

Answer to Exercise 1

Since $f(1, 3) = [2 \ -1] \begin{bmatrix} 1 \\ 3 \end{bmatrix} + 0.5 = -1 + 0.5 = -0.5 < 0$, the point $(1, 3)$ is initially classified into

Class 2, and the corresponding adversarial sample $x' = \begin{bmatrix} x'_1 \\ x'_2 \end{bmatrix}$ should be classified into Class 1, i.e., $f(x'_1, x'_2) > 0$.

$$\frac{\partial f}{\partial x} = \frac{\partial W \cdot x + b}{\partial x} = W$$

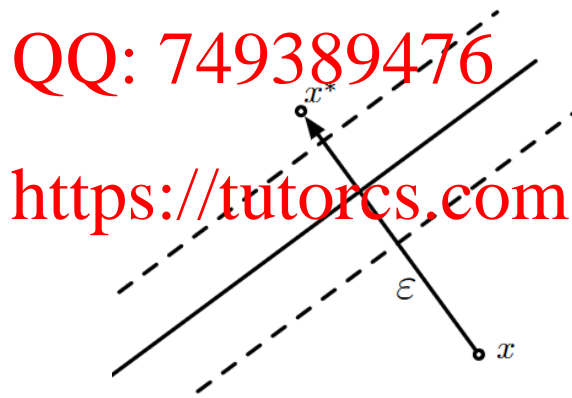
Step 1:

$$\begin{bmatrix} 2 \\ 2 \end{bmatrix} \leftarrow \text{Clip}_3 \left(\begin{bmatrix} 1 \\ 3 \end{bmatrix} + 1 \cdot \text{sgn} \left(\begin{bmatrix} 2 \\ -1 \end{bmatrix} \right) \right)$$

Since $f(2, 2) = [2 \ -1] \begin{bmatrix} 2 \\ 2 \end{bmatrix} + 0.5 = 2 + 0.5 = 2.5 > 0$, i.e., $(2, 2)$ is classified into the other class, it is the adversarial sample for $(1, 3)$.

Note:

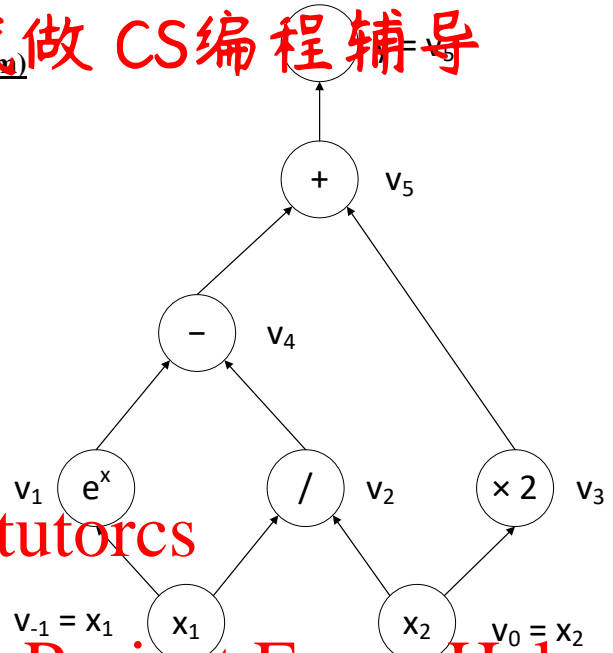
In this case, in order to generate an adversarial sample we perturb a given input in the direction orthogonal to the decision boundary hyperplane.



Answer to Exercise 2

Forward evaluation trace (start from top to bottom)

$$\begin{aligned}
 v_{-1} &= x_1 = 2 \\
 v_0 &= x_2 = 4 \\
 v_1 &= e^{v_{-1}} = e^2 \\
 v_2 &= v_{-1}/v_0 = 0.5 \\
 v_3 &= 2 \cdot v_0 = 8 \\
 v_4 &= v_1 - v_2 = e^2 - 0.5 \\
 v_5 &= v_3 + v_4 = e^2 + 7.5 \\
 y &= v_5
 \end{aligned}$$



Forward derivative trace

1. For calculating $\frac{\partial y}{\partial x_1}$ (start from top to bottom)

$$\begin{aligned}
 v_{-1} &= x_1 = 1 \\
 v_0 &= x_2 = 0 \\
 v_1 &= e^{v_{-1}} \cdot v_{-1} = e^2 \\
 v_2 &= \frac{v_{-1} \cdot v_0 - v_{-1} \cdot v_0}{v_0^2} = \frac{1 \times 4 - 2 \times 0}{16} = \frac{1}{4} \\
 v_3 &= 2 \cdot v_0 = 0 \\
 v_4 &= v_1 - v_2 = e^2 - \frac{1}{4} \\
 v_5 &= v_3 + v_4 = e^2 - \frac{1}{4} \\
 \dot{y} &= v_5 = e^2 - \frac{1}{4}
 \end{aligned}$$

2. For calculating $\frac{\partial y}{\partial x_2}$ (start from top to bottom)

$$\begin{aligned}
 v_{-1} &= x_1 = 0 \\
 v_0 &= x_2 = 1 \\
 v_1 &= e^{v_{-1}} \cdot v_{-1} = 0 \\
 v_2 &= \frac{v_{-1} \cdot v_0 - v_{-1} \cdot v_0}{v_0^2} = \frac{0 \times 4 - 2 \times 1}{16} = -\frac{1}{8} \\
 v_3 &= 2 \cdot v_0 = 2 \\
 v_4 &= v_1 - v_2 = -\frac{1}{8} \\
 v_5 &= v_3 + v_4 = 2 - \frac{1}{8} \\
 \dot{y} &= v_5 = 2 - \frac{1}{8}
 \end{aligned}$$

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Email: tutorcs@163.com

QQ: 749389476

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Reverse adjoint trace (start from bottom to top)

$$\bar{x}_1 = \bar{v}_{-1} = e^2 - \frac{1}{4}$$

$$\bar{x}_2 = \bar{v}_0 = 2\frac{1}{8}$$

$$\bar{v}_{-1} = \bar{v}_{-1} + \bar{v}_1 \cdot \frac{\partial v_1}{\partial v_{-1}} = \frac{1}{4} + e^2$$

$$\bar{v}_0 = \bar{v}_0 + \bar{v}_2 \cdot \frac{\partial v_2}{\partial v_0} = 2 + \frac{1}{8}$$

$$\bar{v}_{-1} = \bar{v}_2 \cdot \frac{\partial v_2}{\partial v_{-1}} = -1$$

$$\bar{v}_0 = \bar{v}_3 \cdot \frac{\partial v_3}{\partial v_0} = 2$$

$$\bar{v}_2 = \bar{v}_4 \cdot \frac{\partial v_4}{\partial v_2} = -1$$

$$\bar{v}_1 = \bar{v}_4 \cdot \frac{\partial v_4}{\partial v_1} = 1$$

$$\bar{v}_3 = \bar{v}_5 \cdot \frac{\partial v_5}{\partial v_3} = 1$$

$$\bar{v}_4 = \bar{v}_5 \cdot \frac{\partial v_5}{\partial v_4} = 1$$

$$\bar{v}_5 = \bar{y} = 1$$



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