



程序代写代做 CS编程辅导



UNSW
SYDNEY



MP4161

Advanced Topics in Software Verification

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13/2022

Last Time

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- Deep and shallow embeddings
- Isabelle records
- Nondeterministic State Monad with Failure
- Monadic Weakest Precondition Rules

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Content

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→ Foundations & Principles

- Intro, Lambda natural deduction [1,2]
- Higher Order (part 1) [2,3^a]
- Term rewriting [3,4]



→ Proof & Specification Techniques

- Inductively defined sets, rule induction [4,5]
- Datatype induction, primitive recursion [5,7]
- General recursive functions, termination proofs [7^b]
- Proof automation (part 2) [8]
- Hoare logic, proofs about programs, invariants [8,9]
- C verification [9,10]
- Practice, questions, exam prep [10^c]

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^aa1 due; ^ba2 due; ^ca3 due

wp

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apply (*wp extra_wp_rules*)



Tactic for automatic verification of **weakest precondition rules**

- Originally developed by Thomas Sewell, NICTA, for the seL4 proofs
- Knows about a huge collection of existing wp rules for monads
- Works best when precondition is a schematic variable
- related tool: **wpc** for Hoare reasoning over **case** statements

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Today we will learn about **AutoCorres** and **C** verification.

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Introduction to AutoCorres and wp

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A Brief Overview of C and Simpl

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C

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Main new problems in verifying C programs:

- expressions with s
- more control flow (for, break, continue, return)
- local variables and
- functions & procedures
- concrete C data types
- C memory model and C pointers

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C is not a nice language for reasoning.

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Things are going to get ugly.

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AutoCorres will help.

C Parser: translates C into Simpl

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Simpl: deeply embedded imperative language in Isabelle.



- generic imperative by Norbert Schirmer, TU Munich
- state space and block definitions/statements can be instantiated
- has operational semantics
- has its own Hoare logic with soundness and completeness proof, plus automated vcg

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C Parser: parses C, produces Simpl definitions in Isabelle

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- written by Michael Norrish, NICTA and ANU
- Handles a non-trivial subset of C
- Originally written to verify LLVM's C implementation
- AutoCorres is built on top of the C Parser

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Commands in Simpl

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```
datatype ('s, 'p, 'f) =  
  Skip  
| Basic "'s =  
| Spec "('s *  
| Seq "('s, 'p, 'f) com" "('s, 'p, 'f) com"  
| Cond "'s set" "('s, 'p, 'f) com" "('s, 'p, 'f) com"  
| While "'s set" "('s, 'p, 'f) com"  
| Call 'p  
| DynCom "'s Assignment Project Exam Help  
| Guard 'f "'s set" "('s, 'p, 'f) com"  
| Throw Email: tutors@163.com  
| Catch "('s, 'p, 'f) com" "('s, 'p, 'f) com"
```

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's = state, 'p = procedure names, 'f = faults

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Expressions with side effects

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$a = a * b;$ $x = f(h);$ $i = ++i - i++;$ $x = f(h) + g(x).$



→ $a = a * b$ — Fine: can be translated into Isabelle

→ $x = f(h)$ — Fine: may have side effects, but can be translated sanely.

→ $i = ++i - i++$ — Seriously? What does that even mean? Make this an error, force programmer to write instead:

$i0 = i; i++; i = i - i0;$ (or just $i = 1$)

→ $x = f(h) + g(x)$ — Ok if g and h do not have any side effects

⇒ Prove all functions in expressions are side-effect free

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Alternative:

Explicitly model nondeterministic order of execution in expressions.

Control flow

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```
c } while (condition);
```

automatically transla

```
c; while (condition) { c }
```

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Similarly:

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```
for (init; condition; increment) { c }
```

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becomes

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```
init; while (condition) { c; increment; }
```

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More control flow: break/continue

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```
while (condition) {  
    foo;  
    if (condition) continue;  
    bar;  
    if (condition) break;  
}
```

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Non-local control flow: **continue** goes to condition, **break** goes to end.

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Can be modelled with exceptions:

- throw exception '**continue**', catch at end of body.
- throw exception '**break**', catch after loop.

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Break/continue

Break/continue example becomes:

```
try {  
    while (condition) {  
        try {  
            foo;  
            if (Q) { exception = 'continue'; throw; }  
            bar;  
            if (P) { exception = 'break'; throw; }  
        } catch { if (exception == 'continue') SKIP else throw; }  
    }  
} catch { if (exception == 'break') SKIP else throw; }
```

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This is not C any more. But it models C behaviour!

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Need to be careful that only the translation has access to exception state.

Return

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```
if (P) return  
foo;  
return y;
```



Similar non-local control flow. **Similar solution:** use
throw/try/catch

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```
try {  
    if (P) { return_val = x; exception = 'return'; throw; }  
    foo;  
    return_val = y; exception = 'return'; throw;  
} catch {  
    SKIP  
}
```

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AutoCorres

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AutoCorres

AutoCorres: reduces the pain in reasoning about C code

- Written by David  NICTA and UNSW
- Converts C/Simpl (ad-hoc) shallow embedding in Isabelle
- Shallow embedding reason about than Simpl

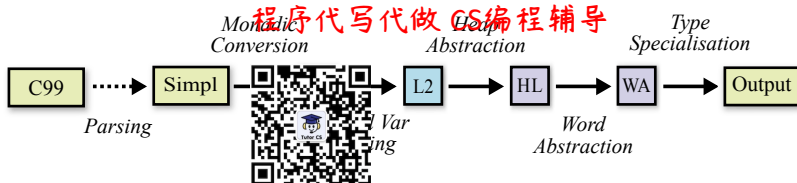
Is self-certifying: produces Isabelle theorems proving its own correctness

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For each Simpl definition C and its generated shallow embedding A :

- AutoCorres proves an Isabelle theorem stating that C **refines** A
- Every behaviour of C has a corresponding behaviour of A
- Refinement guarantees that properties proved about A will also hold for C .
- (Provided that A never fails. c.f. Total Correctness)

AutoCorres Process



L1: initial monadic shallow embedding

L2: local variables introduced by λ -bindings

HL: heap state abstracted into a set of **typed heaps**

WA: machine words abstracted to idealised integers or nats

Output: human-readable output with **type strengthening**, polish

On-the-fly proof: <https://tutorcs.com>

Simpl refines **L1** refines **L2** refines **HL** refines **WA** refines **Output**

Example: C99

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We will use the following example program to illustrate each of the phases.



```
unsigned some_f(unsigned *a, unsigned *b, unsigned  
    unsigned *p = NULL;
```

```
    if (c > 10u){  
        p = a;  
    } else {  
        p = b;  
    }  
  
    return *p;  
}
```

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Example: Simpl

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```
some_func_body ≡  
TRY  
  `p := ptr_coerce (last 0));;  
  IF 0xA < `c THEN  
    `p := `a  
  ELSE  
    `p := `b  
  FI;;  
Guard C_Guard {c_guard `p}  
  (creturn global_exn var `update ret unsigned `update  
   (\s. h_val (hrs_mem (t_hrs_ (globals s))) (p_ `s))));;  
Guard DontReach {} SKIP  
CATCH SKIP END
```

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Example: L1 (monadic shallow embedding)

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```
l1_some_func ≡ L1_init ret__unsigned_ 'update)
  (L1_seq (L1_modify (λs. ptr_coerce (Ptr (scast 0))))
    (L1_seq (L1_consume (λs. 0xA < c_ ' s))
      (L1_modify (λs. s(p_ ' := a_ ' s)))
      (L1_modify (λs. s(p_ ' := b_ ' s))))
    (L1_seq (L1_guard (λs. c_guard (p_ ' s)))
      (L1_seq (L1_modify (λs. s(ret__unsigned_ :=
        h_val (hrs_mem (t_hrs_ ' (globals s))) (p_ ' s))))
        (L1_modify (global_exn_var_ 'update (λ_. Return))))))
```

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State type is the same as Simpl, namely a record with fields:

- **globals**: heap and type information
- **a_**, **b_**, **c_**, **p_** (parameters and local variables)
- **ret__unsigned_**, **global_exn_var_** (return value, exception type)

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Example: L2 (local variables lifted)

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```
l2_some_func a b  
L2_seq (L2_condit 0xA < c)  
  gets (λs. a) [''p''])  
  gets (λs. b) [''p''])  
  (λp. L2_seq (L2_guard (λs. c_guard p))  
    (λ_. L2_gets (λs. h_val (hrs_mem (t_hrs_ ' s)) p) [''ret
```

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State is a record with just the **globals** field

- function now takes its parameters as arguments
- local variable **p** now passed via λ-binding
- **L2_gets** annotated with local variable names
- This ensures preservation by later AutoCorres phases

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Example: HL (heap abstracted into typed heaps)

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```
hl_some_func a
L2_seq (L2_concat (λs. 0xA < c)
              (L2_gets (λs. a) [''p''])
              (L2_gets (λs. b) [''p''])))
(λr. L2_seq (L2_guard (λs. is_valid_w32 s r)
                  (λ_. L2_gets (λs. heap_w32 s r) [''ret''])))
```

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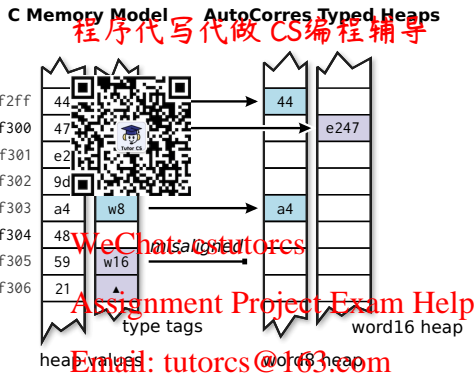
State is a record with a set of **is_valid_** and **heap_** fields:

- These store **pointer validity** and **heap contents** respectively, per type
- above example has only 32-bit word pointers

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Heap Abstraction




C Memory Model: QQ: 749389476

- **Heap** is a mapping from 32-bit addresses to bytes: 32 word \Rightarrow 8 word
- **Heap Type Description** stores type information for each heap location

Example: WA (words abstracted to ints and nats)

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```
wa_some_func a b c
L2_seq (L2_condition (λs. 10 < c)
  L2_gets (λs. a) [''p''])
  L2_gets (λs. b) [''p'']))
(λr. L2_seq (L2_condition (λs. is_valid_w32 s r)
  (λ_. L2_gets s. unat (heap_w32 s r)) [''ret''])
```



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Word abstraction: C **int** → Isabelle int, C **unsigned** → Isabelle
nat

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- Guards inserted to ensure absence of unsigned underflow and overflow
- Signed under/overflow already has guards (it has undefined behaviour)

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In the example, the **unsigned** argument **c** is now of type **nat**

- The function also returns a nat result
- The heap is not abstracted, hence the call to **unat**

Example: Output (type strengthening and polish)

some_func' a b c 程序代写代做 CS编程辅导
DO p ← oreturn (if 10 < c then a else b);
 oguard (λs. d_w32 s p);
 ogets (λs. uap_w32 s p))
OD



Type Strengthening WeChat: cstutorcs

- Tries to convert output to a more restricted monad
- The above is in the **option** monad because it doesn't modify the state, but might fail
- The **type** of the option monad implies it cannot modify state

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Polish:

- Simplify output as much as possible
- The **condition** has been rewritten to a **return** because the condition **10 < c** doesn't depend on the state

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Type Strengthening

Example:

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```
unsign (void){ return 0u; }
```



Monad Type	Kind	Type	Example
pure	Pure function	'a	0
gets	Read-only, non-failing	's \Rightarrow 'a	$\lambda s. 0$
option	Read-only function	's \Rightarrow 'a option	oreturn 0

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Effect information now encoded in function types

Later proofs get this information for free!

Can be controlled by the `ts_force` option of `AutoCorres`

(Reader) Option Monad

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Another standard monad, familiar from e.g. Haskell

Return:



$\equiv \lambda s. \text{Some } x$

Bind:

$\text{obind } a \ b \equiv \lambda s. \text{case } a \ s \text{ of } \text{None} \Rightarrow \text{None} \mid \text{Some } r \Rightarrow b \ r \ s$

→ Infix notation: $|>>$

→ Do notation: $\text{DO } \dots \text{OD}$

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Hoare Logic:

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$\text{ovalid } P \ f \ Q \equiv \forall s \ r. P \ s \wedge f \ s = \text{Some } r \longrightarrow Q \ r \ s$

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$$\text{ovalid } (P \ x) \ (\text{oreturn } x) \ P \quad \frac{\wedge r. \text{ovalid } (R \ r) \ (g \ r) \ Q \quad \text{ovalid } P \ f \ R}{\text{ovalid } P \ (f \ |>> \ g) \ Q}$$

Exception Monad

Exceptions used to model early return, break and continue.

Exception Monad:  $(\text{set} \times \text{bool})$

- Instance of the monadic state monad: return-value type is **sum type** $'e + 'a$
- Sum Type Constructors: $\text{Inl} :: 'e \Rightarrow 'e + 'a$ $\text{Inr} :: 'a \Rightarrow 'e + 'a$

- **Convention:** Inl used for exceptions, Inr used for ordinary return-values

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Basic Monadic Operations

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$\text{returnOk } x \equiv \text{return (Inr } x)$ $\text{throwError } e \equiv \text{return (Inl } e)$
 $\text{lift } b \equiv (\lambda x. \text{case } x \text{ of Inl } e \Rightarrow \text{throwError } e \mid \text{Inr } r \Rightarrow b \ r)$

bindE: $a \gg=E b \equiv a \gg= (\text{lift } b)$

Do notation: $\text{doE } \dots \text{odE}$

Hoare Rules for Exceptions

New kind of Hoare triples to model normal and exceptional cases:

$$\{P\} f \{ \lambda x s. \text{call } e \Rightarrow E e s \mid \text{Inr } r \Rightarrow Q r s \}$$

Weakest Precondition Rules:

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$$\frac{}{\{P\ x\} \text{returnOk } x \{E\}, \{E\} \quad \{E\} \text{throwError } e \{P\}, \{E\}}$$

$$\frac{\bigwedge x. \{R\ x\} b\ x \{Q\}, \{E\} \quad \{P\} a \{R\}, \{E\}}{\{P\} a \Rightarrow E b \{Q\}, \{E\}}$$

(other rules analogous)

Today we have seen

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- The automated proof method **wp**
- The C Parser and translating C into Simpl
- AutoCorres and translating Simpl into monadic form
- The option and exception monads

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