

In the lecture, we have described an algorithm of Karatsuba that multiplies two n -digit integers using $O(n^{\lg 3})$ single-digit additions, subtractions, and multiplications. In this lab we will look at some extensions and applications of this algorithm.

- 1 Describe an algorithm to compute the product of an n -digit number and an m -digit number, where $m < n$, in $O(m^{\lg 3 - 1}n)$ time.
- 2 Describe an algorithm to compute the decimal representation of 2^n in $O(n^{\lg 3})$ time. (The standard algorithm that computes one digit at a time requires $\Theta(n^2)$ time.)
- 3 Describe a divide-and-conquer algorithm to compute the decimal representation of an arbitrary n -bit binary number in $O(n^{\lg 3})$ time. (**Hint:** Let $x = a \cdot 2^{n/2} + b$. Watch out for an extra log factor in the running time.)

Think about later:

- 4 Suppose we can multiply two n -digit numbers in $O(M(n))$ time. Describe an algorithm to compute the decimal representation of an arbitrary n -bit binary number in $O(M(n) \log n)$ time.

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