

Reminders from basic probability theory:

If the probability of reading any individual bit wrongly is called P ,
then the probability of reading any individual bit correctly is $1 - P$,
and the probability of reading a whole sequence of N bits correctly is $(1 - P)^N$.

Reminder from common sense:

For any storage system, even a little bit, P will be very small.
Really small.
But never zero.

Reminder from mathematics:

$(1 - P)^N$ is evaluated as $1 - NP$

$$+ \frac{N(N-1)P^2}{2}$$

$$- \frac{N(N-1)(N-2)P^3}{6}$$

$$+ \frac{N(N-1)(N-2)(N-3)P^4}{24}$$

$$- \frac{N(N-1)(N-2)(N-3)(N-4)P^5}{120}$$

$$+ \frac{N(N-1)(N-2)(N-3)(N-4)(N-5)P^6}{720}$$

.....

..... all the way up to

$$+ P^N$$

which takes a lot of calculating

Another reminder from probability:

If P is very small, then $(1 - P)^N$ is the same as e^{-PN}
which is easy to work out.

Another reminder from mathematics:


e is the special magic number 2.7182818284590452353602874713527.....

So...

Combined error rates are very easy to calculate for any realistic system.

Let's say the single bit error rate is 10^{-5} , meaning that if you attempt to read a single bit there is a 1 in 100,000 chance of getting it wrong. Or that if you experimentally read a bit 100,000 times under identical circumstances you'd expect to get it wrong once. Or that if you read 100,000 bits, you expect one error.

The chances of reading N bits successfully, i.e. without any errors will be


$$e^{-0.00001N}$$

<u>number of bits in a block</u>	<u>chances of reading it successfully</u>
1,000	99%
4,096	96%
10,000	90%
20,000	82%
40,000	67%
100,000	37%
200,000	14%
400,000	1.8%
1,000,000	0.0045%

So you see why block size has to be kept relatively small.

A block on a hard disc has 4096 bits.

An error rate of 10^{-5} for a modern hard disc drive is not good.

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