost[m] \leftarrow PATH-Cost[n]
       PARENT[m] \leftarrow PARENT[n]
       ACTION[m] & ACTION[m] & ACTION[m] & Project Exam Help
       Depth[m] \leftarrow Depth[n]
   return frontier
```

There are four issues with the above implementation.

- 1. In the Graph-Sear in fincial, nodes that the finance of goal graphs should be added to the explored list. Otherwise, nodes labelled by the same state will be expanded multiple times, as in tree-search. For strategies such as depth-first search or greedy search, this can lead to incompleteness when there are loops in the search space.
- 2. One of the main principles of Graph Search sthat at most one node labelled by a given state is on the frontier or the explored list at any one time. At the beginning of the InsertNodes function, successor node n should not systematically be added to the frontier. A node n should only be added at that point if no node m on the frontier or in the explored list is labelled by the same state as n. Otherwise we could compromise both attingity and confidence.
- 3. When a node m, is found on the frontier or in the explored list that is labelled by the same state as n, the various fields of m should only be updated if n represents a better path to that state, that is if g(n) < g(m). Otherwise again optimality is compromised with strategies such as A^* and even with uniform cost search.
- 4. Even if the above problems are fixed, the algorithm will only return the optimal solution if the heuristic is consistent. If the heuristic is only admissible then a node on the explored list should be re-opened when a better path to the state labelling that node is found. With a consistent heuristic, that case cannot happen because the first path to a state that is found (and which is put on the explored list) is the shortest path to that state.



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