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1. Introduction

We introd CH class of models which were developed to account for the personal CH class of models which were developed to asset return date CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive Conditional Heteroscedastic of the CH refer, respectively, to an Autoregressive CH refer, respectively, to an Autoregressive Ch refer the CH refer, respectively, to an Autoregressive Ch refer the CH refer, respectively, to an Autoregressive Ch refer the CH refer, respectively, to an Autoregressive Ch refer the C

2. ARCH Processes

Consider a very simple model for returns (v) which in practice is not an unreasonable characterization for mean returns, namely,

where $\varepsilon_t \sim WN(0,\sigma^2)$ and c is the intercept. This assumption means that the unconditional mean and variance of the innovation ε_t are constant and finite (equal to zero and σ^2 , respectively and that the innovations are scriptly uncorrelated at all leads and lags. In topic 3, we made the further assumption that the innovations were independently and identically distributed so that the innovations were characterized as a strict white noise process that $s_t \in \Omega$ and $s_t \in \Omega$. The assumption of independence means that the conditional probability density function of $\varepsilon_t \mid \Omega_{t-1}$ where $\Omega_{t-1} = \{\varepsilon_{t-1}, \varepsilon_{t-2}, \ldots\}$ is the same as the unconditional probability density function of ε_t . This has the implication that the conditional variance of the innovation, namely, $var(\varepsilon_{t+j} \mid \Omega_t)$ depends only on f and not on the conditioning information set Ω_t . Thus, for example, when f=1

$$\operatorname{var}(arepsilon_t \mid \Omega_{t-1}) = \operatorname{var}(arepsilon_{t+1} \mid \Omega_t)$$

The arrival of "news" at t, namely ε_t , does not affect the value of conditional variance of the innovation one period ahead, namely, at t+1. In other words, the conditional variance does not adapt to the arrival of new conditioning information. In financial markets, however, return volatility responds to the arrival of "news" and the present specification cannot capture this feature of financial data.

To do so, we will continue to assume that the innovations are white noise but that they are *not* strictly white noise by dropping the assumption of independence. In particular, we will assume a particular dependence structure in the conditional variance of the innovation.

The Autoregressive Conditional Heteroscedastic Model of order one (ARCH(1)) for the innovation ε_t is

$\varepsilon_{t} \mid \Omega_{t-1} \sim \mathcal{A}_{0}^{0}, \mathcal{P}_{0}^{2}$ 点局战做 CS编程辅导(2)

where $\sigma_t^2 = \mathrm{var}(\mathbf{r}_{t-1}, \mathbf{r}_{t-2}, \mathbf{r}_{t-2})$ point variance of ε_t based on the information set ially uncorrelated but they are not serially independent becalling in a stribution is assumed normal so that equations (1) and (2) can be est

It is important is a weak white noise process and is covariance stationary. The unconditional variance of ε are constant and finite and are, respectively,

$$E(\varepsilon_t) = 0$$
 WeChat: cstutorcs
 $var(\varepsilon_t) = E(\varepsilon_t - E(\varepsilon_t))^2 = \frac{\alpha_0}{1 - \alpha_1}$

The restrictions $\alpha_0 > 0$, $0 \le \alpha_1 < 1$, ensure that the unconditional variance is positive

and finite and, also, that the conditional variance is always positive. The important point is that the unconditional mean and variance are finite and constant as required for covariance stationarity. Also, as stated earner the ε_t are serially uncorrelated. The conditional mean and variance are

$$E(\varepsilon_{t} \mid \Omega_{t-1}) = E[(\varepsilon_{t} - E(\varepsilon_{t} \mid \Omega_{t-1}))^{2} \mid \Omega_{t-1}]$$

$$\text{http}(\varepsilon_{t}^{2}) \text{//tutorcs.com}$$

$$= \alpha_{0} + \alpha_{1}\varepsilon_{t-1}^{2}$$

$$= \sigma_{t}^{2}$$

The important point here is that the conditional variance is time-varying and thus heteroscedastic. Note that

$$\operatorname{var}(\varepsilon_{t+1} \mid \Omega_t) = \alpha_0 + \alpha_1 \varepsilon_t^2$$

and it follows that $\operatorname{var}(\varepsilon_t \mid \Omega_{t-1}) \neq \operatorname{var}(\varepsilon_{t+1} \mid \Omega_t)$. The arrival of news, namely, ε_t , will affect the conditional variance for next period (at time t+1). This is the key feature of ARCH type models: the conditional variance adapts to the conditioning information set. Clearly, if $\alpha_1 = 0$, there are no conditional variance dynamics and we are back to case of independence where $\varepsilon_t \sim iidWN(0,\alpha_0)$ from which it follows, for example, that $\operatorname{var}(\varepsilon_t \mid \Omega_{t-1}) = \operatorname{var}(\varepsilon_{t+1} \mid \Omega_t)$.

The ARCH model is capable of capturing the feature of volatility clustering that is observed in financial data where large changes in veturns by small changes, of either sign. A large observed ε_{t-1}^2 produces a large conditional variance at time t, that is, a large σ_t^2 , thereby increasing the likelihood of ε_{t-1}^2 process models conditional variance dynamics in an au

Clearly, ir t_t (1), the unconditional and conditional mean of y_t is just c. The continuous t_t is time-varying and equal to:

Equation (1) is referred to as the mean equation and equation (2) as the variance equation. In practice, both equations are estimated jointly using maximum likelihood techniques and an estimate is obtained for each parameter, namely, for c, α_0 and α_1 . There is no need for the mean equation could easy be:

$$y_{t} = \beta_{0} + \beta_{1}X_{t} + \beta_{2}X_{t} + \beta_{3}X_{t} + \beta_{3}X_{t} + \beta_{4}X_{t} + \beta_{5}X_{t} +$$

or

$$y_t = c + \varepsilon h t_t ps://tutorcs.com$$

or

$$y_t = c + \rho y_{t-1} + \varepsilon_t$$

where, in each case, $\varepsilon_t \sim WN(0,\sigma^2)$. Similarly, there is no need to restrict the variance equation to an ARCH specification with one autoregressive lag. The ARCH(q) specification for the variance equation is:

$$\begin{split} & \mathcal{E}_t \mid \Omega_{t-1} \sim N(0, \sigma_t^2) \\ & \sigma_t^2 = \alpha_0 + \alpha_1 \mathcal{E}_{t-1}^2 + \alpha_2 \mathcal{E}_{t-2}^2 + \ldots + \alpha_q \mathcal{E}_{t-q}^2 \\ & \alpha_0 > 0, \ \alpha_i \geq 0 \ \text{for all} \ i = 1 \ to \ q, \ \sum_{i=1}^q \alpha_i < 1 \end{split}$$

The stated restrictions are sufficient to ensure that the conditional and unconditional variances are positive and finite and that at it is contributed as a finite and that at the ARCH(q) process, the unconditional mean, variance and covariance are,

$$E(\varepsilon_t)=0$$

$$\mathrm{var}(\varepsilon_t)=$$

$$\mathrm{cov}(\varepsilon_t,\varepsilon_{t-1})$$
 while the condition

$$\begin{split} E(\varepsilon_t \mid \Omega_{t-1}) &= 0 \\ \text{var}(\varepsilon_t \mid \Omega_t) &= C + \alpha_t^2 + \alpha$$

Consider now the y_t possibly in the particular to realization of y_t , it will always be the case that

$$var(y_t | \Omega Email! \Omega tutores@163.com = \sigma_t^2$$

For example, suppose y_t follows the ARR process given above. Then the conditional mean of y_t is

$$E(y_{t} \mid \Omega_{t-1}) = c + \rho y_{t-1} + E(\varepsilon_{t} \mid \Omega_{t-1})$$

$$= c + \rho y_{t-1}$$

which is the forecast value of y_t on the basis of time t-1 information. Now

$$\begin{split} \operatorname{var}(y_t \mid \Omega_{t-1}) &= E[(y_t - E(y_t \mid \Omega_{t-1}))^2 \mid \Omega_{t-1}] \\ &= E[(c + \rho y_{t-1} + \varepsilon_t - (c + \rho y_{t-1}))^2 \mid \Omega_{t-1}] \\ &= E[\varepsilon_t^2 \mid \Omega_{t-1}] \\ &= \sigma_t^2 \end{split}$$

The two-standard error confidence interval for the one-step ahead forecast of y_t , based on information available at time t-1 (i.e. Ω_{t-1}) for the AR(1) model is:

c+ρy_{t-1} 揭序代写代做 CS编程辅导

In the case of an ARCH(1) process it is



On the basis of til step ahead foreca

two-standard error confidence interval for the one-formation available at time t (i.e. Ω_t) is:

$$c + \rho y_t \pm 2\sqrt{\sigma_{t+1}^2}$$

In the case of an ARCH(1) process it is CStutorCS

$$c + \rho y_t \pm 2\sqrt{\alpha_0 + \alpha_1 \varepsilon_t^2}$$

Notice that not only is no local tened of y uplifted as to be to be also the standard error of the forecast is updated as it depends on ε_t^2 . Thus, the arrival of new information at time t influences not only the forecast but the confidence interval associated with the forecast is updated as 0.30.

2. GARCH Processes

The generalized RCH of GARCO(2,1) mode is:

$$y_{t} = c + \varepsilon_{t}$$

$$\varepsilon_{t} \mid \Omega_{t-1} \text{ https://tutorcs.com}$$
(3)

$$\sigma_{t}^{2} = \alpha_{0} + \alpha_{1} \varepsilon_{t-1}^{2} + \beta_{1} \sigma_{t-1}^{2}
\alpha_{0} > 0, \ \alpha_{1} \ge 0, \ \beta_{1} \ge 0, \ \alpha_{1} + \beta_{1} < 1$$
(4)

Here the conditional variance at time t (σ_t^2) depends not only on last period's squared innovation (ε_{t-1}^2) but also on the conditional variance last period (σ_{t-1}^2). The parameter restrictions ensure that the unconditional variance and the conditional variance are positive and finite and that y_t is covariance stationary. Equation (3) is the mean equation. In this case, it is very simple but it can assume any form, for example, a regression equation or an MA or AR process. Equation (4) is the variance equation. The unconditional mean and the unconditional variance of ε are constant and finite and are, respectively,

$var(\varepsilon_t) = 0$ 程序代 写纸 CS编程辅导 $var(\varepsilon_t) = E(\varepsilon_t - E(\varepsilon_t))^2 = \frac{Sat}{1 - \alpha_1 - \beta_1}$

is $cov(\varepsilon_t, \varepsilon_{t-j}) = 0$ for j > 0. The conditional mean Note that the unce and variance are



 $= \alpha_0 + \alpha_1 \varepsilon_{t-1}^2 + \beta_1 \sigma_{t-1}^2$ **Example 1.1** Cstutorcs

The important point is that the unconditional variance is constant, as must be the case under covariance stationarity whereas the conditional variance is time-varying. He larger two-standard error confidence interval for the one-step ahead forecast of y_t ,

based on information available at time t-1 (i.e. Ω_{t-1}) for the AR(1) model is:

In the case of a GARCH(1,1) process its 3 9476 $c + \rho y_{t-1} \pm 2\sqrt{\alpha_0 + \alpha_1 \varepsilon_{t-1}^2 + \beta_1 \sigma_{t-1}^2}$

On the basis of tind the batton the two stangar Craft Onfidence interval for the onestep ahead forecast of y_t , based on information available at time t (i.e. Ω_t) is:

$$c + \rho y_t \pm 2\sqrt{\sigma_{t+1}^2}$$

In the case of an GARCH(1,1) process it is

$$c + \rho y_t \pm 2\sqrt{\alpha_0 + \alpha_1 \varepsilon_t^2 + \beta_1 \sigma_t^2}$$

Notice that not only is the forecasted value of y updated, as it now depends on y_t , but also the standard error of the forecast is updated as it depends on ε_t^2 and σ_t^2 . Thus, the arrival of new information at time t influences not only the forecast but the confidence interval associated with the forecast.

In practice, it was found that to adequately model volatility, the ARCH(q)specification required a very long number of lags, that is, q was found to be very large. Not only do a large number of lags use up degrees of freedom but with so many

parameters to estimate it is more probable that one or more of the estimated parameters may be negative, totaling the sten respictions to the Carange. The last development of the GARCH model. We will now show that the GARCH(1,1) model is equivalent to a restricted ARCH model of infinite order. Now

Substitute for
$$\sigma_{t-}^2$$

$$\sigma_t^2 = \alpha_0 + \frac{1}{2} \sum_{\text{two ccs}}^{2} \frac{1}{t^2} + \beta_1 \sigma_{t-2}^2$$

$$= \alpha_0 (1 + \beta_1) + \alpha_1 (\varepsilon_{t-1} + \beta_1 \varepsilon_{t-2}^2) + \beta_1^2 \sigma_{t-2}^2$$

Continue in this way to get that: cstutorcs $\sigma_t^2 = \alpha_0(1+\beta_1+\ldots+\beta_1^{j-1}) + \alpha_1(\varepsilon_{t-1}^2+\beta_1\varepsilon_{t-2}^2+\ldots+\beta_1^{j-1}\varepsilon_{t-j}^2) + \beta_1^j\sigma_{t-j}^2$

$$m{\sigma}_{t}^{2} = m{lpha}_{0}(1 + m{eta}_{1} + \ldots + m{eta}_{1}^{j-1}) + m{lpha}_{1}(m{arepsilon}_{t-1}^{2} + m{eta}_{1}m{arepsilon}_{t-2}^{2} + \ldots + m{eta}_{1}^{j-1}m{arepsilon}_{t-j}^{2}) + m{eta}_{1}^{j}m{\sigma}_{t-j}^{2}$$

As $j \to \infty$, Assignment Project Exam Help

$$\sigma_t^2 = \frac{\alpha_0}{1 - \text{Email: tutorcs @ 163.com}} + \alpha_1(\varepsilon_{t-1}^2 + \beta_1 \varepsilon_{t-2}^2 + \dots + \beta_1^{j-1} \varepsilon_{t-j}^2 + \dots)$$

This follows because $\beta_1 < 1$, given the sign restrictions of the GARCH(1,1) model. Thus, the GARCH(1, 1) model is equivalent to an $ARCH(\infty)$ where the coefficients on the lagged squared irrovations decline competities by The GARCH(1,1) is a parsimonious model since there are only three parameters to estimate: $\alpha_0, \alpha_1, \beta_1$.

In many finance applications, particularly in Value-at-Risk calculations and the pricing of options for coasts of the conditional variance are required. We will now derive an expression for the h-step ahead forecast of the conditional variance for the GARCH(1,1) specification. By definition

$$\sigma_t^2 = E(\varepsilon_t^2 \mid \Omega_{t-1})$$

Updating by h periods, we obtain

$$\sigma_{t+h}^2 = E(\varepsilon_{t+h}^2 \mid \Omega_{t+h-1})$$

The optimal forecast of σ_{t+h}^2 based on information available at time t is $E(\sigma_{t+h}^2 \mid \Omega_t)$. By construction.

$$E[\sigma_{t+h}^2 \mid \Omega_t] = E[E(\varepsilon_{t+h}^2 \mid \Omega_{t+h-1}) \mid \Omega_t]$$

$$= E(\varepsilon_{t+h}^2 \mid \Omega_t)$$
(5)

where the last equality follows from the law of iterative expectations. The GARCH(1,1) model is 程序代写代数 CS编程辅导

$$\sigma_{t+h}^2 = \alpha_0 + \alpha_1 \varepsilon_{t+h-1}^2 + \beta_1 \sigma_{t+h-1}^2$$

Take the conditio Ω_t to get

$$E(\sigma_{t+h}^{2} \mid \mathbf{G}) = \mathbf{E}(\sigma_{t+h-1}^{2} \mid \Omega_{t}) + \beta_{1} E(\sigma_{t+h-1}^{2} \mid \Omega_{t})$$

$$(6)$$

where the last equality follows from equation (5). By recursive substitution, we can write equation (6) as

$$\begin{split} E(\sigma_{t+h}^2 \mid \Omega_t) &= \alpha_0 [\mathbf{W} (\mathbf{C}_t \mathbf{F}_t) \mathbf{E}_t \mathbf{E}_$$

where the last step follows because D_{t+1} is though at the Chis formula data also be used to calculate a two standard error confidence band around the optimal h-step ahead forecast of y. Fortunately, EV jews automatically calculates forecasts of the h-step ahead conditional variance using this formula for the case of a GARCH (Cloricess). Provided $\alpha_1 + \beta_1 < 1$, the forecast of the conditional variance will converge to the unconditional variance of ε_t as $h \to \infty$. That is

$$\lim_{h \to \infty} E(\sigma_{t+h}^2 | \Omega_t) = \frac{749389476}{1 - (\alpha_t + \beta_t)} = var(\varepsilon_t)$$

Further if \mathbf{p} this a GARCH OF proses Counter be shown that ε_t^2 has an ARMA(1,1) representation, namely,

$$\varepsilon_t^2 = \alpha_0 + (\alpha_1 + \beta_1)\varepsilon_{t-1}^2 - \beta_1 v_{t-1} + v_t$$

where $v_t = \varepsilon_t^2 - \sigma_t^2$ is the difference between the squared innovation and the conditional variance at time t. (You will be asked to show this result in a tutorial exercise). The term ε_t^2 is a noisy proxy for the conditional variance σ_t^2 : ε_t^2 is an unbiased predictor of σ_t^2 but it is more volatile. Also, recall that real world financial asset returns are typically unconditionally symmetric but leptokurtic (that is, more peaked in the centre and with fatter tails than a normal distribution). It turns out that the implied unconditional distribution of the conditionally normal GARCH process is also symmetric and leptokurtic.

Finally, the GARCH(1,1) can be extended to a GARCH(p,q) process given by

$$\varepsilon_{t} \mid \Omega_{t-1} \sim \mathcal{C}^{0}, \mathcal{C}^{2}, \mathcal{C}^{0}, \mathcal{C}^{2}, \mathcal{C}^{0}, \mathcal{C}^{2}, \mathcal{C}^{0}, \mathcal{C}^{2}, \mathcal{C}^{0}, \mathcal{C}$$

As before, the sta conditional variat of ε are constant

that ε_t is covariance stationary and that the aconditional mean and the unconditional variance spectively,

$$E(\varepsilon_t) = 0$$

$$var(\varepsilon_t) = E(\varepsilon_t - E(\varepsilon_t))^2 = \frac{\alpha_0}{1 - \sum_{i=1}^{q} \sum_{j=1}^{q} \sum_{j=1}^{q} \sum_{i=1}^{q} \sum_{j=1}^{q} \sum_{j=1}^{q} \sum_{j=1}^{q} \sum_{j=1}^{q} \sum_{j=1}^{q} \sum_{i=1}^{q} \sum_{j=1}^{q} \sum_{j=1}^{q$$

The conditional mean and variance are

$E(\varepsilon_{t} \mid \Omega_{t-1})$ Assignment Project Exam Help

$$Q_{t}^{2} \frac{\alpha_{0} + \sum_{i=1}^{q} \alpha_{i} \varepsilon_{t-i}^{2} + \sum_{i=1}^{p} \beta_{i} \sigma_{t-i}^{2}}{749389476}$$

Also, as before, no matter the specific form of the mean equation for y_t , it will always be the case that $\frac{\text{https://tutorcs.com}}{\text{https://tutorcs.com}}$

$$\begin{aligned} \operatorname{var}(y_t \mid \Omega_{t-1}) &= \operatorname{var}(\varepsilon_t \mid \Omega_{t-1}) \\ &= \sigma_t^2 \end{aligned}$$

3. Maximum Likelihood Estimation of the GARCH(1,1) Process

In lecture note 2, we discussed maximum likelihood estimation of the simple linear regression model

$$Y_t = \beta_0 + \beta_1 X_t + u_t$$
 where $u_t \sim iid N(0, \sigma^2)$.

The log-likelihood function for this model is

$$l(\beta_0, \beta_1, \sigma^2 \mid Y_t, X_t \mid t = 1, ..., T) = -\frac{T}{2} \ln(2\pi) - \frac{T}{2} \ln \sigma^2 - \frac{1}{2\sigma^2} \sum_{t=1}^{T} (Y_t - \beta_0 - \beta_1 X_t)^2$$

Now lets assume the conditional mean equation is $Y_t = \delta_0 + \delta_1 X_t + \varepsilon_t$ **CS编程辅导**

The log-likelihood function for this model is

Once we substitute $\varepsilon_{t-1}^2 = (Y_{t-1} - \delta_0 - \delta_1 X_{t-1})^2$ and σ_{t-1}^2 in the log-likelihood function, it is then possible to maximize the log-likelihood virtle property act of act of the parameters $(\delta_0, \delta_1, \alpha_0, \alpha_1, \beta_1)$. The values of ε_0^2 and σ_0^2 have to be set and they are usually set equal to the unconditional variance of the ε 's from the estimated mean equation, which is

$$\hat{\sigma}_{ols}^2 = \frac{1}{T} \sum_{t=1}^{T} e_t^2$$
 where the e^7 are the Solution EV iews actually uses a more

sophisticated approach. Because the first-order conditions are nonlinear, they are solved using an iterative search procedure. In order to implement such a procedure, starting values for the parameter hand the hard of degree of the condition of the parameter hand of the starting values for these parameters, respectively. In the absence of GARCH effects, α_0 can be interpreted as the unconditional variance of the ε 's. Thus, an appropriate starting value of α_0 is $\hat{\sigma}_{ols}^2$. For α_1 and β_1 , arbitrarily select a small number (say, 0.05) for both as a starting value. The search procedure will iterate from these starting values and continue until a convergence criterion is satisfied. Hopefully, the resulting estimates will correspond to a global and not just a local maximum of the log-likelihood function.

4. Tests for ARCH\GARCH Effects

To see whether there are ARCH\GARCH effects evident in the data, first estimate the mean equation by OLS and save the residuals. Denote the OLS residuals from the mean equation as e_t . Consider the autocorrelations of the squared OLS residuals, that is, of e_t^2 . If the autocorrelations for the squared residuals are large and exceed the Bartlet bands, that is an indication of the presence of ARCH\GARCH effects

in the data. Alternatively, one may use an LM test for ARCH/GARCH. Estimate the auxiliary regression 子代女 CS编程辅导

$$e_t^2 = \gamma_0 + \gamma_1 e_{t-1}^2 + \ldots + \gamma_q e_{t-q}^2 + v_t$$

where the e's are _____ om the mean equation and v_t is an error term. Obtain the R^2 from _____ e LM test statistic is

$$TR^2 \sim \chi_q^2$$

where T is number of OLS residuals. The null and alternative hypotheses are

$$H_0: \gamma_i = 0$$
 for all $i = 1, 2, ..., q$.
 $H_1: \gamma_i \neq 0$ for all $i = 1, 2, ..., q$.

Large values of TR^2 lead to a rejection of the null hypothesis of no ARCH\GARCH effects. Alternatively, SRF1 to the null hypothesis of no ARCH\GARCH effects. Alternatively, SRF1 to the null hypothesis of no ARCH\GARCH effects.

5. Tests of Model Adequacy

It can be shown that if ε_t tutores @163.com

$$\frac{\varepsilon_t}{\sigma_t} = v_t \sim (0.1) (0.1) (0.1) (0.1) (0.1)$$

This provides a means to check on the adequacy of the estimated ARCH\GARCH model. Standardize the residuals e by the conditional standard deviation from the fitted ARCH\GARCH model σ_t to get (e_t/σ_t) . If the ARCH\GARCH model is adequate, then the standardized residuals should be uncorrelated and homoscedastic. Standard tests can be applied to the standardized residuals to see whether that is the case.

Finally, the standardized residuals should appear normally distributed. When the assumption of conditional normality does not hold, the ARCH\GARCH parameter estimates will still be consistent provided the mean and variance equations are correctly specified. However, the standard errors are no longer correct. In this case, we treat the log-likelihood function as being approximately correct but calculate robust standard errors. This approach is known as Quasi-Maximum Likelihood and the resulting standard errors are known as Bollerslev-Wooldridge standard errors. The Jarque-Bera test can be applied to the standardized residuals to test for normality.

6. An Application to the NYSE Composite Index

Figure 1 shows a graph of the percentage daily logarithmic change in the NYSE Composite Index (which is the percentage daily log return, denoted sr_t) over the period

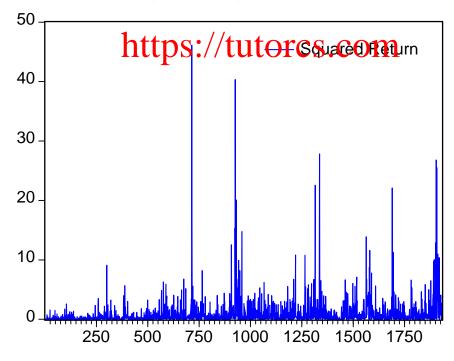
January 3, 1995 to August 30, 2002, a total of 1,931 observations. Figure 2 shows a graph of the squared return that s, s_i^2 . Usuallity clustering is appropriate that the paper whereby large changes tend to be followed by large changes and small changes by small changes.

Figure 1: Daily I January 3.

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Figure 2: NYSE Composite Log Squared Returns

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On the basis of the autocorrelation and partial autocorrelation function for returns (that is, for sr_t), it was decided to find MA(1) its delfor returns. The refuls are reported in Table 1 where it can be seen that the coefficient on the MA(1) term is statistically significant. An LM test for ARCH\GARCH effects is applied to the estimated residuals from the material are reported in Table 2.

 Table 1: Estimation
 Table 1: Estimation

Output

Description:

Outpu

Dependent Variabl	Tutor CS	.			
Variable	IND YEAR	St	d. Error	t-Statistic	Prob.
С			0.024568	1.437292	0.1508
Dependent Variable Variable C MA(1)	ह्या. २ अस्पूर्	/ 	0.02271	3.310311	0.0009

R-squared	0.005155	Mean dependent var	0.0353
Adjusted R-squared S.E. of regression	0004639	601 dependent vec	1.006207
S.E. of regression	1.003871	Akaike info criterion	2.84664
Sum squared resid	1942.955	Schwarz criterion	2.852407
Log likelihood	-2745.007	F-statistic	9.989889

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Table 2: LM Test for ARCH Effects in Residuals from MA(1) Model for Stock Hearth 211: LULOTCS @ 163.COM

ARCH Test: F-statistic Obs*R-squared Dependent Variable: R	_	AFCObabili	-	0.0000
Variable	Coefficient	Std. Error	t-Statistic	Prob.
c h ₁	101462217	/010681 06	16.78 67 03	P:0000
RESID^2(-1)	0 142459	0.022803	6.247313	0.0000
RESID^2(-2)	0.075486	0.023027	3.278114	0.0011
RESID^2(-3)	0.11154	0.022954	4.859341	0.0000
RESID^2(-4)	0.010104	0.023093	0.43754	0.6618
RESID^2(-5)	0.110557	0.022955	4.81633	0.0000
RESID^2(-6)	0.026927	0.023041	1.168689	0.2427
RESID^2(-7)	0.066393	0.022816	2.909882	0.0037
R-squared	0.094366	Mean de	pendent var	1.010337
Adjusted R-squared	0.091056	S.D. dependent var		2.507305
S.E. of regression	2.390429	Akaike info criterion		4.584974
Sum squared resid	10942.6	Schwarz criterion		4.608112
Log likelihood	-4400.45	F-statistic	С	28.5059
Durbin-Watson stat	2.003779	Prob(F-s	tatistic)	0

In Table 2, the TR statistic 518.47, i Dighl significant with Thus, the null hypothesis of no ARCH\GARCH effects is emphatically rejected. Many of the lagged squared residuals are statistically significant indicating that volatility clustering is a fea

varying volatility in the returns on the NYSE As a first nodel to sr_i . The results are shown in Table 3. index, we fitted a of as comprising a mean equation for sr_t , specified Here the model for quation for sr_t , specified as an ARCH(5) process. as an MA(1) proc Both are estimate Lod of maximum likelihood. All the coefficients in the ARCH specifi that the conditional variance is always positive, and the coefficients on the lagged squared residuals sum to 0.731, a number less than one as required for a finite unconditional variance. The estimated coefficients on the lagged squared residuals are all statistically significant. This suggests that even higher-order ARCH models may be required clowever, ARCH type models with long lags are not parsimonious and it is usually preferable to estimate a GARCH(1,1) specification for the variance equation.

Table 3: Estimation of MA(S-ARCH(S) Moder for Stock Returns X am Help

Dependent Variable: SR Method: ML - ARCH (Marquardi) Normal tiestileutions @ 163.com

Included observations: 1930 after adjustments

Convergence achieved after 14 iterations

MA backcast: 1, Variance backcast: DN 2 Q GARCH = C(3) + C(4) RESID(-1)^2 + C(5) RESID(-2)^2 C(6)*RESID(

-3)^2 + C(7)*RESID(-4)^2 + C(8)*RESID(-5)^2

Mean Equation

	iviean Equation			
,	44Coefficient/4.	Std Error	z-Statistic	Prob.
C	http://phi/t	0.020863	3.509306	0.0004
MA(1)	0.112154	0.024659	4.548241	0.0000
	Variance Equati	on		
0	•		4 4 4 4 0 0	0.0000
С	0.328317	0.023205	14.1483	0.0000
RESID(-1)^2	0.163148	0.022114	7.377523	0.0000
RESID(-2)^2	0.256414	0.02566	9.992863	0.0000
RESID(-3)^2	0.086334	0.024299	3.553029	0.0004
RESID(-4)^2	0.163758	0.028341	5.778146	0.0000
RESID(-5)^2	0.061118	0.026263	2.327107	0.0200
R-squared	0.002734	Mean dep	endent var	0.0353
Adjusted R-squared	d -0.000898	S.D. dependent var		1.006207
S.E. of regression	1.006659	Akaike info criterion		2.661503
Sum squared resid	1947.682	Schwarz	criterion	2.684571
Log likelihood	-2560.35	F-statistic	;	0.752859
Durbin-Watson stat	2.074987	Prob(F-st	atistic)	0.627095

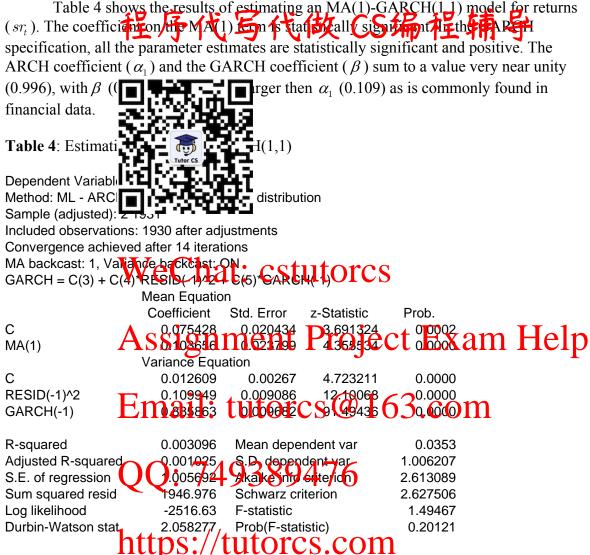


Table 5 shows the results of performing an LM test for remaining heteroscedasticity (that is, ARCH\GARCH effects) in the standardized MA(1)-GARCH(1,1) residuals. The TR^2 statistic of 3.87 is not statistically significant at conventional significance levels (it has a p-value of 0.57). Furthermore, in the auxiliary regression, none of the coefficients on the lagged squared standardized residuals are significant indicating that there is no remaining heteroscedasticity to be modeled.

Table 5: LM Test 存在其中 frect 写 Standal to de les Sus 编译 辅导 MA(1)-GARCH(1,1) Model



Figure 3 presents a histogram of the standardized MA(1)-GARCH(1,1) residuals and associated summary statistics. The distribution appears symmetric and fat-tailed. The coefficient of kurtosis is quite high and the Jarque-Bera test clearly rejects normality. This suggests that the standard errors reported in Table 1 and not correct and that robust standard errors should be used instead. Table 6 reports estimates of the MA(1)-GARCH(1,1) model for returns with robust standard errors. Notice the coefficient estimates do not change just the standard errors. Nevertheless on the basis of the robust (Bollerslev-Wooldridge) standard errors there is no change in inference in this case.

程序代写代做 CS编程辅导 Figure 3: Histogram of Standardized Residuals from MA(1)-GARCH(1,1) Model

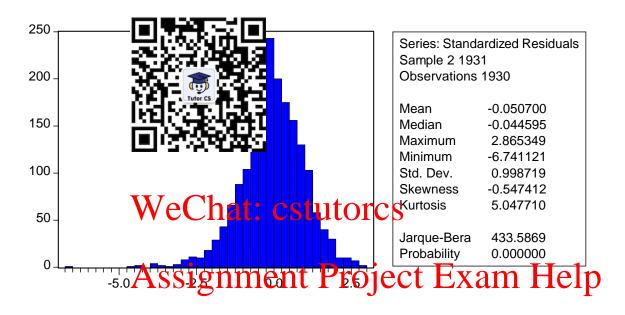


Table 6: MA(1)-GARCH(1,1) Model for Returns with Robust Standard Errors Email: tutorcs @ 103.com

Dependent Variable: SR

Method: ML - ARCH (Marquardt) - Normal distribution

Sample (adjusted): 21931 After adjustments 9476

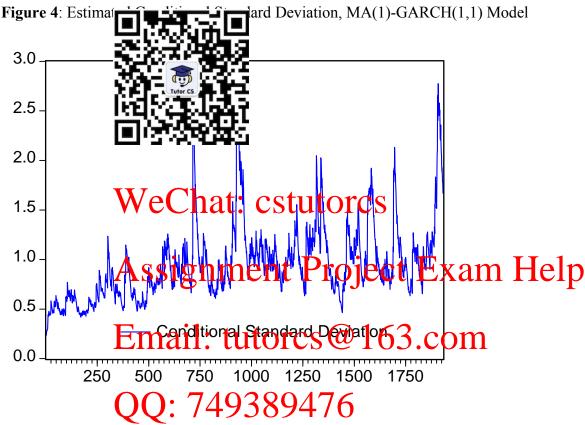
Convergence achieved after 14 iterations

Bollerslev-Wooldrige robust standard errors & covariance

MA backcast: 1, Variance backcast: QN

	Mean Equa	lion			
	Coefficient	Std. Error	z-Statistic	Prob.	
С	0.075428	0.018001	4.190173	0.0000	
MA(1)	0.103656	0.026223	3.952926	0.0001	
Variance Equation					
С	0.012609	0.004079	3.091308	0.0020	
RESID(-1)^2	0.109949	0.023523	4.674078	0.0000	
GARCH(-1)	0.885863	0.01969	44.99032	0.0000	
R-squared	0.003096	Mean dep	endent var	0.0353	
Adjusted R-squared	0.001025	S.D. dependent var		1.006207	
S.E. of regression	1.005692	Akaike info criterion		2.613089	
Sum squared resid	1946.976	Schwarz criterion		2.627506	
Log likelihood	-2516.63	F-statistic		1.49467	
Durbin-Watson stat	2.058277	Prob(F-sta	atistic)	0.20121	

Figure 4 shows the time series of the estimated conditional standard deviation implied by the estimated MA(1) GARGH(11) Library labels. Clearly planting a great deal and is highly volatile.



Now we estimate the MA(1)-GARCH(1,1) model for returns using observations 1-1531, leaving 400 observations for use in an out-of-sample forecasting exercise. Specifically, the MA(1)-GARCH(11) model for returns is estimated over observations 1-1531 and used to generate a dynamic forecast of the conditional standard deviation for the out-of-sample observations 1532-1931. The results are shown in Figure 5. The forecast begins just following a reduction in volatility (that is, in the conditional standard deviation). The forecast is for a gradual increase in volatility. The long-run volatility forecast is the unconditional standard deviation of sr_t . Letting b_1 denote the MA(1) coefficient, the formula for the unconditional variance is

$$\begin{split} \operatorname{var}(sr_t) &= (1 + b_1^2) \operatorname{var}(\boldsymbol{\varepsilon}_t) \\ &= \frac{(1 + b_1^2) \alpha_0}{1 - (\alpha_1 + \boldsymbol{\beta})} = \frac{(1 + (0.1037)^2) 0.0126}{1 - (0.1099 + 0.8859)} = 3.0323 \end{split}$$

Thus, $\sigma = 1.7413$ which is the value the forecast of the conditional standard deviation is approaching in Figure 5.



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