

Prove that each of the following problems is NP-hard.

- 1 Given an undirected graph G , does G contain a simple path that visits all but 374 vertices?
- 2 Given an undirected graph G , does G have a spanning tree with at most 374 leaves?
- 3 Recall that a 5-coloring of a graph G is a function that assigns each vertex of G a “color” from the set $\{0, 1, 2, 3, 4\}$, such that for any edge uv , vertices u and v are assigned different “colors”. A 5-coloring is *careful* if the colors assigned to adjacent vertices are not only distinct, but differ by more than 1 (mod 5). Prove that deciding whether a given graph has a careful 5-coloring is NP-hard. (**Hint:** Reduce from the standard 5COLOR problem.)

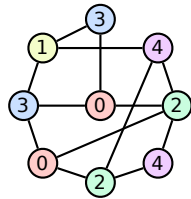


Figure 1: A careful 5-coloring.

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