

Solution to Homework Assignment 5

Solution to Problem 1: The bandwidth of the message is 5k Hz.

a) For LSSB modulation, the modulated signal has the same bandwidth as the message: $B_T = 5\text{k}$ Hz.

b) For DSB-SC AM the modulated signal is twice the bandwidth of the message: $B_T = 10\text{k}$ Hz.

b) For conventional AM the modulated signal is twice the bandwidth of the message: $B_T = 10\text{k}$ Hz.



Solution to Problem 2:

a)

$$\text{sinc}(2Bt) \Rightarrow \frac{1}{2B} \text{rect}\left(\frac{f}{2B}\right).$$

$$\text{sinc}^2(2Bt) \Rightarrow \frac{1}{4B^2} \text{rect}\left(\frac{f}{2B}\right) * \text{rect}\left(\frac{f}{2B}\right) = \frac{1}{2B} \Delta\left(\frac{f}{4B}\right)$$

$$m(t) = 2B \text{sinc}^2(2Bt) \Rightarrow M(f) = \Delta\left(\frac{f}{4B}\right).$$

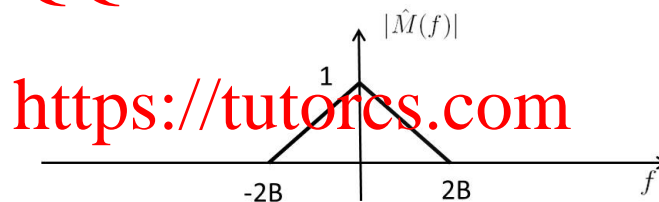
Thus,

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$$\hat{M}(f) = -j \text{sgn}(f) M(f) = -j \text{sgn}(f) \Delta\left(\frac{f}{4B}\right).$$

The frequency spectrum is shown in Figure 1 (where $B = 2\text{k}$).

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Figure 1: Frequency spectrum for the message in Problem 3.

b) $A_c = 100$, $f_c = 10\text{k}$, and $B = 2\text{k}$.

$$s_{\text{USSB}}(t) = 50m(t) \cos(20,000\pi t) - 50\hat{m}(t) \sin(20,000\pi t),$$

By following similar frequency analysis for LSSB AM in lecture notes, it can be shown that (details are omitted)

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$$S_{\text{USSB}}(f) = 50 [M_+(f - 10,000) + M_-(f + 10,000)]$$

$$S_{\text{USSB}}(f) = \begin{cases} 50 \left[-\frac{f-10,000}{4,000} + 1 \right] & 10,000 < f < 14,000 \\ 50 \left[\frac{f+10,000}{4,000} + 1 \right] & -14,000 < f < -10,000 \\ 0 & \text{otherwise} \end{cases}$$

The magnitude spectrum

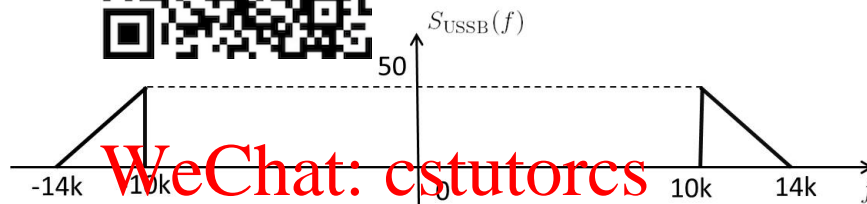


Figure 2: The magnitude spectrum of the USSB wave.

Assignment Project Exam Help

Solution to Problem 3: In the QAM system,

(a)

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$$\varphi_{QAM}(t) = m_1(t) \cos(2\pi f_c t) + m_2(t) \sin(2\pi f_c t)$$

$$= \text{sinc}(t) \cos(2\pi f_c t) + \text{sinc}^2(t) \sin(2\pi f_c t)$$

To calculate the bandwidth of $\varphi_{QAM}(t)$, we should find the Fourier transform of $m_1(t)$ and $m_2(t)$, i.e.,

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$$m_1(t) = \text{sinc}(t) \Leftrightarrow M_1(f) = \text{rect}(f) \Rightarrow B_1 = \frac{1}{2} \text{ Hz}$$

$$m_2(t) = \text{sinc}^2(t) \Leftrightarrow M_2(f) = \text{tri}(f/2) \Rightarrow B_2 = 1 \text{ Hz}$$

$$\Rightarrow B_{\varphi_{QAM}} = 2 \max\{B_1, B_2\} = 2 \text{ Hz.}$$

(b) The required bandwidth of the low-pass filter is half of $B_{\varphi_{QAM}}$, i.e., $B_{LPF} = 1 \text{ Hz}$.

(c)

$$m_1(t) = \text{sinc}(t) \Leftrightarrow M_1(f) = \text{rect}(f) \Rightarrow B_1 = \frac{1}{2} \text{ Hz}$$

$$m_2(t) = \frac{1}{2} \text{sinc}^2(2t) \Leftrightarrow M_2(f) = \frac{1}{4} \text{tri}(f/4) \Rightarrow B_2 = 2 \text{ Hz}$$

$$\Rightarrow B_{\varphi_{QAM}} = 2 \max\{B_1, B_2\} = 4 \text{ Hz}$$

$$\Rightarrow B_{LPF} = \frac{B_{\varphi_{QAM}}}{2} = 2 \text{ Hz}$$

(d) We get the LSB version of the SSB signal.