# COMP 251程序代写代做 CS编程辅导



Structures (Winter 2021)

Algorithm Paradigms – DP3 + Greedy

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#### Announcements 技术人员代表 CS编程辅导



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#### **Outline**

#### 程序代写代做 CS编程辅导

- Complete Search
- Divide and Conque
- Dynamic Programn
  - Introduction.
  - Examples.
- Greedy.
  - Introduction.
  - Examples.

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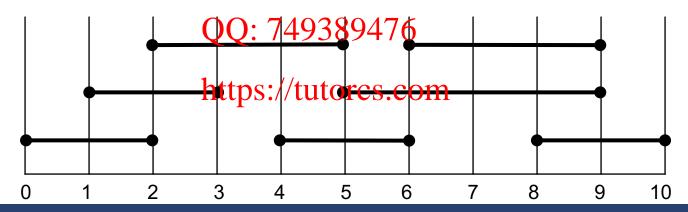
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- Input: Set S of n activities, a<sub>1</sub>, a<sub>2</sub>, ..., a<sub>n</sub>.
  - s<sub>i</sub> = start time of activ
  - f<sub>i</sub> = finish time of activition
- Output: Subset A of maximum number of compatible activities.
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  - 2 activities are compatible, if their intervals do not overlap.

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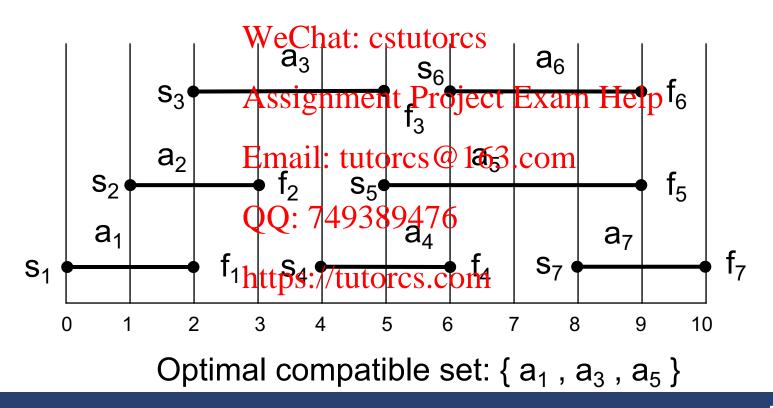
Example:

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**In the Property of the Proper** 



Step 1: Identify the in words).

Step 1.1: Identify the pc 1.1 problems.

Let  $S_{ii}$  = subset of activities in S that start after  $a_i$  finishes and finish before a<sub>i</sub> starts.

S. WeChat: cstutorcs
$$S_{ij} = \left\{ a_k \in S : \forall i, j \quad f_i \leq s_k < f_k \leq s_j \right\}$$
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- A<sub>ii</sub> = optimal solution to S<sub>ii</sub> = itutores@163\com f(i)
- $\sigma$  c[i,j] = size of A<sub>ii</sub>

$$A_{ij} = A_{ik} \cup \{a_k\} \cup A_{kj}$$

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$$c[i,j] = size of A_{ij}$$

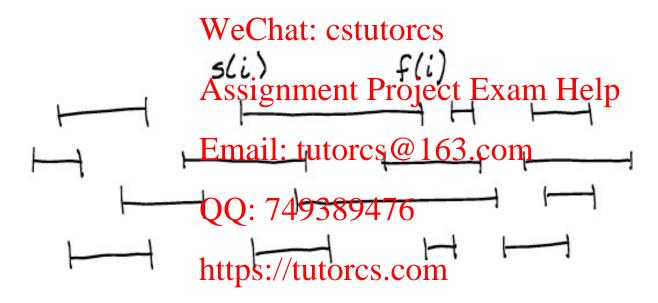
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Step 2: Find the re

Step 2.1: What decision is the step at every step?.

Which activity a<sub>k</sub> negative for the optimal set.





Step 2: Find the reason.

Step 2.1: What decisic the see at every step?.

- Which activity a<sub>k</sub> n leading for the optimal set.
  - Subproblem: Selecting the maximum to the subproblem in the subproblem.
  - Let c[i, j] = size of maximum-size subset of mutually compatible activities in  $S_{ij}$ .

$$c[i,j] = \begin{cases} & \text{Email: tutorcs@163.com} \\ & 0 & \text{if } S_{ij} = \emptyset \\ & \text{QQ: 749389476} \\ & \max\{c[i,k] + c[k,j] + 1\} & \text{if } S_{ij} \neq \emptyset \\ & \text{https://tutorcess.com} \end{cases}$$

Note: We do not know (yet) which k to use for the optimal solution.

**Step 2:** Find the recurrence.

Which activity a<sub>k</sub> ner the optimal set.

$$c[i,j] = \begin{cases} & \text{if } S_{ij} = \emptyset \\ & \max\{c[i,k] + c[k,j] + 1\} \text{ if } S_{ij} \neq \emptyset \end{cases}$$

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Step 3: Recognize and solve the base cases.

Step 4: Implement a methodology.

- We could then developed it is it is ive algorithm and memoize it, or we could work bottom-up the table entries as we go along. But we would be overlooking another important characteristic of the activity-selection problem that we can use the great advantage.
  - What if we could choose an activity to add to our optimal solution without having to first solve all the subproblems? That could save us from having to consider all the choices inherent in recurrence.
    - we need consider only one choice: the greedy choice

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#### Intuition:

- We should choose **A State** that leaves the resource available for as many other activitie **District** ble.
- Of the activities we end up choosing, one of them must be the first one to finish.
- Choose the activity in significant the English of the English of





#### Theorem:

Let  $S_{ij} \neq \emptyset$ , and let  $a_i \neq \emptyset$  activity in  $S_{ij}$  with the earliest finish time  $f_m = \min\{\{i,j\}, i,j\}$ . Then:

- 1.  $a_m$  is used in some maximum-size subset of mutually compatible activities to  $a_m$  is used in some maximum-size subset of mutually
- 2.  $S_{im} = \emptyset$ , so that choosing  $a_m$  leaves  $S_{mj}$  as the only nonempty subproblem.



#### **Proof:**

- (1)  $a_m$  is used in sor mutually compatible activities  $a_m$  mum-size subset of mutually
- Let A<sub>ij</sub> be a maximum-size subset of mutually compatible activities in S<sub>ij</sub> (i.e. Var bottimal solution of S<sub>ij</sub>).
- Order activities in Agin monotonically increasing order of finish time, and let ak be the first activity in Aii.
- If  $a_k = a_m \Rightarrow done$ . Email: tutorcs@163.com
- Otherwise, let A'iQQAi748389476 a<sub>m</sub> }
- A'<sub>ij</sub> is valid because a finishes before a<sub>k</sub>
- Since |A<sub>ij</sub>|=|A'<sub>ij</sub>| and Ā<sub>ij</sub> maximal ⇒ A'<sub>ij</sub> maximal too.

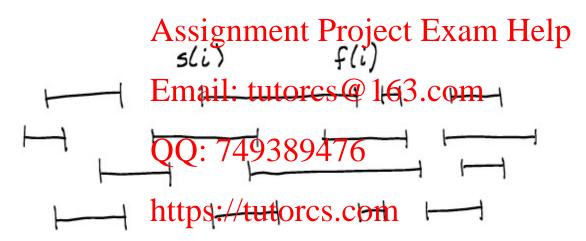
#### **Proof:**

(2)  $S_{im} = \emptyset$ , so that chest subproblem.



 $\mathbf{S}_{m}$  leaves  $S_{mj}$  as the only nonempty

If there is  $a_k \in S_{im}$  then  $f_i \le s_k < f_k \le s_m < f_m \Rightarrow f_k < f_m$  which contradicts the hypothesis  $t_m = s_m < s_m <$ 





# subproblems in optimal solution # choices to consider

e theorem	After theorem
<b>1</b> 2	1
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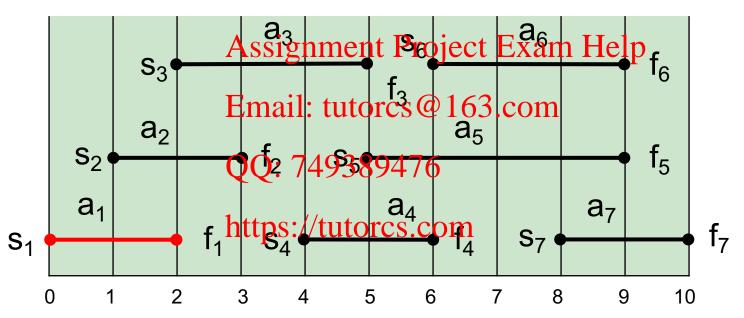
 $A_{ij} = A_{ik} \cup \{a_k\} \cup A_{kj}$   $A_{ij} = \{a_m\} \cup A_{mj}$ Email: tutorcs@163.com

We can now solve the problem, and top-down:

- Choose  $a_m \in S_{ij}$  with the earliest finish time (greedy choice).
- Solve  $S_{mi}$ .

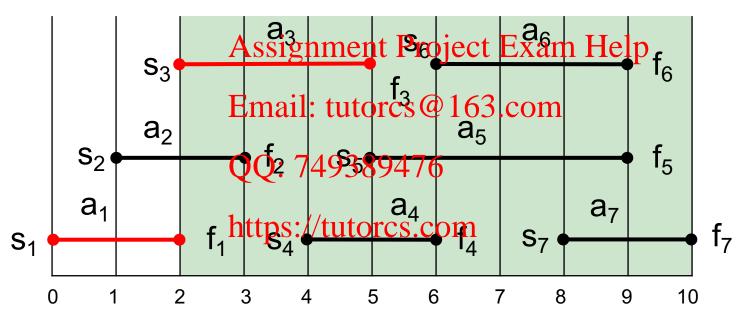
i	1	4	5	6	7
Si	0	4	5	6	8
fi	2	6	9	9	10

Activities sorted by finishing time.



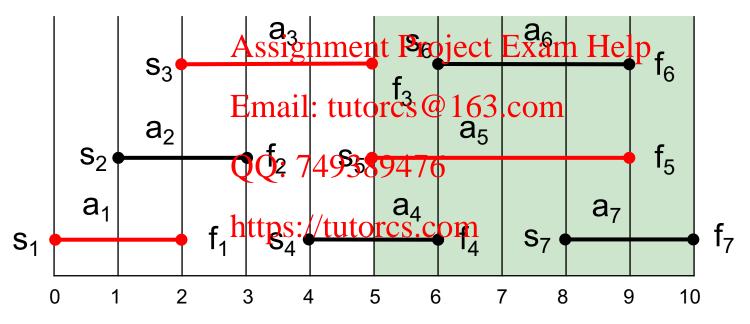
i	1	4	5	6	7
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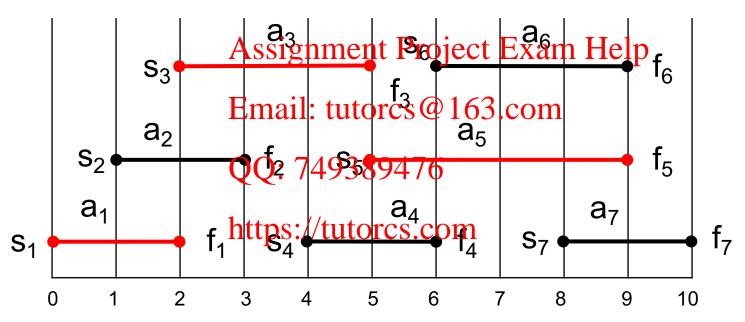
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Activities sorted by finishing time.



```
Recursive-
                                                                                                                                                                                했;Selector (s, f, i, n)
                                                                                                                                                                                           rac{1}{2} = \frac{1}{2} rac{1}{2} rac{
                                                               do m ← m+1
                          if m \le n WeChat: cstutorcs
                                                               then returnment Project Exam Help
                                                                                                                      Recursive-Activity-Selector(s, f, m, n)
                                                               else retmails tutorcs@163.com
                                                                                                                           <del>00: 749389476</del>
```

Initial Call: Recursive-Activity-Selector (s, f, 0, n+1) Complexity: ⊕(n) https://tutorcs.com

Note 1: We assume activities are already ordered by finishing time. Note 2: Straightforward to convert the algorithm to an iterative one.

```
\mathbb{T}VITY-SELECTOR (s, f)
forwechat: testutores
  \inf s[m] \ge f[k]
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  Email: tutores@163.com
return A
  QQ: 749389476
```

Note 1: We assume activities where the ordered by finishing time.

Note 2: Straightforward to convert the algorithm to an iterative one.

- Greedy template. Consider jobs in some natural order.
- Take each job provies compatible with the ones already taken.
- [Earliest start time] Consider jobs in ascending order of s<sub>i</sub>.

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- Greedy template. Consider jobs in some natural order.
- Take each job proving compatible with the ones already taken.
- [Shortest interval] Jobs in ascending order of f<sub>i</sub>—s<sub>i</sub>.

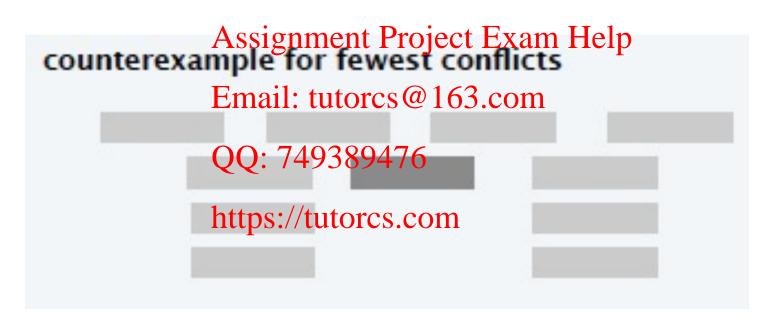
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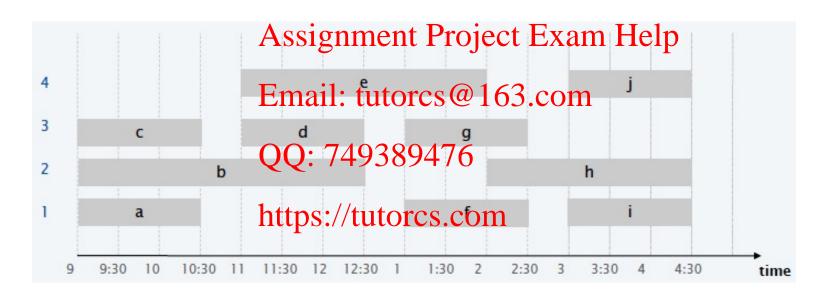
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- Greedy template. Consider jobs in some natural order.
- Take each job proving compatible with the ones already taken.
- [Fewest conflicts] For each job j, count the number of conflicting jobs c<sub>i</sub>. Spherite in a seeding order of c<sub>i</sub>.



#### Problem:

- Lecture j starts at sj a les at fj.
- Goal: find minimum representations to schedule all lectures so that no two lectures ( same time in the same room.
- Ex. This schedule uses 4 classrooms to schedule 10 lectures. WeChat: cstutorcs



#### Problem:

- Lecture j starts at sj a les at fj.
- Goal: find minimum representations to schedule all lectures so that no two lectures ( same time in the same room.
- Ex. This schedule uses 3 classrooms to schedule 10 lectures. WeChat: cstutorcs

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- Greedy template. Consider lectures in some natural order.
- Assign each lecture a vailable classroom (which one?); allocate a new classification and are available.
- [Earliest finish time] Consider lectures in ascending order of f<sub>j</sub>. (solution of the previous lexample) cs

# Assignment Project Exam Help counterexample for earliest finish time Email: tutorcs@163.com QQ: 749389476 https://tutorcs.com

- Greedy template. Censider lectures in some natural order.
- Assign each lecture vailable classroom (which one?); allocate a new classical none are available.
- [Shortest interval] Consider lectures in ascending order of f<sub>j</sub> S<sub>j</sub>. WeChat: cstutorcs

coun	Assignment Project Exam Help  terexample for shortest interval Email: tutorcs@163.com
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1	https://tutorcs.com

- Greedy template. Consider lectures in some natural order.
- Assign each lecture vailable classroom (which one?); allocate a new classical none are available.
- [Fewest conflicts] For each lecture j, count the number of conflicting lectures of chadulations conflicting order of ci.

- Greedy template. Cansider lectures in some natural order.
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- [Earliest start time] Consider lectures in ascending order of si.

```
EARLIEST STARC THAT FIRST (1, st, Q2, C.S, s_n, f_1, f_2, ..., f_n)

SORT lectures by start time so that s_1 \le s_2 \le E \times s_n. Help d \leftarrow 0 Assignment Project Exam Help

FOR j = 1 To n ail: tutores @ 163.com

If lecture j is compatible with some classroom

Schedule lecture j in any such classroom k.

ELSE

Allocate a new classroom d + 1.

Interest of allocated classroom d + 1.

Schedule lecture j in classroom d + 1.

d \leftarrow d + 1

RETURN schedule.
```

## Greedy— Definitions 程序代写代做 CS编程辅导

Kleinberg and Tardos: "... builds up a solution in small steps, choosing a decision at each step myo little ort sighted) to optimize some underlying criterion."

Cormen, Leiserson, Rivest makes the choice that looks best in the moment... it makes a locally optimal choice in the hope that the choice will lead to a globally optimal solution at: cstutores

Levitin: ".. choice must be (1) feasible i e satisfy the problem constraints, (2) the best local choice among all feasible choices available at that step, and (3) irrevocable". Email: tutorcs@163.com

Hackerearth "...If we make a choice that seems best at the moment and solve the remaining subproblems later, we still reach optimal solution. We never have to reconsider pur previous choices".

#### Greedy-Typical Steps

- Cast the optimization problem as one in which we make a choice and are left subproblem to solve.
- Prove that there is a prove that the prove that there is a prove that the prove the prove that the prove that the prove that the prove the prove
- Show that greedy choice and optimal solution to subproblem ⇒ optimal solution to the problem.
- Make the greedy choice and solve top-down.
- You may have to preprodest imput to put into greedy order (e.g. sorting activities by finish time).

#### Greedy– Elements

No general way to gen

- Greedy-choice P
   □
  - We can build a globally optimal solution by making a locally optimal (greedy) choice. WeChat: cstutorcs
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