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COMP4418 Knowledge Representation and Reasoning



Commonsense Reasoning: Non-Monotonic Reasoning

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Strictness of FOL

To reason from $P(a)$ to $Q(a)$, need either

- facts about a itself
- universals, e.g. $\forall x(P(x) \rightarrow Q(x))$
 - something that applies to all instances
 - all or nothing!

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But most of what we learn about the world is of *generics*

- e.g., encyclopedia entries for ferris wheels, violins, turtles, wildflowers

Properties are not strict for all instances, because

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- genetic / manufacturing varieties
 - early ferris wheels
- borderline cases
 - toy violins
- imagined cases
 - flying turtles
- cases in exceptional circumstances
 - dried wildflowers
- ...

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Generics vs Universals

Violins have four strings

vs.

All violins have four strings

vs.

All violins that are not E_1 or E_2 or ... have four strings

(exceptions usually cannot be enumerated)

Similarly, for general properties of individuals

Alexander the great: ruthlessness

Ecuador: exports

pneumonia: treatment

Goal: be able to say a P is a Q in general, but not necessarily

reasonable to conclude $Q(a)$ given $P(a)$ unless there is a good reason not to

Here: qualitative version (no numbers)

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Varieties vs Defaults

General statements

- statistical: Most P 's are Q 's.
 - People living in Quebec speak French.
- normal: All normal P 's are Q 's.
 - Polar bears are white.
- prototypical: The prototypical P is a Q .
 - Owls hunt at night.

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Representational

- conversational: Unless I tell you otherwise, a P is a Q .
 - default slot values in frames
 - disjointness in IS-A hierarchy (sometimes)
 - closed-world assumption (below)

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Epistemic rationales

- familiarity: If a P was not a Q , you would know it.
 - an older brother
 - very unusual individual, situation or event
- group confidence: All known P 's are Q 's.
 - NP-hard problems unsolvable in polynomial time.

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Persistence rationale

- inertia: A P is a Q if it used to be a Q .
 - colours of objects
 - locations of parked cars (for a while!)

Nonmonotonic Reasoning

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- Suppose you are told “Tweety is a bird”
- What conclusions would you draw?
- Now, consider being further informed that “Tweety is an emu”
- What conclusions would you draw now? Do they differ from the conclusions that you would draw without this information? In what way(s)?
- Nonmonotonic reasoning is an attempt to capture a form of *commonsense* reasoning

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Nonmonotonicity

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Closed World Assumption



Predicate Completion

Circumscription

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Default Logic

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Nonmonotonic Consequence

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Nonmonotonic Reasoning

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- In classical logic the more (premises) we have, the more conclusions we can draw
- This property is known as *Monotonicity*



If $\Delta \subseteq \Gamma$, then $Cn(\Delta) \subseteq Cn(\Gamma)$

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(where Cn denotes classical consequence)

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- However, the previous example shows that we often do not reason in this manner
- Might a nonmonotonic logic—one that does not satisfy the Monotonicity property—provide a more effective way of reasoning?

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Why Nonmonotonicity?

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- Problems with the classic approach to consequence
 - It is usually not possible to say down all we would like to say about a domain
 - Inferences in classical logic simply make implicit knowledge explicit; we would also like to reason with tentative statements
 - Sometimes we would like to represent knowledge about something that is not *entirely* true or false; uncertain knowledge
- Nonmonotonic reasoning is concerned with getting around these shortcomings

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Makinson's Classification

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Makinson has suggested the classification of nonmonotonic logics:

- Additional background assumptions
- Restricting the set of valuations
- Additional rules

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David Makinson, *Bridges from Classical to Nonmonotonic Logic*, Texts in Computing, Volume 5, King's College Publications, 2005.

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Nonmonotonicity

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- Classical logic satisfies the following property
- Monotonicity: If $\Delta \subseteq \Gamma$, then $Cn(\Delta) \subseteq Cn(\Gamma)$
(equivalently, $\Gamma \vdash \phi$ implies $\Gamma \cup \Delta \vdash \phi$)
- However, we often draw conclusions based on ‘what is normally the case’ or ‘true by default’
- More information can lead us to retract previous conclusions
- We shall adopt the following notation
 - \vdash classical consequence relation
 - \vdash_{\sim} nonmonotonic consequence relation

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Consequence Operation Cn

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Other properties of consequence operation Cn :

Inclusion $\Delta \subseteq Cn(\Delta)$

Cumulative Transitivity $\Delta \subseteq \Gamma \subseteq Cn(\Delta)$ implies $Cn(\Gamma) \subseteq Cn(\Delta)$

Compactness If $\phi \in Cn(\Delta)$ then there is a finite $\Delta' \subseteq \Delta$ such that $\phi \in Cn(\Delta')$

Disjunction in the Premises $Cn(\Delta \cup \{a\}) \cap Cn(\Delta \cup \{b\}) \subseteq Cn(\Delta \cup \{a \vee b\})$

Note: $\Delta \vdash \phi$ iff $\phi \in Cn(\Delta)$

alternatively: $Cn(\Delta) = \{\phi : \Delta \vdash \phi\}$

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Example

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Suppose I tell you 'Tweety is a bird'

You might conclude 'Tweety flies'

I then tell you 'Tweety is an emu'

You conclude 'Tweety does not fly'

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$bird(Tweety) \vdash flies(Tweety)$

$bird(Tweety) \wedge emu(Tweety) \vdash \neg flies(Tweety)$

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The Closed World Assumption

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- A *complete* theory is one for which for every ground atom in the language, either the atom or its negation appears in the theory
- The *closed world assumption* (CWA) completes a base (non-closed) set of formulae by including the negation of a ground atom whenever the atom does not follow from the base
- In other words, if we have no evidence as to the truth of (ground atom) P , we assume that it is false
- Given a base set of formulae Δ we first calculate the *assumption* set Δ_{asm} iff for ground atom P , $\neg P \in \Delta_{asm}$ iff for ground atom P , $P \notin \Delta$
- $CWA(\Delta) = Cn\{\Delta \cup \Delta_{asm}\}$



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Example

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$$\Delta = \{P(a), P(b), P(a) \rightarrow Q(a)\}$$

$$\Delta_{asm} = \{\neg Q(b)\}$$



Theorem: The CWA applied to a consistent set of formulae Δ is inconsistent iff there are positive ground literals L_1, \dots, L_n such that $\Delta \models L_1 \vee \dots \vee L_n$ but $\Delta \not\models L_i$ for $i = 1, \dots, n$.

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- Note that in the example above we limited our attention to the object constants that appeared in Δ however the language could contain other constants. This is known as the *Domain Closure Assumption* (DCA).
- Another common assumption is the *Unique-Names Assumption* (UNA).
If two ground terms can't be proved equal, assume that they are not.

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Predicate Completion

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Idea: The only objects that satisfy a predicate are those that must

- For example, suppose we have a predicate $P(x)$. Can view this as

$$\forall x. x = a \rightarrow P(x)$$

the *if*-half of a definition **WeChat: cstutorcs**

- Can add the *only if* part: **Assignment Project Exam Help**

$$\forall x. P(x) \rightarrow x = a$$

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$$\forall x. P(x) \leftrightarrow x = a$$

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Predicate Completion

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- **Definition:** A clause is solitary in a predicate P if whenever the clause contains a positive instance of P , it contains only one instance of P .
 - For example, $Q(a) \vee P(a) \vee R(b)$ is not solitary in P
 $Q(a) \vee R(a) \vee P(b)$ is solitary in P
- Completion of a predicate is only defined for sets of clauses solitary in that predicate

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Predicate Completion

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- Each clause can be written:

$$\forall y. Q_1 \wedge \dots \wedge Q_m \rightarrow P(t) \quad (\text{contained in } Q_i)$$

$$\forall y. \forall x. (x = t) \wedge Q_1 \wedge \dots \wedge Q_m \rightarrow P(x)$$

$$\forall x. (\forall y. (x = t) \wedge Q_1 \wedge \dots \wedge Q_m \rightarrow P(x)) \quad (\text{normal form of clause})$$

- Doing this to every clause gives us a set of clauses of the form:

$$\forall x. E_1 \rightarrow P(x)$$

...

$$\forall x. E_n \rightarrow P(x)$$

- Grouping these together we get:

$$\forall x. E_1 \vee \dots \vee E_n \rightarrow P(x)$$

- Completion becomes: $\forall x. P(x) \leftrightarrow E_1 \vee \dots \vee E_n$
and we can add this to the original set of formulae

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Example

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- Suppose $\Delta = \{\forall x. Emu(x) \rightarrow Bird(x),$
 $Bird(Tweety) \rightarrow \neg Emu(Tweety)\}$

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- We can write this as

$$\forall x. (Emu(x) \vee x = Tweety) \rightarrow Bird(x)$$

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- Predicate completion of P in Δ becomes

$$\Delta \cup \{\forall x. Bird(x) \rightarrow Emu(x) \vee x = Tweety\}$$

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Circumscription

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- **Idea:** Make extension of as small as possible

- Example:

$\forall x. Bird(x) \wedge \neg Ab(x) \rightarrow Flies(x)$
 $Bird(Tweety), Bird(Sam), Tweety \neq Sam, \neg Flies(Sam)$

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- Want to be able to conclude $Flies(Tweety)$ but $\neg Flies(Sam)$
- Accept interpretations where Ab predicate is as “small” as possible
- That is, we *minimise abnormality*

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Circumscription

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- Given interpretations $I_1 = \langle D, I_1 \rangle$, $I_2 = \langle D, I_2 \rangle$, $I_1 \leq I_2$ iff for every predicate $P \in \mathbf{P}$, $I_1[P] \subseteq I_2[P]$.
- $\Gamma \models_{\text{circ}} \phi$ iff for every interpretation I such that $I \models \Gamma$, either $I \models \phi$ or there is a $I' < I$ and $I' \models \Gamma$.

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- ϕ is true in all minimal models

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- Now consider

$\forall x. Bird(x) \wedge \neg Ab(x) \rightarrow Flies(x)$

$\forall x. Emu(x) \rightarrow Bird(x) \wedge \neg Flies(x)$

$Bird(Tweety)$

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Reiter's Default Logic (1980)

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- Add default rules of the form $\frac{\alpha:\beta}{\gamma}$
 - “If α can be proven and β is consistent to assume β , then conclude γ ”
- Often consider *normal* defaults $\frac{\alpha:\beta}{\beta}$
- Example: $\frac{bird(x):flies(x)}{flies(x)}$
- Default theory $\langle D, W \rangle$
 - D – set of defaults; W – set of facts
- *Extension* of default theory contains as many default conclusions as possible and must be consistent (and is closed under classical consequence Cn)
- Concluding whether formula ϕ follows from $\langle D, W \rangle$
 - Sceptical inference: ϕ occurs in every extension of $\langle D, W \rangle$
 - Credulous inference: ϕ occurs in *some* extension of $\langle D, W \rangle$

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Examples

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- $W = \{\}; D = \{\frac{p}{\neg p}\}$ – no extensions
- $W = \{p \vee r\}; D = \{\frac{p:q}{q}\}$ – one extension $\{p \vee r\}$
- $W = \{p \vee q\}; D = \{\frac{\neg p}{\neg p}, \frac{\neg q}{\neg q}\}$ – two extensions $\{\neg p, p \vee q\}, \{\neg q, p \vee q\}$
- $W = \{emu(Tweety), \forall x. emu(x) \rightarrow bird(x)\}; D = \{\frac{bird(x):flies(x)}{flies(x)}\}$ – one extension
- What if we add $\frac{emu(x):\neg flies(x)}{\neg flies(x)}$?
- Poole (1988) achieves a similar effect (but not quite as general) by changing the way the underlying logic is used rather than introducing a new element into the syntax

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Default Theories—Properties

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Observation: Every normal default theory (default rules are all normal) has an extension



Observation: If a normal default theory has several extensions, they are mutually inconsistent

Observation: A default theory has an inconsistent extension iff D is inconsistent

Theorem: (Semi-monotonicity)

Given two normal default theories $\langle D, W \rangle$ and $\langle D', W \rangle$ such that $D \subseteq D'$ then, for any extension $\mathcal{E}(D, W)$ there is an extension $\mathcal{E}(D', W)$ where $\mathcal{E}(D, W) \subseteq \mathcal{E}(D', W)$

(The addition of normal default rules does not lead to the retraction of consequences.)

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Nonmonotonic Consequence

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- Abstract study and analysis of nonmonotonic consequence relation \vdash in terms of general properties (Lehmann and Magidor (1991))

- Some common properties include:

Supraclassicality If $\phi \vdash \psi$, then $\phi \vdash \psi$ WeChat: cstutorcs

Left Logical Equivalence If $\vdash \phi \leftrightarrow \psi$ and $\phi \vdash \chi$, then $\psi \vdash \chi$ Assignment Project Exam Help

Right Weakening If $\vdash \psi \rightarrow \chi$ and $\phi \vdash \psi$, then $\phi \vdash \chi$

And If $\phi \vdash \psi$ and $\phi \vdash \chi$, then $\phi \vdash \psi \wedge \chi$ Email: tutorcs@163.com

- Plus many more!

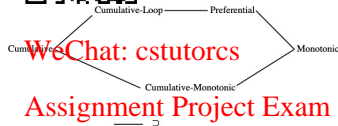
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- Kraus, Lehman and Magidor (1991) study various classes of nonmonotonic consequence relations



- This has been extended since. A good reference for this line of work is Schlechta (1997)

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Summary

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- Nonmonotonic reasoning to capture a form of commonsense reasoning
- Nonmonotonic reasoning deals with inferences based on defaults or 'what is usually the case'
- Belief change and nonmonotonic reasoning: two sides of the same coin?
- Can introduce abstract study of nonmonotonic consequence relations in same way as we study classical consequence relations
- Similar links exist with conditionals
- One area where nonmonotonic reasoning is important is reasoning about action (dynamic systems)



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