

CS 239 Quantum Programming Spring 2019

Midterm Exam

程序代写代做 CS编程辅导

May 1, 2019: 100 minutes. Write your name and UCLA id on the first page you submit; staple the pages you



Each of questions 1-10 is worth 5 points, and each of questions 11-13 is worth 10 points.

1. Describe briefly the principles about quantum mechanics upon which quantum computing is based.
2. What is a qubit?
3. Is the following matrix unitary? Justify your answer.

$$\text{WeChat: } \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix}$$

4. Calculate the following tensor product.

$$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \otimes \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

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5. Calculate the following tensor product.

$$\text{QQ: } \left(\frac{3}{5}|0\rangle - \frac{4}{5}|1\rangle \right) \otimes \left(\frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle \right)$$

6. What state do we get if we apply $(H \otimes I) CNOT$ to the following state?

$$\sqrt{\frac{1}{3}}|00\rangle + \sqrt{\frac{2}{3}}|11\rangle$$

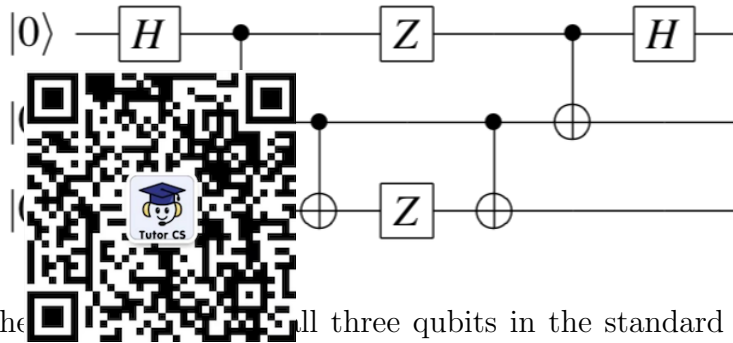
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7. For the following state, suppose we measure the second qubit in the standard basis and get 0. Show the resulting state. Justify your answer.

$$\frac{3}{5}|00\rangle - \frac{2}{5}|01\rangle + \frac{2}{5}|10\rangle + \frac{2\sqrt{2}}{5}|11\rangle$$

8. Suppose we apply $H^{\otimes 3}$ to three qubits in the state $|111\rangle$, after which we measure the first two qubits in the standard basis. What is the probability that we will get 11?

9. Consider the following circuit with three qubits.



Suppose that at the end of the circuit all three qubits are measured in the standard basis. What is the probability that we will get 000? Justify your answer.

10. Consider the following state.

$$\frac{1}{3}|00\rangle + \frac{1}{3}|01\rangle - \frac{2}{3}|11\rangle$$

Suppose we measure the first qubit in the standard basis. What is the probability of getting 0, and if that happens, what is the state of the second qubit? Also suppose we measure the second qubit in the standard basis. What is the probability of getting 1, and if that happens, what is the state of the first qubit?

11. Show, step by step, that the Deutsch-Jozsa algorithm works for the case of $f(x) = x$.

12. For the case of $n = 3$ and a function f where

$$\begin{aligned} f(000) &= f(011) = 010 & f(100) &= f(111) = 110 \\ f(001) &= f(010) = 101 & f(101) &= f(110) = 001 \end{aligned}$$

give two different examples of equations that the first step of Simon's algorithm may produce. Explain what those equations mean.

13. Show, step-by-step, that Grover's algorithm works for the case of 2 qubits and a function f where $f(10) = 1$ and $f(00) = f(01) = f(11) = 0$.