

程序代写代做 CS编程辅导



COM

Foundations of Computer Science

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Lecture 3: Sets and Formal Languages
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- No lecture on Monday
- Consultation this Sunday moved to Monday 8pm
- Quiz 2 released on Tuesday
- Assignment 1 released today, due date will be pushed back

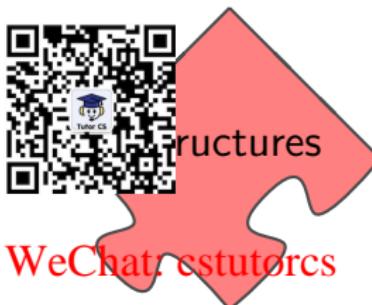
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Topic 1: Structures

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		[LLM]	[RW]
Week 2	Sets and Formal Languages; Set Theory	4.1, 4.2	Ch. 1
Week 3	Relations	4.4	Ch. 3
Week 4	Functions	4.3, 13.7	Ch. 3
Week 5	Graph Theory	Ch. 11, 12	Ch. 6

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Structures in Computer Science

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Sets:

- Sets are the building blocks of nearly all mathematical structures
- Data structures based around sets can be a space-efficient storage system
- Set theory is a good introduction to formal reasoning (logic)



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Formal languages: Email: tutorcs@163.com

- Formal languages are essential for compilers and programming language design QQ: 749389476
- Formal languages <https://tutorcs.com> introduction to recursive structures (recursion and induction)

Structures in Computer Science

Relations:

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- Relations are the building blocks of nearly all structures used in Computer Sci
- Databases are collections of relations
- Any ordering is a relation
- Common data structures (e.g. graphs) are relations
- Functions/procedures/programs compute relations between their input and output

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Functions:

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- Functions, methods, procedures in programming
- Computer programs "are" functions
- Graphical transformations
- Algorithmic analysis

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Structures in Computer Science

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Graphs:

- Route planning
on systems, robotics
- Optimisation, e. roles, utilisation of network structures, bandwidth allocation
- Compilers using graph colouring to assign registers to program variables
- Circuit layout (Untangle game)
- Determining the significance of a web page (Google's pagerank algorithm)
- Modelling the spread of a virus in a computer network or news in social network



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Outline

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Introduction to Sets



Defining Sets

Set Operations

Formal Languages

Feedback

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Introduction to Sets



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Sets

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Definition

A **set** is a collection we write $x \in A$.



(elements). If x is an element of A

NB

- Elements are taken from a universe, \mathcal{U} , but this can be quite complex. e.g. numbers, and sets of numbers, and sets of sets of numbers, etc.
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- Not all “well-defined” universes are possible. e.g.
 - No “set of all sets” (Cantor’s paradox)
 - No “sets which do not contain themselves” (Russell’s paradox)**QQ: 749389476**
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Sets

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- A set is defined as a collection of its elements. Order and multiplicity of elements is not considered.
- We distinguish between an element and the set comprising this single element. Thus always $a \neq \{a\}$.
- Set $\emptyset = \{\}$ is empty (no elements);
- Set $\{\{\}\}$ is nonempty — it has one element.

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Subsets

Definition

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For sets S and T , we say S is a **subset** of T , written $S \subseteq T$, if every element of S is an element of T .



NB

- $S \subseteq T$ includes the case of $S = T$
- $S \subset T$ — a **proper subset**: $S \subseteq T$ and $S \neq T$
- $\emptyset \subseteq S$ for all sets S
- $S \subseteq \mathcal{U}$ for all sets S
- $\mathbb{N}_{>0} \subset \mathbb{N} \subset \mathbb{Z} \subset \mathbb{Q} \subset \mathbb{R}$
- An element of a set; and a subset of that set are two different concepts

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$$a \in \{a, b\}, \quad a \not\subseteq \{a, b\}; \quad \{a\} \subseteq \{a, b\}, \quad \{a\} \notin \{a, b\}$$

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Defining sets

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Sets are typically described by:

- ① Explicit enumeration of their elements



- $S_1 = \{a, a, b, b, b, c\}$
 $= \{b, c, a\} = \dots$ three elements
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- $S_2 = \{a, \{a\}\}$ two elements
- $S_3 = \{a, b, \{a, b\}\}$ three elements
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- $S_4 = \{\}$ zero elements
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- $S_5 = \{\{\}\}$ one element
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- $S_6 = \{\{\}, \{\{\}\}\}$ two elements
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Defining sets

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② Defining a subset of the universal set \mathcal{U} . Including:

- Specifying the properties their elements must satisfy. A typical description is a logical property $P(x)$. For example, with $\mathcal{U} = \mathbb{N}$: “ x is even”:

$$\{x : x \in \mathbb{N} \text{ and } x \text{ is even}\} = \{0, 2, 4, \dots\}$$

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- Derived sets of integers

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$$2\mathbb{Z} = \{2x : x \in \mathbb{Z}\} \quad \text{the even numbers}$$

$$3\mathbb{Z} + 1 = \{3x + 1 : x \in \mathbb{Z}\}$$

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- Using interval notation.

Intervals

Intervals of numbers (applies to any type)

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$$[a, b] = \{x : a \leq x \leq b\}$$

$$(a, b) = \{x : a < x < b\}$$

$$[a, b) = \{x : a \leq x < b\}$$

$$(a, b] = \{x : a < x \leq b\}$$

$$(-\infty, b] = \{x : x \leq b\}$$

$$(-\infty, b) = \{x : x < b\}$$

$$[a, \infty) = \{x : a \leq x\}$$

$$(a, \infty) = \{x : a < x\}$$

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NB

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$(a, a) = (a, a] = [a, a) = \emptyset$; however $[a, a] = \{a\}$.

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Intervals of \mathbb{N}, \mathbb{Z} are finite: if $m \leq n$

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$$[m, n] = \{m, m + 1, \dots, n\}$$

Examples

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Examples

- $[1, 5] = \{1, 2, 3, 4, 5\}$ (when $\mathcal{U} = \mathbb{Z}$)
- $[1, 5] = \{1, 1.1, 1.01, 1.001, \dots, 2, \dots, \pi, e, \dots\}$ (when $\mathcal{U} = \mathbb{R}$)
- Number of multiples of k between n and m (inclusive) in $[n, m]$:



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$$\left\lfloor \frac{m}{k} \right\rfloor - \left\lfloor \frac{n-1}{k} \right\rfloor$$

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- $0 \leq (m \% n) < n$ ($m \% n \in [0, n)$)

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Defining sets

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③ Constructions from other, already defined, sets

- Union (\cup), intersection (\cap), complement (\cdot^c), set difference (\setminus), symmetric difference (\oplus)
- Power set $\text{Pow}(X) = \{ A \mid A \subseteq X \}$
- Cartesian product (\times)

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Outline

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Introduction to Sets



Defining Sets

Set Operations

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Formal Languages

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Basic Set Operations

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Definition

$A \cup B$ – **union** (a or



$A \cup B = \{x : x \in A \text{ or } x \in B\}.$

$A \cap B$ – **intersection** (a and b):

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$A \cap B = \{x : x \in A \text{ and } x \in B\}$.

A^c – **complement** (with respect to a universal set \mathcal{U}):

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We say that A, B are **disjoint** if $A \cap B = \emptyset$

Basic Set Operations

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Other set operations

Definition

$A \setminus B$ – **set difference**: the complement (a but not b):



$$A \setminus B = A \cap B^c$$

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$A \oplus B$ – **symmetric difference** (a and not b or b and not a ; also known as a or b exclusively; $a \text{ xor } b$):

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$$A \oplus B = (A \setminus B) \cup (B \setminus A)$$

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Venn Diagrams

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A **Venn Diagram** is a simple graphical approach to visualize the basic set operations.



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Venn Diagrams

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A **Venn Diagram** is a simple graphical approach to visualize the basic set operations.



$A \cup B$
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Venn Diagrams

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Venn Diagrams

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A **Venn Diagram** is a simple graphical approach to visualize the basic set operations.



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Venn Diagrams

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A **Venn Diagram** is a simple graphical approach to visualize the basic set operations.



$A \setminus B$
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Venn Diagrams

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A **Venn Diagram** is a simple graphical approach to visualize the basic set operations.



$A \oplus B$
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Set Operations and Subset

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Fact

$$A \cup B = B \quad \text{iff} \quad A \cap B = A \quad \text{iff} \quad A \subseteq B$$

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There is a correspondence between set operations and logical operators (to be discussed in Week 7).

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Exercises

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Exercises

RW: 1.4.7 (a)

$A \oplus A$ WeChat: cstutorcs

RW: 1.4.7 (b)

$A \oplus \emptyset$ Assignment Project Exam Help

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Exercises

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Exercises

RW: 1.4.7 (a)

$A \oplus A = \emptyset$ WeChat: cstutorcs

RW: 1.4.7 (b)

$A \oplus \emptyset = A$ Assignment Project Exam Help

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Power set

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Definition

The **power set** of a set X , $\text{Pow}(X)$, is the set of all subsets of X .

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Example

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$$\text{Pow}(\{a, b\}) = \{\emptyset, \{a\}, \{b\}, \{a, b\}\}$$

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Cardinality

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Definition

The **cardinality** of a set (X) (various notation) is the number of elements in that set.



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 $|X| = \#(X) = \text{card}(X)$

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Fact

Always $|\text{Pow}(X)| = 2^{|X|}$

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Exercises

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Exercises

- $|\emptyset| = ?$
- $\text{Pow}(\emptyset) = ?$
- $|\text{Pow}(\emptyset)| = ?$
- $\text{Pow}(\text{Pow}(\emptyset)) = ?$
- $|\text{Pow}(\text{Pow}(\emptyset))| = ?$
- $|\{a\}| = ?$
- $\text{Pow}(\{a\}) = ?$
- $|\text{Pow}(\{a\})| = ?$
- $|[m, n]| = ?$



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Exercises

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Exercises

$$\bullet \quad |\emptyset| = ?$$



$$\bullet \quad \text{Pow}(\emptyset) = ?$$

$$\bullet \quad |\text{Pow}(\emptyset)| = ?$$

$$\bullet \quad \text{Pow}(\text{Pow}(\emptyset)) = ?$$

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1
 $\{\emptyset, \{\emptyset\}\}$

$$\bullet \quad |\text{Pow}(\text{Pow}(\emptyset))| = ?$$

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$$\bullet \quad |\{a\}| = ?$$

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$$\bullet \quad \text{Pow}(\{a\}) = ?$$

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1
 $\{\emptyset, \{a\}\}$

$$\bullet \quad |\text{Pow}(\{a\})| = ?$$

2
 $n - m + 1$

$$\bullet \quad |[m, n]| = ?$$

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Exercises

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Exercises

RW: 1.3.2 Find the cardinalities of sets

(a) $|\left\{ \frac{1}{n} : n \in [1, 4] \cap \mathbb{N} \right\}| = ?$

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(b) $|\left\{ n^2 - n : n \in [0, 4] \cap \mathbb{N} \right\}| = ?$

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(c) $|\left\{ \frac{1}{n^2} : n \in \mathbb{N}_{>0} \text{ and } 2|n \text{ and } n < 11 \right\}| = ?$

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(d) $|\left\{ 2 + (-1)^n : n \in \mathbb{N} \right\}| = ?$

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Exercises

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Exercises

RW: 1.3.2 Find the cardinalities of sets

(a) $|\left\{ \frac{1}{n} : n \in [1, 4] \right\}| = ?$ WeChat: cstutorcs 4

(b) $|\left\{ n^2 - n : n \in [0, 4] \right\}| = ?$ Assignment Project Exam Help 4

(c) $|\left\{ \frac{1}{n^2} : n \in \mathbb{N}_{>0} \text{ and } 2|n \text{ and } n < 11 \right\}| = ?$ 5

(d) $|\left\{ 2 + (-1)^n : n \in \mathbb{N} \right\}| = ?$ Email: tutorcs@163.com 2

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Exercises

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Exercises

RW: 1.4.8 Relate the cardinalities to $|A \cap B|$, $|A|$, $|B|$

- $|A \cup B|$
- $|A \setminus B|$
- $|A \oplus B|$

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Exercises

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Exercises

RW: 1.4.8 Relate the cardinalities to $|A \cap B|$, $|A|$, $|B|$

- $|A \cup B| = |A| + |B| - |A \cap B|$
hence $|A \cup B| + |A \cap B| = |A| + |B|$
- $|A \setminus B| = |A| - |A \cap B|$
- $|A \oplus B| = |A| + |B| - 2|A \cap B|$

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Cartesian Product

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Definition

The **Cartesian product** of sets S and T is the set of **ordered pairs**:

$$S \times T = \{ (s, t) : s \in S, t \in T \}$$

The **Cartesian product** of a collection of n sets S_1, S_2, \dots, S_n is the set of **ordered n -tuples**:

$$\times_{i=1}^n S_i \stackrel{\text{def}}{=} \{ (s_1, \dots, s_n) : s_k \in S_k, \text{ for } 1 \leq k \leq n \}$$

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When all the S_i are equal:

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$$S^2 = S \times S, \quad S^3 = S \times S \times S, \dots, \quad S^n = \times_1^n S, \dots$$

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Cartesian product

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Fact

- $\emptyset \times S = \emptyset$, for every S
- $|S \times T| = |S| \cdot |T|$
- $|\times_{i=1}^n S_i| = \prod_{i=1}^n |S_i|$

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Examples

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Examples

Let $A = \{0, 1\}$ and $B = \{a, b\}$



$$\begin{aligned}A \times B &= \{(0, a), (0, b), (1, a), (1, b)\} \\&= \{\text{WeChat: estutors}, (0, b), (1, b)\}\end{aligned}$$

$$B \times A = \{\text{Assignment, Project, Exam, Help}\} \neq A \times B$$

$$A^2 = \{(0, 0), (0, 1), (1, 0), (1, 1)\}$$

$$\begin{aligned}A^3 &= \{\text{QQ: 749389476}, (0, 0, 0), (0, 0, 1), (0, 1, 0), (0, 1, 1), \\&\quad (1, 0, 0), (1, 0, 1), (1, 1, 0), (1, 1, 1)\}.\end{aligned}$$

Exercise

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Exercise

Let A, B, C be sets. WeChat: cstutorcs

Is $A \times (B \times C) = (A \times B) \times C$? Assignment Project Exam Help

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Exercise

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Exercise

Let A, B, C be sets. WeChat: cstutorcs

Is $A \times (B \times C) = (A \times B) \times C$? In general, no

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Outline

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Introduction to Sets



Defining Sets

Set Operations

Formal Languages

Feedback

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Formal Languages: Symbols

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Σ — **alphabet**, a finite nonempty set



Examples (of various alphabets and their intended uses)

$\Sigma = \{a, b, \dots, z\}$ for single words (in lower case)

$\Sigma = \{0, 1\}$ for binary integers

$\Sigma = \{0, 1, \dots, 9\}$ for decimal integers

The above cases all have a natural ordering; this is not required in general, thus the set of all Chinese characters forms a (formal) alphabet.

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Formal Languages: Words

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Definition

A **word** is a finite string (sequence) of symbols from Σ .

The **empty word**, λ , is the unique word with no symbols.



Examples

$w = aba$, $w = 01101\ldots$, etc.

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$\text{length}(w)$ — # of symbols in w

$\text{length}(aaa) = 3$, $\text{length}(\lambda) = 0$

The only operation on words (discussed here) is **concatenation**,

written as juxtaposition vw , vvv , abv , wbv , ...

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$$\lambda w = w = w\lambda$$

$$\text{length}(vw) = \text{length}(v) + \text{length}(w)$$

Examples

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Examples

Let $w = abb$, $v = ab$, $u = ba$

- $vw = ababb$ WeChat: cstutorcs
- $ww = abbabb = vubb$ Assignment Project Exam Help
- $w\lambda v = abbab$
- $\text{length}(vw) = \text{length}(ababb) = 5$ Email: tutorcs@163.com

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Formal Languages: Sets of words

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Definition

- Σ^k or $\Sigma^{=k}$: The set of words of length k
- $\Sigma^{\leq k}$: The set of words of length at most k
- Σ^* : The set of all words
- Σ^+ : The set of all nonempty words

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We often identify $\Sigma^1 = \Sigma$

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$$\Sigma^* = \Sigma^0 \cup \Sigma^1 \cup \Sigma^2 \cup \dots; \quad \Sigma^{\leq n} = \bigcup_{i=0}^n \Sigma^i$$

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$$\Sigma^+ = \Sigma^1 \cup \Sigma^2 \cup \dots = \Sigma^* \setminus \{\lambda\}$$

Formal Languages: Languages

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Definition

A **language** is a subset of Σ^* .

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Typically, only the subsets that can be formed (or described) according to certain rules are of interest. Such a collection of 'descriptive/formative' rules is called a **grammar**.

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Examples

Example (Decimal numbers) 程序代写代做 CS编程辅导

The “language” of all numbers written in decimal to at most two decimal places can be defined as follows:

- $\Sigma = \{-, ., 0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$
- Consider all words $w \in \Sigma^*$ which satisfy the following:
 - w contains at most one instance of $-$, and if it contains an instance then it is the first symbol.
 - w contains at most one instance of $.$, and if it contains an instance then it is preceded by a symbol in $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$, and followed by either one or two symbols in that set.
 - w contains at least one symbol from $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$

NB

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According to these rules 123, 123.0 and 123.00 are all (distinct) words in this language.

Examples

Example (HTML documents)

Take

$$\Sigma = \{<\text{html}>, </\text{html}>, <\text{head}>, </\text{head}>, <\text{body}>, \dots\}.$$

The (language of) **HTML documents** is loosely described as follows:



- Starts with "<html>"
- Next symbol is "<head>"
- Followed by zero or more symbols from the set of HeadItems (defined elsewhere)
- Followed by "</head>"
- Followed by "<body>"
- Followed by zero or more symbols from the set of BodyItems (defined elsewhere)
- Followed by "</body>"
- Followed by "</html>"

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Exercises

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Exercises

RW: 1.3.10 Number of elements in the sets

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(e) Σ^* where $\Sigma = \{a, b, c\}$?

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(f) $\{ w \in \Sigma^* : \text{length}(w) \leq 4 \}$ where $\Sigma = \{a, b, c\}$?

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Exercises

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Exercises

RW: 1.3.10 Number of elements in the sets

(e) Σ^* where $\Sigma = \{a, b, c\}$? — $|\Sigma^*| = \infty$

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(f) $\{ w \in \Sigma^* : \text{length}(w) \leq 4 \}$ where $\Sigma = \{a, b, c\}$?

$|\Sigma^{\leq 4}| = 3^0 + 3^1 + \dots + 3^4 = \frac{3^5 - 1}{3 - 1} = \frac{243 - 1}{2} = 121$

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Set Operations for Languages

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Languages are sets, so the standard set operations (\cap , \cup , \setminus , \oplus , etc) can be used to manipulate languages.

Two set operations translate to languages uniquely:

- Concatenation ($X Y$ juxtaposition):

$$XY = \{xy : x \in X \text{ and } y \in Y\}$$

- Kleene star: X^* is the set of words that are made up by concatenating 0 or more words in X

- $X^0 = \{\lambda\}; X^{i+1} = XX^i$

- $X^* = X^0 \cup X^1 \cup X^2 \cup \dots$

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The set of all finite words over Σ is the Kleene star of Σ (hence notation).

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Set Operations for Languages

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Example

Let $A = \{aa, bb\}$ and $B = \{\lambda, c, aa, bb, cc\}$ be languages over $\Sigma = \{a, b, c\}$.



- $A \cup B = \{\lambda, c, aa, bb, cc\}$
- $AB = \{aa, bb, aac, bbd, cc\}$
- $AA = \{aaaa, aabb, bbaa, bbbb\}$
- $A^* = \{\lambda, aa, bb, aaaa, aabb, bbaa, bbbb, aaaaaa, \dots\}$
- $B^* = \{\lambda, c, cc, ccc, cccc, \dots\}$
- $\{\lambda\}^* = \{\lambda\}$
- $\emptyset^* = \{\lambda\}$

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Outline

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Introduction to Sets



Defining Sets

Set Operations

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Formal Languages

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Feedback

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Weekly Feedback

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I would appreciate any comments/suggestions/requests you have on this week's lecture.



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