

程序代写代做 CS编程辅导



COMP4418 Knowledge Representation and Reasoning

Propositional Logic 2

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COMP4418, Week 1

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Propositional Logic

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- Thus far we have considered propositional logic as a knowledge representation language
- We can now write sentences in this language (syntax)
- We can also determine the truth or falsity of these sentences (semantics)
- What remains is to *reason*; to draw new conclusions from what we know (proof theory) and to do so using a computer to automate the process
- References:
 - Stuart J. Russell and Peter Norvig, *Artificial Intelligence: A Modern Approach*, Prentice-Hall International, 1995. (Chapter 6)

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Overview

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- Normal Forms
- Resolution
- Refutation Systems
- Correctness of resolution rule
- Conclusion

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— soundness and completeness revisited

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Motivation

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*If either George or Herb
Kenneth lose
George wins*



Therefore, Jack loses

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$(G \vee H) \rightarrow (\neg J \wedge \neg K)$

G

$\neg J$

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Normal Forms

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- A *normal form* is a “standard” version of a formula
- Common normal forms:
 - Negation Normal Form* — *n* symbols occur in front of propositional letters only (e.g., $(P \vee \neg Q) \rightarrow (P \wedge (\neg R \vee S))$)
(A literal is a propositional letter or the negation of a propositional letter.)
 - Conjunctive Normal Form (CNF)* — a conjunct of disjunctions (e.g., $(P \vee Q \vee \neg R) \wedge (\neg S \vee \neg R)$)
 - Disjunctions of literals* are known as clauses
 - Disjunctive Normal Form (DNF)* — a disjunct of conjunctions (e.g., $(P \wedge Q \wedge \neg R) \vee (\neg S \wedge \neg R)$)

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Negation Normal Form

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- To simplify matters, let us suppose we are only dealing with formulae containing the connectives \neg , \wedge , \vee
- A (sub)formula $\phi \rightarrow \psi$ is equivalent to $\neg\phi \vee \psi$
- A (sub) formula $\phi \leftrightarrow \psi$ is equivalent to $\phi \rightarrow \psi$ and $\psi \rightarrow \phi$
- DeMorgan's laws:
 - $\neg(\phi \wedge \psi) \equiv \neg\phi \vee \neg\psi$
 - $\neg(\phi \vee \psi) \equiv \neg\phi \wedge \neg\psi$
- Double Negation: $\neg\neg P \equiv P$
- To put a formula in negation normal form, repeatedly apply De Morgan's laws and double negation
- For example, $\neg(P \vee (\neg R \wedge P)) \equiv \neg P \wedge \neg(\neg R \wedge P) \equiv \neg P \wedge (R \vee \neg P)$

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Conjunctive Normal Form

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- Note the following distributive identities:

$$(\phi \wedge \psi) \vee \chi \equiv (\phi \vee \chi) \wedge (\psi \vee \chi)$$

$$(\phi \vee \psi) \wedge \chi \equiv (\phi \wedge \chi) \vee (\psi \wedge \chi)$$

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- To put a formula in conjunctive normal form (CNF) firstly put the formula into negation normal form and then repeatedly apply the identities above
- For example, $R \rightarrow (P \wedge Q) \equiv (\neg R \vee P) \wedge (\neg R \vee Q)$

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Resolution Rule

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Resolution Rule:



- Where β is a literal (i.e., a propositional letter or its negation)

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Resolution Rule

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- Resolution is essentially equivalent to the transitivity of material implication
- In fact, it is a form of the well known cut rule in logic

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Applying Resolution

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- The resolution rule is sound
- What does that mean?
- How can we use the resolution rule?
 - Convert premises into CNF
 - Repeatedly apply resolution rule to the resultant clauses
 - Each clause produced can be inferred from the original premises
 - If you have a query sentence goal, it follows from the premises if and only if each of the clauses in CNF(goal) is produced by resolution
- There is a better way ...

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Refutation Systems

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- If we would like to prove a formula ϕ is a theorem (i.e., $\vdash \phi$), we start with $\neg\phi$ and produce a contradiction
- A “proof by contradiction”
- Similarly, if we wish to prove $\psi_1, \dots, \psi_n \vdash \phi$, start with $\neg\phi$ and together with ψ_1, \dots, ψ_n produce a contradiction
- Resolution can be used to implement a refutation system
- Repeatedly apply resolution rule until *empty clause* results

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Applying Resolution

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- Negate conclusion (resolution refutation system)
- Convert premises and negated conclusion into CNF (*clausal form*)
- Repeatedly apply Resolution Rule, Double Negation
- If *empty clause* results you have a contradiction and can conclude that the conclusion follows from the premises

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Resolution — Example 1

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$(G \vee H) \rightarrow (\neg J \wedge \neg K), G \vdash \neg J$
 $CNF[(G \vee H) \rightarrow (\neg J \wedge \neg K)] \equiv (\neg G \vee \neg J) \wedge (\neg H \vee \neg J) \wedge (\neg G \vee \neg K) \wedge (\neg H \vee \neg K)$

1. $\neg G \vee \neg J$ [Premise]

2. $\neg H \vee \neg J$ [Premise]

3. $\neg G \vee \neg K$ [Premise]

4. $\neg H \vee \neg K$ [Premise]

5. G [Premise]

6. $\neg\neg J$ [\neg Conclusion]

7. J [6. Double Negation]

8. $\neg G$ [1, 7. Resolution]

9. \square [5, 8. Resolution]



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Resolution — Example 2

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$P \rightarrow \neg Q, \neg Q \rightarrow R \vdash P \rightarrow R$

$P \rightarrow R \equiv \neg P \vee R$

$CNF[\neg(\neg P \vee R)] \equiv \{\neg\neg P, \neg R\}$

1. $\neg P \vee \neg Q$ [Premise]

2. $\neg\neg Q \vee R$ [Premise]

3. $\neg\neg P$ [\neg Conclusion]

4. $\neg R$ [\neg Conclusion]

5. P [3. Double Negation]

6. $\neg Q$ [1, 5. Resolution]

7. R [2, 6. Resolution]

8. \square [4, 7. Resolution]



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Resolution — Example 3

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$\vdash ((P \vee Q) \wedge \neg P) \rightarrow Q$

$CNF[\neg(((P \vee Q) \wedge \neg P) \rightarrow Q)] \rightarrow (P \vee Q) \wedge \neg P \wedge \neg Q$

1. $P \vee Q$ [\neg Conclusion]

2. $\neg P$ [\neg Conclusion]

3. $\neg Q$ [\neg Conclusion]

4. Q [1, 2. Resolution]

5. \square [3, 4. Resolution]

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Soundness and Completeness — Recap

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- An inference procedure (for a logic) is *sound* if and only if it preserves truth
- In other words \vdash is sound iff whenever $\lambda \vdash \rho$, then $\lambda \models \rho$
- A logic is *complete* if and only if it is capable of proving all truths
- In other words, whenever $\lambda \models \rho$, then $\lambda \vdash \rho$

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Decidability

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- A logic is *decidable* if and only if there is a mechanical procedure that, when asked $\lambda \vdash \rho$, can eventually halt and answer “yes” or halt and answer “no”
- Propositional logic is decidable

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Heuristics in applying Resolution

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- Clause elimination — can ignore certain types of clauses
 - Pure clauses: contain L where $\neg L$ doesn't appear elsewhere
 - Tautologies: clauses containing both L and $\neg L$
 - Subsumed clauses: another clause exists containing a subset of the literals
- Ordering strategies
 - Unit preference: resolve unit clauses (only one literal) first
- Many others ...

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Conclusion

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- We have now investigate knowledge representation and reasoning formalism
- This means we can draw conclusions from the knowledge we have; we can reason
- Have enough to build a knowledge-based agent
- However, propositional logic is a weak language, there are many things we can't express in it
- It cannot be used to express knowledge about objects, their properties and the relationships that exist between objects
- For this purpose we need a more expressive language: *first-order logic*



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