COM[illegible]0

Foundations of Computer Science

Lecture 1: Course Introduction

Online stream and Pre-course polls

Online stream

Pre-course poll

Acknowledgement of Country

I would like to acknowledge and pay my respect to the Bedegal people who are the Traditional Custodians of the land on which UNSW is built, and of Elders past and present.

Outline

Who am I?

Why are we here?

How will you be assessed?

What do I expect from you?

COMP9020 22T2 Staff

Lecturer:	Paul
Email:	paul.hunter@unsw.edu.au
Lectures:	Mondays 12-2pm and Fridays 11am-1pm
Consults:	Wednesdays 8-9pm and Sundays 8-9pm
Research:	Theoretical CS: Algorithms, Formal verification

Interactions

Lectures:

- Online stream (n[illegible]
- Recordings availa[illegible]360 (through Moodle)

Consultations:

- Zoom: https://unsw.zoom.us/j/87192636642 (passcode: 1+1=2)
- Group-based, student-driven
- Wiki for questions

Other points of contact:

- Course forums
- Email

Outline

Who am I?

Why are we here?

How will you be assessed?

What do I expect from you?

What is Computer

"Computer science no more about computers than astronomy is about telescopes"

– E. Dijkstra

Course Aims

Computer Science is

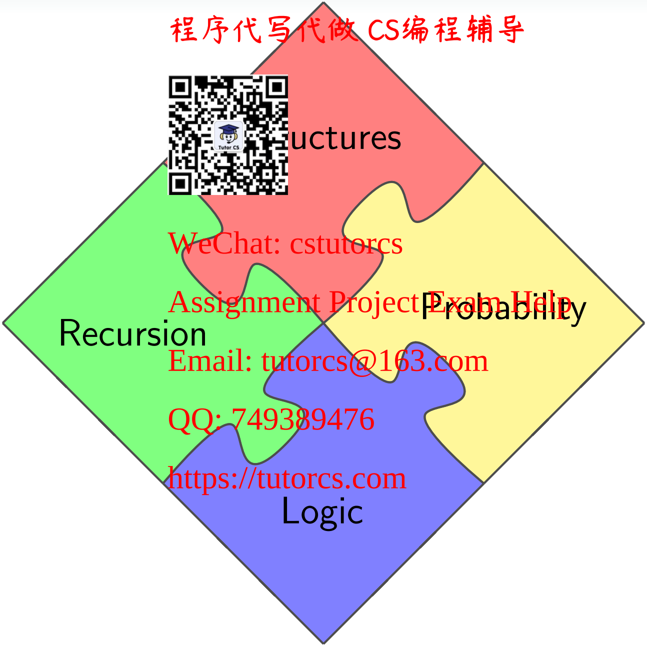
Course Aims

Computer Science is [illegible]ploring the ability, and limitation, of computers to solve p[illegible]t covers:

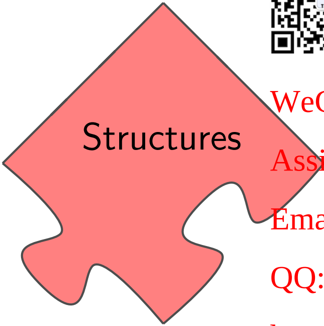
- **What** are computers capable of solving?
- **How** can we get computers to solve problems?
- **Why** do these approaches work?

This course aims to increase your level of mathematical maturity to assist with the fundamental problem of **finding, formulating, and proving** properties of programs.

Course Topics

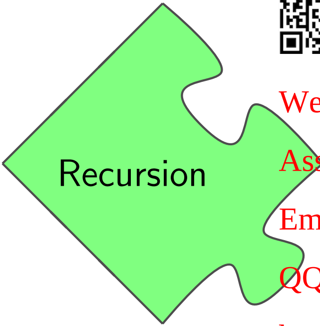


Course Topics



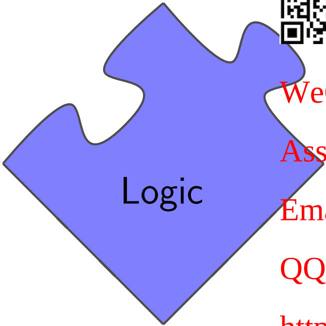
- Week 2: Set Theory
- Week 2: Formal Languages
- Week 3: Relations
- Week 4: Functions
- Week 5: Graph Theory

Course Topics



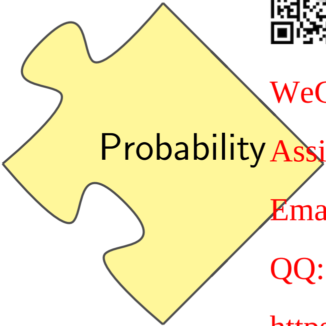
- Week 6: Recursion
- Week 7: Algorithmic Analysis
- Week 7: Induction

Course Topics



- Week 8: Boolean Logic
- Week 8: Propositional Logic

Course Topics



- Week 9: Combinatorics
- Week 9: Probability
- Week 10: Statistics

Course Material

All course informatio[illegible]d on the course website

ww[illegible]v.edu.au/∼cs9020/

Content includes:

- Lecture slides and recordings
- Quizzes and Assignments
- Course Forums
- Practice questions
- Challenge questions

Course Material

Textbooks:

- KA Ross and CR Wright: Discrete Mathematics
- E Lehman, FT Leighton, A Meyer:
  Mathematics for Computer Science

Alternatives:

- K Rosen: Discrete Mathematics and its Applications

Outline

Who am I?

Why are we here?

How will you be assessed?

What do I expect from you?

Assessment Summary

60% exam, 30% assi[illegible] 10% quizzes:

- 9 quizzes, worth [illegible]7 marks each
- 3 assignments, [illegible]o 10 marks each
- final exam (3 hours) worth up to 60 marks

Quizzes are available for 48 hours before the first lecture of the week. Assignments due on Mondays of weeks 5, 8 and 11.

You must achieve 40% on the final exam to pass

Your final score will be taken from your 6 best quiz results, 3 assignments and final exam.

Late policy and Special Consideration

All assessments are submitted through the course website

Lateness policy

- Assignments: 5% of total grade off raw mark per 24 hours or part thereof
- Quizzes: Late submissions not accepted
- Exam: Late submissions not accepted

If you cannot meet a deadline through illness or misadventure you need to apply for Special Consideration.

More information

View the course outl

https://webcms3.cse.unsw.edu.au/COMP9020/22T2/outline

Particularly the sections on **Student conduct** and **Plagiarism**.

Outline

Who am I?

Why are we here?

How will you be assessed?

What do I expect from you?

Learning Objectives

I am always looking t[illegible] **demonstrate**:

- Your understand[illegible] material
- Your ability to work with the material

NB

How you get an answer is as, if not more important than what the answer is.

Why?

Mathematical communication

Guidelin d mathematical writing

Mathematical writing e:

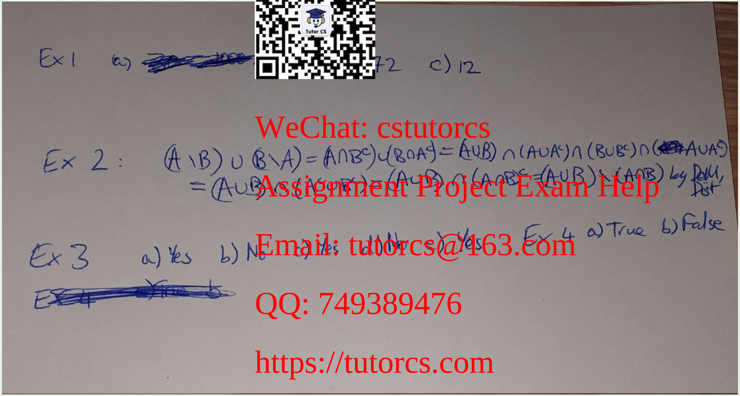
- Clear
- Logical
- Convincing

NB

All submitted work must be typeset. Diagrams may be hand drawn.

Examples

Example (Bad)



Examples

Example (Good)

Ex. 2

$$
\begin{aligned}
(A \setminus B) \cup (B \setminus A) &= (A \cap B^c) \cup (B \cap A^c) && \text{(Def.)}\\
&= ((A \cap B^c) \cup B) \cap ((A \cap B^c) \cup A^c) && \text{(Dist.)}\\
&= (A \cup B) \cap (B^c \cup B) \\
&\quad \cap (A \cup A^c) \cap (B^c \cup A^c) && \text{(Dist.)}\\
&= (A \cup B) \cap (A^c \cup B^c) && \text{(Ident.)}\\
&= (A \cup B) \cap (A \cap B)^c && \text{(DeM.)}\\
&= (A \cup B) \setminus (A \cap B) && \text{(Def.)}
\end{aligned}
$$

Examples

Example (Good)

Ex. 4a

We will show that if [illegible]$_2$ are symmetric, then $R_1 \cap R_2$ is symmetric.

Suppose $(a, b) \in R_1 \cap R_2$.

Then $(a, b) \in R_1$ and $(a, b) \in R_2$.

Because R_1 is symmetric, $(b, a) \in R_1$, and because R_2 is symmetric, $(b, a) \in R_2$.

Therefore $(b, a) \in R_1 \cap R_2$.

Therefore $R_1 \cap R_2$ is symmetric.

Proofs

A large component of your work in this course is giving **proofs** of **propositions.**

A **proposition** is a statement that is either true or false.

Example

Propositions:

- $3 + 5 = 8$
- All integers are either even or odd
- There exist a, b, c such that $1/a + 1/b + 1/c = 4$

Not propositions:

- $3 + 5$
- x is even or x is odd
- $1/a + 1/b + 1/c = 4$

Proposition structure

Common proposition[illegible]s include:

If A then B	$(A \Rightarrow B)$
A if and only if B	$(A \Leftrightarrow B)$
For all x, A	$(\forall x.A)$
There exists x such that A	$(\exists x.A)$

$\forall$ and $\exists$ are known as **quantifiers**.

Proofs

A large component o[illegible]rk in this course is giving **proofs** of **propositions.**

A proof of a proposition is an argument to convince the reader/marker that the proposition is true.

A **proof** of a proposition is a finite sequence of logical steps, starting from base assumptions (**axioms** and **hypotheses**), leading to the proposition in question.

Proofs

Example

Prove: $3 \times 2 = 2 \times 3$

$$\begin{aligned}
3 \times 2 &= (2+1) \times 2 \\
&= (2 \times 2) + (1 \times 2) \\
&= (1 \times 2) + (2 \times 2) \\
&= 2 + (2 \times 2) \\
&= (2 \times 1) + (2 \times 2) \\
&= 2 \times (1 + 2) \\
&= 2 \times 3.
\end{aligned}$$

Proofs: How much detail?

- Depends on the context (question, expectation, audience, etc)
- Each **step** should be justified (excluding basic algebra and arithmetic)

Proofs: pitfalls

Starting from the pr… and deriving true **is not valid**.

Example

Prove: $0 = 1$

$$
\begin{array}{lrcl}
 & 0 & = & 1 \\
\text{So (mult. by 2)} & 0 & = & 2 \\
\text{So (subtract 1)} & -1 & = & 1 \\
\text{So} & (-1)^2 & = & (1)^2 \\
\text{So} & 1 & = & 1 \quad \text{which is true.}
\end{array}
$$

Does this mean that $0 = 1$?

Proofs: pitfalls

Make sure each step is logically valid

Example

$$
\begin{array}{lrcl}
 & -20 & = & -20 \\
\text{So} & 25 - 45 & = & 16 - 36 \\
\text{So} & 5^2 - 2 \cdot 5 \cdot \frac{9}{2} & = & 4^2 - 2 \cdot 4 \cdot \frac{9}{2} \\
\text{So} & 5^2 - 2 \cdot 5 \cdot \frac{9}{2} + \left(\frac{9}{2}\right)^2 & = & 4^2 - 2 \cdot 4 \cdot \frac{9}{2} + \left(\frac{9}{2}\right)^2 \\
\text{So} & (5 - \frac{9}{2})^2 & = & (4 - \frac{9}{2})^2 \\
\text{So} & 5 - \frac{9}{2} & = & 4 - \frac{9}{2}
\end{array}
$$

Does this mean that $5 = 4$?

Proofs: pitfalls

Make sure each step is logically valid

Example

Suppose $a = b$. Then

$$
\begin{array}{lrcl}
 & a^2 & = & ab \\
\text{So} & a^2 - b^2 & = & ab - b^2 \\
\text{So} & (a-b)(a+b) & = & (a-b)b \\
\text{So} & a+b & = & b \\
\text{So} & a & = & 0
\end{array}
$$

This is true no matter what value a is given at the start, so does that mean everything is equal to 0?

Proofs: pitfalls

For propositions of the form $\forall x.A$ where x can have infinitely many values:

- You cannot enumerate infinitely many cases in a proof.
- Only considering a finite number of cases is not sufficient.

Example

For all n, $n^2 + n + 41$ is prime

True for $n = 0, 1, 2, \ldots, 39$. Not true for $n = 40$.

Proofs: pitfalls

The order of quantifi[illegible]rs when it comes to propositions:

Example

- For every number x, there is a number y such that y is larger than x
- There is a number y such that for every number x, y is larger than x

Proof strategies: direct proof

Proposition form	[illegible]eed to do this
$A \Rightarrow B$	Assume A and prove B
$A \Leftrightarrow B$	Prove "If A then B" and "If B then A"
$\forall x.A$	Show A holds for every possible value of x
$\exists x.A$	Find a value of x that makes A true

Proof strategies: contradiction

To prove A is true, a[illegible]s false and derive a contradiction.
That is, start from the negation of the proposition and derive false.

Example

Prove: $\sqrt{2}$ is irrational

Proof: Assume $\sqrt{2}$ is rational ...

Negating propositions

Proposition form	Negation
A and B	not A or not B
A or B	not A and not B
$A \Rightarrow B$	A and not B
$A \Leftrightarrow B$	A and not B, or B and not A
$\forall x.A$	$\exists x.$ not A
$\exists x.A$	$\forall x.$ not A

To prove a proposition of the form “If A then B” you can prove “If not B then not A”

Example

Prove: If $m + n \geq 73$ then $m \geq 37$ or $n \geq 37$.

Proof strategies: dealing with $\forall$

How can we check infinitely many cases?

- Choose an **arbitrary element**: an object with no assumptions about it (may have to check several cases)
- Induction (see week 5)

Example

Prove: For every integer n, n^2 will have remainder 0 or 1 when divided by 4.

Note: "Arbitrary" is not the same as "random".