## CS/ECE 374 A (Spring 2022) Homework 3 (due Feb 10 Thursday at 10am)

**Instructions:** As in previous homeworks.

**Problem 3.1:** For each of the following languages in parts (a), (b), and (c), describe an NFA that accepts the language, using as few states as you can. Provide a short explanation of your solution. Below,  $\#_0(x)$  and  $\#_1(x)$  denote the number of 0's and the number of 1's in x respectively.

- (a) (30 pts) all strings  $x \in \{0,1\}^*$  such that (x ends with 10101 or 11011) and  $(\#_0(x))$  is divisible by 3 or  $\#_1(x)$  is divisible by 3).
- (b) (30 pts) the language defined by the regular expression  $(((01)^*0+2)(100)^*1)^* \cdot (1^*+0^*2^*)$ over the alphabet  $\{0, 1, 2\}$ .
- (c) (10 pts) all strings in  $\{0,1\}^*$  that contains the pattern 0?1?0, where "?" denotes "don't care" (i.e., a single symbol that is either 0 or 1); in other words, the language defined by the regular expression  $(0+1)^* \cdot 0(0+1)1(0+1)0 \cdot (0+1)^*$ .
- (d) (3Aps Construction). [Note: don't include unreachable states; also, several accepting states can be collapsed into one in this DFA.]

https://tutorcs.com Problem 3.2: Given a language L over the alphabet  $\Sigma$ , define

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Prove that if L is regular, then MOVE-BACK<sub>8</sub>(L) is regular.

(For example, if  $010010100110011 \in L$ , then  $011001010010011 \in MOVE-BACK_8(L)$ .)

[Hint: given an NFA (or DFA) for L, construct an NFA for MOVE-BACK<sub>8</sub>(L). Give a formal description of your construction. Provide an explanation of how your NFA works, including the meaning of each state. A formal proof of correctness of your NFA is not required.

 $<sup>^{1}</sup>$ ...and also 0101010101010101  $\in$  MOVE-BACK<sub>8</sub>(L), and 010011010010011  $\in$  MOVE-BACK<sub>8</sub>(L), ...,  $010010100110011 \in \text{MOVE-BACK}_8(L)$ .

For a different example: MOVE-BACK<sub>8</sub> $(0^*1^*) = 0^*1^* + 0^*101^* + 0^*1001^* + 0^*10^31^* + \cdots + 0^*10^81^*$ .