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COMP9517: Computer Vision

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Tracking

Motion Tracking

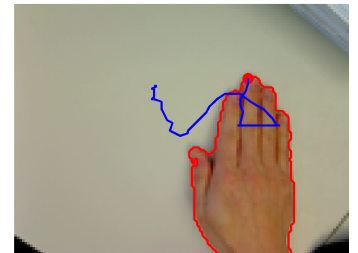
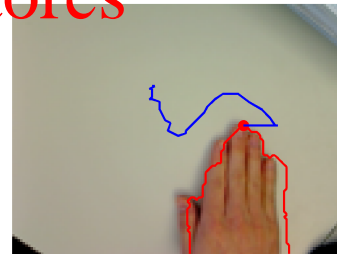
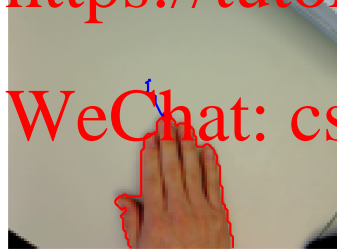
- Tracking is the problem of generating an inference about the motion of an object given a sequence of images

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Applications

- **Motion capture**

- Record motion of people to control cartoon characters in animations
- Modify the motion record to obtain slightly different behaviours

- **Recognition from motion**

- Determine the identity of a moving object
- Assess what the object is doing

- **Surveillance**

- Detect and track objects in a scene for security
- Monitor their activities and warn if anything suspicious happens

- **Targeting**

- Decide which objects to target in scene
- Make sure the objects get hit

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Difficulties in Tracking

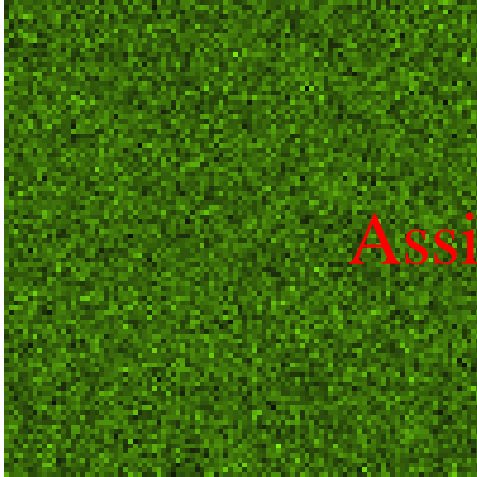
- **Loss of information** caused by projection of the 3D world on a 2D image
- **Noise** in images
- Complex object **motion**
- **Non-rigid** or articulated nature of objects
- Partial and full object **occlusions**
- Complex object **shapes**
- Scene **illumination** changes
- **Real-time** processing requirements

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Example Tracking Problem



Single moving microscopic particle

- Imaged with signal-to-noise ratio (SNR) of 1.5

Human visual motion perception

- Not so accurate and reproducible in quantification
- Good at integrating spatial and temporal information
- Powerful in making associations and predictions

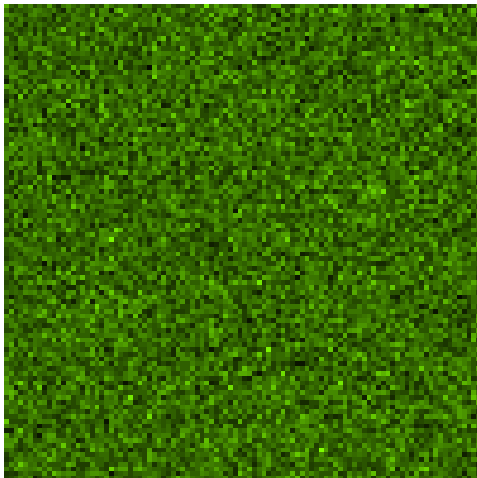
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Computer vision challenges

- Integration of spatial and temporal information
- Modeling and incorporation of prior knowledge
- Probabilistic rather than deterministic approach

Bayesian estimation methods...



Motion Assumptions

- When moving objects do not have unique texture or colour, the characteristics of the motion itself must be used to connect detected points into trajectories
- Assumptions about each moving object:
 - Location changes smoothly over time
 - Velocity (speed and direction) changes smoothly over time
 - Can be at only one location in space at any given time
 - Not in same location as another object at the same time

Topics

- **Bayesian inference**

Using *probabilistic models* to perform tracking

- **Kalman filtering**

Using *linear model assumptions* for tracking

- **Particle filtering**

Using *nonlinear models* for tracking

- **Trajectory analysis**

Using measures to *quantify motion*

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Bayesian Inference

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Problem Definition

- A moving object has a **state** which evolves over time

Random variable: X_i can contain any quantities of interest
Specific value: x_i (position, velocity, acceleration, shape, intensity, colour, ...)

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- The state is **measured** at each time point

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Random variable: Y_i in computer vision the
Specific value: y_i measurements are typically
features computed from the images

- Measurements are combined to estimate the state

Three Main Steps

- **Prediction:** use the measurements $(y_0, y_1, \dots, y_{i-1})$ up to time $i-1$ to predict the state at time i

$$P(X_i | Y_0 = y_0, Y_1 = y_1, \dots, Y_{i-1} = y_{i-1})$$

- **Association:** select the measurements at time i that are related to the object state

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- **Correction:** use the incoming measurement y_i to update the state prediction

$$P(X_i | Y_0 = y_0, Y_1 = y_1, \dots, Y_{i-1} = y_{i-1}, Y_i = y_i)$$

Independence Assumptions

- Current state depends only on the immediate past

$$P(X_i | X_0, X_1, \dots, X_{i-1}) = P(X_i | X_{i-1})$$

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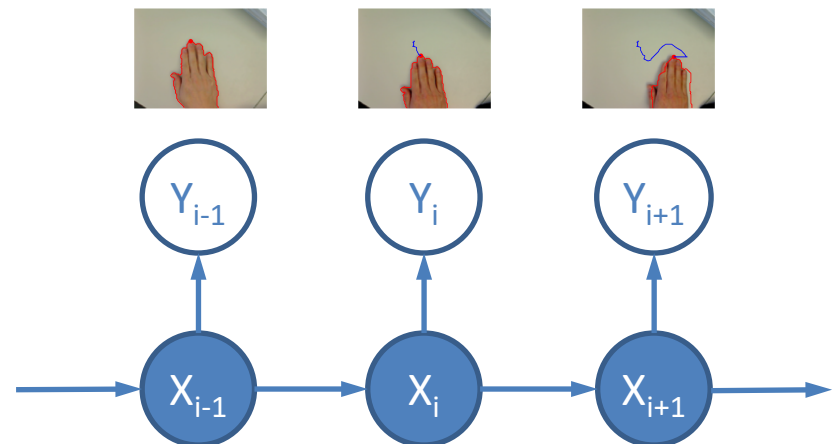
- Measurements depend only on the current state

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$$P(Y_i, Y_j, \dots, Y_k | X_i) = P(Y_i | X_i) P(Y_j, \dots, Y_k | X_i)$$

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These assumptions imply
the tracking problem has
the structure of inference
on a hidden Markov model



Tracking by Bayesian Inference

- Prediction

$$\begin{aligned}
 P(X_i | y_0, y_1, \dots, y_{i-1}) &= \int \boxed{P(X_i, X_{i-1} | y_0, y_1, \dots, y_{i-1})} dX_{i-1} \\
 &= \int P(X_i | X_{i-1}, \cancel{y_0, y_1, \dots, y_{i-1}}) P(X_{i-1} | y_0, y_1, \dots, y_{i-1}) dX_{i-1} \\
 &= \int \underbrace{P(X_i | X_{i-1})}_{\text{dynamics model}} \underbrace{P(X_{i-1} | y_0, y_1, \dots, y_{i-1})}_{\text{posterior of previous time}} dX_{i-1}
 \end{aligned}$$

dynamics
model

posterior of
previous time

$$\begin{aligned}
 P(X_i, X_{i-1} | y_0, y_1, \dots, y_{i-1}) &= \frac{P(X_i, X_{i-1}, y_0, y_1, \dots, y_{i-1})}{P(y_0, y_1, \dots, y_{i-1})} \\
 &= \frac{P(X_i | X_{i-1}, y_0, y_1, \dots, y_{i-1}) P(X_{i-1}, y_0, y_1, \dots, y_{i-1})}{P(y_0, y_1, \dots, y_{i-1})} \\
 &= P(X_i | X_{i-1}, y_0, y_1, \dots, y_{i-1}) \frac{P(X_{i-1}, y_0, y_1, \dots, y_{i-1})}{P(y_0, y_1, \dots, y_{i-1})} \\
 &= P(X_i | X_{i-1}, y_0, y_1, \dots, y_{i-1}) P(X_{i-1} | y_0, y_1, \dots, y_{i-1})
 \end{aligned}$$

Tracking by Bayesian Inference

- Correction

$$\begin{aligned}
 P(X_i | y_0, y_1, \dots, y_i) &= \frac{P(X_i, y_0, y_1, \dots, y_i)}{P(y_0, y_1, \dots, y_i)} \\
 &= \frac{P(y_i | X_i, y_0, y_1, \dots, y_{i-1}) P(X_i | y_0, y_1, \dots, y_{i-1}) P(y_0, y_1, \dots, y_{i-1})}{P(y_0, y_1, \dots, y_i)} \\
 &= P(y_i | X_i) P(X_i | y_0, y_1, \dots, y_{i-1}) \underbrace{\frac{P(y_0, y_1, \dots, y_{i-1})}{P(y_0, y_1, \dots, y_i)}}_{\text{constant}} \\
 &\propto \underbrace{P(y_i | X_i)}_{\text{measurement model}} \underbrace{P(X_i | y_0, y_1, \dots, y_{i-1})}_{\text{prediction of current state}}
 \end{aligned}$$

Tracking by Bayesian Inference

In summary, tracking by Bayesian inference is done by iterative prediction and correction:

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- Prediction

$$P(X_i | Y_{0:i-1}) = \int P(X_i | X_{i-1}) \underbrace{P(X_{i-1} | Y_{0:i-1})}_{\text{Posterior at time } i-1} dX_{i-1}$$

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Posterior at time $i - 1$

- Correction

$$P(X_i | Y_{0:i}) \propto P(Y_i | X_i) P(X_i | Y_{0:i-1})$$

Posterior at time i

Posterior at time i

$$Y_{0:k} = (Y_0 = y_0, Y_1 = y_1, \dots, Y_k = y_k)$$

Tracking by Bayesian Inference

To make tracking by Bayesian inference work in practice you need to design two models:

- Dynamics model $P(X_i | X_{i-1})$
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- Measurement model $P(Y_i | X_i)$
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The specific design choices are application dependent

Tracking by Bayesian Inference

Final estimates are computed from the posterior:

- Example 1: expected a posteriori (EAP)

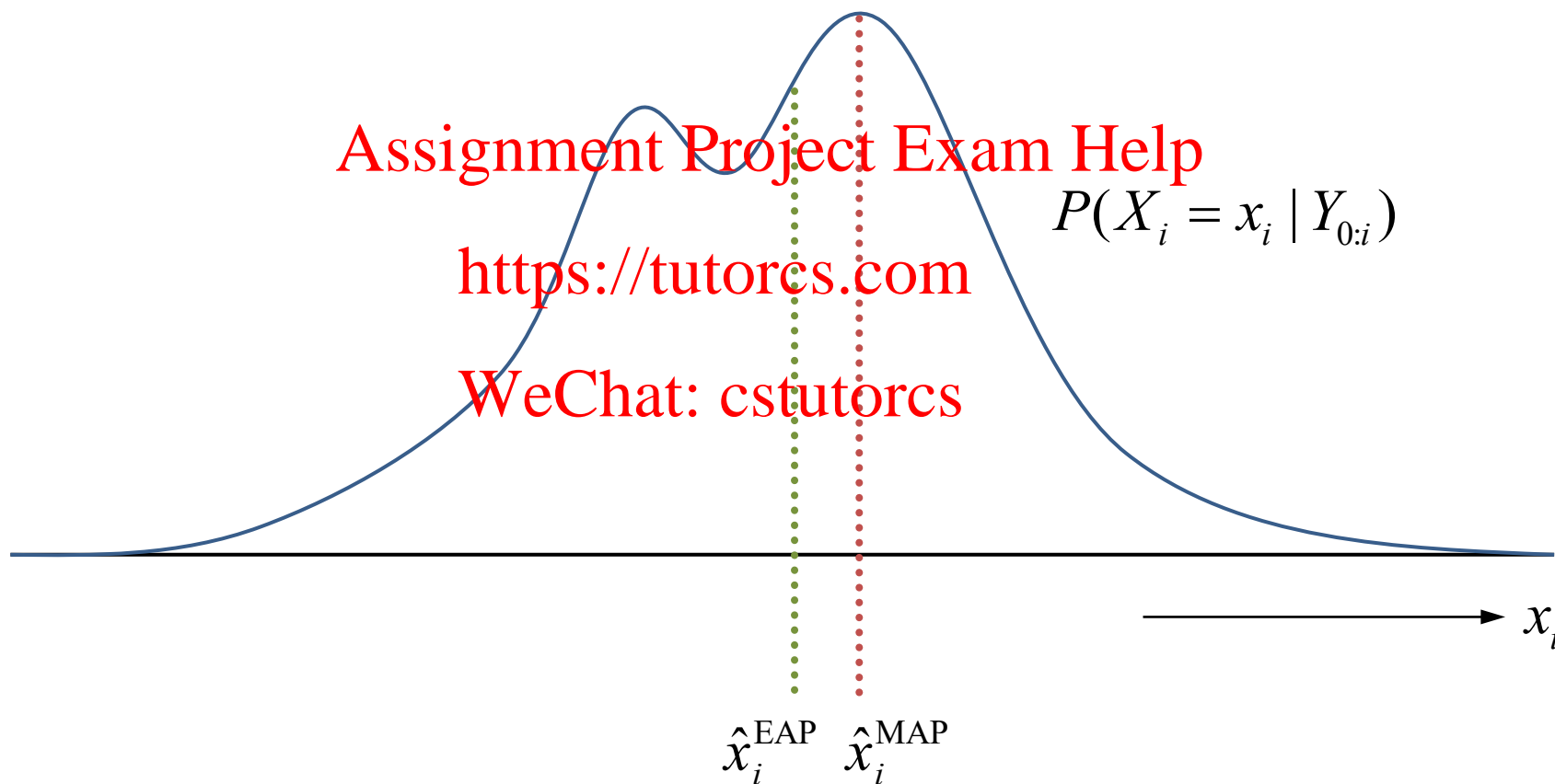
$$\hat{x}_i = \int x_i P(X_i = x_i | Y_{0:i}) dx_i$$

- Example 2: maximum a posteriori (MAP)

$$\hat{x}_i = \arg \max_{x_i} P(X_i = x_i | Y_{0:i})$$

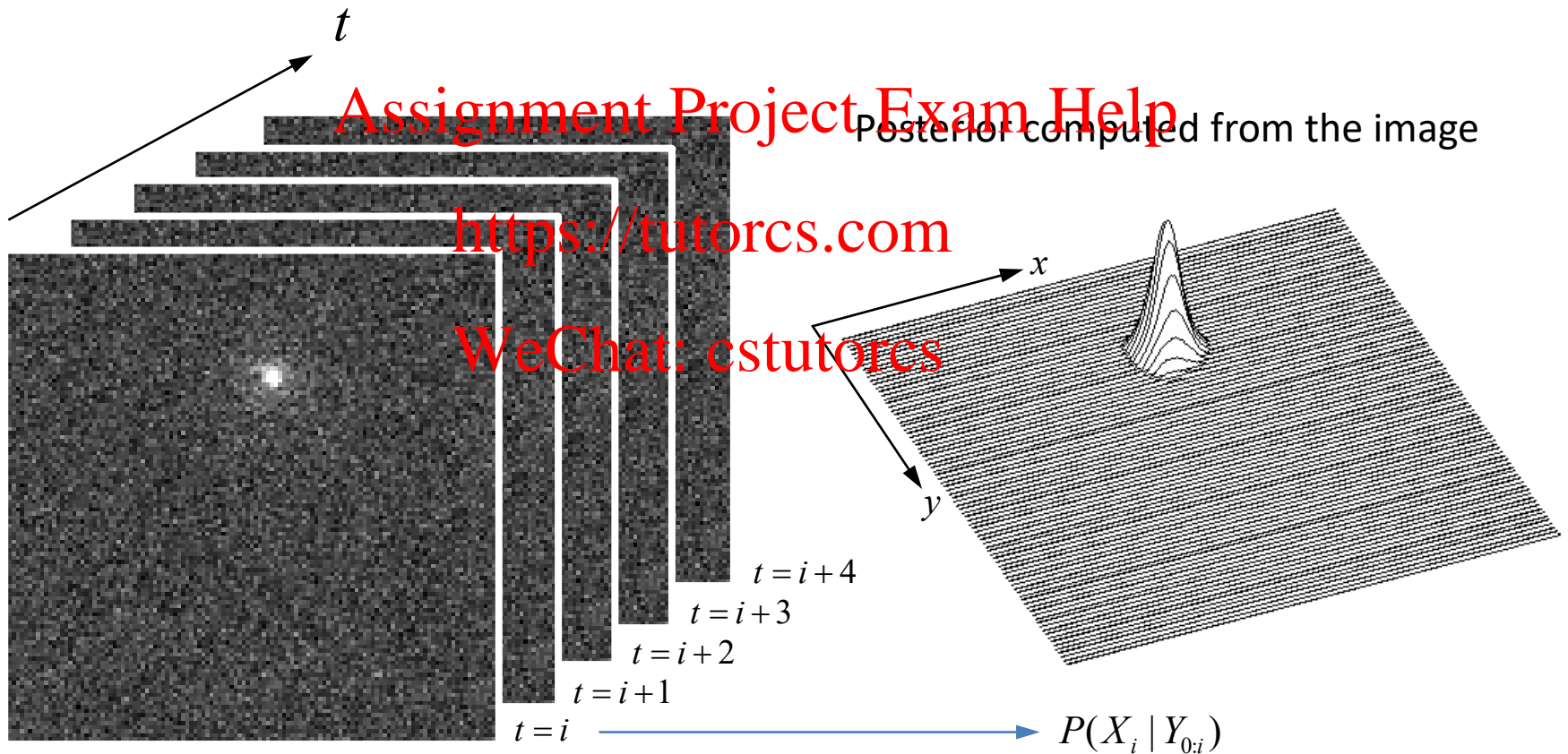
These are the most popular ones but others are possible

Tracking by Bayesian Inference



Bayesian Tracking Example

Estimating the coordinates of a moving particle:

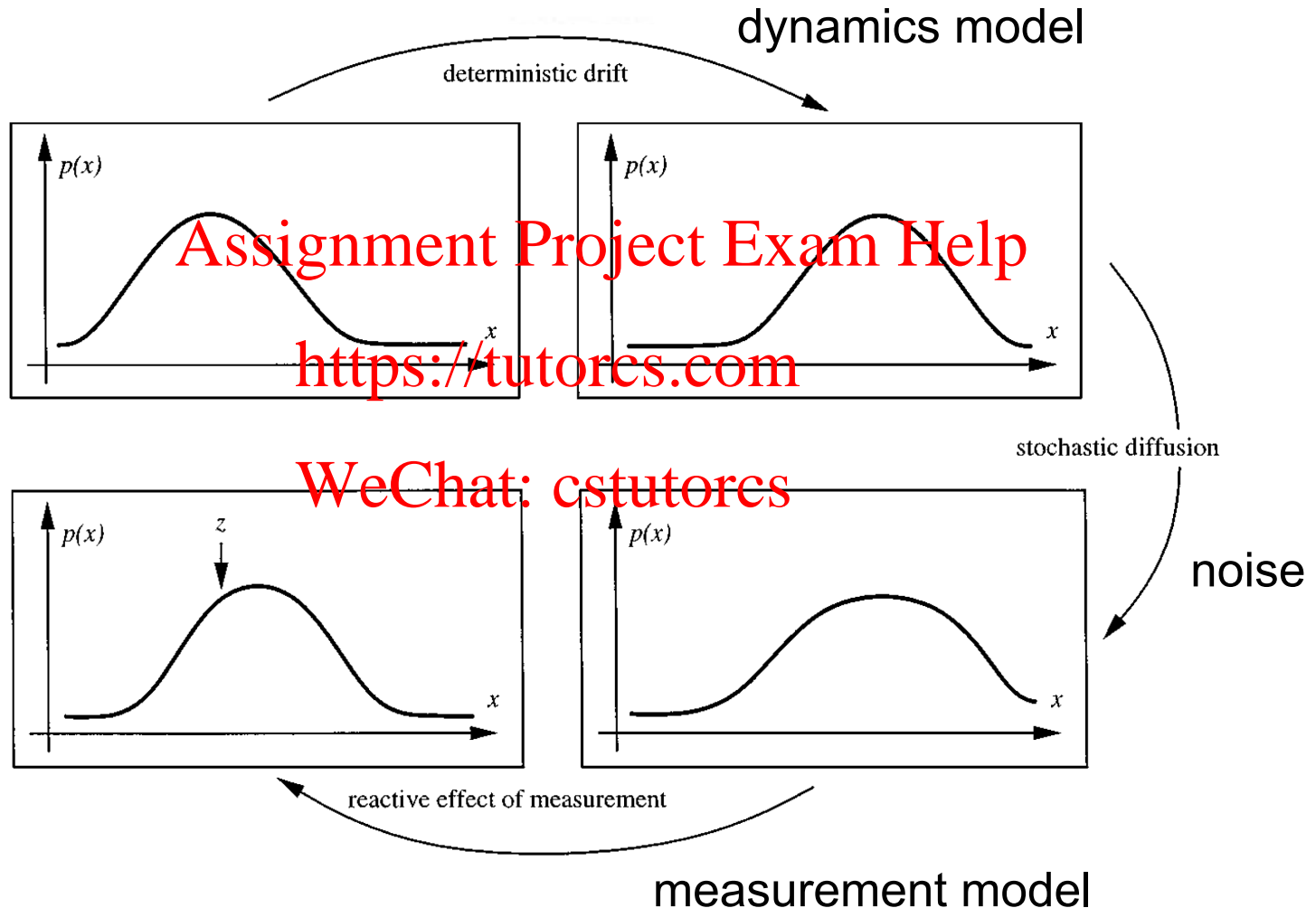


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Kalman Filtering

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Probability Density Propagation



Linear / Gaussian Assumption

If we assume the dynamics (state transition) model and the measurement model to be linear, and the noise to be additive Gaussian, then all the probability densities will be Gaussians:

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$$x \sim N(\mu, \Sigma)$$

- The state is advanced by multiplying with some known matrix and then adding a zero-mean normal random variable:

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$$x_i = Ax_{i-1} + q_{i-1}$$

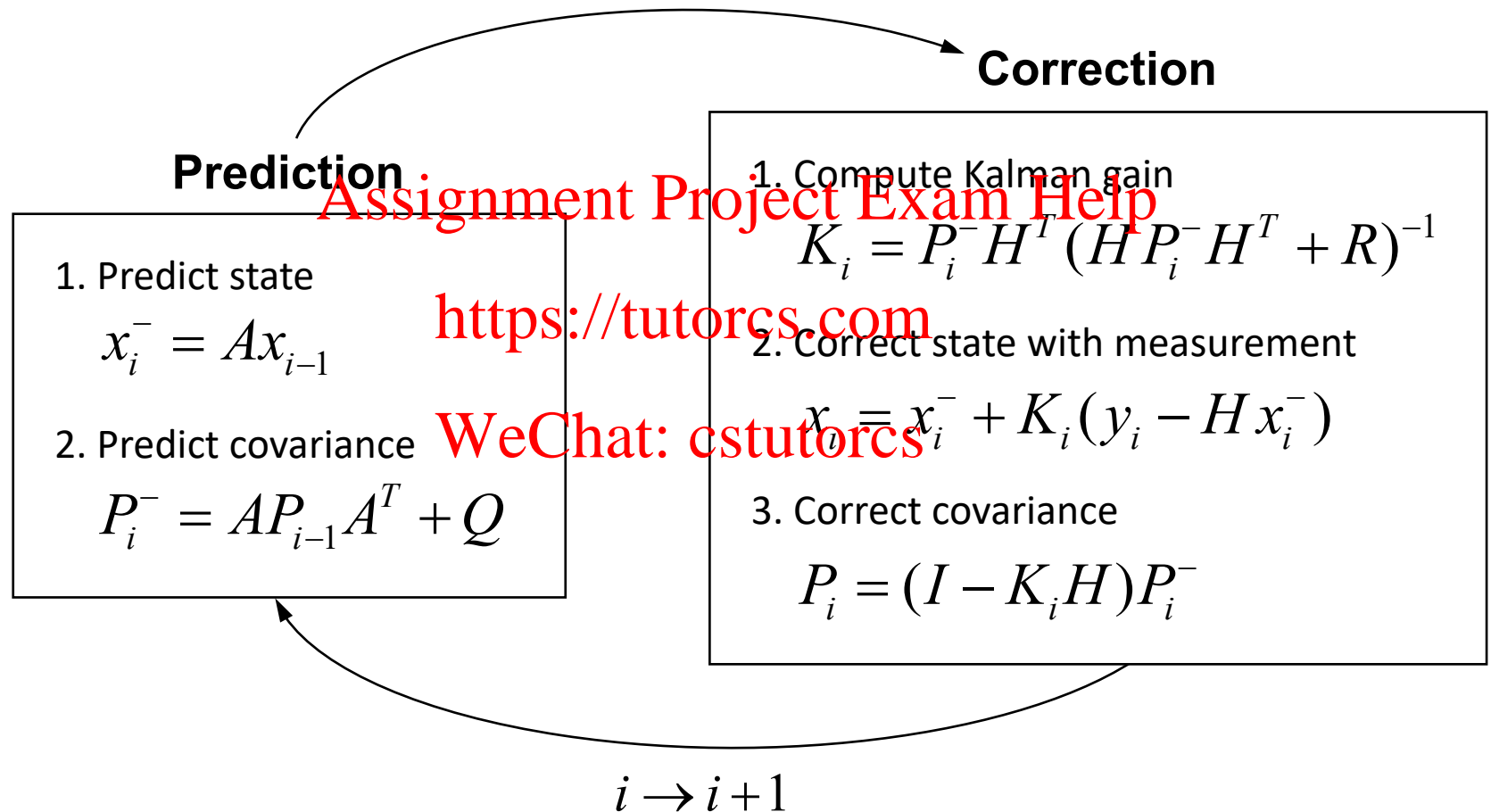
- The measurement is obtained by multiplying the state by some matrix and then adding a zero-mean normal random variable:

$$y_i = Hx_i + r_i$$

$$x_i \sim N(Ax_{i-1}, Q)$$

$$y_i \sim N(Hx_i, R)$$

Kalman Filtering

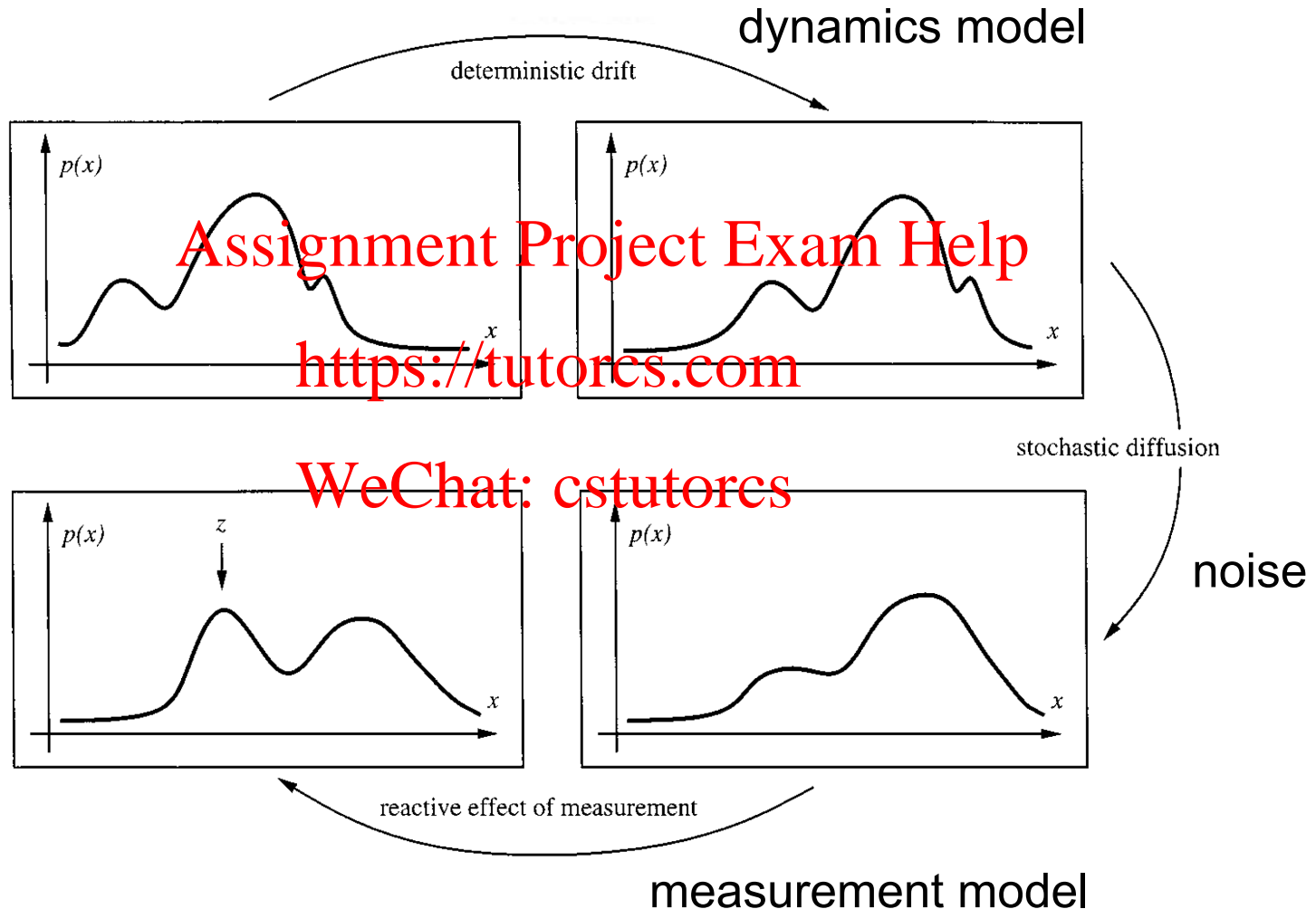


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Particle Filtering

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Probability Density Propagation



Non-Linear / Non-Gaussian Case

- Represent the conditional state density by a set of samples (particles) with corresponding weights (importance)

$$P(X_i | Y_{0:i}) \rightarrow \{s_i^{(n)}, \pi_i^{(n)}\}_{n=1}^M$$

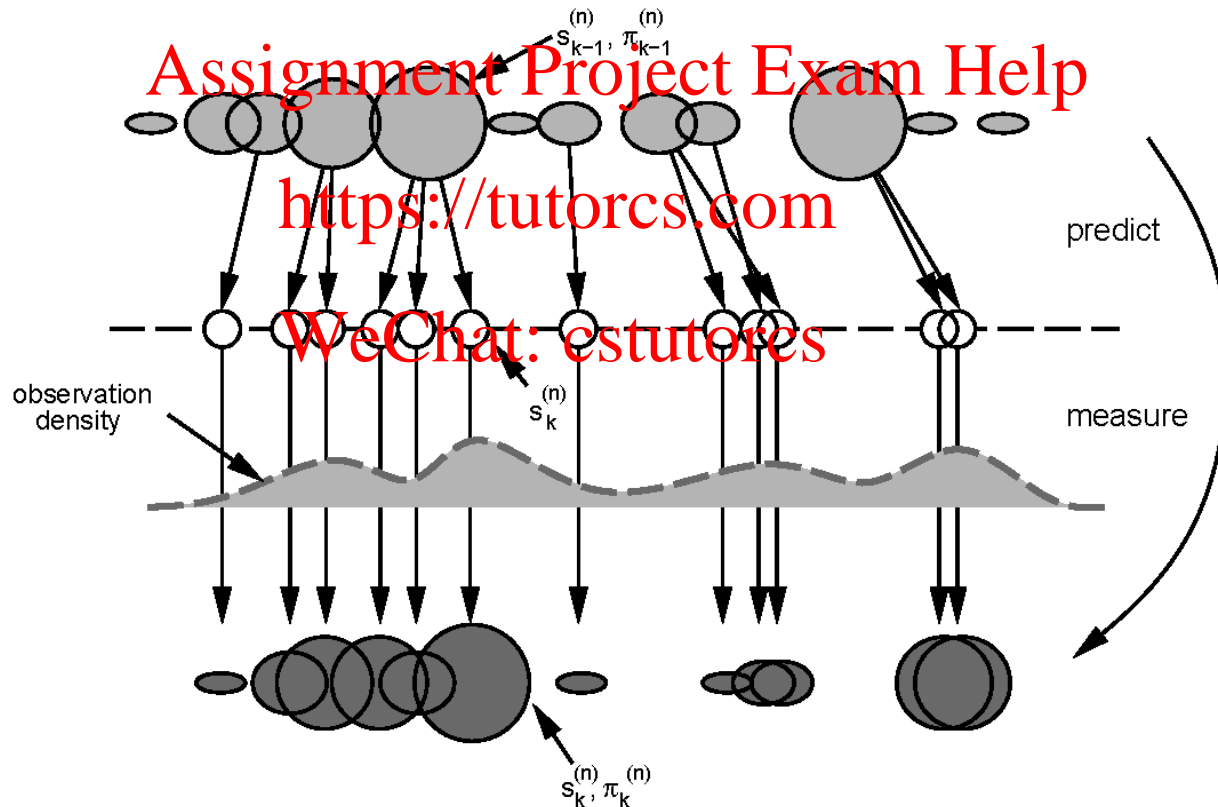
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Particle Filtering

- Propagate each sample using the dynamics model and obtain its new weight using the measurement model



Particle Filtering Algorithm

Iterate

From the “old” sample-set $\{\mathbf{s}_{t-1}^{(n)}, \pi_{t-1}^{(n)}, c_{t-1}^{(n)}, n = 1, \dots, N\}$ at time-step $t - 1$, construct a “new” sample-set $\{\mathbf{s}_t^{(n)}, \pi_t^{(n)}, c_t^{(n)}\}, n = 1, \dots, N$ for time t .

Construct the n^{th} of N new samples as follows:

1. **Select** a sample $\mathbf{s}_t^{(n)}$ as follows:
 - (a) generate a random number $r \in [0, 1]$, uniformly distributed.
 - (b) find, by binary subdivision, the smallest j for which $c_{t-1}^{(j)} \geq r$
 - (c) set $\mathbf{s}_t^{(n)} = \mathbf{s}_{t-1}^{(j)}$
2. **Predict** by sampling from

$$p(\mathbf{x}_t | \mathbf{x}_{t-1} = \mathbf{s}_{t-1}^{(n)})$$

to choose each $\mathbf{s}_t^{(n)}$.

3. **Measure** and weight the new position in terms of the measured features \mathbf{z}_t :

$$\pi_t^{(n)} = p(\mathbf{z}_t | \mathbf{x}_t = \mathbf{s}_t^{(n)})$$

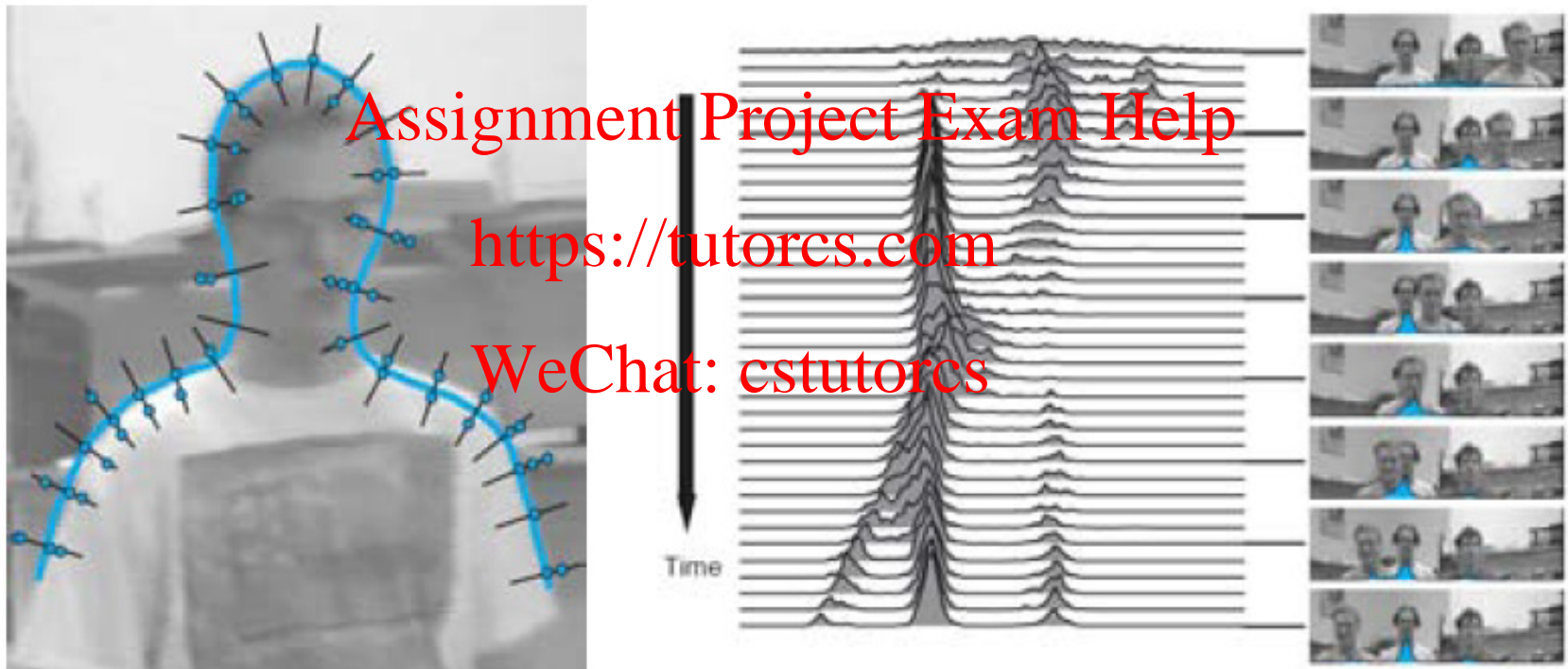
then normalise so that $\sum_n \pi_t^{(n)} = 1$ and store together with cumulative probability as $(\mathbf{s}_t^{(n)}, \pi_t^{(n)}, c_t^{(n)})$ where

$$\begin{aligned} c_t^{(0)} &= 0, \\ c_t^{(n)} &= c_t^{(n-1)} + \pi_t^{(n)} \quad (n = 1 \dots N) \end{aligned}$$

[NIPS 1996](#)

Example Application

Tracking of active contour representations of objects



Particle filtering is also known variously as sequential Monte Carlo (SMC) filtering, bootstrap filtering, the condensation algorithm...

Example Application

Tracking of object location in the presence of clutter



Walking pedestrian represented by a state vector consisting of a center position and a bounding box:

$$s_i = (x, y, w, h)_i$$

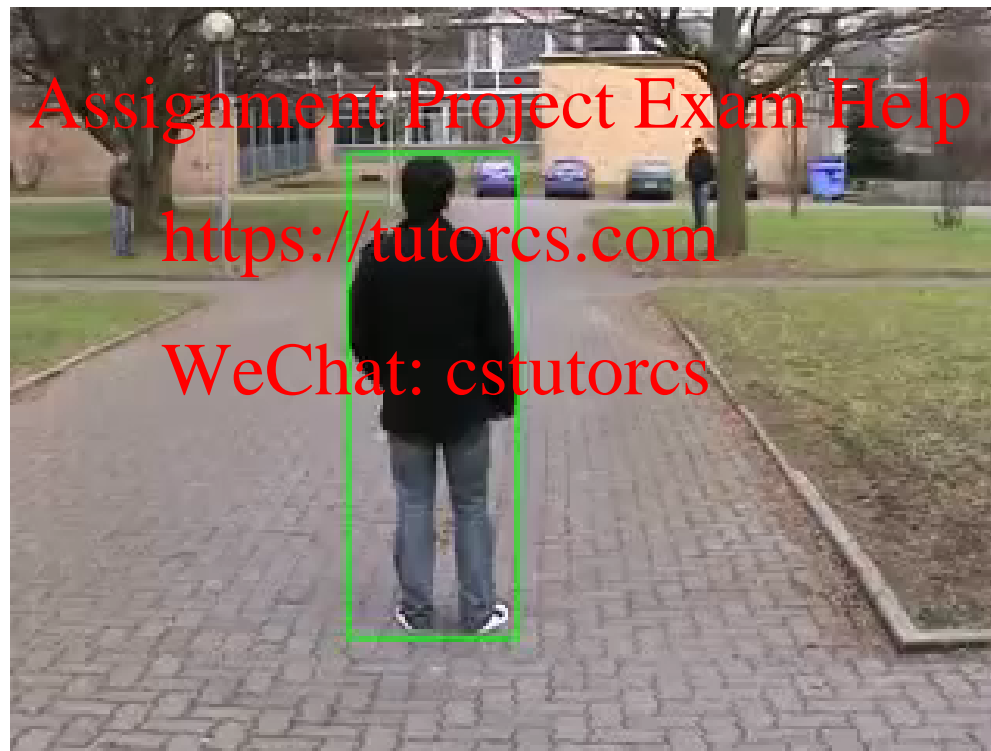
$$s_i^{(n)} \quad (\text{samples})$$

$$\hat{s}_i \quad (\text{estimated})$$

$$\tilde{s}_i \quad (\text{truth/annotated})$$

Example Application

Tracking of object location in the presence of clutter

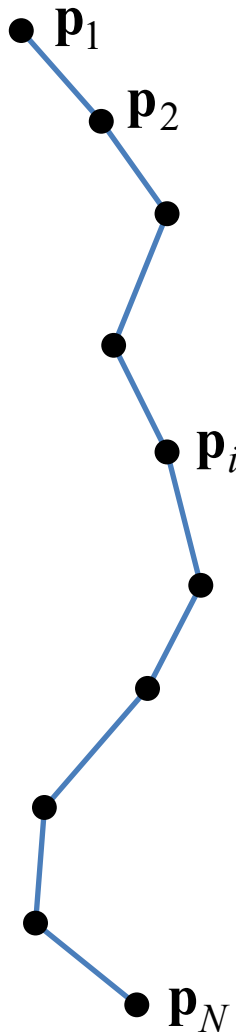


https://www.youtube.com/watch?v=j-duyzShJ_o

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Trajectory Analysis

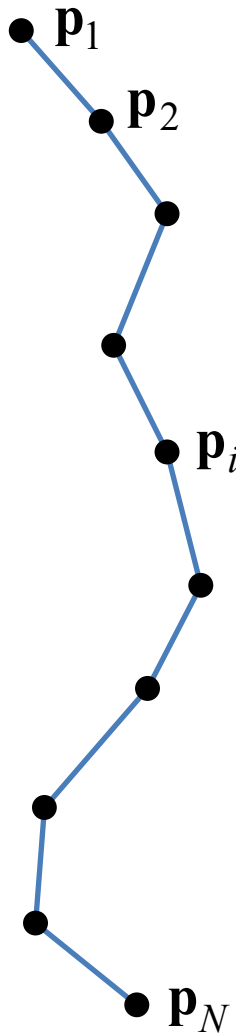
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Motion Features

| Measure | Definition |
|----------------------------------|--|
| Total distance traveled | $d_{\text{tot}} = \sum_{i=1}^{N-1} d(\mathbf{p}_i, \mathbf{p}_{i+1})$ |
| Net distance traveled | $d_{\text{net}} = d(\mathbf{p}_1, \mathbf{p}_N)$ |
| Maximum distance traveled | $d_{\text{max}} = \max_i d(\mathbf{p}_1, \mathbf{p}_i)$ |
| Total trajectory time | $t_{\text{tot}} = (N-1)\Delta t$ |
| Confinement ratio | $r_{\text{con}} = d_{\text{net}}/d_{\text{tot}}$ |
| Instantaneous angle | $\alpha_i = \arctan(y_{i+1} - y_i)/(x_{i+1} - x_i)$ |
| Directional change | $\gamma_i = \alpha_i - \alpha_{i-1}$ |
| Instantaneous speed | $v_i = d(\mathbf{p}_i, \mathbf{p}_{i+1})/\Delta t$ |
| Mean curvilinear speed | $\bar{v} = \frac{1}{N-1} \sum_{i=1}^{N-1} v_i$ |
| Mean straight-line speed | $v_{\text{lin}} = d_{\text{net}}/t_{\text{tot}}$ |
| Linearity of forward progression | $r_{\text{lin}} = v_{\text{lin}}/\bar{v}$ |
| Mean squared displacement | $\text{MSD}(n) = \frac{1}{N-n} \sum_{i=1}^{N-n} d^2(\mathbf{p}_i, \mathbf{p}_{i+n})$ |

<https://doi.org/10.1016/B978-0-12-391857-4.00009-4>

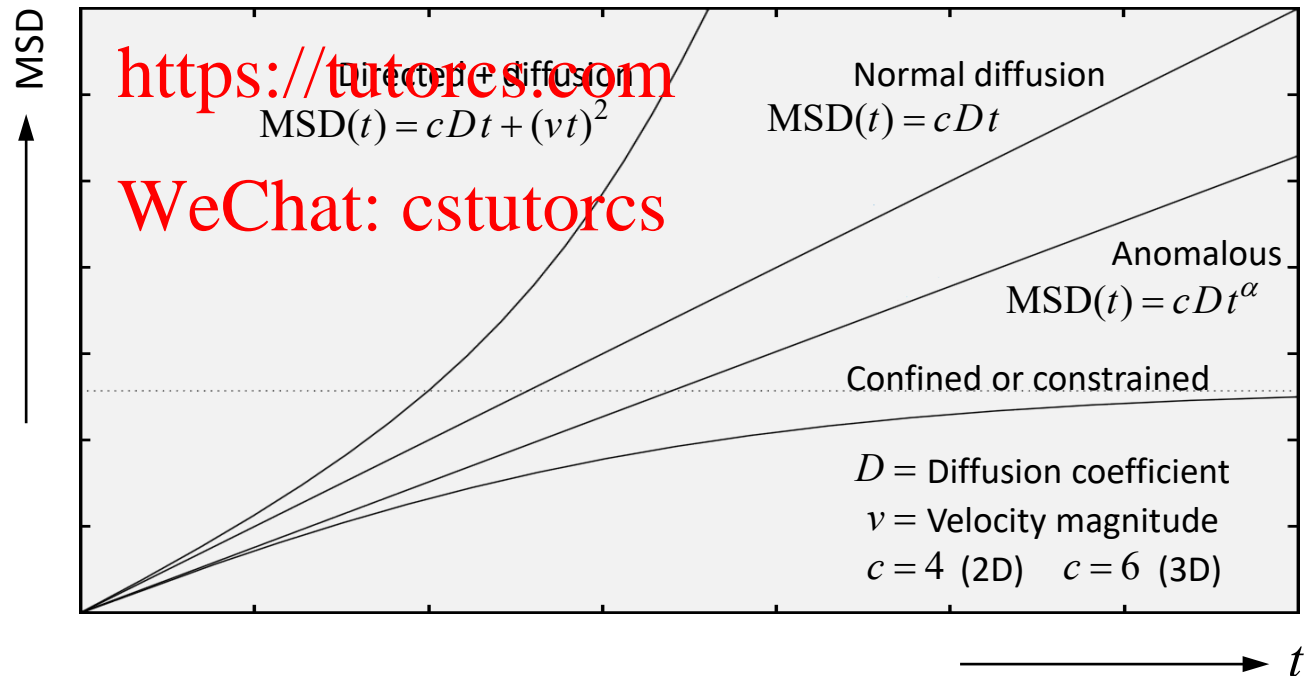


MSD Analysis

Distance between track points: $d(\mathbf{p}_i, \mathbf{p}_j) = \|\mathbf{p}_j - \mathbf{p}_i\|_2$

MSD for a given time lag t : $\text{MSD}(t) = \frac{1}{N-t} \sum_{i=1}^{N-t} d^2(\mathbf{p}_i, \mathbf{p}_{i+t})$

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References and Acknowledgements

- Chapters 5 and 8 of Szeliski 2010
- Chapter 18 of Forsyth and Ponce 2011
- Chapter 9 of Shapiro and Stockman 2001
- Paper by M. Isard and A. Blake 1998
<https://tutorcs.com>
CONDENSATION: Conditional density propagation for visual tracking
Available online via the UNSW Library
- Some images drawn from the above references