

# COMP 251

程序代写代做 CS编程辅导

Algorithms



Structures (Winter 2022)

Algorithm Paradigms – Dynamic Programming 1  
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# Announcements

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# Outline

程序代写代做 CS编程辅导

- Complete Search
- Divide and Conquer
- Dynamic Programming
  - Introduction.
  - Examples.
- Greedy.



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# Dynamic Programming— What is it?

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- What's the following equal to

$$1+1 = ?$$



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# Dynamic Programming— What is it?

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- What's the following equal to

$$1+1 = 21$$

$$1+1 = ?$$



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# Dynamic Programming— What is it?

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- What's the following equal to

$$1+1+1+1+1+1+1+1+1+1+1+1+1+1+1+1+1+1+1+1 = 21$$

$$1+1 = 22$$



subproblem

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“DP is just a fancy way to remembering stuff to save time later!”

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Jonathan Paulson

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Famous saying:

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Algorithms who cannot  
remember the past are  
condemned to recompute it.

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# Dynamic Programming— What is it?

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- What's the following equal to

$$1+1+1+1+1+1+1+1+1+1+1+1+1+1+1+1+1+1+1+1 = 21$$

$$1+1 = ?$$



subproblem

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DP breaks a problem into smaller overlapping sub-problems and avoids the computation of the same results more than once.

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Famous saying:

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Those who cannot  
remember the past are  
condemned to repeat it.

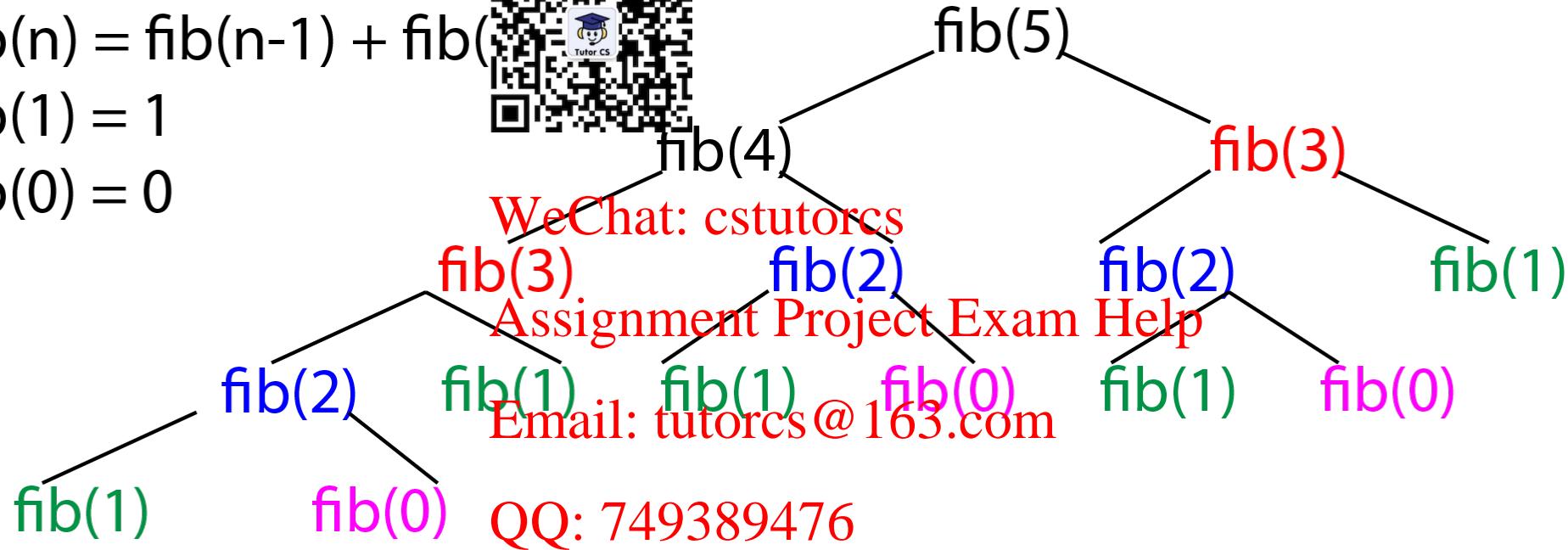
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Algorithms who cannot  
remember the past are  
condemned to recompute it.

# Dynamic Programming— What is it?

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$\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$   
 $\text{fib}(1) = 1$   
 $\text{fib}(0) = 0$



$\text{fib}(n):$   
    if  $n \leq 1$   
        return  $n$   
    return  $\text{fib}(n - 1) + \text{fib}(n - 2)$

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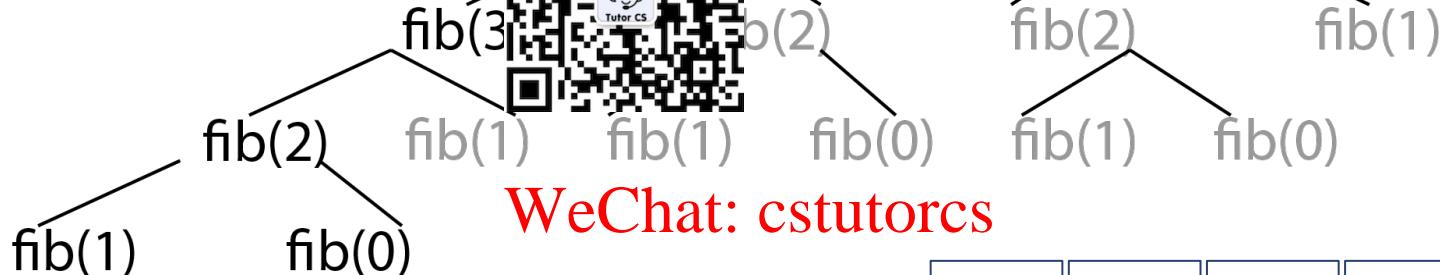
# Dynamic Programming— What is it?

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$$\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$$

$$\text{fib}(1) = 1$$

$$\text{fib}(0) = 0$$



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```
fib(n):  
    if n <= 1  
        return n  
    else  
        if FibArray[n-1] == 0  
            FibArray[n-1] = fib(n-1)  
        if FibArray[n-2] == 0  
            FibArray[n-2] = fib(n-2)  
        FibArray[n] = FibArray[n-2] + FibArray [n-1]  
    return FibArray[n]
```

FibArray = fib(0) fib(1) fib(2) fib(3) fib(4) fib(5)

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FibArray[n-1] = fib(n-1)

If FibArray[n-2] == 0

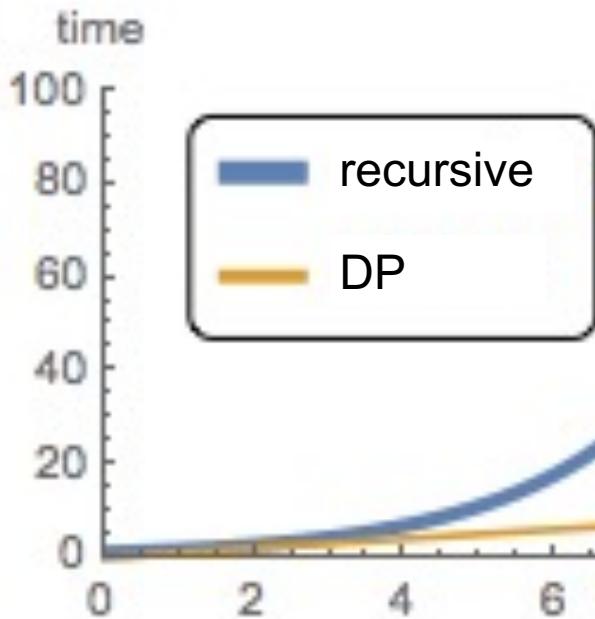
FibArray[n-2] = fib(n-2)

FibArray[n] = FibArray[n-2] + FibArray [n-1]

return FibArray[n]

# Dynamic Programming— What is it?

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DP looks through all possible sub-problems and never re-computes the solution to any sub-problem. This implies correctness and efficiency, which we can not say of most techniques. This alone makes DP special

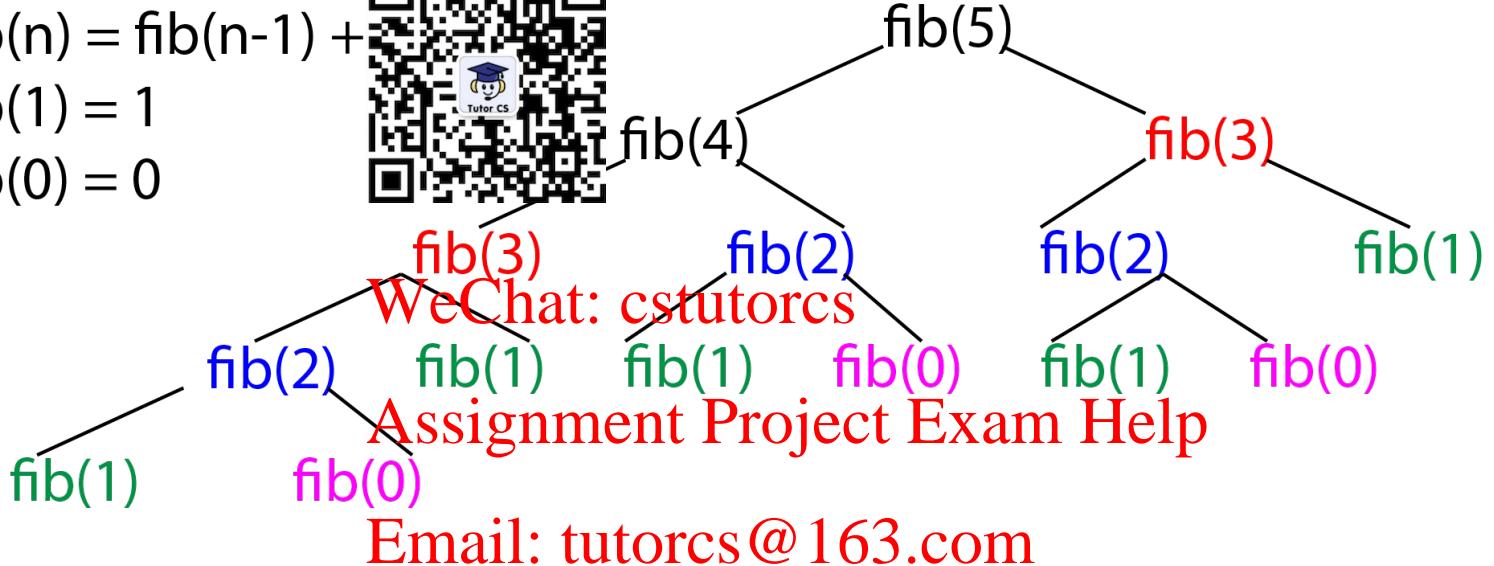
# Dynamic Programming— When to use it?

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$$\text{fib}(n) = \text{fib}(n-1) +$$

$$\text{fib}(1) = 1$$

$$\text{fib}(0) = 0$$



Key ingredients to make DP works

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1. This problem has optimal sub-structures.

- Solution for the sub-/problem is part of the solution of the original problem.

2. This problem has overlapping sub-problems.

# Dynamic Programming— How to solve it?

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## Steps for Solving DP Problems

1. Define subproblems

$\text{fib}(n-1)$  and  $\text{fib}(n-2)$  are subproblems of  $\text{fib}(n)$

2. Write down the recurrence that relates subproblems.

$$\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$$

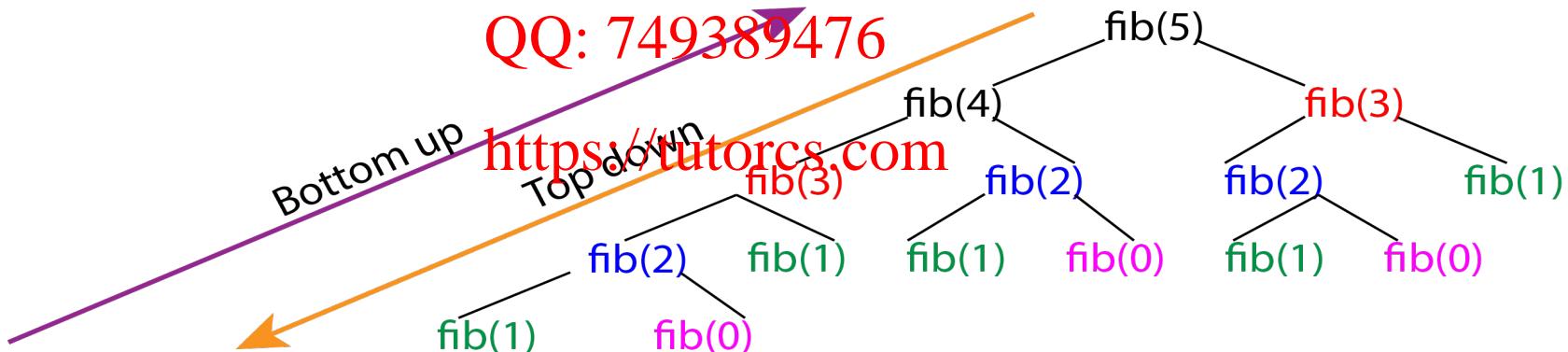
3. Recognize and solve the base cases.

$$\text{fib}(0) = 0; \text{fib}(1) = 1$$

4. Implement a solution

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- Memoization: Top down approach => FibArray[]
- Tabulation: Bottom up approach



# Top-Down VS Bottom-Up

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## ↗ Top Down (Memoization)



- ↗ I will be an expert in dynamic programming. How? I will work hard like crazy. How? I will practice more and try to improve. How? I'll actively participate in David classes. How? I will attend all David's classes. Then, I'm going to learn dynamic programming.  
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## ↗ Bottom Up (Tabulation)

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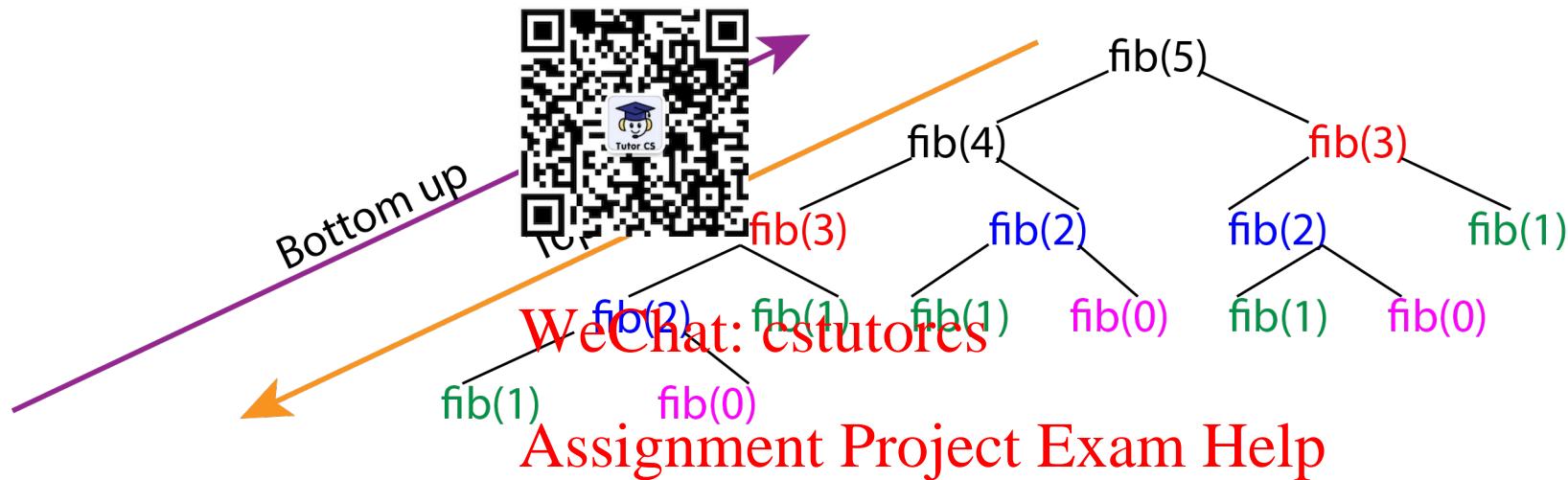
- ↗ I'm going to learn dynamic programming. Then, I will attend all David's classes. Then, I will actively participate in David classes. Then, I'll practice even more and try to improve. After working hard like crazy, I will be an expert in dynamic

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# DP - Top-Down

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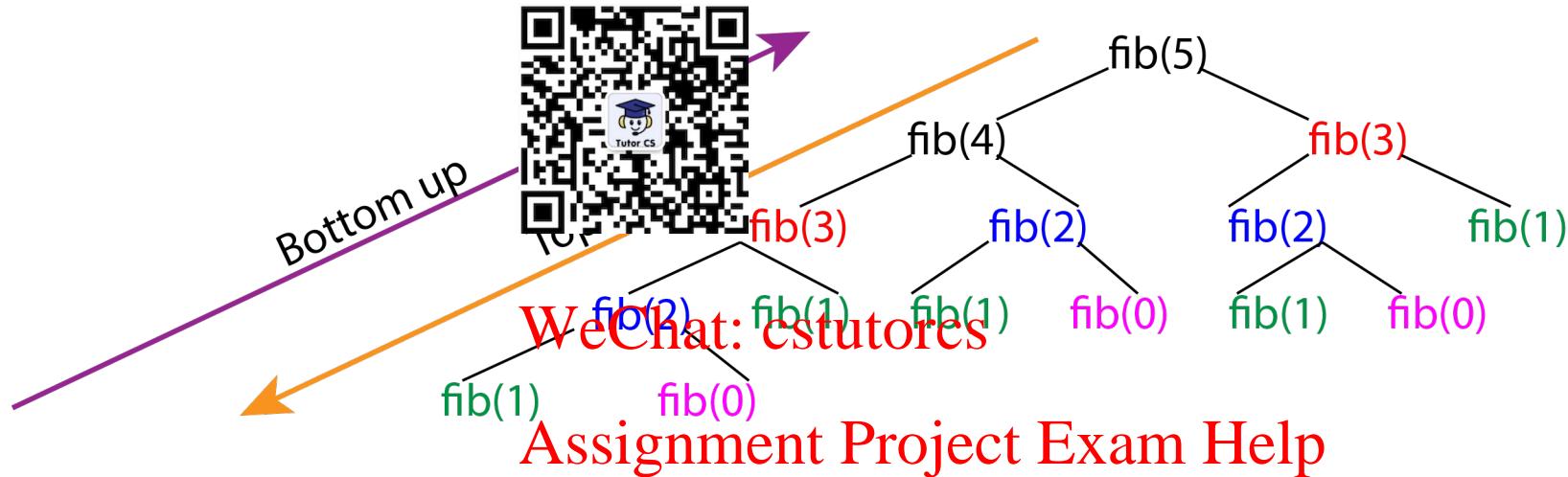


1. Initialize a DP ‘memo’ table with dummy values, e.g. -1.
  - The dimension of the DP table must be the size of distinct sub-problems.
2. At the start of recursive function, simply check if this current state has been computed before.
  - (a) If it is, simply return the value from the DP memo table, O(1).
  - (b) If it is not, compute as per normal (just once) and then store the computed value in the DP memo table so that further calls to this sub-problem is fast.

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# DP – Bottom-Up

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1. Identify the Complete Search recurrence.
2. Initialize some parts of the DP table with known initial values.
3. Determine how to fill the rest of the DP table based on the Complete Search recurrence, usually involving one or more nested loops to do so.

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# DP - Top-Down VS Bottom-Up

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## Top-Down

### Pro:

1. It is a natural transformation from normal complete search recursion.
2. Compute sub-problems only when necessary.

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## Bottom-Up

### Pro:

1. Faster if many sub-problems are revisited as there is no overhead from recursive calls.
2. Can save memory space with DP “on-the-fly” technique.

### Cons:

1. Slower if many sub-problems are revisited due to recursive calls overhead.
2. If there are  $M$  states, it can use up to  $O(M)$  table size which can lead to memory problems.

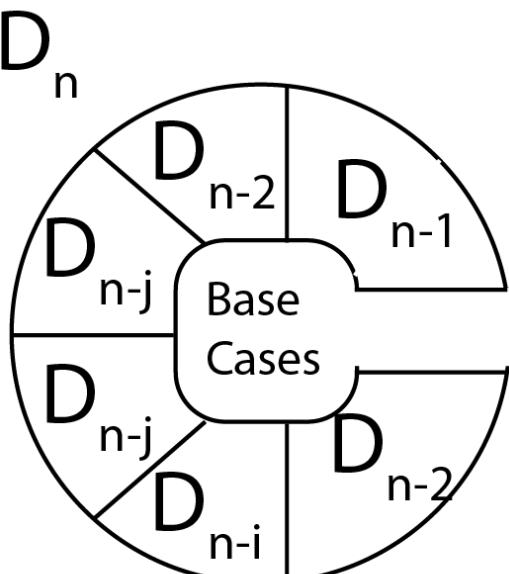
### Cons:

1. For some programmers who are inclined with recursion, this may be not intuitive.
2. If there are  $M$  states, bottom-up DP visits and fills the value of *all* these  $M$  states.

# DP – Take home picture

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## Paradigm



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Overlapping subproblems

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AND

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Optimal substructure

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## Solution



Memoization  
Top-Down Approach

OR

Tabulation  
Bottom-up Approach

# DP – Examples

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# DP – 1-dimensional

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**Problem:** Given  $n$ , find the number of different ways to write  $n$  as the sum of the numbers 1, 2, 3, 4.

**Example:** for  $n = 5$ , the number is 6

$$5 = 1 + 1 + 1 + 1 + 1 \quad \text{WeChat: cstutorcs}$$

$$= 1 + 1 + 3$$

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$$= 1 + 3 + 1$$

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$$= 3 + 1 + 1$$

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$$= 1 + 4$$

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$$= 4 + 1$$



# DP – 1-dimensional

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Step 1: Identify the problems (in words).

Step 1.1: Identify the problems.



Let  $D_{n-i}$  be the number of ways to write  $n-i$  as the sum of 1, 3, 4.

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$$D_5 = \boxed{1 + 1 + 1 + 1} + 1 \\ D_4$$

$$D_5 = \boxed{1 + 1} + 3 \\ D_2$$

$$D_5 = \boxed{1 + 3} + 1 \\ D_4$$

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$$D_5 = \boxed{3 + 1} + 1 \\ D_4$$

$$D_5 = \boxed{1} + 4 \\ D_1$$

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$$D_5 = \boxed{4} + 1 \\ D_4$$

# DP – 1-dimensional

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## Step 2: Find the recurrence.

Step 2.1: What decision do we make at every step?

- Consider one solution  $n = x_1 + x_2 + \dots + x_m$
- If  $x_m = 1$ , the rest of the terms must sum to  $n - 1$ . Thus, the number of sums that end with  $x_m = 1$  is equal to  $D_{n-1}$

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$$D_5 = \boxed{1 + 1 + 1 + 1} + 1$$

$$D_5 = \boxed{1} + 4$$

$$D_5 = \boxed{1 + 3} + 1$$

$$D_5 = \boxed{1 + 1} + 3$$

$$D_1$$

$$D_5 = \boxed{3 + 1} + 1$$

$$D_2$$
  
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$$D_5 = \boxed{4} + 1$$

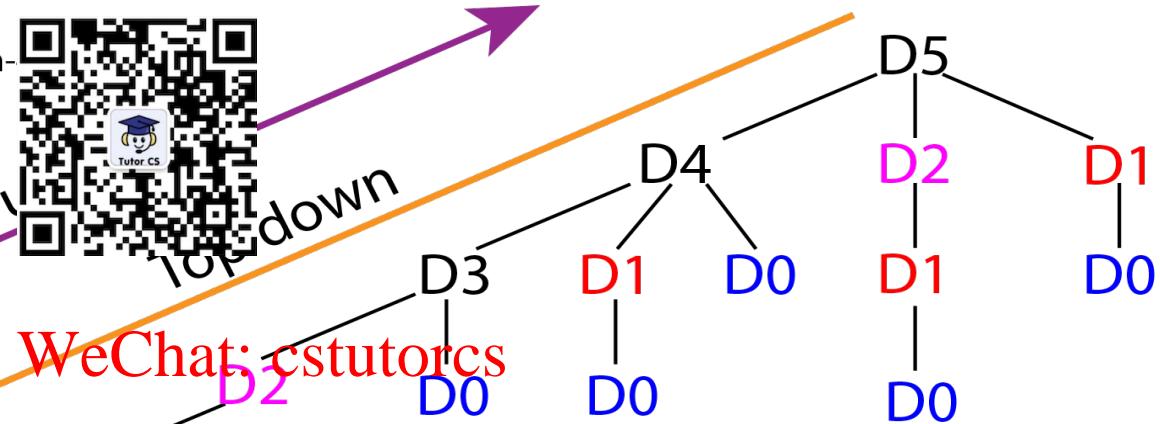
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$D_4$

# DP – 1-dimensional

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$$D_n = D_{n-1} + D_{n-3} + D_{n-5}$$
$$D_0 = 1$$



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ANS: 6 different ways

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Key ingredients to make DP works

1. This problem has optimal sub-structures
  - Solution for the sub-problem is part of the solution of the original problem.
2. This problem has overlapping sub-problems.

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# DP – 1-dimensional

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## Step 3: Recognize the base cases.

- ↗  $D_0 = 1$ , and  $D_n = 0$  for all  $n < 0$ .
- ↗ Alternatively, can set  $D_0 = D_1 = D_2 = 1$ , and  $D_3 = 2$



## Step 4: Implement a solving methodology.

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D[0] = D[1] = D[2] = 1; D[3] = 2;  
for(i = 4; i < n, i++)  
    D[i] = D[i-1] + D[i-3] + D[i-4];  
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# DP – 1-dimensional – weighted interval scheduling

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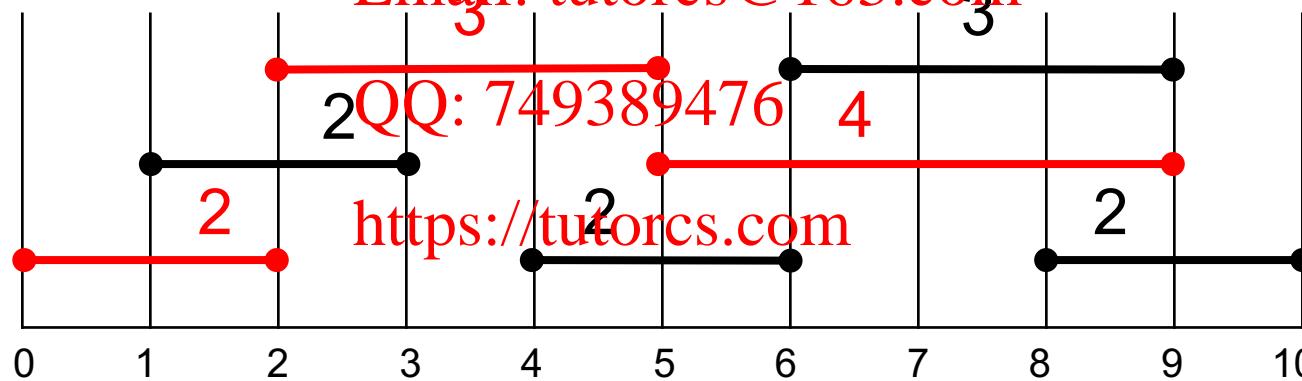
- **Input:** Set  $S$  of  $n$  activities  $a_1, a_2, \dots, a_n$ .
  - $s_i$  = start time of activity  $i$
  - $f_i$  = finish time of activity  $i$
  - $w_i$  = weight of activity  $i$
- **Output:** find maximum weight subset of mutually compatible activities.
  - 2 activities are compatible if their intervals do not overlap.



# DP – 1-dimensional – weighted interval scheduling

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Example:



# weighted interval scheduling – Data Structure

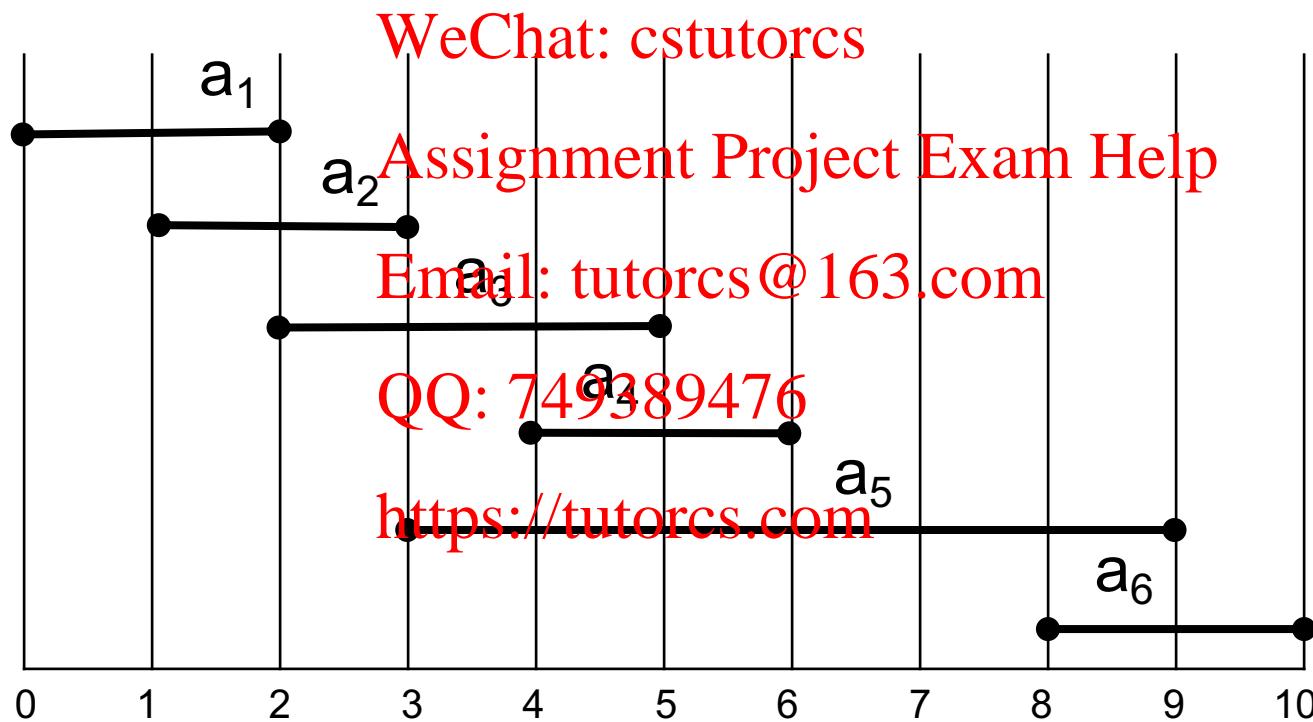
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**Notation:** All activities are sorted by finishing time  $f_1 \leq f_2 \leq \dots \leq f_n$



**Definition:**  $p(j) = \max\{i < j \text{ such that activity/job } i \text{ is compatible with activity/job } j\}$ .

**Examples:**  $p(6)=4$ ,  $p(5)=2$ ,  $p(4)=2$ ,  $p(2)=0$ .



# weighted interval scheduling – Data Structure

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Let  $S(i)$  be a set of intervals in maximal solution of problem when we can use only  $\{1, 2, \dots, i\}$ .

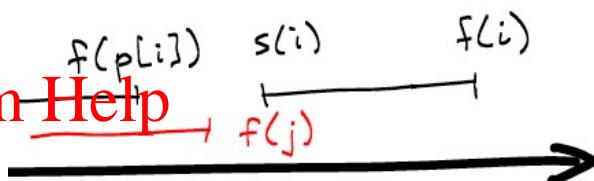


Claim: If  $i \in S(i)$  then

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$S(i)$  cannot contain  $j$  where  $p[i] < j < i$ .

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Proof:

To have  $p[i] < j < i$ , we would need

$f(p[i]) < f(j)$  and  $f(j) < s(i)$ .

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But this would contradict the definition of  $p[i]$ .

# weighted interval scheduling

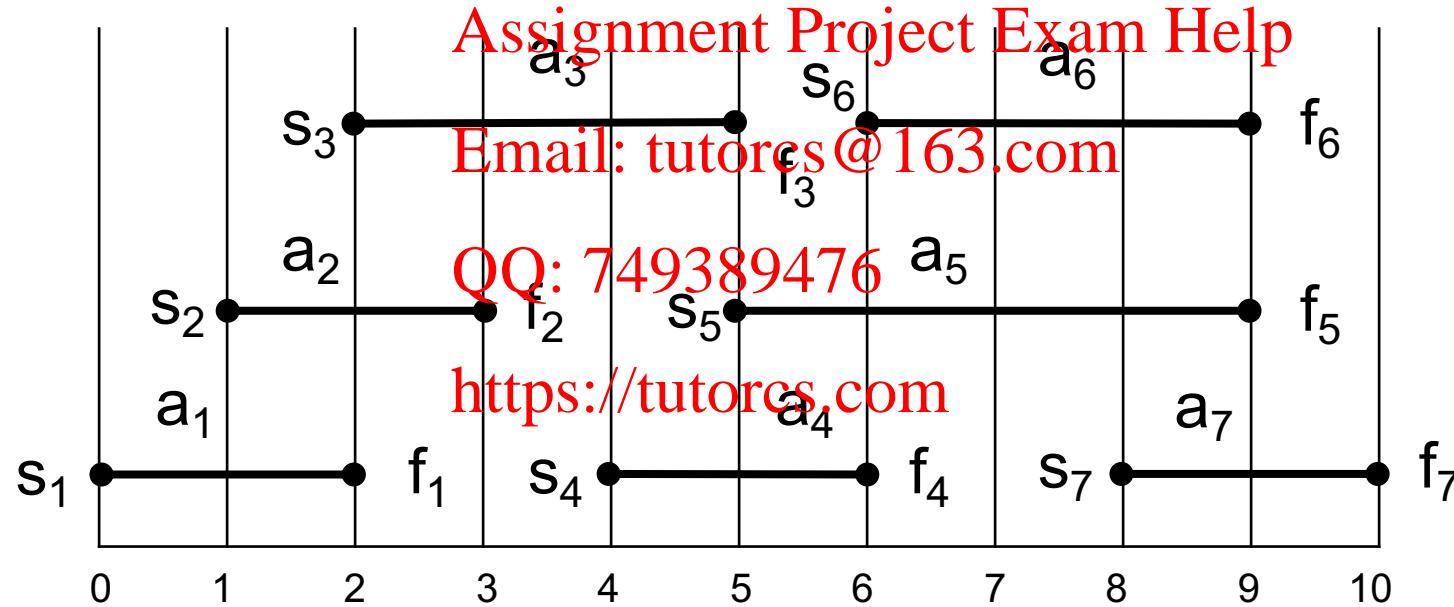
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Step 1: Identify the problems (in words).

Step 1.1: Identify the problems.



Let  $\text{OPT}(j)$  be the maximum total weight of compatible activities 1 to  $j$  (i.e., value of the optimal solution to the problem including activities 1 to  $j$ ).



# weighted interval scheduling

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## Step 2: Find the recurrence.



Step 2.1: What decisions do we make at every step?

Case 1: OPT selects activity j

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- Add weight  $w_j$
- Cannot use incompatible activities
- Must include optimal solution on remaining compatible activities { 1, 2, ...,  $p(j)$  }. Email: tutorcs@163.com

Case 2: OPT does not select activity j

- Must include optimal solution on other activities { 1, 2, ...,  $j-1$  }.

Optimal substructure property

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# weighted interval scheduling

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Step 2: Find the recurrence.



j

- ↗ Case 1: OPT selects activity j
  - ↗ Add weight  $w_j$
  - ↗ Cannot use incompatible activities
  - ↗ Must include optimal solution on remaining compatible activities { 1, 2, ..., p(j) }.

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- ↗ Case 2: OPT does not select activity j
  - Must include optimal solution on other activities { 1, 2, ..., j-1 }.

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$$OPT(j) = \begin{cases} 0 & \text{if } j = 0 \\ \max\{w_j + OPT(p(j)), OPT(j - 1)\} & \text{Otherwise} \end{cases}$$

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# weighted interval scheduling

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$$OPT(j) = \begin{cases} 0 & \text{if } j = 0 \\ \max\{w_j(p(j)), OPT(j - 1)\} & \text{Otherwise} \end{cases}$$



Input: n, s[1..n], f[1..n], v[1..n]

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Sort jobs by finish time so that  $f[1] \leq f[2] \leq \dots \leq f[n]$ .

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Compute  $p[1], p[2], \dots, p[n]$ .

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**Compute-Opt(j)**

if  $j = 0$

    return 0.

else

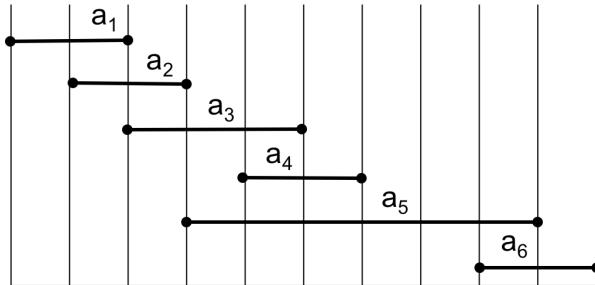
    return  $\max(v[j] + \text{Compute-Opt}(p[j]), \text{Compute-Opt}(j-1))$ .

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# weighted interval scheduling – recursion tree

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**Observation:**  $\text{OPT}(j)$  is calculated multiple times ...

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Case 2

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$\text{OPT}(5)$

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$\text{OPT}(4)$

$w_6 + \text{OPT}(4)$

$w_6 + w_4 + \text{OPT}(2)$

$w_6 + \text{OPT}(3)$

$w_5 + \text{OPT}(2)$

$w_6 + w_4 + w_2$

$w_6 + w_4 + \text{OPT}(1)$

$w_6 + w_3 + \text{OPT}(1)$

$w_6 + \text{OPT}(2)$

$w_5 + w_2$

$w_5 + \text{OPT}(1)$

...

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# weighted interval scheduling – top down

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**Memoization:** Cache results of each subproblem; lookup as needed.



Input:  $n, s[1..n], p[1..n], v[1..n]$

Sort jobs by finish time so that  $f[1] \leq f[2] \leq \dots \leq f[n]$ .

Compute  $p[1], p[2], \dots, p[n]$ .

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```
for j = 1 to n  
    M[j] ← empty.
```

$M[0] \leftarrow 0.$

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**M-Compute-Opt(j)**

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if  $M[j]$  is empty

$M[j] \leftarrow \max(v[j], M\text{-Compute-Opt}(p[j]), M\text{-Compute-Opt}(j-1))$

return  $M[j]$ .

# weighted interval scheduling – bottom-up

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**Observation:** When we compute  $M[j]$ , we only need values  $M[k]$  for  $k < j$ .



Input:  $n$ ,  $s[1..n]$ ,  $t[1..n]$ ,  $v[1..n]$

Sort jobs by finish time so that  $f[1] \leq f[2] \leq \dots \leq f[n]$ .

Compute  $p[1], p[2], \dots, p[n]$ .

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```
M[0] ← 0.  
for j = 1 TO n  
    M[j] ← max {v[j] + M[p(j)], M[j-1]}
```

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**Main Idea of Dynamic Programming:** Solve the sub-problems in an order that makes sure when you need an answer, it's already been computed.

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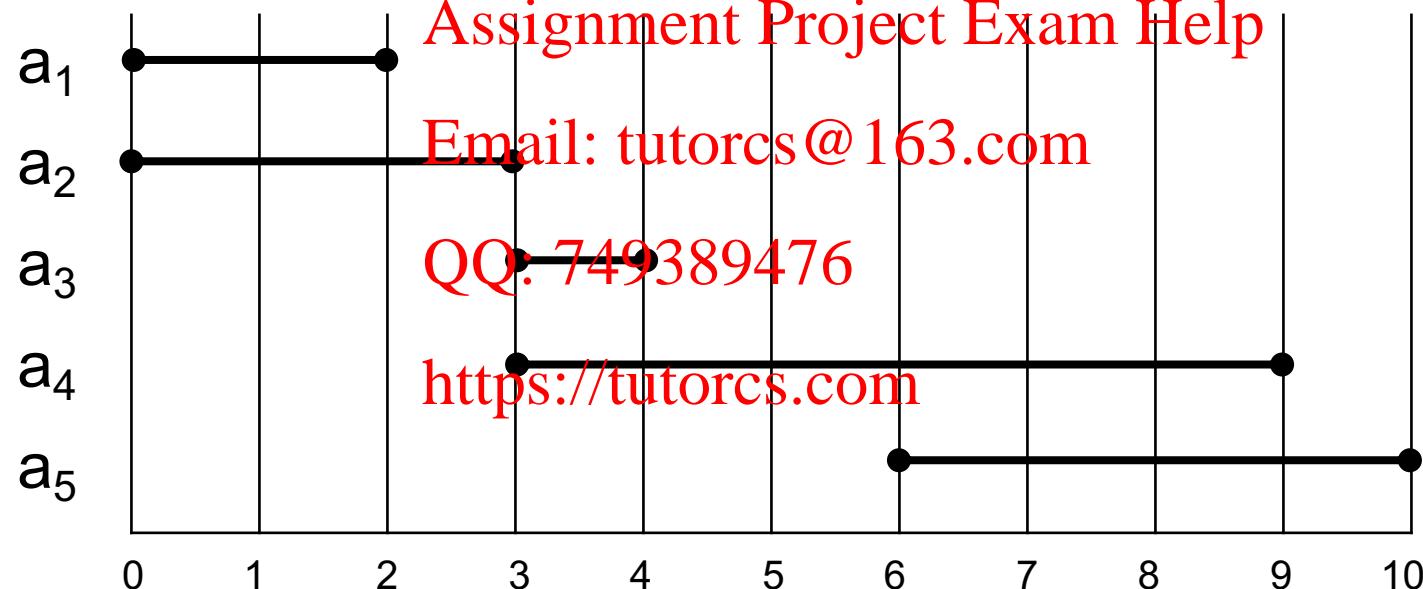
# weighted interval scheduling

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activity	1	2	3	4	5
predecessor	0	2	2	2	3
Best weight M	-	-	-	-	-
$V_j + M[p(j)]$	-	-	-	-	-
$M[j-1]$	-	-	-	-	-

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(1) Activities sorted by finishing time. (2) Weight equal to the length of activity.



# weighted interval scheduling

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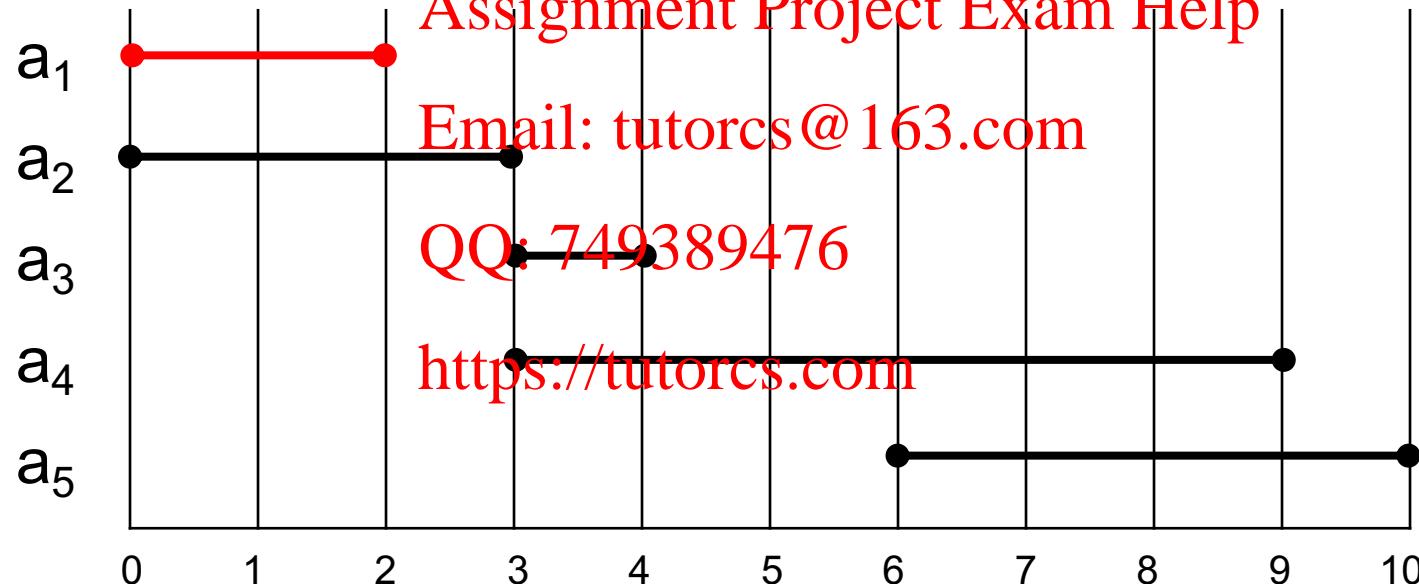
activity	1	2	3	4	5
predecessor	QR code	0	2	2	3
Best weight M	QR code	-	-	-	-
$V_j + M[p(j)]$	QR code	-	-	-	-
$M[j-1]$	0	-	-	-	-

$M[0]=0$

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(1) Activities sorted by finishing time. (2) Weight equal to the length of activity.

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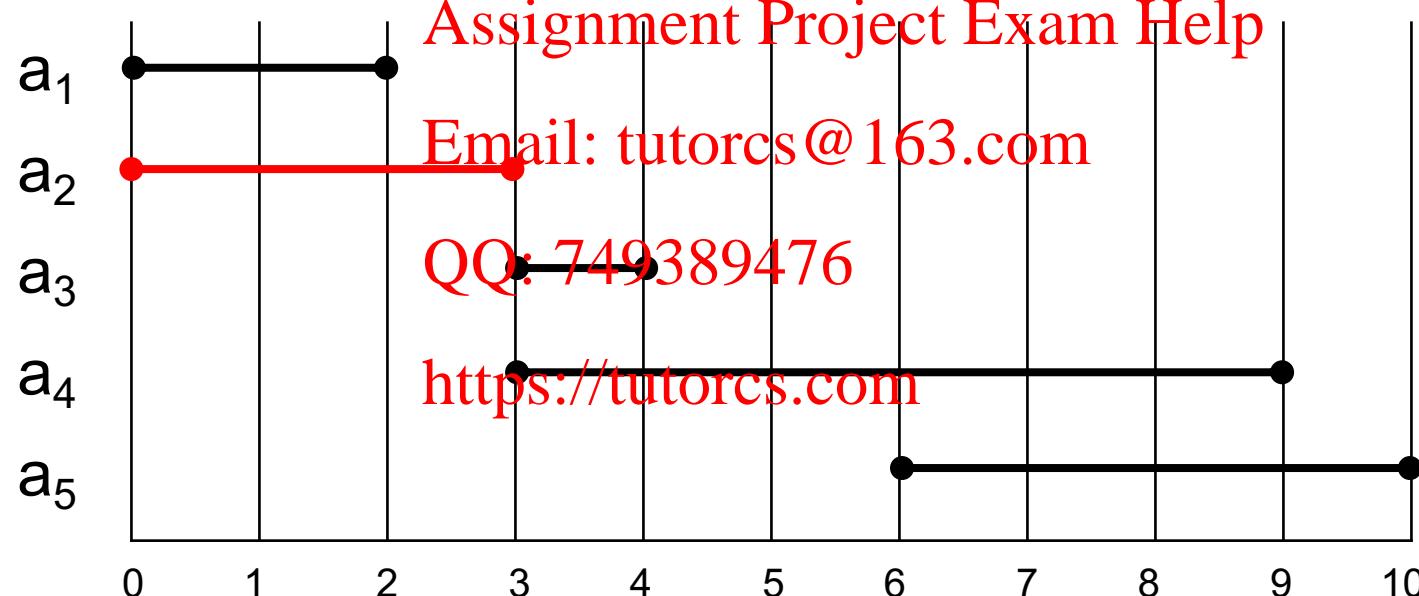
# weighted interval scheduling

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activity	1	2	3	4	5
predecessor		0	2	2	3
Best weight M		3	-	-	-
$V_j + M[p(j)]$		3	-	-	-
$M[j-1]$	0	2	-	-	-

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(1) Activities sorted by finishing time. (2) Weight equal to the length of activity.



# weighted interval scheduling

程序代写代做 CS 编程辅导

activity	1	2	3	4	5
predecessor		0	2	2	3
Best weight M	3	4	-	-	
$V_j + M[p(j)]$	3	4	-	-	
$M[j-1]$	0	2	3	-	-

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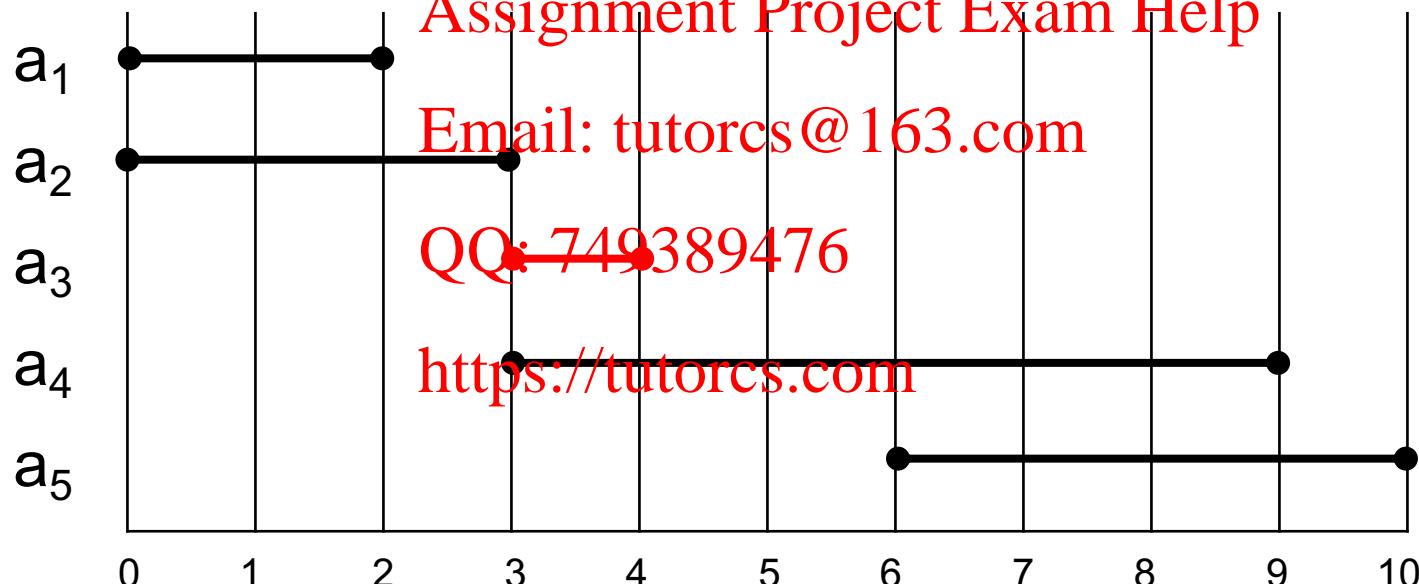
(1) Activities sorted by finishing time. (2) Weight equal to the length of activity.

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# weighted interval scheduling

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activity	1	2	3	4	5
predecessor		0	2	2	3
Best weight M		3	4	9	-
$V_j + M[p(j)]$		3	4	9	-
$M[j-1]$	0	2	3	4	-

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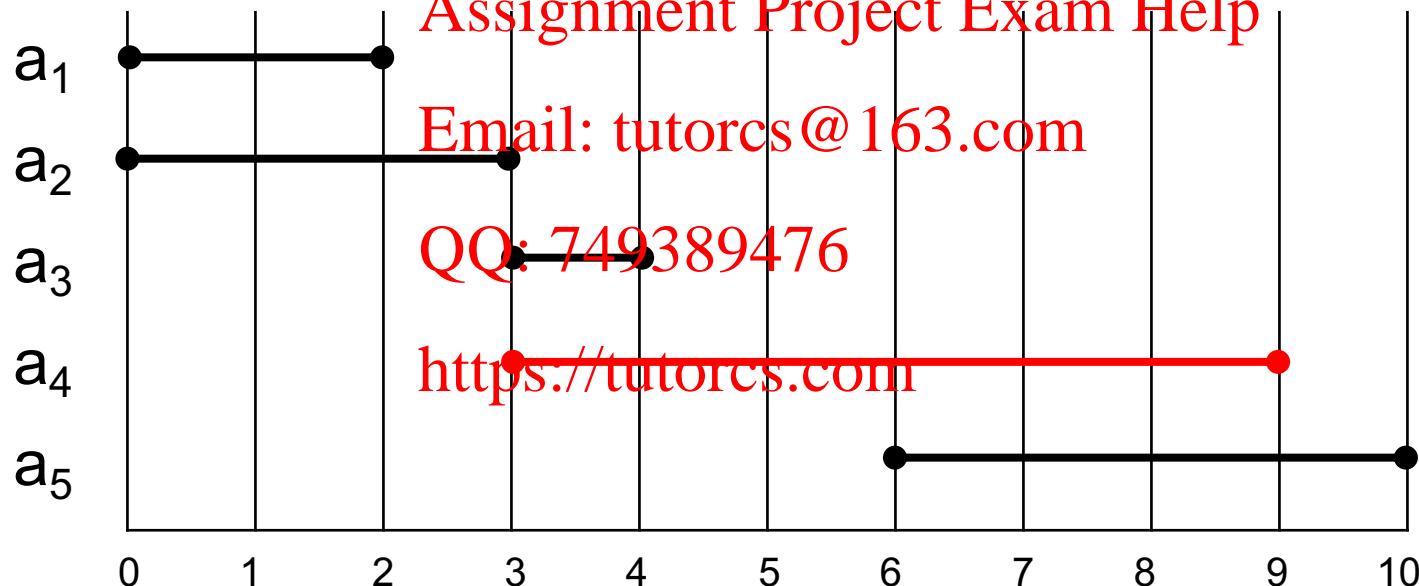
(1) Activities sorted by finishing time. (2) Weight equal to the length of activity.

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# weighted interval scheduling

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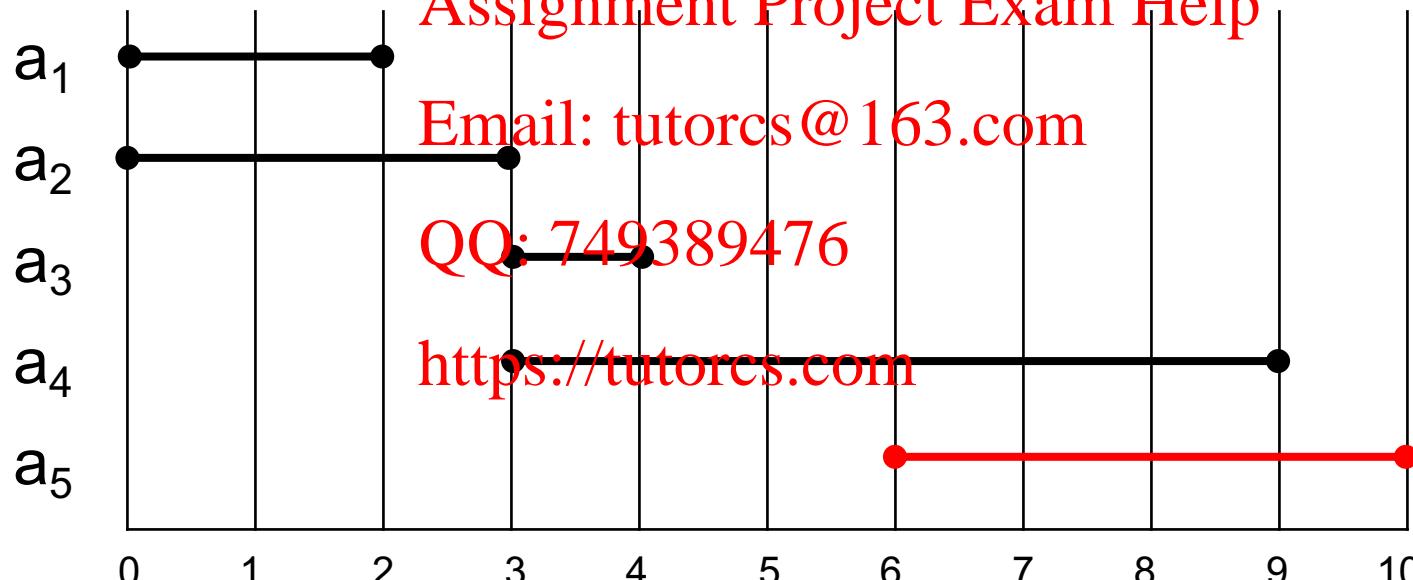
activity	1	2	3	4	5
predecessor	0	2	2	3	
Best weight M	3	4	9	9	
$V_j + M[p(j)]$	3	4	9	8	
$M[j-1]$	0	2	3	4	9

Your  
solution

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(1) Activities sorted by finishing time. (2) Weight equal to the length of activity.

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# weighted interval scheduling – finding tasks

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Dyn. Prog. algorithm computes optimal value.

Q: How to find solution?

A: Backtrack!



```
Find-Solution(j)
if j = 0
    return {}
else if (v[j] + M[p[j]] > M[j-1])
    return {j} ∪ Find-Solution(p[j])
else
    return Find-Solution(j-1).
```

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Analysis. # of recursive calls  $\leq n \Rightarrow O(n)$ .

# weighted interval scheduling - reconstruction

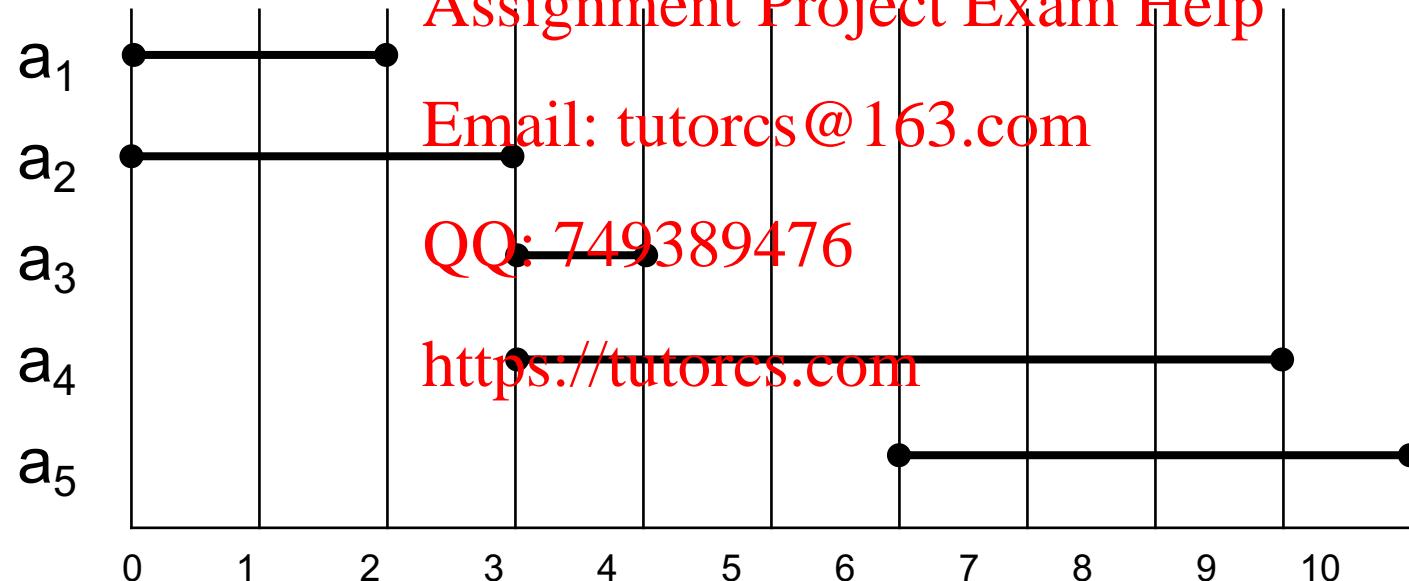
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# weighted interval scheduling - reconstruction

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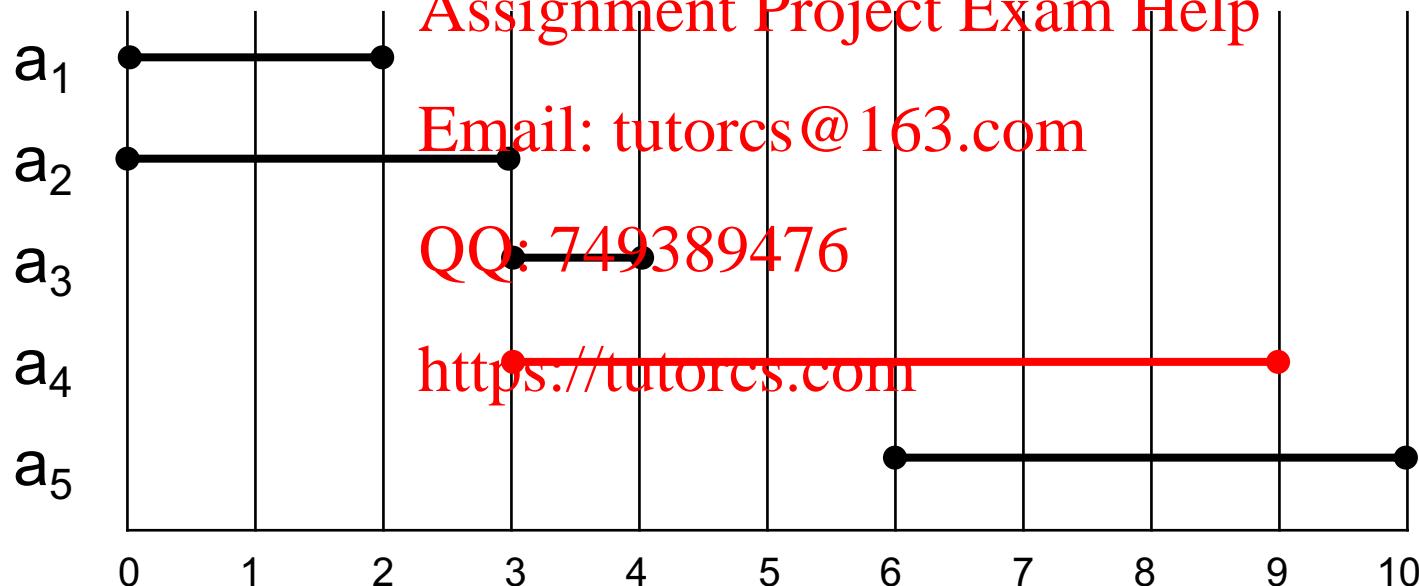
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# weighted interval scheduling - reconstruction

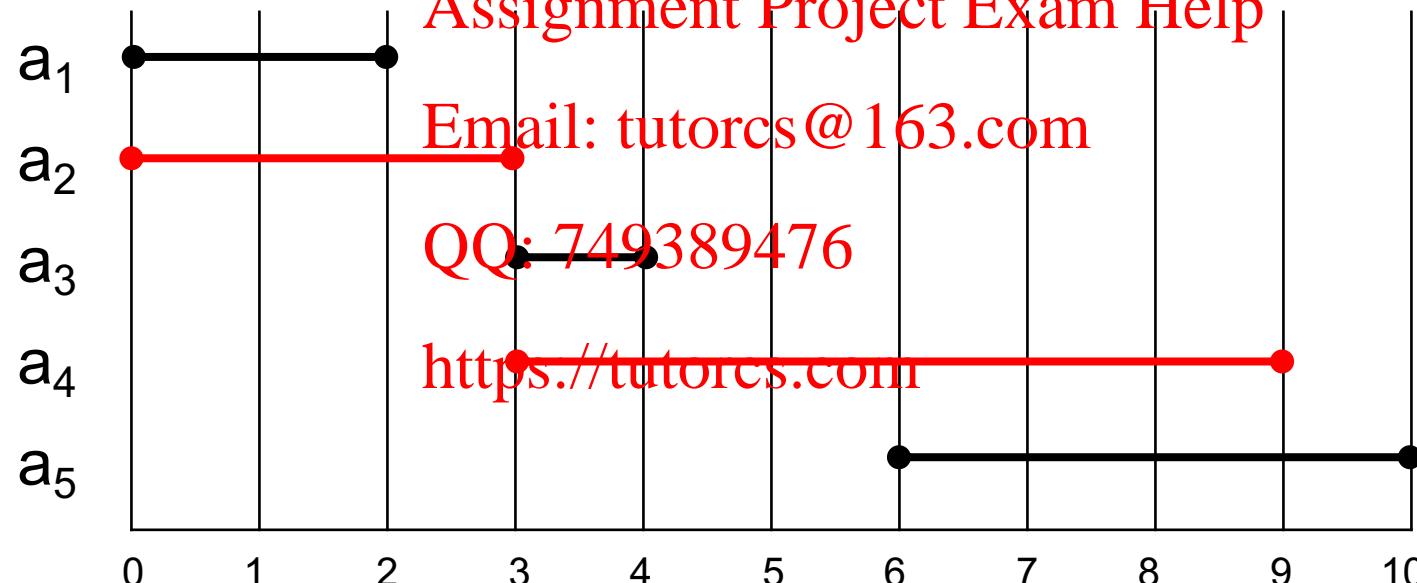
程序代写代做 CS编程辅导

activity	1	2	3	4	5
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(1) Activities sorted by finishing time. (2) Weight equal to the length of activity.

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# weighted interval scheduling – running time

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**Claim.** Memoized version of algorithm takes  $O(n \log n)$  time.

- Sort by finish time.   $\Theta(n \log n)$ .
  - Computing  $p(\cdot)$  via binary search
  - M-COMPUTE-OPT( $j$ ): each invocation takes  $O(1)$  time and either
    - (i) returns an existing value  $M[j]$
    - (ii) fills in one new entry  $M[j]$  and makes two recursive calls
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- Progress measure  $\Phi = \#$  nonempty entries of  $M[]$ .
    - initially  $\Phi = 0$ , throughout  $\Phi \leq n$ .
    - (ii) increases  $\Phi$  by 1 at most  $2n$  recursive calls.
  - Overall running time of M-COMPUTE-OPT( $n$ ) is  $O(n)$ . ■

**Remark.**  $O(n)$  if jobs are presorted by start and finish times.

# Outline

程序代写代做 CS编程辅导

- Complete Search
- Divide and Conquer
- Dynamic Programming
  - Introduction.
  - Examples.
- Greedy.



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