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程序代写代做 CS编程辅导



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5.1 (Binary)

Arithmetic

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CSU11021 – Introduction to Computing I

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Decimal numeral system

2

We are most familiar with the decimal numeral system

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10 symbols: **0, 1, 2, 3, 4, 5, 6, 7, 8, 9**

What happens if I want to represent this number of apples?

Counting the apples ... 1, 2, 3, 4, 5, 6 ... we've run out of digits!

... but, if we write down a digit represent the count of 10s of apples

... followed by another digit representing the count of single (unit) apples

... then we can express the number of apples as **11** or $(1 \times 10^1) + (2 \times 10^0)$

This method of expressing a value is known as a “positional”

because the position of a digit corresponds to the magnitude of its contribution to the overall quantity (number of 1000s of apples, number of 100s of apples, number of 10s of apples and number of single apples)

with the rightmost digit (the least significant digit) corresponding to $10^0 (=1)$

the next rightmost digit corresponding to 10^1 , then 10^2 , then 10^3 etc.



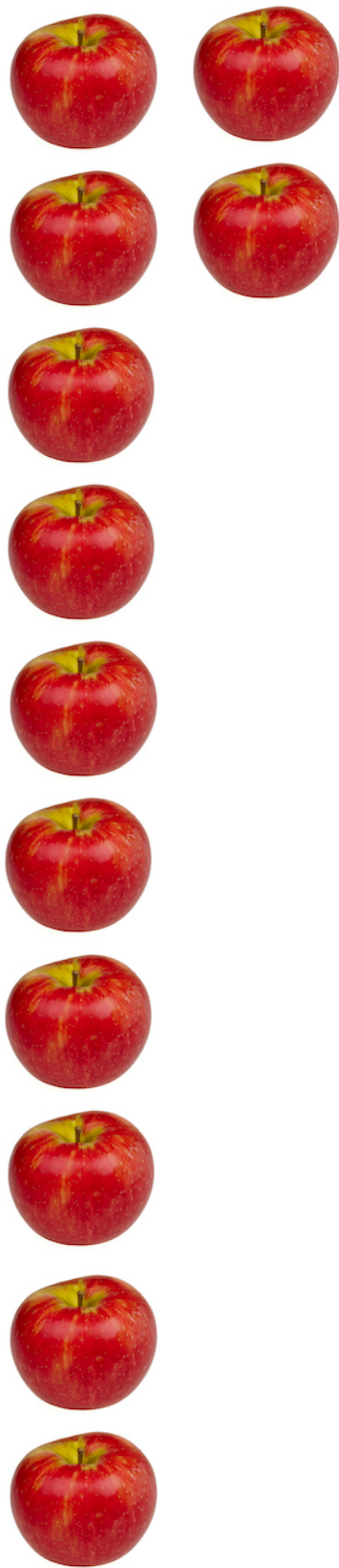
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Binary numeral system

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Binary is another positional numeral system

2 symbols: **0**, **1**

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What happens if we want to represent the same number of apples in binary?

Counting the apples ... 0, 1 ... we've used 1 digit!



... but, if we write down a digit representing the count of 2s of apples

... followed by another digit representing the count of single (unit) apples

... we can count up to 11 apples

... so we need another digit, this time representing the count of 4s of apples ($4=2^2$)

... now we can represent 111 apples

Still not enough digits!

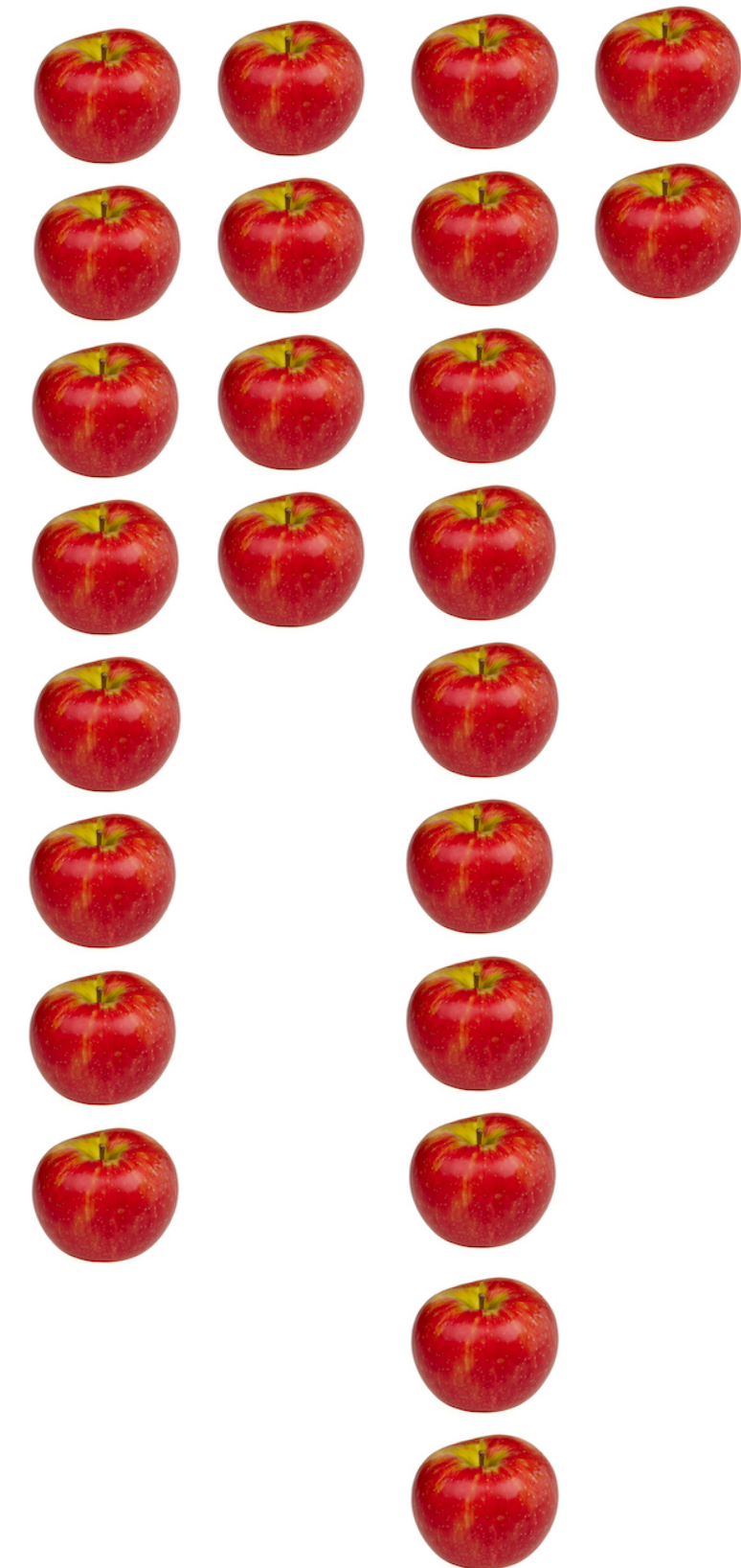
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If we follow the same pattern with one more digit, we can represent the number of apples as **1100** or $(1 \times 2^3) + (1 \times 2^2) + (0 \times 2^1) + (0 \times 2^0)$

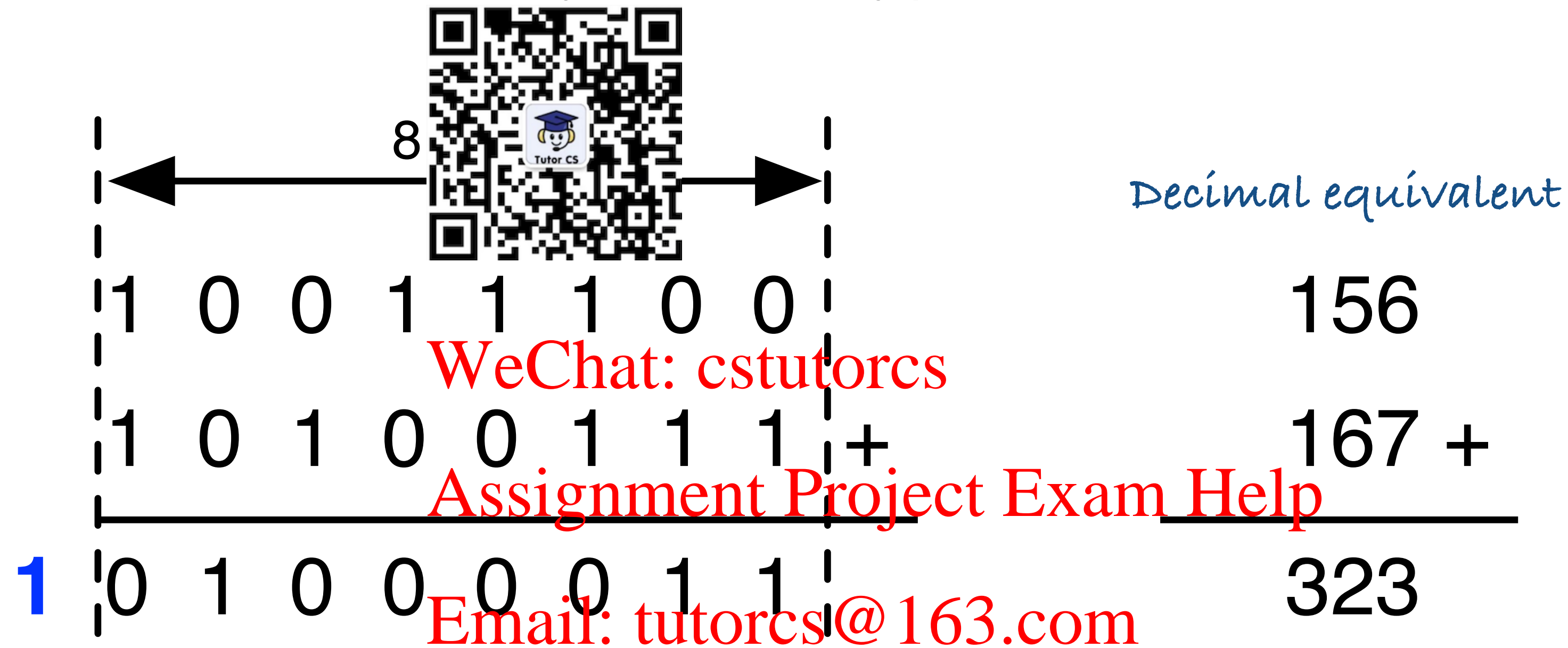
Binary 程序代写代做 CS编程辅导 Decimal equivalent

0 0 0 0 0		0		6
0 0 0 0 1		1	+	11
<hr style="border: 0.5px solid black;"/>				<hr style="border: 0.5px solid black;"/>
0 0 0 1 0		0 0 0 1		17
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0 0 0 1 0		1 1 0		22
0 0 0 0 1		0 1 1	+	11
<hr style="border: 0.5px solid black;"/>				<hr style="border: 0.5px solid black;"/>
0 0 1 0 0		0 0 0 1		33

What happens if we run out of digits?

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Adding two numbers each stored in 1 byte (8 bits) may produce a 9-bit result



Added $156_{10} + 167_{10}$ and expected to get 323_{10}

8-bit result was 01000011_2 or 67_{10}

Largest number we can represent in 8-bits is 255

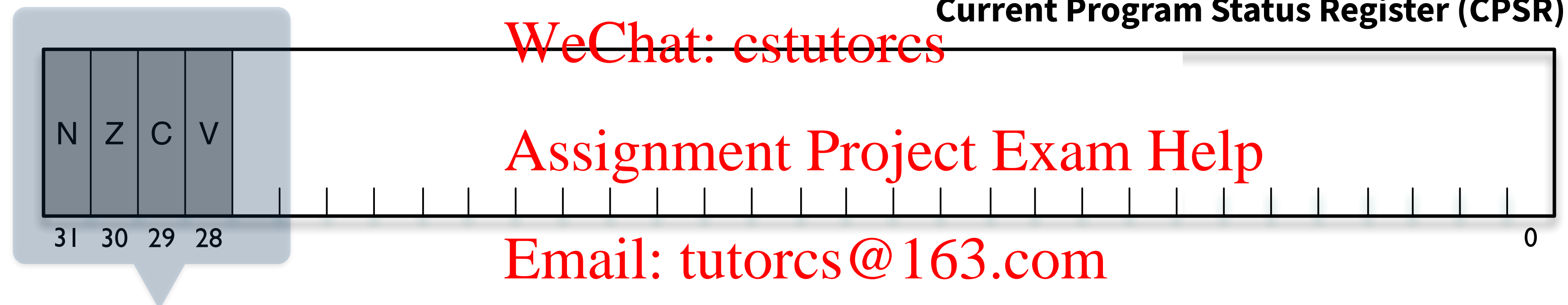
The “missing” or “left-over” 1 is called a **carry** (or **carry-out**)



8-bits just for illustration here.
Our ARM processor has 32-bit registers and performs 32-bit arithmetic so we get a carry-out if our result requires 33 bits.

Some instructions can **optionally** update the Condition Code Flags to provide information about the result of the execution of the instruction

e.g. whether the result of an operation is zero, or negative or whether a carry occurred



Condition Code Flags

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N – Negative	Z – Zero
V – oVerflow	C – Carry

The Condition Code Flags (N, Z, C, V) can be **optionally** updated to reflect the result of an instruction

S-bit in a machine code instruction is used to tell the processor whether the Condition Code Flags should be updated, based on the result

e.g. want to update Condition Code Flags during an ADD instruction

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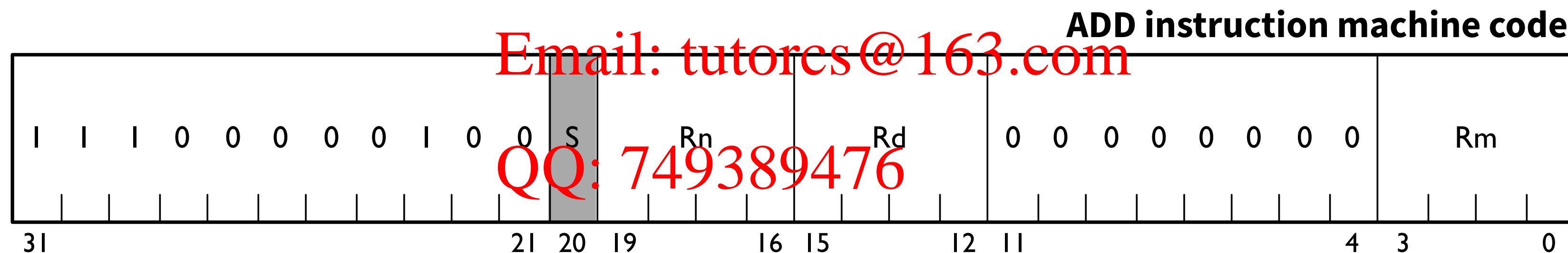
Condition Code Flags only updated if (machine code) S-bit (bit 20) is 1

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In assembly language, we cause the Condition Code Flags to be updated by appending “S” to the instruction mnemonic (e.g. ADDS, SUBS, MOVS)

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ADDS causes the Condition Code Flags to be updated

REMEMBER: 32-bit arithmetic!!

Expected result?

Does the result fit in 32-bits?

Will the carry flag be set?

Examine by running the program ...

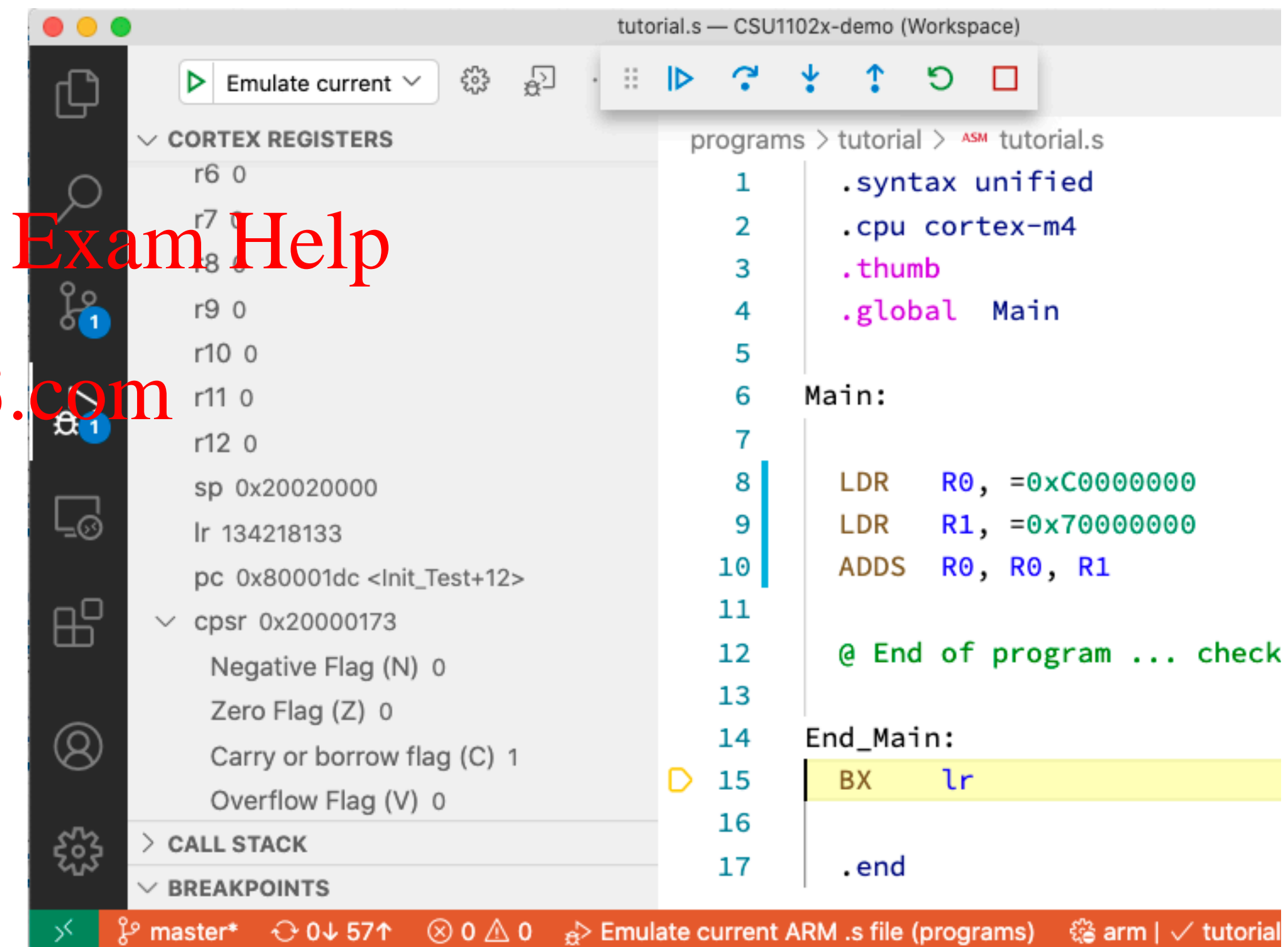
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CMP (CoMPare) instruction performs a subtraction **without storing the result of the subtraction**

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Processor remembers the results of the CMP result by **updating the Condition Code Flags**



Allows us to determine equality (=) or inequality (< ≤ ≥ >)

Don't care about absolute value of result

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(i.e. don't care **by how much** x is greater than y, only whether it is or not.)

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CMP always sets the Condition Code Flags (so no need for **CMPS**)

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```
CMP      R2, #0    @ subtract 0 from R2, ignoring result but
                @ updating the CC flags
BEQ      EndWh     @ if the result was zero then branch to EndWh
...      ...       @ otherwise (if result was not zero) then keep
                @ going (with sequential instruction path)
```

EndWh:

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BEQ – Branch if Equal

(or more precisely
branch if the Zero flag
is set)



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5.2 Negative numbers and 2s complement

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What does the binary value stored in memory at address 0xA0000138 represent?



Interpretation!

How can we represent signed values, and negative values such as -17_{10} in particular, in memory?

How can we tell whether any given value in memory represents an unsigned value, a signed value, an ASCII character or something else?

(we can't **tell** ... as programmers we have to **know**)

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address	memory
	• • •
0xA0000142	????????
0xA0000141	????????
0xA0000140	????????
0xA0000139	????????
0xA0000138	01001101
0xA0000137	????????
0xA0000136	????????
0xA0000135	????????
0xA0000134	????????
	• • •
	← 8 bits = 1 byte →



Represent signed values in the range $[-2^{31-1}, +2^{31-1}]$

Two representations of zero ($+0$ and -0)

Would need special way to handle signed arithmetic (i.e. a separate circuit)

Remember: **interpretation!** (is it -8 or 2,147,483,656?)

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A 12-hour clock is an example of modulo-12 arithmetic

If we add 4 hours to 10 o'clock we get 2 o'clock

If we subtract 4 from 2 o'clock we get 10 o'clock (not -2 o'clock!)

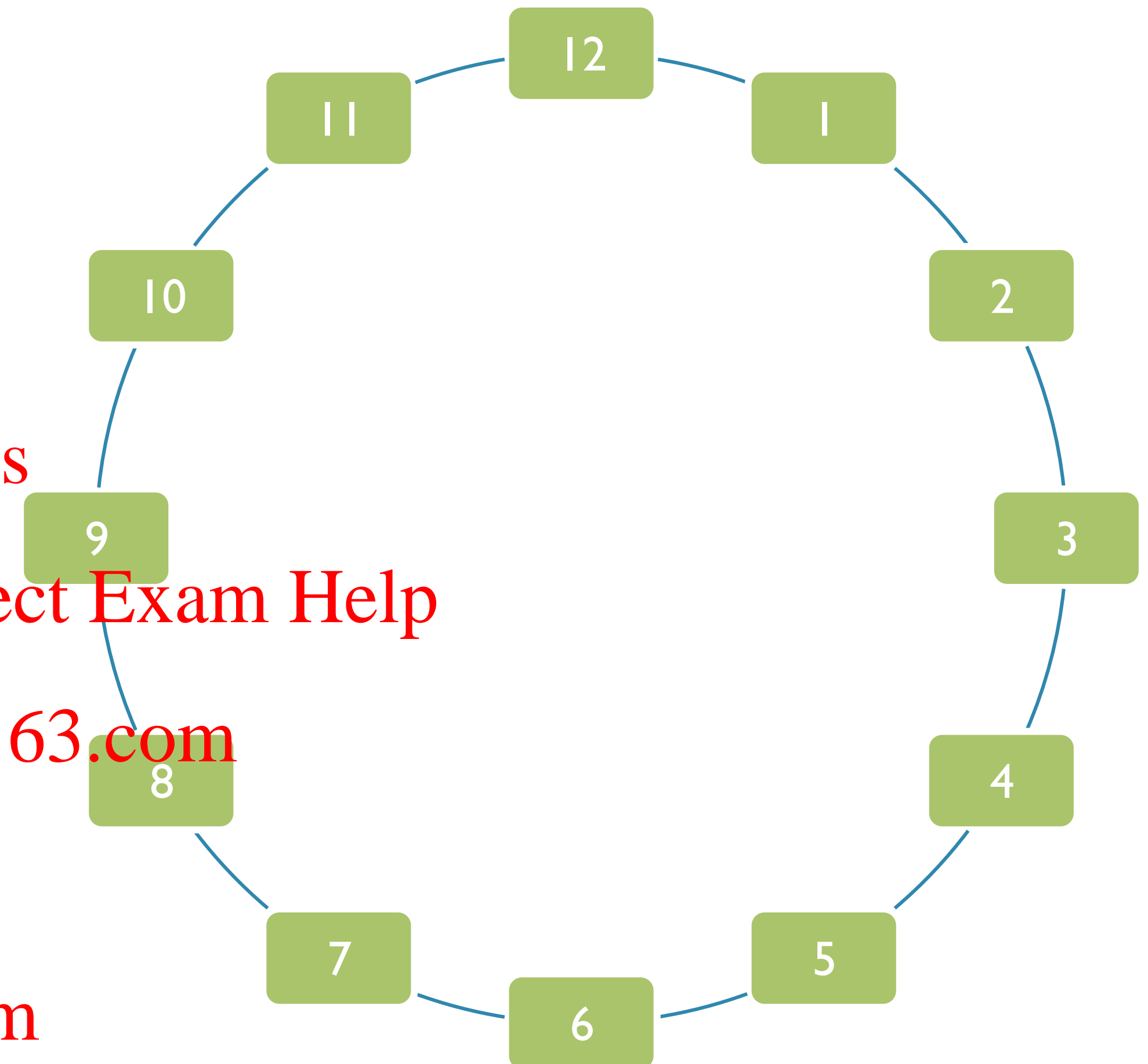
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2's Complement

14

Can represent 16 values with a 4-bit number system ($2^4 = 16$)

Ignoring carries from 4-bit addition gives us modulo-16 arithmetic (handy)

$$(15 + 1) \bmod 16 = 0$$

$$\text{and } -1 + 1 = 0$$

$$(14 + 2) \bmod 16 = 0$$

$$\text{and } -2 + 2 = 0$$

$$(14 + 4) \bmod 16 = 2$$

$$\text{and } -2 + 4 = 2$$

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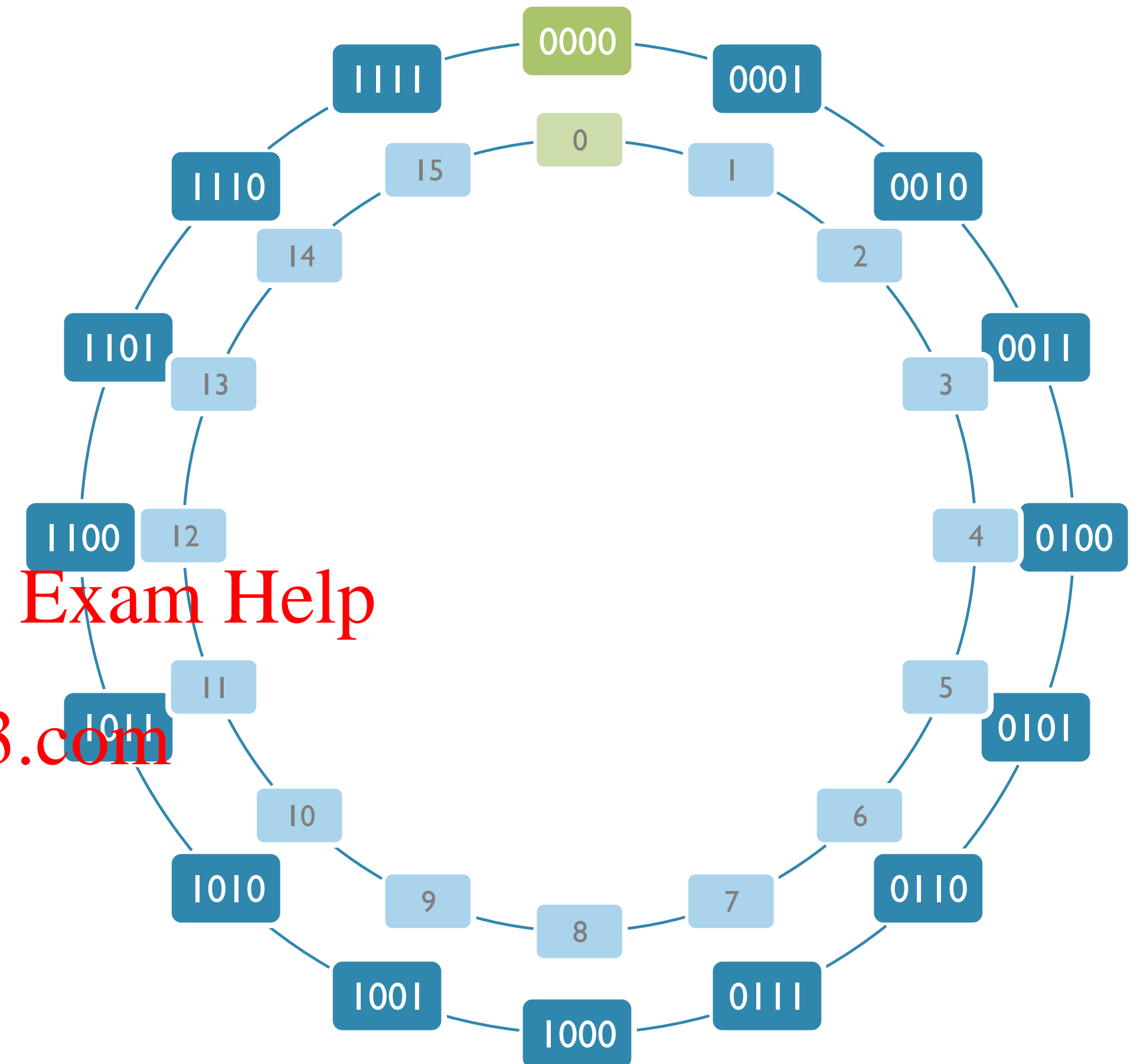
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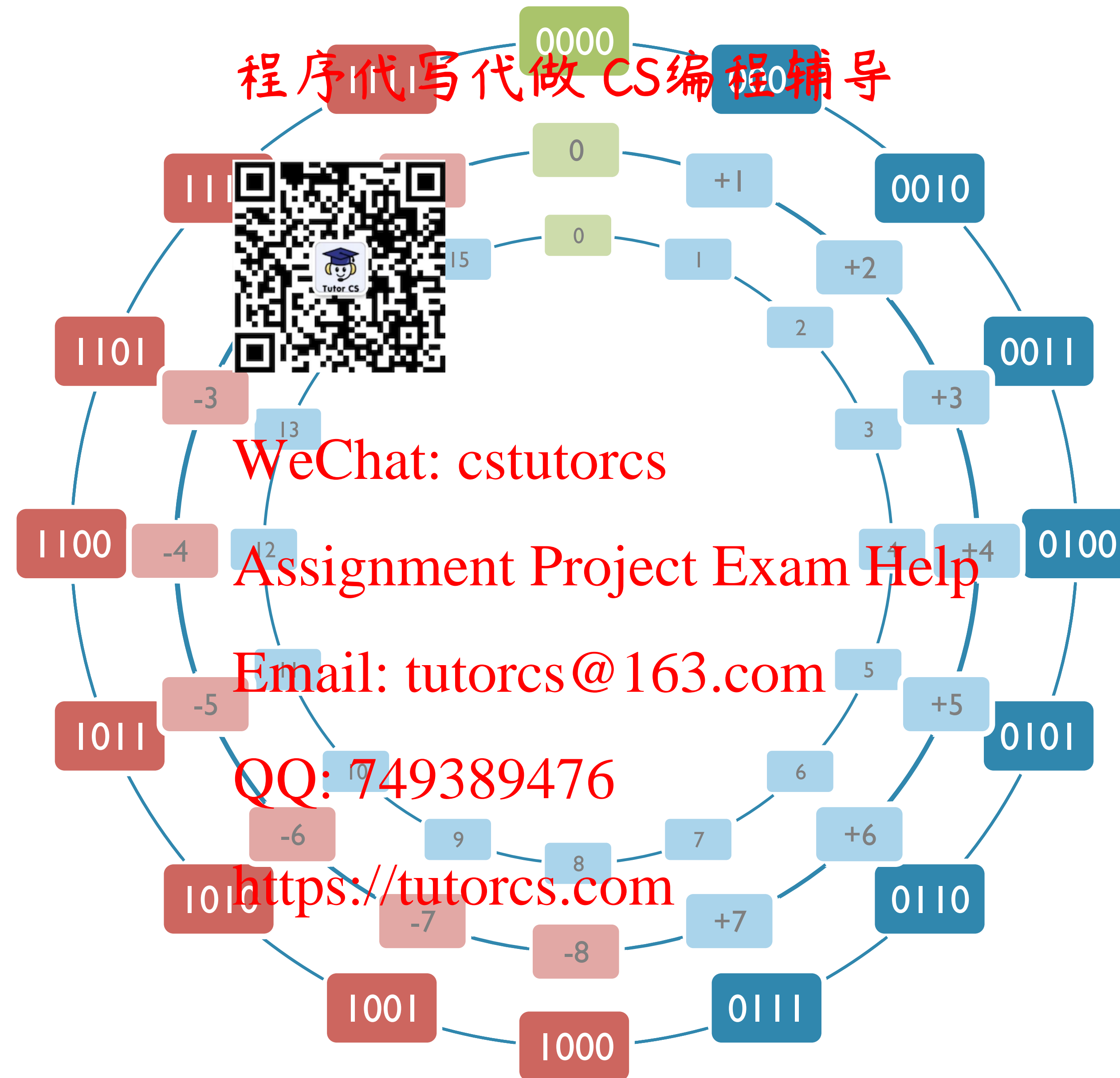
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2's Complement Examples

16

Represent -97_{10} using 2's complement

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$$97_{10} = 01100001_2$$

Inverting gives 10011110_2

Adding 1 gives 10011111_2



Again, 8-bit values for illustration only here! In practice, we'll be working with 32-bit values

Interpreted as a 2's complement signed integer

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$$10011111_2 = -97_{10}$$

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Interpreted as an unsigned integer

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$$10011111_2 = 159_{10}$$

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$$(159 + 97) \bmod 256 = 0$$

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Correct interpretation is the responsibility of the programmer, not the CPU


CPU does not “know” whether a value 10011111_2 in R0 is -97_{10} or 159_{10}

2's Complement Examples

17

Adding 01100001_2 ($+97_{10}$) and 10011111_2 (-97_{10})

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	←		→		
	0	1		0	1
	1	0		1	1
	<hr/>				+
1	0	0	0	0	0

Decimal equivalent

+97
-97 +
<hr/>
0

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Ignoring the carry bit gives us the correct result of 0

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Changing sign of $1001\ 1111_2$ (-97_{10})

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Invert bits and add 1 again

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Inverting gives 01100000_2

Adding 1 gives 01100001_2 ($+97_{10}$)

Write an Assembly Language program to change the sign of the value stored in R0

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Sign of a 2's Complement value can be changed by inverting the value (bits) and adding 1



```
LDR    r0, =7
MVN    r0, r0
ADD    r0, r0, #1
```

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; value = 7 (simple test value)
; value = NOT value (invert bits)
; value = value + 1 (add 1)
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ARM Instruction Set provides a single instruction for this purpose

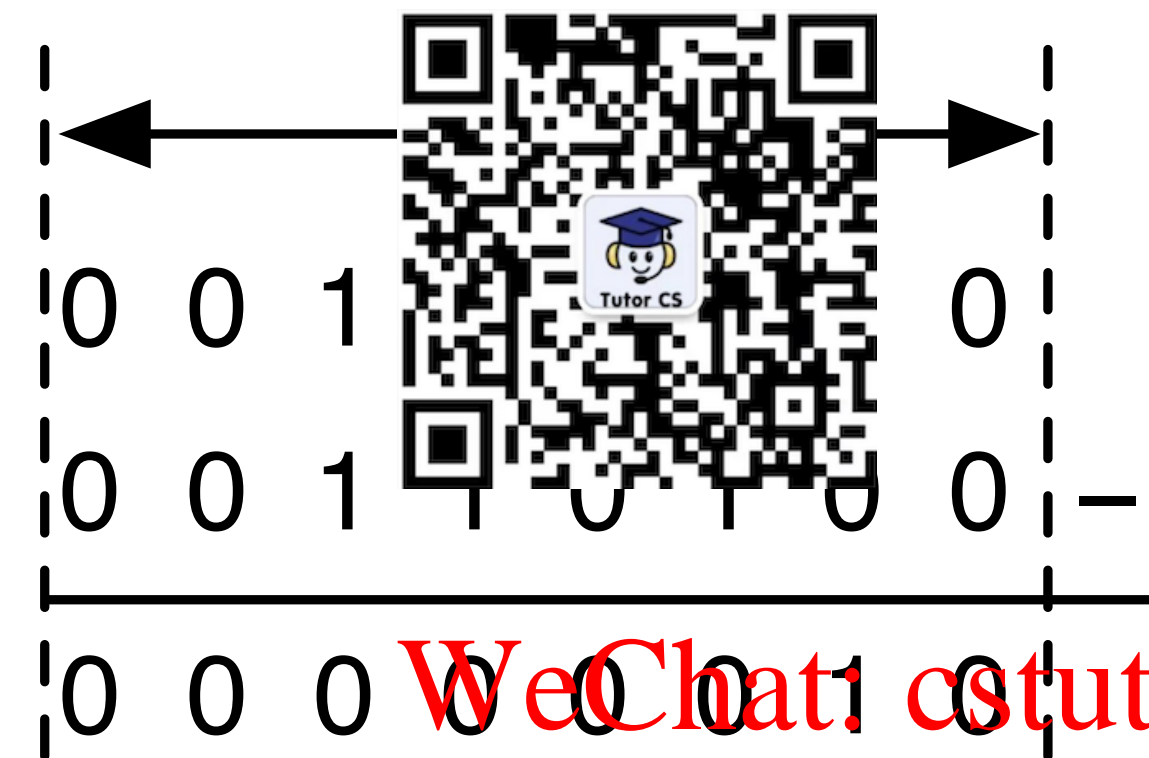
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```
LDR    r0, =7
NEG    r0, r0
```

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; value = 7 (simple test value)
; value = -value

A – B

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Decimal equivalent

+54

+52 –

+2

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A + TwosComplement(B)

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Decimal equivalent

+54

–52 +

+2


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1

A – B

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1 0 0 0 0 1 0 0 1

0 1 1 1

1 0 0 0 1 0 0 1

Decimal equivalent

+8	
+127	–
<hr/>	
–119	

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A + TwosComplement(B)

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8 bits

0 0 0 0 1 0 0 0

1 0 0 0 1 0 0 1

0 1 0 0 0 1 0 0 1

Decimal equivalent

+8	
–127	+
<hr/>	
–119	

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5.3 overflow

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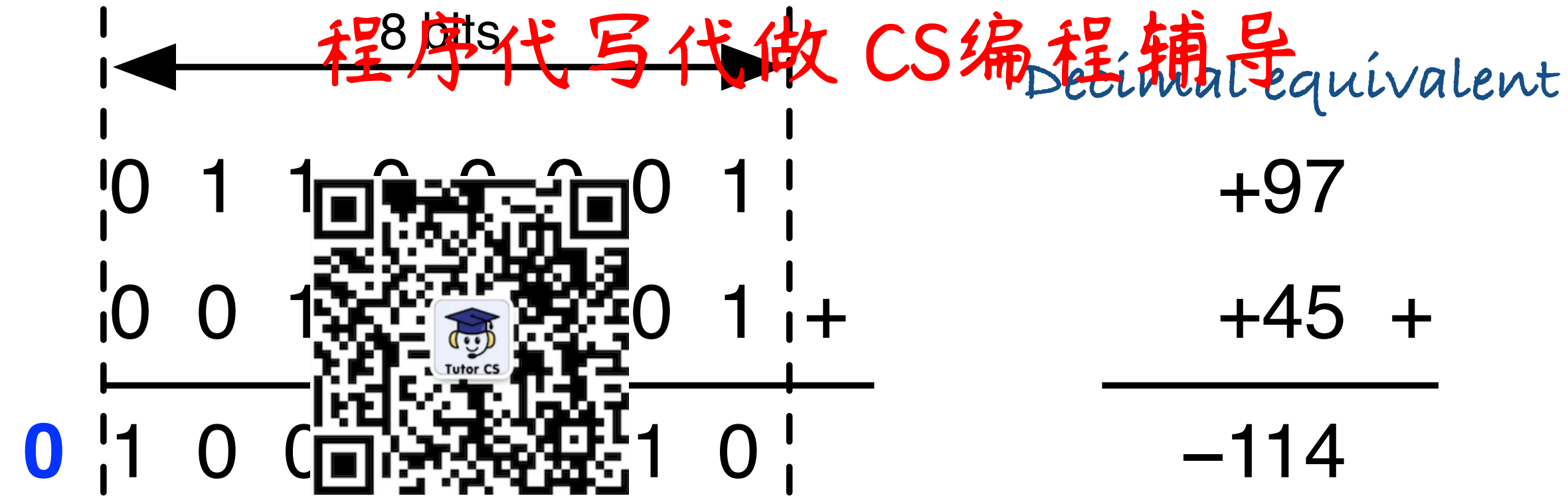
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Result is 10001110_2 (142_{10} , or -114_{10})

If we were interpreting the two added values and the result as **signed integers**, we got an incorrect result:

We added two +ve numbers and obtained a -ve result

With 8-bits, the highest +ve integer we can represent is +127

10001110_2 (-114_{10})

The result is outside the range of the signed number system

If the result of an addition or subtraction gives a result that is outside the range of the signed number system, then an oVerflow has occurred



The processor sets the overflow Condition Code Flag after performing an arithmetic operation to indicate whether an overflow has occurred

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Current Program Status Register

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Carry and overflow flags always set by the processor regardless of our signed or unsigned interpretation of stored values



Processor does not “know” our interpretation is

e.g. we could interpret the binary value 10001110_2 as either 142_{10} (unsigned) or -114_{10} (signed)

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(we could also interpret it as the code for ‘A’ or as the colour blue)

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The C and V flags are set by the processor and it is our responsibility to choose:

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whether to interpret C or V (are we interpreting the values as unsigned or signed?)

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how to interpret C or V

Addition rule ($r = a + b$) 程序代写代做 CS编程辅导

$$V = 1 \text{ if } \begin{matrix} \text{MSB}(a) = \text{MSB}(b) \text{ and} \\ \text{MSB}(r) \neq \text{MSB}(a) \end{matrix}$$

i.e. oVerflow occurs for addition if the operands have the same sign and the result has a different sign

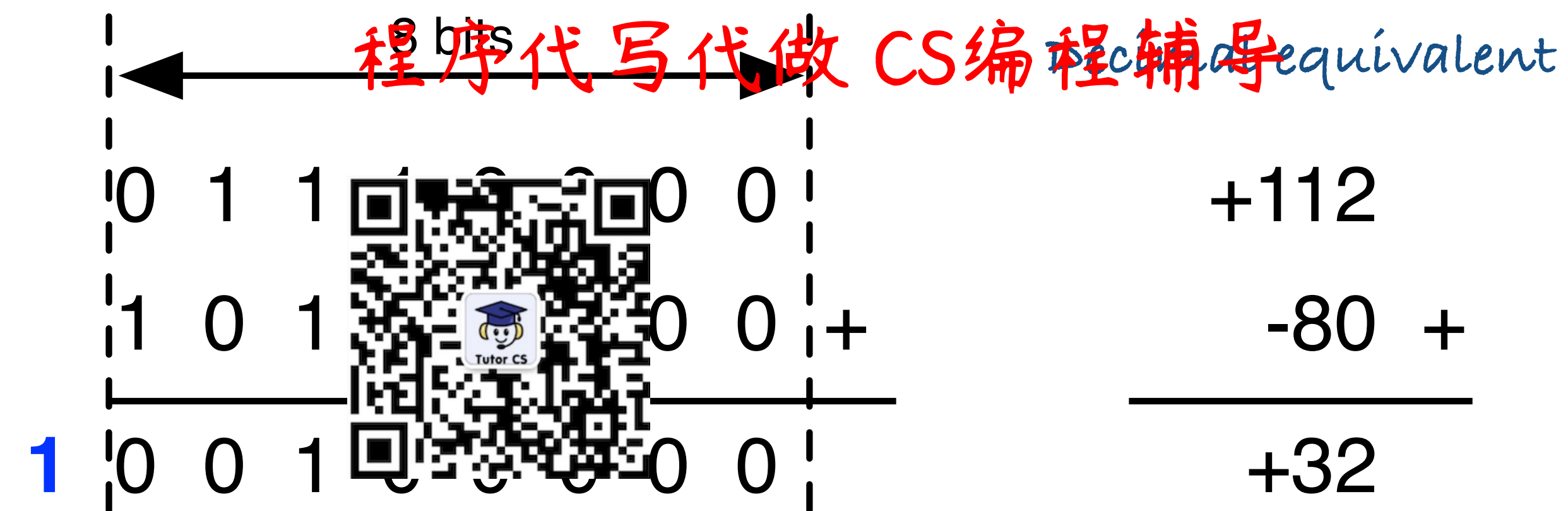
Subtraction rule ($r = a - b$)

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$$V = 1 \text{ if } \begin{matrix} \text{MSB}(a) \neq \text{MSB}(b) \text{ and} \\ \text{MSB}(r) \neq \text{MSB}(a) \end{matrix}$$

i.e. oVerflow occurs for subtraction if the operands have different signs and the sign of the result is different from the sign of the first operand



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Signed interpretation: $(+112) + (-80) = +32$

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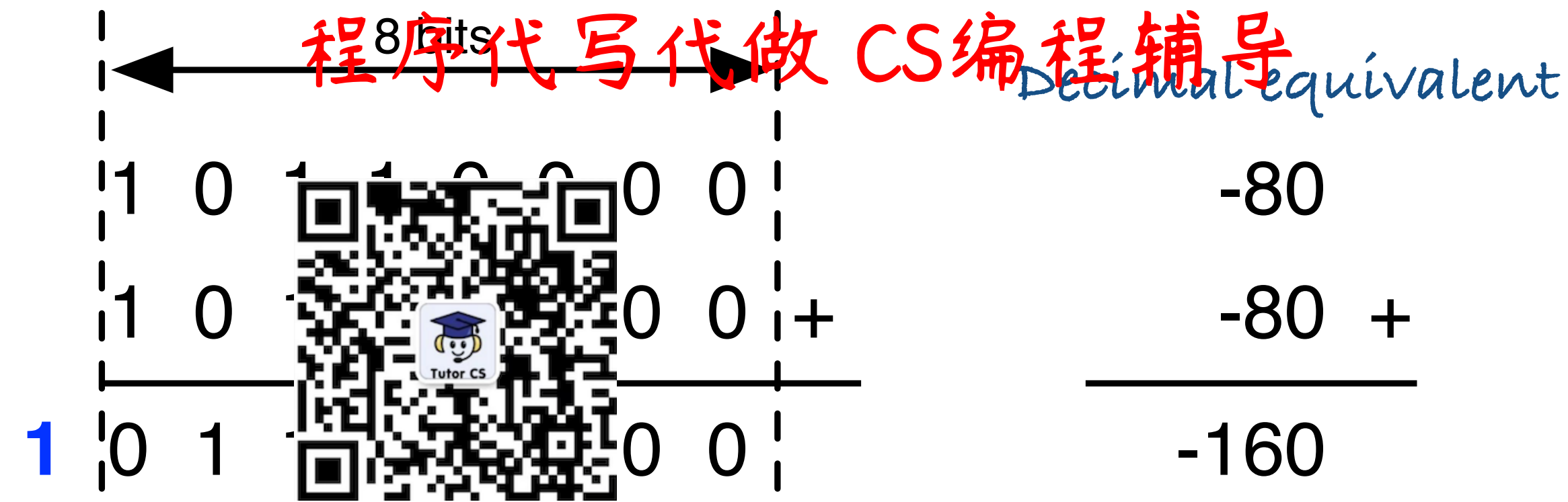
Unsigned interpretation: $112 + 176 = 288$

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By examining the V flag ($V=0$), we know that if we were interpreting the values as signed integers, the result is correct

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If we were interpreting the values as 8-bit unsigned values, $C = 1$ tells us that the result was too large to fit in 8-bits

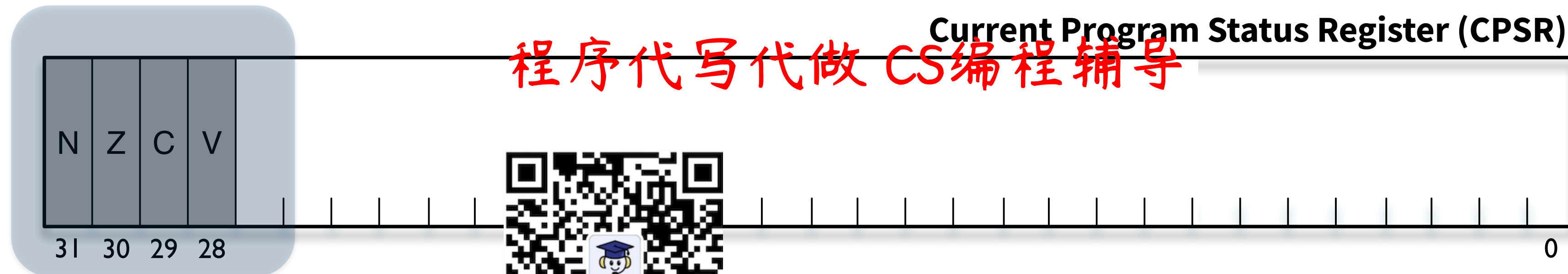


Signed: $(-80) + (-80) = -160$

Unsigned: $176 + 176 = 352$

By examining the V flag ($V = 1$), we know that if we were interpreting the values as signed integers, the result is outside the range of the signed number system

If we were interpreting the values as 8-bit unsigned values, $C = 1$ tells us that the result was too large to fit in 8-bits



Many instructions can optionally cause the processor to update the Condition Code Flags (N, Z, V, and C) to reflect certain properties of the result of an operation

Append “S” to instruction in assembly language (e.g. ADDS)

Set S-bit in machine code instruction

N flag set to 1 if result is **N**egative (i.e. if MSB is 1)

Z flag is set to 1 if result is **Z**ero (i.e. all bits are 0)

C flag set if **C**arry occurs (addition) or borrow does not occur (subtraction)

V flag set if o**V**erflow occurs for addition or subtraction

Remember: Processor updates NZVC regardless of our interpretation of values as signed or unsigned



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5.4 Condition Assignment Project Exam Help Code Flag examples

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```
LDR    R0, =0xC0000000  
LDR    R1, =0x70000000  
ADDS   R0, R0, R1
```



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Is the Carry flag set?

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Is the oVerflow flag set?

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Is the Zero flag set?

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Is the Negative flag set?

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```
LDR    R0, =0xC0000000  
LDR    R1, =0x40000000  
ADDS   R0, R0, R1
```



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Is the Carry flag set?

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Is the overflow flag set?

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Is the Zero flag set?

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Is the Negative flag set?

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```
LDR    R0, =0xC0000000  
LDR    R1, =0x90000000  
ADDS   R0, R0, R1
```



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Is the Carry flag set?

Is the oVerflow flag set?

Is the Negative flag set?

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```
LDR    R0, =0xC0000000  
LDR    R1, =0x30000000  
ADD    R0, R0, R1
```



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Is the Carry flag set?