#### 程序代写代做 CS编程辅导



# COMP44 nowledge Representation and Reas g

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## Goal

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Deductive reasoning in language as close as possible to full FOL

$$\neg, \land, \lor, \exists, \forall$$

Knowledge Level:

given KB, 
$$\alpha$$
, determine if K

or given an open 
$$\alpha(x_1, x_2, \dots x_n)$$
, find  $t_1, t_2, \dots t_n$  such that  $KB \models \alpha(t_1, t_2, \dots t_n)$ 

When KB is finite  $\{\alpha_1, \alpha_2, \dots, \alpha_k\}_{gnment Project Exam Help}$ 

$$\mathsf{KB} \models \alpha$$

iff 
$$\models [\{\alpha_1 \land \alpha_2 \land \ldots \land \alpha_k\}]$$
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iff KB  $\cup \{\neg \alpha\}$  is unsatisfiable Q: 749389476

iff KB 
$$\cup \{\neg \alpha\} \models \mathsf{FALSE}$$

So want a procedure to test for tradidity, or satisfiability, or for entailing FALSE.

# **Clausal Representation**

Formula = set of clauses Clause = set of literals Literal = atomic sentence or it's negation positive literal and negative literal positive predicate and negative predicate in FOL Notation:

- If p is a literal, then  $\bar{p}$  is its complement  $\bar{p} \Rightarrow \neg p$
- To distinguish clauses from formulas:





[ and ] for clauses:  $[p, \neg r, s]$  WeChat: cstutorcs { and } for formulas:  $\{[p, \neg r, s], [p, r, s], [\neg p]\}$  [] is the empty clause;  $\{\}$  is the empty formula

So {} is different from {[]}! Assignment Project Exam Help

#### Interpretation:

- Formula understood as *conjunction* of clauses Email: tutorcs@163.com
- Clause understood as disjunction of clauses
- Literals understood normally

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So:

- $\{[\rho,\neg q],[r],s]\} \text{ is a representation of } ((\rho \vee \texttt{hothers.com}))$
- [] is a representation of FALSE
- {} is a representation of TRUE

## **Resolution Rule of Inference**

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Given two clauses, infer a new clause:

From clause  $\{p\} \cup C_1$  and  $\{\neg p\} \cup C_2$ ,

infer clause  $C_1 \cup C_2$ .

 $C_1 \cup C_2$  is called a *resolvent* of input

Example:

From clauses [w, p, q] and  $[w, s, \neg p]$  have [w, q, s] as resolvent wrt p.

Special Case:

[p] and  $[\neg p]$  resolve to []

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Tith respect to p.

 $C_1$  and  $C_2$  are empty

A derivation of a clause c from a set  $c_n$  of plauses, where the last clause  $c_n = c$ , and for each  $c_n$  either

1.  $c_i \in S$ , or

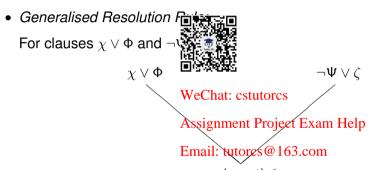
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2.  $c_i$  is a resolvent of two earlier qlauses in the derivation

Write:  $S \vdash c$  if there is a derivation

## **Resolution Rule of Inference**

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- Where  $\theta$  is a unifier for atomic formulae  $\Phi$  and  $\Psi$
- $\chi \vee \zeta$  is known as the *residering* tutorcs.com



## Rationale

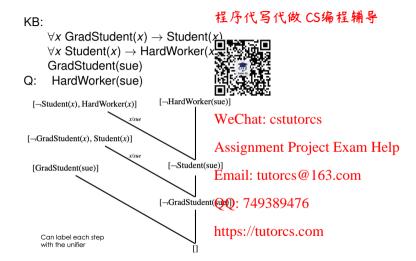
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```
Resolution is a symbol-level rule of inference, but has a connection to
knowledge-level logical interpretatio
Resolvent is entailed by input clause
Suppose I \models (p \lor \alpha) and I \models (\neg p \lor \square
                     Case 1: I \models p
                                           then I \models \beta, so I \models (\alpha \lor \beta). WeChat: cstutores
                      Case 2: 1 \nvDash p
                                           then I \models \alpha, so I \models (\alpha \lor \beta). Assignment Project Exam Help
                      Either way, I \models (\alpha \lor \beta).
                     So: \{(p \lor \alpha), (\neg p \lor \beta)\} \models (\alpha \lor \beta) Email: tutores@163.com
Special case:
                       [p] and [\neg p] resolve to [],
                                                                                                                                                                                 OO: 749389476
                     so \{[p], [\neg p]\} \models \mathsf{FALSE}
                    that is: \{[p], [\neg p]\} is unsatisfiable through the statement of the sta
```

## **Derivations and entailment**

```
Can extend the previous argument t起的協區低做 CS编程辅导
                If S \vdash c then S \models c
                Proof: by induction on the lengt
                                 Show (by looking at the two s at s = c_i.
But the converse does not hold in adia : .....
                Can have S \models c without having
                Example: \{ [\neg p] \} \models [\neg p, \neg q], i.e., \neg p \models (\neg p \lor \neg q)
                 but no derivation
However. . . .
Resolution is sound and complete for Institution is sound as a second and complete for Institution is sound as a second and complete for Institution is sound as a second and complete for Institution is sound as a second and complete for Institution is sound as a second and complete for Institution is sound as a second and complete for Institution is sound as a second and complete for Institution is sound as a second and complete for Institution is second as a second and complete for Institution is second as a second and complete for Institution is second as a second and complete for Institution is second as a second and complete for Institution is second as a second and complete for Institution is second as a second as a second and complete for Institution is second as a second and complete for Institution is second as a second and complete for Institution is second as a second and complete for Institution is second as a secon
                  Theorem: S \vdash [] iff S \models []
                         Result will carry over to quantified that see (later) 63.com
So for any set S of clauses:
                                                                                                                                      OO: 749389476
                  S is unsatisfiable iff S \vdash [].
                         Provides method for determining satisfiability:
                                 Search all derivations to see if [] is produced
                          Also provides method for determining all entailments
```

# **Example**



# The 3 block example

```
already in CNF
 Q = \exists x \exists y [On(x,y) \land Green(x) \land \neg
                                  Note: ¬Q has no existentials to ₩
                                  yields \{ [\neg On(x,y), \neg Green(x), \neg Green
                                                                                                                                                           [-On(x,y), -Green(x), Green(y)] We Chat: cstutorcs
                                  [On(b,c)]
                                                                                                                                                                                                                                                                Assignment Project Exam Help
                                                        [-Green(b), Green(c)]
                                                                                                                                                                                                       \{x/a, y/b\}
                                                                                                                                                                                                                                                                       Email: tutores@163.com
                 [¬Green(c)]
                                                                                                                                                  [-Green(a), Green(b)]
                                                                                                                                                                                                                                                            [Green(a)] 749389476
                                                                           [-Green(b)]
                                                                                                                                                                                             [Green(b)]
                                                                                                                                                                                                                                                                       https://tutorcs.com
                            Note: Need to use
                            On(x,y) twice, for 2 cases
```

## **Arithmetic**

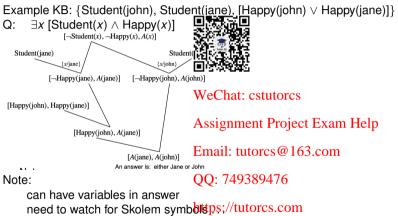
程序代写代做 CS编程辅导 KB: Plus(zero, x, x) $Plus(x,y,z) \rightarrow Plus(succ(x),y,s)$ Q:  $\exists u \text{ Plus}(2,3,u)$ where for readability, we use 0 for zero. 3 for succ(succ(succ(zero))) etc. WeChat: cstutorcs  $[\neg \text{Plus}(x,y,z), \text{Plus}(\text{succ}(x),y,\text{succ}(z))]$  $[\neg Plus(2,3,u)]$ Assignment Project Exam Help [Plus(0,x,x)] $[\neg Plus(1,3,v)]$ Email: tutorcs@163.com x/0, v/3, v/succ(w), z/w OO: 749389476  $\neg \text{Plus}(0,3,w)$ Can find the answer x/3. w/3 in the derivation u/succ(succ(3))https://tutorcs.com i.e u/5to keep them distinct Can derive Plus(2.3.5)

# **Answer predicates**

```
In full FOL, have possibility of derivin 程本所来 所说 (Se编 传统) derive P(t) for any t
     e.g. the three-blocks problem
          \exists x \exists v \ [On(x,v) \land Green(x) \ \blacksquare
          but cannot derive which blo
Solution: answer-extraction process it is
     replace query \exists x P(x) by \exists x [P(P)]
       where A is a new predicate symbol called the answer predicate
     instead of deriving [], derive any clause containing fust the answer predicate
     can always convert a derivation of []
Example KB: {Student(john), Student(jahe), Habby Foiert Exam Help
     \exists x [Student(x) \land Happy(x)]
                                        Email: tutorcs@163.com
                     [-Student(x), -Happy(x), A(x)] OQ: 749389476
          Happy(john)
Student(jane)
         Student(iohn)
                    Student(john), A(john)]
                                        https://tutorcs.com
                  [A(john)]
                           An answer is: John
```

# Disjunctive answers

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## **A Problem**

程序代写代做 CS编程辅导 KB:  $LessThan(succ(x), y) \rightarrow LessThan(x, y)$ Q: LessThan(zero, zero) Should fail since KB  $\not\models Q$ [LessThan(x,y),  $\neg$ LessThan(succ(x),y)]  $[\neg LessThan(0,0)]$ WeChat: cstutores x/0, y/0[-LessThan(1,0)]Assignment Project Exam Help [-LessThan(2,0)] Email: tutores@163.com OO: 749389476

Infinte branch of resolvents

cannot use a simple depth-first procedure to search for []

# Undecidability

Is there a way to detect when this happens? No! FOL is very powerful CS编程辅导

- can be used as a full pro@震源即 language
- just as there is no way to general when a program is looping

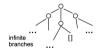
There can be no procedure the third this

```
Proc[Clauses] =

If Clauses are unsatisfiable estutores
then return YES
else return NO

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```

However: Resolution is complete some branch will contain [], for unsat clauses



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So breadth-first search guaranteed to find [] search may not terminate on satisfiable clauses

# Overly specific unifiers

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```
In general, no way to guarantee effice ven termination
     later: put control into users' han
One major way:
    reduce redundancy in search, by search as general as possible
Example:
    ..., P(g(x), f(x), z) [\neg P(y, f(W) \in S hat: estutores
    unified by
      \theta_1 = \{x/b, y/g(b), z/a, w/b\}^{Assignment} Project Exam Help
    and by
      \theta_2 = \{x/f(z), y/g(f(z)), z/a, \frac{\text{Email}}{w/f(z)}\} \text{ tutorcs} (0.163 \text{ com}), f(f(z)), a).
Might not be able to derive [] from clauses having overly specific substitutions
    wastes time in search!
```

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# Most general unifiers

heta is a most general unifier of literals  $I_1$  an 製作、写代做 CS编程辅导

- 1.  $\theta$  unifies  $l_1$  and  $l_2$
- 2. for any other unifier  $\theta'$ , there is an  $\theta'$  bution  $\theta^*$  such that  $\theta' = \theta \theta^*$ note: composition  $\theta\theta^*$  require  $\theta^*$  to terms in  $\theta$ for previous example, an MGL 📆 🕮  $\theta = \{x/w, y/g(w), z/a\}$ for which  $\theta_1 = \theta \{ w/b \}$ WeChat: cstutores

 $\theta_2 = \theta \{ w/f(z) \}$ Theorem: Can limit search to MGUs only without loss of completeness (with certain caveats) Computing an MGU, given a set of lits {//ASSIgnment Project Exam Help

1. Start with  $\theta = \{\}$ .

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  2. If all the  $l_i\theta$  are identical, then done; otherwise, get disagreement set, DSe.g.  $P(a, f(a, g(z), \dots, P(a, f(a)u, \frac{1}{14938}))$  disagreement set,  $DS = \{u, g(z)\}$
- 3. Find a variable  $v \in DS$ , and a term  $t \in DS$  not containing v. If not, fail.
- 4.  $\theta = \theta \{ v/t \}$

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5. Go to 2

Note: there is a better linear algorithm

### **Herbrand Theorem**

Some 1st-order cases can be handled by converting them to a propositional form Given a set of clauses S

• the Herbrand universe of S is the Herbrand universe of S in S in the Herbrand universe of S is the Herbrand universe of S in the Herbrand universe of S is the Herbrand universe of S in the Herbrand universe of S is the Herbrand universe of S in the Herbrand universe of S is the Herbrand universe of S in the Herbrand universe of S is the Herbrand universe of S in the Herbrand universe of S is the Herbrand universe of S in the Herbrand universe of S in the Herbrand universe of S is the Herbrand universe of S in the Herbrand univers

• the Herbrand base of *S* is WeChat: cstutorcs

 $\{c\theta|c\in S \text{ and } \theta \text{ replaces the variables in } c \text{ by terms from the Herbrand universe} \}$ Assignment Project Exam Help Theorem: S is satisfiable iff Herbrand base is (applies to Horn clauses also)

Theorem: S is satisfiable iff Herbrand base is (applies to Horn clauses also)

Herbrand base has no variables, and so is essentially propositional, though usually infinite

- finite, when Herbrand universe is finite can use propositional methods (guarantee)
- sometimes other "type" restrictions can be used to keep the Herbrand base finite include f(t) only if t is the correct type



## Resolution is difficult!

First-order resolution is not guaranteed to terminate. What can be said about the propositional case 代故 CS编程辅导

- Recently shown by Haken that  $c_1, c_2, \ldots, c_n$  such that the shortest derivation of [] contains  $c_1, c_2, \ldots, c_n$  such that the
- Even if we could always find a first immediately, the most clever search procedure will still require exponential time or be sublems

Problem just with resolution?

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Probably not.

- Determining if set of clauses is satisfiable shown by Qook to be INP-complete
  - o no easier than an extremely large variety of computational tasks
  - any search task where whanki searched for tan be recast as a satisfiability problem

satisfiability QQ: 749389476

does graph of cities allow for a full tour of size *k* miles? can *N* queens be pure the arrange of the second all safely?

. . .

· Satisfiability is strongly believed

# Implications for KR

Problem: want to produce entailments of 程序的问题的 in making in the in the intermediate i

- full theorem-proving may be too difficult for KR!
- need to consider other options
  giving control to user
  procedural representation
  less expressive languages
  e.g. Horn clauses (and a major theme later)

e.g. Horn clauses (and a major theme later)
In some applications, it is reasonable to Well-Chat: cstutores

• e.g. mathematical theorem proving, where we only care about specific formula

Best to hope for in general: reduce redundant project Exam Help

• refinements to resolution to improve search Email: tutorcs@163.com

Main example: MGU, as before

but many other possibilities OO: 749389476
 need to be careful to preserve completeness

ATP: automated theorem proving <a href="https://tutorcs.com">https://tutorcs.com</a>
 area that studies strategies for proving difficult theorems
 main application: mathematics, but relevance also to KR



# **Strategies**

1. Clause elimination

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• pure clause contains literal / such that tappear in any other clause clause cannot lead to []

- tautology
  - clause with a literal and its legatoriany path to [] can bypass tautology wet hat: cstutores
- subsumed clause

a clause such that one with a sypherical is liferal is already present path to [] need only pass through short clause can be generalized to allow substitutions @ 163.com

- 2. Ordering strategies
  many possible ways to order search, but best and simplest is
  - unit preference prefer to resolve unit clauses first Why? Given unit clause and another clause, resolvent is a smaller one ← []

# **Strategies 2**

- 3. Set of support
  - KB is usually satisfiable, so not very useful to resolve among clauses with only ancestors in KB

  - always resolve with at least on always resolve with a least on
  - preserves completeness (som
- 4. Connection graph
  - pre-compute all possible unificationshat: cstutorcs
  - build a graph with edges between any two unifiable literals of opposite polarity label edge with MGU

Resolution procedure: Email: tutorcs@163.com

repeatedly:

select link OO: 749389476

compute resolvent

inherit links from parehtspatietusususum

Resolution as search:
 find sequence of links L<sub>1</sub>, L<sub>2</sub>,... producing []

# **Strategies 3**

#### 5. Special treatment for equality

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- use new inference rule: param
- from  $\{(t=s)\} \cup C_1$  and  $\{P(\ldots)\} \cup C_2$  where  $t\theta = t'\theta$
- infer  $\{P(\ldots s\ldots)\}\theta \cup C_1\theta \cup C_2\theta$ .
- collapses many resolution steps into one; see also: theory resolution (later)

#### 6. Sorted logic

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- terms get sorts:
  - x:Male mother: [Person  $\stackrel{\textstyle \stackrel{\textstyle \leftarrow}{}}{\stackrel{\textstyle \leftarrow}{}}$  matter and  $\stackrel{\textstyle \leftarrow}{}$  mother:
- keep taxonomy of sorts
- QQ: 749389476
- refuse to unify P(s) with P(t) unless sorts are compatible
- assumes only "meaningful" paths will lead to I

# Finally ...

7. Directional connectives

• given [¬p, q], can interpret as either

from p, infer qto prove q, prove pprocedural reading of -



In 1st case:

would only resolve  $[\neg p, q]$  with [p, q] producing  $[q, \dots]$ 

In 2nd case:

would only resolve [-p. Assignment Project Fram Help

Intended application: Email: tutores@163.com

> forward: Battleship(x)  $\rightarrow$  Gray(x)

do not ward to 7493 896 something is gray by proving it is a battleship

backward:  $Human(x) \rightarrow Has(x,spleen)$ 

do not wanted control from someone being human.

that she has each property

• the basis for the procedural representations