

CMPSC/Mathematics 451  
MATLAB Program One  
Due 26 February 2020  
Spring 2020

You are to write a MATLAB function to implement the Hager–Higham method to estimate the condition number of the matrix  $A$  in the one-norm. This is explained in the notes on Canvas and in class.

Your function should have the form

`[kappa,z,jmax]=cond1(L,U,p,A).`

Thus, here  $L$ ,  $U$ , and  $p$  are outputs from the command `[L,U,p]=lu(A,'vector')`.

Here **kappa** is the condition number  $\kappa_1(A) = \|A\|_1 \|A^{-1}\|_1$ , **z** is the vector such that  $\|z\|_\infty = 1$ ,  $\|A^{-1}z\|_\infty = \|A^{-1}\|_\infty = \|A^{-T}\|_1$ , and **jmax** is a column of the identity matrix such that  $\|A^{-1}e_{jmax}\|_1 = \|A^{-1}\|_1$ . Test your routine with the matrices generated by the m-files **matrix1.m**, **matrix2.m**, **matrix3.m** posted on Canvas in the **MATLAB codes** folder.

Your code should do no more than four iterations and it should be short. You can check your answer with the MATLAB function **cond**. The MATLAB statement `kappa1 = cond(A,1)` gives you the condition number in the one-norm. If  $A$  is well-conditioned, your value of **kappa** should be close to `kappa1`. If  $A$  is badly conditioned, they should both be very large.

A possible starting vector for **z** could be the one recommended by Higham (in the notes) or it could be the one produced from the MATLAB statements

$$\begin{aligned} f &= randn(n,1); \\ z &= f/norm(f,Inf); \end{aligned}$$

where  $n$  is the dimension of  $A$ .