COMPSCI 3MI3 - Principles of Programming Languages

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McMaster University

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Adapted from "Types and Programming Languages" by Benjamin C. Pierce

About :=

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The left-hand-side of := is a **location** of a memory cell.

When these can be stored to multiple times (without allocation), called Ausgrafient Project Exam Help

- Memory allocation, aka creating a reference.
- A "store" peration, at a assignment. COM
 A "retrieve" operation, aka dereferencing.

Depending on the programming language, some or all of these operations may be implicit in the trammar.

• Python hides allocation and retrieval, but storage is explicit.

- C/C++ hides retrieval, with allocation and storage being explicit.
- In ML, all three operations are explicit.
- Haskell buries these very deeply in a library.

References

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(T-Deref)

$$\frac{\Gamma \vdash t_1 : Ref \ T_1 \qquad \Gamma \vdash t_2 : T_1}{\Gamma \vdash t_1 := t_2 : \textit{Unit}}$$

(T-Assign)

A Sample Program

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```
let y = ref 0 in
let z = ref 1 in

x := 12;
y := 13ttps://tutorcs.com
z := !x + !y;
!z
```

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ref is like new in Java.

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Sharing is not necessarily bad

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```
let c = ref 0 in

let inc_c = \lambda x : Unit. (c := succ (!c); !c) in

let dec_ttps!//tutorcs.com

inc_c unit;

dec_c unit
```

The values of Co... Threather Spiritores

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Heap / Store

Aas Sarg In Month Altes, Proposition of the Some set of store locations. Use / to range over £.

A memory store is then a (partial) function from $\mathcal L$ to values. $\frac{\mathcal L}{\mathcal L} = \frac{\mathcal L}{\mathcal L} = \frac$ Vocabulary:

- - We will use μ to denote memory stores.
 - Reference pi (be platlocation tutores
 - "memory store" wil be just store.

Store passing style

Attach μ directly to terms:

$$t \mid \mu$$

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New evalunity s://tutorcs.com

$$(\lambda x : T_{11}.t_{12})v_2 \mid \mu \to [x \mapsto v_2]t_{12} \mid \mu$$

(E-AppAbs)

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 $\overline{t_1 t_2 \mid \mu \rightarrow t_1' t_2 \mid \mu'}$

$$\frac{t_2 \mid \mu \to t_2' \mid \mu'}{t_1 \ t_2 \mid \mu \to t_1 \ t_2' \mid \mu'}$$

(E-App1)

(E-App2)

Dereferencing

New evaluation rules for dereferencing.

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(E-DerefLoc)

WeChat. $\overset{t_1 \mid \mu \rightarrow t'_1 \mid \mu'}{\text{Cstutores}}$

(E-Deref)

- Dereferencing a location: if we have a value for that location, return it.
- Otherwise evaluate t_1 (possibly with an effect)

Note: ! 5 is stuck.

Assignment

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(E-Assign1)

 $t_2 \mid \mu \to t_2' \mid \mu'$

(E-Assign2)

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• $[l\mapsto v_2]\mu$ means "a store which maps l to v, with all other locations mapping to the same things as in μ ."

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ref $v_1 \mid \mu \rightarrow l \mid \mu \oplus l \mapsto v_1$

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(E-Ref)

- E-RefV: we select a fresh location l not already used in μ . Extend with the real mapping STUTORS
- The term ref v evaluates to this fresh location l.

Typing the store

Skip entirely: a first "simple" approach that does not scale.

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Typing the store

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Assignment de l'urboj ectio Exampe Help instantiating value.

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Typing the store

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Assignment Projectio Examp Help instantiating value.

Create a typing store \(\Sigma\) in parallel with contexts \(\Sigma\) $\Sigma(l) = T_1$ (T-Loc) $\Gamma \mid \Sigma \vdash l : Ref T_1$

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 Γ starts off empty, and has typings added as the program is traversed.
- \bullet Σ will be the same
- Write empty Γ and emptr Σ as Ø.

Typing Allocation

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(T-Ref)

 $\begin{array}{c} \overset{\Gamma \mid \Sigma \vdash t_1 : \textit{Ref } T_{11}}{\text{WeChat:}} \\ \overset{\Gamma \mid \Sigma \vdash t_1 : \textit{Ref } T_{11}}{\text{CStutores}} \end{array}$

 $\Gamma \mid \Sigma \vdash t_1 := t_2 : Unit$

(T-Deref)

(T-Assign)

Typed Stores

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A store μ is said to be well typed with respect to a typing context Γ and a store typing Tife the dom(the

- $\forall l \in dom(\mu) \mid \mu(l) : \Sigma(l)$

We write this Echat: cstutorcs

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$$\begin{array}{c} https://tutores'.com \\ & (\Gamma \mid \Sigma \vdash t : T) \\ & \wedge (\Gamma \mid \Sigma \vdash \mu) \\ & \Rightarrow (\Gamma \mid \Sigma \vdash t' : T) \end{array}$$

But stepping can change and thus as utores

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```
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\Rightarrow (\exists \Sigma' \supseteq \Sigma \mid U)
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\wedge (\Gamma \mid \Sigma \vdash \mu)
```

Technical lemmas

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$$(\Gamma, x : S \mid \Sigma \vdash t : T) \land (\Gamma \mid \Sigma \vdash s : S) \implies (\Gamma \mid \Sigma \vdash [x \mapsto s]t : T])$$
 (1)

LEMMA: Tresposion/tvertories.com

$$(\Gamma \mid \Sigma \vdash \mu) \land (\Sigma(l) = T) \land (\Gamma \mid \Sigma \vdash \nu : T) \implies (\Gamma \mid \Sigma \vdash [l \mapsto \nu]\mu)) \quad (2)$$

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$$(\Gamma \mid \Sigma \vdash t : T) \land (\Sigma' \supseteq \Sigma) \implies (\Gamma \mid \Sigma' \vdash t : T)$$
 (3)

Progress

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Suppose $\emptyset \mid \Sigma \vdash t : T$ for some T and Σ . Then either t is a value, or else, for any store μ such that $\emptyset \mid \Sigma \vdash \mu$, there is some term t' and store μ' such that $t \mid \mu$ **https://tutorcs.com**

Proof Sketch

- Induction on typing derivations.
 The canonical forms remain needs two additional cases, stating that all values of type Ref T are locations, and similarly for Unit.