Assignment Project Exam Help luring Wiachines

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"Most General" computer?

- DFA/PDAs are simple models of computation.
 - Accept only the regular (Et anguages 1 p
- Is there a kind of computer that can accept any language, or compute any function?
- Recall counting argument: WeChat: cstutorcs
 - $-\{L \mid L\subseteq \{0,1\}^*\}$ (just the set of languages) uncountably infinite
 - {P : P is a finite length computer program} is countably infinite

Most General Computer

- If not all functions are computable, which are?
- Is there a "most general" model of computer?

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- What languages can they recognize? https://tutorcs.com

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David Hilbert

- Early 1900s crisis in math foundations
 - attempts to formalize resulted in paradoxes, etc.
- 1920, Hilbierther Pogiest Fxam Help "mechanizers matthematics
- Finite axioms, inference rules turn crank, determine truth needed: axioms consistent & complete



Kurt Gödel

• German logician, at age 25 (1931) proved:

"There are true statements that can't be proved" Assignment Project Exam Help

(i.e., "no" to Hilbert)
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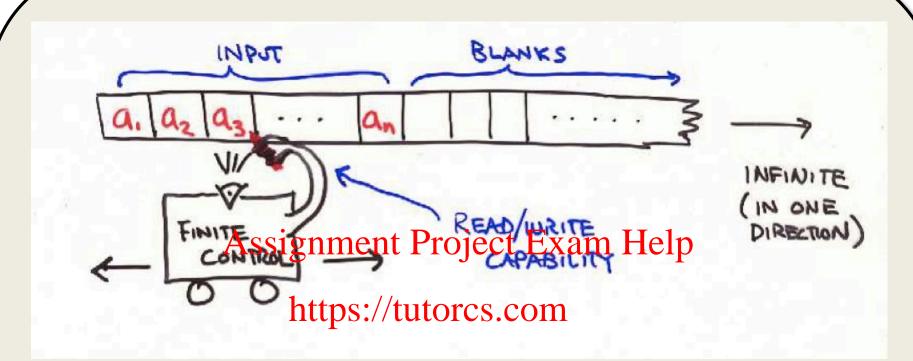
- Shook the foundations of WeChat: cstutorcs
 - mathematics
 - philosophy
 - science
 - everything



Alan Turing

- British mathematician
 - cryptanalysis during WWII
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 arguably, father of AI, Theory

 - several books, movies
- Defined "computer", "sprtogram" and (1936) at age 23 provided foundations for investigating fundamental question of what is computable, what is not computable.



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- DFA with (infinite) tape.
- One move: read, write, move, change state.

High-level Goals

- Church-Turing thesis: TMs are the most general computing devices. So far no counter example
- Every TM can be represented as a string. Think of TM as a progration of the string o
- Existence of Universal Turing Machine which is the model/inspiration for stored program computing. UTM can simulate any TM
- Implications for what can be computed and what cannot be computed

Formal Definition

 $M = (Q, \Sigma, \Gamma, \delta, q_{0}, B, q_{accept}, q_{reject})$, where:

- Q is a finite set of states
- Assignment Project Exam Help

 Σ is a finite input alphabet
- δ as defined on next page com
- Γ is a finite tape appropriate type (Σsa subset of Γ)
- q₀ is the initial state (in Q)
- B in $\Gamma \Sigma$ is the blank symbol
- q_{accept}, q_{reject} are unique accept, reject states in Q

Transition Function

$$\delta: Q \times \Gamma \to Q \times \Gamma \times \{L, R, S\}$$

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current symbol new symbol direction to state scanned latages://tuterweiteom move on tape

$$\delta(q,a) = (p,b,L)$$
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from state q, on reading a:

go to state *p*write *b*move head Left

Graphical Representation

$$\delta(q,a) = (p, b, L)$$

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a/b, L https://tutorcs.com

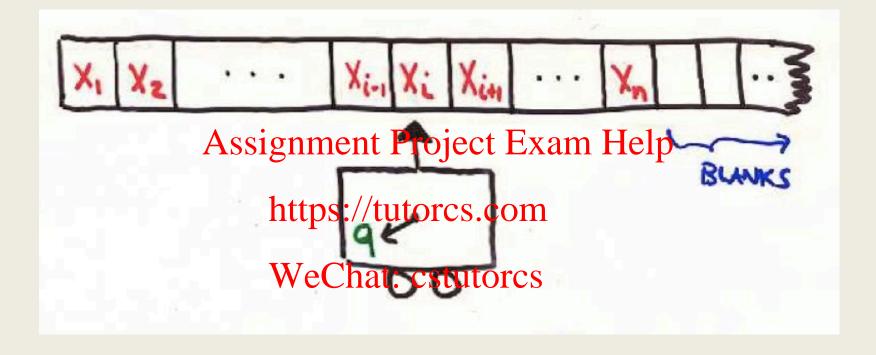
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Note: we allow $\delta(q,a)$ to be undefined for some choices of q, a (in which case, M "crashes")

ID: Instantaneous Description

- Contains all necessary information to capture "state of the computation" Assignment Project Exam Help
- Includes
 - state q of M
 https://tutorcs.com
 - location of reachwritesheldes
 - contents of tape from left edge to rightmost nonblank (or to head, whichever is rightmost)

ID: Instantaneous Description



ID: $X_1X_2...X_{i-1} q X_iX_{i+1}...X_n$ (q in Q, X_i in Γ)

Relation "→" on IDs

If
$$\delta(q, X_i) = (p, Y, L)$$
, then

$$X_1X_2...X_{i-1} q X_iX_{i+1}...X_n \rightarrow X_1X_2...X_{i-2} p X_{i-1} Y X_{i+1}$$

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current ID

next ID

If $\delta(q,X_i)$ is undefined, then there is no next ID If M tries to move off left edge, there is no next ID (in both cases, the machine "crashes")

Capturing many moves...

Define \rightarrow^* as the reflexive, transitive closure of \rightarrow

Thus, ID → ADISTINATION, Where the Among the ID, necessarily reached breakly reached by the reached

Initial ID: q_0w (more often, assume ... $\$q_0w$)

Accepting ID: $\alpha_1 q_{accept} \alpha_2$ for any α_1 , α_2 in Γ^*

(reaches the accepting state with any random junk left on the tape)

Definition of Acceptance

M accepts *w* iff for some α_1, α_2 in Γ^* ,

 $q_0 w \rightarrow^* \alpha_1 q_{accept} \alpha_2$ Assignment Project Exam Help

M accepts if at any time it enters the accept state

Regardless of whether or not WeChat: cstutorcs it has scanned all of the input

it has moved back and forth many times

it has completely erased or replaced w on the tape

$$L(M) = \{w \mid M \ accepts \ w\}$$

Non-accepting computation

M doesn't accept w if any of the following occur:

- M enters q_{reject}
- M moves off felt edge of tape
- M has no applicable utext stransition
- M continues computing farever

If M accepts – we can tell: it enters q_{accept} If M doesn't accept – we may not be able to tell

(c.f. "Halting problem" – later)

"Recursive" vs "Recursively Enumerable"

Recursively Enumerable (r.e.) Languages:
 = {L | there is a TM M such that L(M) = L}

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• Recursive Languages (also called "decidable")
= \{L \mid \text{there is a } \frac{\text{https://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://thtp://t
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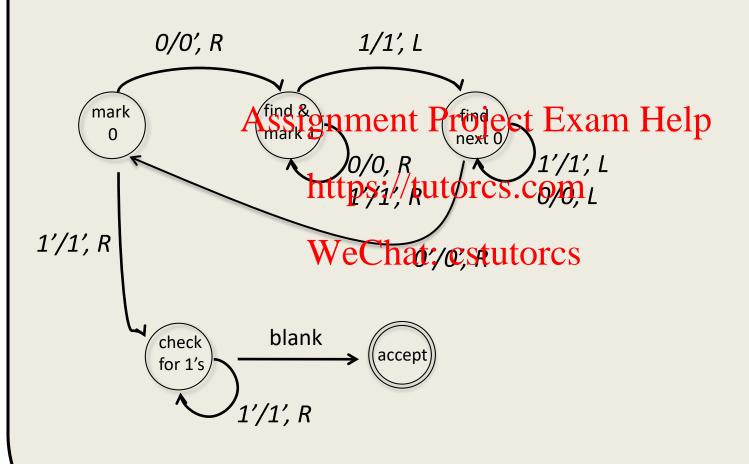
Recursive languages: nice; run M on w and it will eventually enter either q_{accept} or q_{reject}

R.E. languages: not so nice; can know if w in L, but not necessarily if w is not in L.

Fundamental Questions

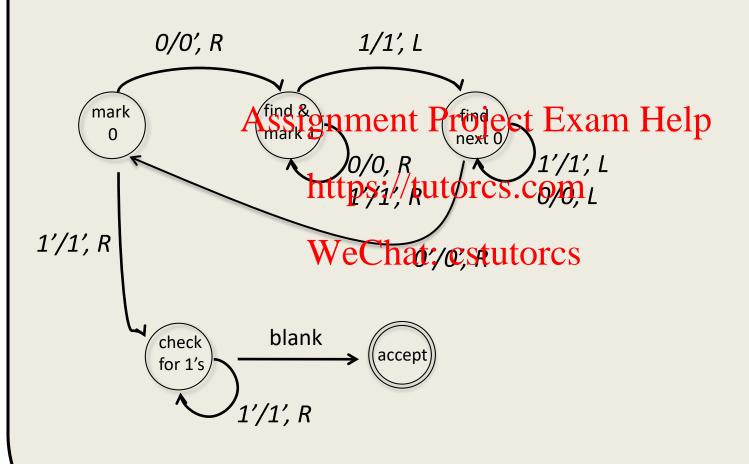
- Which languages are R.E.?
- Which are recursive?
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- What is the difference? https://tutorcs.com
- What properties make a language decidable? WeChat: cstutorcs

Machine accepting $\{0^n1^n \mid n \ge 1\}$



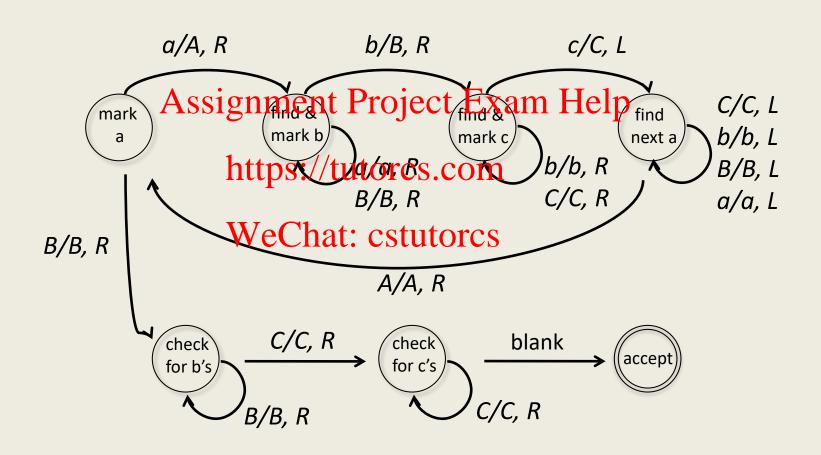
(This technique is known as "checking off symbols")

Machine accepting $\{0^n1^n \mid n \ge 1\}$



(This technique is known as "checking off symbols")

Machine accepting $\{a^nb^nc^n \mid n \geq 1\}$



(This technique is known as "checking off symbols")

Machine to add two n-bit numbers

("high-level" description)

- Assume input is $a_1a_2...a_n#b_1b_2...b_n$
- Pre-process phase Assignment Project Exam Help
 - sweep right, replacing 0 with 0' and 1 with 1'
 https://tutorcs.com
- Main loop:
 - erase last bit b_i , and remember it
 - move left to corresponding bit a_i
 - add the bits, plus carry, overwrite a_i with answer
 - remember carry, move right to next (last) bit b_{i-1}

Program Trace (some missing steps)

```
$10011#11001
                                       $1'0'0'1'0#1'1'0'0'
$1'0'0'1'1'#1'1'0'0'1'
                                      $1'0'0'1'0#1'1'0'0'
                             b = 1
$1'0'0'1'1'#1'1'0'0'<u>1'</u>
                                       $1'0'0'1'0#1'1'0'0'
$1'0'0'1'1'#1'A'\0'0'\0'ment Proje\1'10\0\11'\1'0'0'
$1'0'0'1'1'#1'1'<u>0'0'</u>
https://tutorcs.com
                                                                    b = 0
$1'0'0'1'1'#1'<u>1'</u>0'0'
                                      $1'0'0'1'0#1'1'0'
                      WeChat: cstutorcs
$1'0'0'1'<mark>0</mark>#1'<u>1'</u>0'
                                                                    c = 1
$1'0'0'1'1'#<u>1'</u>1'0'0
                                       $1'0'0'1'<mark>0</mark>#1'1'0'
$1'0'0'1'1'#1'1'0'0'
                                       $1'0'0'1'<mark>0</mark>#1'1'0'
$1'0'0'1'1"#1'1'0'0'
                                       $1'0'0'<u>0</u>0#1'1'0'
$1'0'0'1'0#1'1'0'0'
                                                                   c = 1
                           c = 1
                                        $1'0'0'<mark>00</mark>#1'1'0'
                                                                 etc
```

Some TM programming tricks

- checking off symbols
- shifting over Assignment Project Exam Help
- using finite control memory https://tutorcs.com
- subroutine calls

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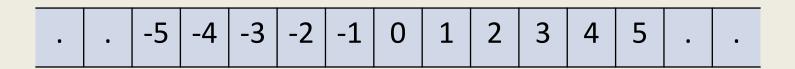
"Extensions" of TMs

- 2-way infinite tape
- multiple tracks
- multiple tapsesnment Project Exam Help
- multi-dimensional/TMs.com
- nondeterministic TMs
- --- bells & whistles cstutores

Goal:

Convince you of the power of the basic model

"Extensions" of TMs: 2-way infinite tape



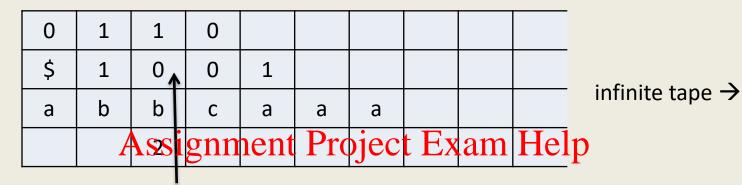
Simulate with any infinite tane Help

Must modify transitions appropriately

- remember in finite control if negative or positive
- if positive, $R \rightarrow RR$; $L \rightarrow LL$
- if negative, $R \rightarrow LL$; $L \rightarrow RR$
- must mark left edge & deal with 0 cell differently

Extension: multiple tracks

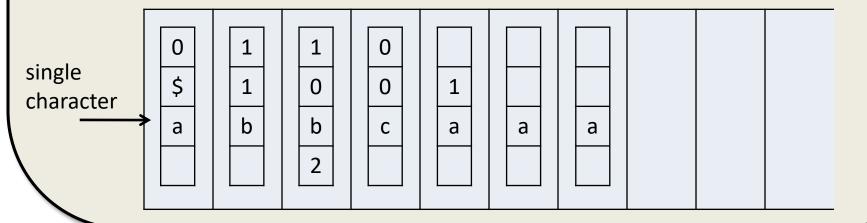
4 tracks



M can address any particular tracking the fell it is scanning

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Can simulate 4 tracks with a single track machine, using extra "stacked" characters:



Multiple tracks

4 tracks

0	1	1	0						
\$	1	0	0	1					
а	b	b	С	а	а	а			
		155	gnn	nent	Pro	niec	t Ex	am	Hel

infinite tape →

M: $\delta(q, -10\text{ttp}) = /(\text{nutore} \cdot 1.00) \text{m}$

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Then in M' $\delta(q,$

 $\begin{array}{c|c} x \\ \hline 0 \\ y \\ z \end{array} = (p, \begin{array}{c} x \\ \hline 0 \\ y \\ \hline 1 \end{array}$

"If in state q reading 0 on second track, then go to state p, write 1 on fourth track, and move right"

, R)

for *every* x, y, z in Γ

Extension: multiple tapes

k-tape TM

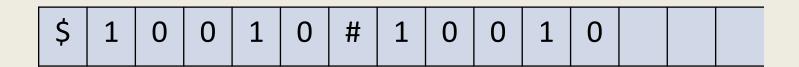
- k different (2-way infinite) tapes
 Assignment Project Exam Help
 k different independently controllable heads
- input initially on tape 1; tapes 2, 3, ..., k, blank.
- single move: WeChat: cstutorcs
 - read symbols under all heads
 - print (possibly different) symbols under heads
 - move all heads (possibly different directions)
 - go to new state

k-tape TM transition function

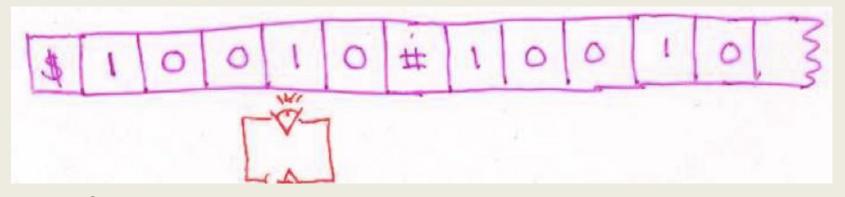
$$\delta(q,a_1, a_2, \dots a_k) = (p, b_1, b_2, \dots b_k, D_1, D_2, \dots D_k)$$
Assignment Project Exam Help
Symbols scanned on Symbols to be written Directions to be moved the k different tapes on the k different tapes (D_i is one of L, R, S)

Utility of multiplectanesstutores

makes programming a whole lot easier



is input string of form w#w?



 $\Omega(n^2)$ steps provably required xam Help



≈ 3n/2 steps easily programmed

Can't compute more with k tapes

Theorem: If L is accepted by a k-tape TM M, then L is accepted by some 1-tape TM M'. Assignment Project Exam Help

Intuition: M'usasp2k/tuacks.tomimulate M

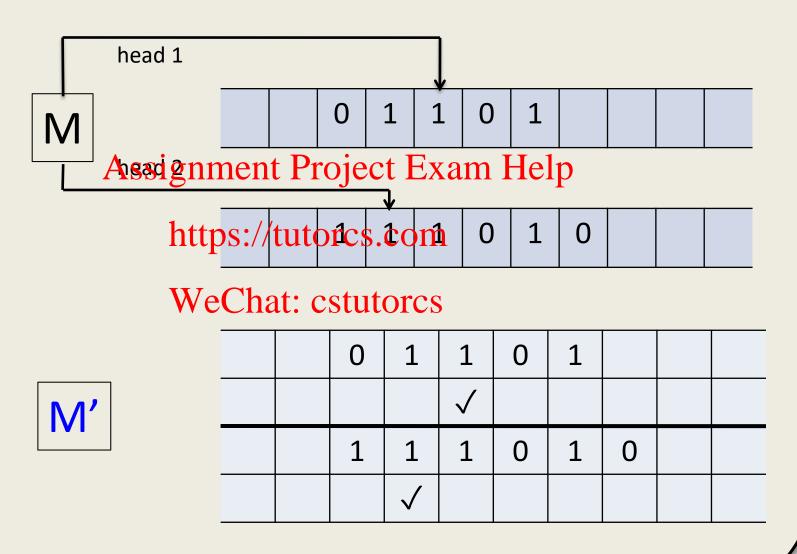


BUT....

M has k heads!

How can M' be in k places at once?

Snapshot of simulation (k = 2)



Track 2i-1 holds tape i. Track 2i holds position of head i

To make a move, M' does:

Phase 1: Sweep from leftmost edge to rightmost "\" on any track, noting symbols Assignment Project Exam Help \'ed, and what track they are on. Save this info in finite controls.com

Now, M' knows Ward hat the own of sM to make

Phase 2: Sweep from right to left edge implementing the move of M

Thus, each move of M requires M' to do a Assignment Project Exam Help complete sweep across, and back.

https://tutorcs.com

Not hard to show that if M takes t steps to complete its computation, then M' takes $O(t^2)$ steps.