

## Advanced Topics in Software Verification

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<sup>a</sup>a1 due; <sup>b</sup>a2 due; <sup>c</sup>a3 due

#### More on Automation

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Last time: safe and unsafe, heuristics: use safe before unsafe

## be automated

Automated methodies ast, clarify etc) are not hardwired. lim rules can be declared.

#### Syntax: WeChat: cstutores

[<kind>!] for safe rules (<kind> one of intro, elim, dest) for unsaisenment Project Exam Help

## EApplication ( / pughly):

do safe rules first, search/backtrack on unsafe rules only

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#### **Example:**

declare attribute glottaply://tdeplare.comjl [intro!] allE [elim]

remove attribute globally **declare** allE [rule del]

apply (blast intro: somel) use locally

annly (blast del: conil) delete locally

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# Demo: Automation Assignment Project Exam Help

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#### **Exercises**

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- ightharpoonup derive the classical factor rule ( $\neg P \Longrightarrow False$ )  $\Longrightarrow P$  in Isabelle
- → define **nor** and **na**
- → show nor x x :
- → derive safe intro and elim rules for them
- $\rightarrow$  use these in an automated prospection  $x \times x = x$

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# Defining Higher Order Logic Assignment Project Exam Help

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## What is Higher Order Logic?

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- → Propositional Long \*\*\* → Propositional Long \*\*\* → Inc. \*\* → Inc
  - no quantified
  - all variables
- → First Order Logi
  - quantification over values, but not over functions and predicates,
  - terms and formulas syntactically distinct Assignment Project Exam Help
- → Higher Order Logic:
  - quantificatio Example vertex thing in the fluction of the properties of
  - consistency by types
  - formula =  $tek R \circ 749389476$

## **Defining Higher Order Logic**

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#### Default types:

bool



- → bool sometimes called part: cstutorcs
- → ⇒ sometimes called *fun*

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#### **Default Constants:**

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$$\rightarrow$$
 ::  $bool \Rightarrow bool \Rightarrow bool$ 

= QQ: 749389476  $bool$ 
 $\epsilon$  ::  $(\alpha \Rightarrow bool) \Rightarrow \alpha$ 

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## **Higher Order Abstract Syntax**

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**Problem:** Define syr**ing and are like**  $\forall$ ,  $\exists$ ,  $\varepsilon$ 

One approach:  $\forall :: m \Rightarrow bool$ 

**Drawback:** need to ut substitution,  $\alpha$  conversion again.

But: Already have binder help stitutions  $\alpha$  conversion in meta logic

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**So:** Use  $\lambda$  to encode all other binders. OD: 749389476

## **Higher Order Abstract Syntax**

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Example:

HOAS usual syntax WeChat: cstutorcs

 $\begin{array}{c} \mathsf{ALL} \ (\lambda \overset{\times}{\mathsf{Assignment}} \overset{\times}{\mathsf{Project}} \overset{\times}{\mathsf{Exam}} \overset{=}{\mathsf{Help}} \\ \mathsf{ALL} \ \overset{\wedge}{\mathsf{P}} \overset{\times}{\mathsf{Nept}} \overset{=}{\mathsf{Nept}} \overset{=}{\mathsf{N$ 

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Isabelle can translate usual binder syntax into HOAS.

#### Side Track: Syntax Declarations

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- → infixl/infixr: short form for left/right associative binary operators

  Example: or :: bookarl:bookbresbook68infixm" ∨ " 30)
- ⇒ binders: declaration must be of the form  $c :: (\tau_1 \Rightarrow \tau_2) \Rightarrow \tau_3$  (binder  $B^{n-1} 1$ )

  B x. P x translated this  $T_1 < T_2 < T_3 < T_4 < T_4 < T_5 < T_5 < T_6 < T_7 < T_$

More in Isabelle/Isar Reference Manual (8.2)

#### Back to HOL

#### 程序代写代做 CS编程辅导

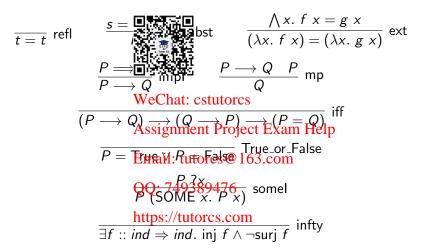
Base: bool, 
$$=$$
,  $\rightarrow$ ,  $\varepsilon$ 

And the rest is define  $=$ ,  $\rightarrow$ ,  $\varepsilon$ 

True  $=$  ( $\lambda x$ )  $=$  ( $\lambda$ 

#### The Axioms of HOL

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#### That's it.

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- → 3 basic constants
- → 3 basic types
- → 9 axioms



With this you can define and derive all the rest.

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Isabelle knows 2 more sxigms ent Project Exam Help

$$\frac{x=y}{x\equiv y}$$
 eq\_reflection tutorcs@163.com (THE  $x. x=a$ ) =  $a$  the\_eq\_trivial

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## The Definitions in Isabelle

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#### **Deriving Proof Rules**

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In the following, we

- → look at the definit re detail
- → derive the traditique is the sules from the axioms in Isabelle

Convenient for deriving rules: named assumptions in lemmas

```
WeChat: cstutorcs
lemma [name:]
assumes [maoma Projecp@pam Help
assumes [name2:] "< prop >2"
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::
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```

**proves:**  $\llbracket < prop >_1; < prop >_2; \dots \rrbracket \implies < prop >$ 

#### True

## 程序代写代做 CS编程辅导

consts True :: bool

True  $\equiv (\lambda x :: bool. )$ 

Intuition:

right hand side is always true

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**Proof Rules:** 

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 $(\lambda x :: bqq h x)$ 

unfold True\_def

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## Demo

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#### **Universal Quantifier**

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consts ALL ::  $(\alpha \Rightarrow b \cap A) \Rightarrow b \circ o \circ A$ ALL  $P \equiv P = (\lambda \otimes A) \Rightarrow b \circ o \circ A$ 

#### Intuition:

- $\rightarrow$  ALL *P* is Higher Order Abstract Syntax for  $\forall x. P x.$
- → P is a function the the state of the property of the proper
- → ALL P should be true iff P yields true for all x, i.e. if it is equivalent to the function XX! True.

Proof Rules: Email: tutorcs@163.com

$$\frac{\bigwedge x. P \times QQ}{\forall x. P \times}$$
 QQ: 749389476  $\frac{P?x \Longrightarrow R}{R}$  allE https://tutorcs.com

**Proof**: Isabelle Demo

#### **False**

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consts False :: bool

False  $\equiv \forall P.P$ 

Intuition:

Everything can be derived from False.

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**Proof Rules:** 

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Proof: Isabelle DemoQ: 749389476

## Negation

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**consts** Not :: bool = 1 P = P False

#### Intuition:

Try P = True and P = False and the traditional truth table for  $\longrightarrow$ . WeChat: cstutorcs

Proof Rules: Assignment Project Exam Help

 $\frac{A = \text{Erfialse tutorcs@} \frac{163.c4m}{P} \text{ notE}}{\sqrt{QQ}: 749389476}$ 

Proof: Isabelle Demattps://tutorcs.com

#### Existential Quantifier

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consts EX :: 
$$(\alpha \Rightarrow b_{\square}) \rightarrow b_{\square} ol$$
  
EX  $P \equiv \forall Q. \ (\forall x \in Q) \rightarrow Q$ 

#### Intuition:

- $\rightarrow$  EX P is HOAS for  $\exists x. P x.$  (like  $\forall$ )
- → Right hand side is Wharacterigation posses with  $\forall$  and  $\longrightarrow$
- → Note that inner ∀ binds wide: (∀x. P x → Q)

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  Remember lemma from last time:
- $(\forall x. P x \longrightarrow Q)$  Enterly: Putores@963.com

#### Proof Rules:

## Conjunction

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**consts** And :: 
$$bool = bool (\_ \land \_)$$
 $P \land Q \equiv \forall R. (P \longrightarrow B) \longrightarrow R$ 
Intuition:

- → Mirrors proof rules for ∧
- → Try truth table for Chathe stutores

#### **Proof Rules:**

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$$\frac{A \quad B}{A \land B} \stackrel{\text{Email:}}{\text{conjl}} \frac{\text{Autogcs}}{\text{QQ:}} \frac{\text{QA:}}{749389476} \frac{\text{Comp}}{\text{C}} C \text{conjE}$$

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**Proof**: Isabelle Demo

## Disjunction

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#### Intuition:

- → Mirrors proof rules for ∨ (case distinction)
- Try truth table for truth table for the chain stutores

#### **Proof Rules:**

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$$\frac{A}{A \vee B} \frac{B}{A \vee B} \stackrel{\text{Email: tuxpyce} @ 163 com}{\text{disjl}1/2} \frac{B \Longrightarrow C}{C} \text{ disjE}$$

$$\frac{A}{A \vee B} \frac{B}{A \vee B} \stackrel{\text{Email: tuxpyce} @ 163 com}{C} \frac{B}{C} \stackrel{\text{disjE}}{}$$

Proof: Isabelle Demohttps://tutorcs.com

#### If-Then-Else

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consts If :: 
$$bool \Rightarrow \alpha \qquad \alpha \qquad \text{(if\_then\_else\_)}$$
If  $P \times y \equiv \text{SOME} \qquad \text{(if\_then\_else\_)}$ 
 $z = y \qquad \text{(if\_then\_else\_)}$ 

#### Intuition:

- $\rightarrow$  for P = True, right leads at the stallarses to SOME z. z = x
- ightharpoonup for P = False, right hand side collapses to SOME z, z = yAssignment Project Exam Help

Proof Rules: Email: tutorcs@163.com

if True then s else  $t \ominus G$ : if False then s else t = t

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**Proof**: Isabelle Demo

## 程序代写代做 CS编程辅导



## That was HUL

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## We have learned today ...

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- → More automation
- → Defining HOL
- → Higher Order Abs
- → Deriving proof rules

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