



程序代写代做 CS 编程辅导



MP4161



UNSW
SYDNEY

Advanced Topics in Software Verification

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HOL

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13/2022

Content

程序代写代做 CS编程辅导

→ Foundations & Principles

- Intro, Lambda calculus [1,2]
- Higher Order Logic (part 1) [2,3^a]
- Term rewriting [3,4]



→ Proof & Specification Techniques

- Inductively defined sets, rule induction [4,5]
- Datatype induction, primitive recursion [5,7]
- General recursive functions, termination proofs [7^b]
- Proof automation, Isar (part 2) [8]
- Hoare logic, proofs about programs, invariants [8,9]
- C verification [9,10]
- Practice, questions, exam prep [10^c]

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^aa1 due; ^ba2 due; ^ca3 due

More on Automation

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Last time: safe and unsafe, heuristics: use safe before unsafe



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More on Automation

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be automated

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Automated methods (last, clarify etc) are not hardwired.
Safe/unsafe slim rules can be declared.

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Safe/unsafe rules can be declared.

Syntax:

[<kind>!]

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for safe rules (<kind> one of intro, elim, dest)

[<kind>]

for unsafe rules

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More on Automation

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Syntax:

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Application (roughly):

do safe rules first, search/backtrack on unsafe rules only

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Application (roughly):

do safe rules first, search/backtrack on unsafe rules only

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Example:

declare attribute globally declare conjl [intro!] allE [elim]

remove attribute globally declare allE [rule del]

use locally apply (blast intro: somel)

delete locally apply (blast del: conjl)

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Exercises

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- derive the classical contradiction rule ($\neg P \implies \text{False}$) $\implies P$ in Isabelle
- define **nor** and **nan**
- show $\text{nor } x \ x = \text{False}$
- derive safe intro and elim rules for them
- use these in an automated proof of $\text{nor } x \ x = \text{nand } x \ x$

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Defining Higher Order Logic

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What is Higher Order Logic?

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→ Propositional Logic

- no quantifiers
- all variables have domain



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What is Higher Order Logic?

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→ Propositional Logic

- no quantifiers
- all variables have global scope



→ First Order Logic:

- quantification over values, but not over functions and predicates,
- terms and formulas are syntactically distinct

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What is Higher Order Logic?

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→ Propositional Logic

- no quantifiers
- all variables have type bool



→ First Order Logic:

- quantification over values, but not over functions and predicates,
- terms and formulas are syntactically distinct

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→ Higher Order Logic:

- quantification over everything, including predicates
- consistency by types
- formula = term of type bool
- definition built on λ^\rightarrow with certain default types and constants

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Defining Higher Order Logic

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Default types:



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Defining Higher Order Logic

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Default types:

bool



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Defining Higher Order Logic

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Default types:

bool



⇒ _

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Defining Higher Order Logic

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Default types:

bool



\Rightarrow _

ind

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Defining Higher Order Logic

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Default types:

bool



\Rightarrow _

ind

→ **bool** sometimes called o

→ \Rightarrow sometimes called fun

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Defining Higher Order Logic

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Default types:

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Defining Higher Order Logic

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Default types:

bool



\Rightarrow _

ind

→ bool sometimes called o

→ \Rightarrow sometimes called fun

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= :: $\alpha \Rightarrow \alpha \Rightarrow \text{bool}$

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Defining Higher Order Logic

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Default types:

bool



\Rightarrow _

ind

→ bool sometimes called o

→ \Rightarrow sometimes called fun

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= $\lambda \alpha : \alpha \Rightarrow \alpha \Rightarrow \alpha$

ϵ ~~QQ: 749389476~~ $(\alpha \Rightarrow \alpha) \Rightarrow \alpha$

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Higher Order Abstract Syntax

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Problem: Define syntax for binders like $\forall, \exists, \varepsilon$



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Higher Order Abstract Syntax

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Problem: Define syntax for binders like $\forall, \exists, \varepsilon$



One approach: $\forall :: v : \alpha \rightarrow \beta \rightarrow \text{bool}$

Drawback: need to think about substitution, α conversion again.

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Higher Order Abstract Syntax

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Problem: Define syntax for binders like $\forall, \exists, \varepsilon$

One approach: $\forall :: v : T \rightarrow \text{bool}$

Drawback: need to think about substitution, α conversion again.

But: Already have binder, substitution, α conversion in meta logic

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Higher Order Abstract Syntax

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Drawback: need to think about substitution, α conversion again.

But: Already have binder, substitution, α conversion in meta logic

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So: Use λ to encode all other binders.

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Higher Order Abstract Syntax

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Example:



HOAS

$\Rightarrow \text{bool}) \Rightarrow \text{bool}$

usual syntax

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Higher Order Abstract Syntax

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Example:



HOAS

$\Rightarrow \text{bool}) \Rightarrow \text{bool}$

usual syntax

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ALL $(\lambda x. x = 2)$

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Higher Order Abstract Syntax

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Example:



HOAS

$\Rightarrow \text{bool}) \Rightarrow \text{bool}$

usual syntax

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ALL $(\lambda x. x = 2)$ $\forall x. x = 2$

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Higher Order Abstract Syntax

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Example:



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Higher Order Abstract Syntax

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Example:



$\Rightarrow \text{bool}) \Rightarrow \text{bool}$

HOAS

usual syntax

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ALL $(\lambda x. x = 2)$ $\forall x. x = 2$

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Higher Order Abstract Syntax

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Example:



HOAS

$\Rightarrow \text{bool}) \Rightarrow \text{bool}$

usual syntax

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ALL $(\lambda x. x = 2)$ $\forall x. x = 2$

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Isabelle can translate usual binder syntax into HOAS.

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Side Track: Syntax Declarations

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→ mixfix:

consts drvbl :: *ct*



⇒ *bool* ("_,- ⊢ _")

Legal syntax now:



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Side Track: Syntax Declarations

程序代写代做 CS编程辅导

→ mixfix:

consts drvbl :: *ct* → *ct* → *bool* ("_,-_ ⊢ _,-_")

Legal syntax now:



"_,-_ ⊢ _,-_")

→ priorities:

pattern can be annotated with priorities to indicate binding strength

Example: drvbl :: *ct* → *ct* → *fm* → *bool* ("_,-_ ⊢ _,-_") [30, 0, 20] 60)

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Side Track: Syntax Declarations

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- mixfix:

consts drvbl :: *ct* → *ct* → *fm* → *bool* ("_,-_ ⊢ _")

Legal syntax now:



- priorities:

pattern can be annotated with priorities to indicate binding strength

Example: drvbl :: *ct* → *ct* → *fm* → *bool* ("_,-_ ⊢ _" [30, 0, 20] 60)

- infixl/infixr: short form for left/right associative binary operators

Example: or :: *bool* → *bool* → *bool* (infixr "||" 30)

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Side Track: Syntax Declarations

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- mixfix:

consts drvbl :: $ct \rightarrow ct \rightarrow bool$ ("_,-_ ⊢ _,-_")

Legal syntax now:



- priorities:

pattern can be annotated with priorities to indicate binding strength

Example: $drvbl :: (ct \Rightarrow ct \Rightarrow fm) \Rightarrow bool$ ("_,-_ ⊢ _,-_" [30, 0, 20] 60)

- infixl/infixr: short form for left/right associative binary operators

Example: $or :: bool \Rightarrow bool \Rightarrow bool$ (infixr "||" 30)

- binders: declaration must be of the form

$c :: (\tau_1 \Rightarrow \tau_2) \Rightarrow \tau_3$ (binder ' B ' < p >)

$B\ x.\ P$ x translated into $c\ P$ (and vice versa)

Example $ALL :: (\alpha \Rightarrow bool) \Rightarrow bool$ (binder " \forall " 10)

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Side Track: Syntax Declarations

程序代写代做 CS编程辅导

- mixfix:

consts drvbl :: *ct* → *ct* → *fm* → *bool* ("_,-_ ⊢ _")

Legal syntax now:



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pattern can be annotated with priorities to indicate binding strength

Example: drvbl :: *ct* → *ct* → *fm* → *bool* ("_,-_ ⊢ _" [30,0,20] 60)

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B *x*. *P* *x* translated into *c P* (and vice versa)

Example ALL :: $(\alpha \Rightarrow \text{bool}) \Rightarrow \text{bool}$ (binder " \forall " 10)

More in <https://tutorcs.com> Reference Manual (8.2)

Back to HOL

程序代写代做 CS编程辅导

Base: $\text{bool}, \Rightarrow, \text{ind}, =, \longrightarrow, \varepsilon$

And the rest is



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Back to HOL

程序代写代做 CS编程辅导

Base: $\text{bool}, \Rightarrow, \text{ind}, =, \longrightarrow, \varepsilon$

And the rest is defin



True \equiv

All $P \equiv$

Ex $P \equiv$

False \equiv

$\neg P \equiv$

$P \wedge Q \equiv$

$P \vee Q \equiv$

If $P \times y \equiv$

inj $f \equiv$

surj $f \equiv$

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Back to HOL

程序代写代做 CS编程辅导

Base: $\text{bool}, \Rightarrow, \text{ind}, =, \longrightarrow, \varepsilon$

And the rest is defin

True $\equiv (\lambda x :: \text{bool}. x) (\lambda x. x)$

All $P \equiv$

Ex $P \equiv$

False \equiv

$\neg P \equiv$

$P \wedge Q \equiv$

$P \vee Q \equiv$

If $P \times y \equiv$

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Ex $P \equiv$

False \equiv WeChat: cstutorcs

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$P \vee Q \equiv$

If $P \times y \equiv$ Email: tutorcs@163.com

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surj $f \equiv$

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Back to HOL

程序代写代做 CS编程辅导

Base: $\text{bool}, \Rightarrow, \text{ind} =, \rightarrow, \varepsilon$

And the rest is defin



$$\text{True} \equiv (\lambda x : \text{bool}. x) (\lambda x. x)$$

$$\text{All } P \equiv P = (\lambda x : \text{bool}. x)$$

$$\text{Ex } P \equiv \forall Q. (\forall x. P x \rightarrow Q) \rightarrow Q$$

$$\text{False} \equiv \forall P. P = \text{False}$$

$$\neg P \equiv P \rightarrow \text{False}$$

$$P \wedge Q \equiv \forall R. (P \rightarrow Q \rightarrow R) \rightarrow R$$

$$P \vee Q \equiv \forall R. (P \rightarrow R) \rightarrow (Q \rightarrow R) \rightarrow R$$

$$\text{If } P x y \equiv \text{SOME } z. (P = \text{True} \rightarrow z = x) \wedge (P = \text{False} \rightarrow z = y)$$

$$\text{inj } f \equiv \forall x y. f x = f y \rightarrow x = y$$

$$\text{surj } f \equiv \forall y. \exists x. y = f x$$

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The Axioms of HOL

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$t = t$ refl

$s = s$ subst


$$\frac{\bigwedge x. f\ x = g\ x}{(\lambda x. f\ x) = (\lambda x. g\ x)} \text{ ext}$$

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The Axioms of HOL

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$$\frac{}{t = t} \text{ refl}$$

$$\frac{s = s}{\text{subst}}$$

$$\frac{\bigwedge x. f x = g x}{(\lambda x. f x) = (\lambda x. g x)} \text{ ext}$$

$$\frac{P = P}{P \rightarrow Q} \quad \frac{P \rightarrow Q \quad P}{Q} \text{ mp}$$

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The Axioms of HOL

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$$t = t \text{ refl}$$

$$\frac{s = s}{\text{subst}}$$

$$\frac{\bigwedge x. f x = g x}{(\lambda x. f x) = (\lambda x. g x)} \text{ ext}$$

$$\frac{P = P}{P \rightarrow Q}$$

$$\frac{P \rightarrow Q \quad P}{Q} \text{ mp}$$

$$\frac{\text{WeChat: cstutorcs}}{(P \rightarrow Q) \rightarrow (Q \rightarrow P) \rightarrow (P = Q)} \text{ iff}$$

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The Axioms of HOL

程序代写代做 CS编程辅导

$t = t$ refl

$s = \boxed{\text{QR code}}$ subst

$\frac{\bigwedge x. f x = g x}{(\lambda x. f x) = (\lambda x. g x)}$ ext

$\frac{P = Q}{P \rightarrow Q}$

$\frac{P \rightarrow Q \quad P}{Q}$ mp

$\frac{\text{WeChat: cstutorcs}}{(P \rightarrow Q) \rightarrow (Q \rightarrow P) \rightarrow (P = Q)}$ iff

$\frac{\text{Assignment Project Exam Help}}{P = \text{True} \vee P = \text{False}}$ True_or_False

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The Axioms of HOL

程序代写代做 CS编程辅导

$t = t$ refl

$s = \boxed{\text{QR code}}$ subst

$\frac{\bigwedge x. f x = g x}{(\lambda x. f x) = (\lambda x. g x)}$ ext

$\frac{P = Q}{P \rightarrow Q}$

$\frac{P \rightarrow Q \quad P}{Q}$ mp

$\frac{\text{WeChat: cstutorcs}}{(P \rightarrow Q) \rightarrow (Q \rightarrow P) \rightarrow (P = Q)}$ iff

$P = \text{True} \vee P = \text{False}$ Assignment Project Exam Help
True_or_False

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$\frac{P ? x}{P (\text{SOME } x. P x)}$ somel

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The Axioms of HOL

程序代写代做 CS编程辅导

$$\frac{}{t = t} \text{ refl}$$

$$\frac{s = s}{\text{subst}}$$

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$$\frac{P = P}{P \rightarrow Q}$$

$$\frac{P \rightarrow Q \quad P}{Q} \text{ mp}$$

$$\frac{\text{WeChat: cstutorcs}}{(P \rightarrow Q) \rightarrow (Q \rightarrow P) \rightarrow (P = Q)} \text{ iff}$$

$$\frac{P = \text{True} \vee P = \text{False}}{\text{Assignment Project Exam Help}} \text{ True_or_False}$$

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$$\frac{P ? x}{P (\text{SOME } x. P x)} \text{ somel}$$

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$$\frac{\exists f :: \text{http://tutorcs.com} \text{ surj } f}{\text{infty}} \text{ infty}$$

That's it.

程序代写代做 CS编程辅导

- 3 basic constants
- 3 basic types
- 9 axioms



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That's it.

程序代写代做 CS编程辅导

- 3 basic constants
- 3 basic types
- 9 axioms



With this you can define and derive all the rest.

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That's it.

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- 3 basic constants
- 3 basic types
- 9 axioms



With this you can define and derive all the rest.

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Isabelle knows 2 more axioms:

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$$\frac{x = y}{x \equiv y} \text{ eq-reflection} \quad \frac{\text{(THE } x \equiv x \text{)} = a}{a} \text{ the_eq_trivial}$$

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程序代写代做 CS编程辅导



Demo: The Definitions in Isabelle

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Deriving Proof Rules

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In the following, we will



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Deriving Proof Rules

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In the following, we will

→ look at the definition in detail



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Deriving Proof Rules

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In the following, we will

- look at the definitions in detail
- derive the traditional proofs from the axioms in Isabelle



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Deriving Proof Rules

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In the following, we will

- look at the definition of proof detail
- derive the traditional proof rules from the axioms in Isabelle

Convenient for deriving rules: **Named assumptions in lemmas**

lemma [name]

assumes [name₁] : " $< prop >_1$ "

assumes [name₂] : " $< prop >_2$ "

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shows " $< prop >$ " : $< proof >$

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Deriving Proof Rules

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In the following, we will

- look at the definition of detail
- derive the traditional proofs from the axioms in Isabelle



Convenient for deriving rules: **Named assumptions in lemmas**

lemma [name]

assumes [name₁] : " $< prop >_1$ "

assumes [name₂] : " $< prop >_2$ "

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shows " $< prop >$ " : $< proof >$

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proves: $\llbracket < prop >_1; < prop >_2; \dots \rrbracket \implies < prop >$

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True

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consts True :: *bool*

True $\equiv (\lambda x :: \text{bool}. x)$



Intuition:

right hand side is always

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True

程序代写代做 CS编程辅导

consts True :: *bool*

True ≡ ($\lambda x :: \text{bool}. x$)



Intuition:

right hand side is always

Proof Rules:

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$\frac{}{\text{True}}$ True_{def}

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Proof:

$$\frac{(\lambda x :: \text{bool}. x) = (\lambda x. x)}{\text{QQ: 749389476}} \frac{\text{refl}}{\text{unfold True_def}}$$

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Demo

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Universal Quantifier

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consts ALL :: $(\alpha \Rightarrow \text{bool}) \rightarrow \text{bool}$
ALL $P \equiv P = (\lambda x.$



Intuition:

- ALL P is Higher Order Abstract Syntax for $\forall x. P x$.
- P is a function that takes an x and yields a truth value.
- ALL P should be true iff P yields true for all x , i.e.

if it is equivalent to the function $\lambda x. \text{True}$

Proof Rules:

$$\frac{\bigwedge x. P x \quad \text{Email: tutorcs@163.com} \quad \forall x. P x \quad P ?x \implies R}{\forall x. P x \quad R} \text{ allI} \quad \frac{\forall x. P x \quad P ?x \implies R}{R} \text{ allE}$$

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Proof: Isabelle Demo <https://tutorcs.com>

False

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consts False :: *bool*
False ≡ $\forall P.P$



Intuition:

Everything can be derived from False.

Proof Rules:

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$$\frac{\text{False}}{P} \text{FalseE} \qquad \frac{}{\text{True} \neq \text{False}}$$

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Proof: Isabelle Demo Email: tutorcs@163.com

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Negation

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consts Not :: *bool* \Rightarrow *bool* (\neg)

$\neg P \equiv P \rightarrow \text{False}$



Intuition:

Try $P = \text{True}$ and $P = \text{False}$ and the traditional truth table for \rightarrow .

Proof Rules:

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 $\frac{A \implies \text{False}}{\neg A}$ notI $\frac{\neg A \quad A}{P}$ notE
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Existential Quantifier

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consts EX :: $(\alpha \Rightarrow \text{bool}) \rightarrow \text{bool}$

EX $P \equiv \forall Q. (\forall x. P x) \rightarrow Q$



Intuition:

- EX P is HOAS for $\exists x. P x$. (like \forall)
- Right hand side is characterization of \exists with \forall and \rightarrow
- Note that inner \forall binds wide: $(\forall x. P x) \rightarrow Q$
- Remember lemma from last time: $(\forall x. P x) \rightarrow Q = ((\exists x. P x) \rightarrow Q)$

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Proof Rules:

$$\frac{P ?x}{\exists x. P x} \text{ exI} \quad \frac{\exists x. P x \quad \bigwedge_{x: P} P x \Rightarrow R}{R} \text{ exE}$$

Proof: Isabelle Demo **QQ: 749389476**

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Conjunction

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consts And :: *bool* \Rightarrow *bool* \rightarrow *bool* ($_ \wedge _$)

$P \wedge Q \equiv \forall R. (P \rightarrow C) \wedge (Q \rightarrow C) \rightarrow R$



Intuition:

- Mirrors proof rules for \wedge
- Try truth table for P , Q , and R

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Proof Rules:

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$$\frac{A \quad B}{A \wedge B} \text{ conjI} \quad \frac{A \wedge B \quad [A; B] \Rightarrow C}{C} \text{ conjE}$$

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Proof: Isabelle Demo

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Disjunction

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consts Or :: $bool \Rightarrow bool \rightarrow bool$ ($_ \vee _$)

$P \vee Q \equiv \forall R. (P \rightarrow (P \vee Q) \rightarrow R) \rightarrow R$



Intuition:

- Mirrors proof rules for \vee (case distinction)
- Try truth table for P , Q , and R

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Proof Rules:

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$$\frac{A}{A \vee B} \quad \frac{B}{A \vee B} \quad \text{disjI1/2} \quad \frac{\frac{A \vee B}{A \implies C} \quad \frac{A \implies C}{B \implies C}}{C} \quad \text{disjE}$$

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Proof: Isabelle Demo

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If-Then-Else

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consts If :: $\text{bool} \Rightarrow \alpha \Rightarrow \alpha \Rightarrow \alpha$ (if_then_else_)

If $P x y \equiv \text{SOME } z.$  $\rightarrow z = x) \wedge (P = \text{False} \rightarrow z = y)$

Intuition:

- for $P = \text{True}$, right hand side collapses to $\text{SOME } z. z = x$
- for $P = \text{False}$, right hand side collapses to $\text{SOME } z. z = y$

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Proof Rules:

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$$\frac{}{\text{if True then } s \text{ else } t = s} \text{ ifTrue} \quad \frac{}{\text{if False then } s \text{ else } t = t} \text{ ifFalse}$$

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Proof: Isabelle Demo QQ: 749389476

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We have learned today ...

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→ More automation



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We have learned today ...

程序代写代做 CS编程辅导

- More automation
- Defining HOL



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We have learned today ...

程序代写代做 CS编程辅导

- More automation
- Defining HOL
- Higher Order Abstr



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We have learned today ...

程序代写代做 CS编程辅导

- More automation
- Defining HOL
- Higher Order Abstr
- Deriving proof rules



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