### University of New South Wales, School of Economics

## 程序代码的S编程辅导

Question 1. Consider

$$y_{t} = \alpha + b_{t}y_{t}$$

$$N(0, \sigma^{2})$$

 $(y_t)$  and  $corr(y_t, y_{t-i})$  for i = 1, 2. Calculate unc (a)

$$E(y_t) = \alpha + b_1 E(y_{t-1}) + E(\varepsilon_t) = \alpha + b_1 E(y_{t-1}) + 0$$

Impose stationarity:  $E(y_{t}) = E(y_{t-1})$  (because for non-stationary time-series unconditional mean does not exist).

 $E(y_t) = \frac{\alpha}{1-h}$  Assignment Project Exam Help

In a similar way Email: tutorcs@163.com

$$var(y_t) = 0 + b_1^2 var(y_{t-1}) + \sigma^2$$

$$var(y_t) = \frac{\sigma^2 Q}{1-b} Q: 749389476$$

$$corr(y_t, y_{t-i}) = cov(y_t, y_{t-i}) / var(y_t)$$
**https://tutorcs.com**

We are going to use the fact that covariance is a linear operator in each of its arguments

and assume stationarity

Proof of linearity (just as illustration), x, y, z -random variables; a, b - constants:

$$cov(a + bx + y, z) = E[(a + bx + y - E(a + bx + y))(z - E(z))] =$$

$$= E[(a - E(a))(z - E(z)) + (bx - E(bx))(z - E(z)) + (y - E(y))(z - E(z))] =$$

$$= 0 + bE[(x - E(x))(z - E(z))] + E[(y - E(y))(z - E(z))] = b cov(x, z) + cov(y, z)$$

$$cov(y_{t}, y_{t-1}) = cov(\alpha + b_{t}y_{t-1} + \varepsilon_{t}, y_{t-1}) = cov(\alpha, y_{t-1}) + cov(b_{t}y_{t-1}, y_{t-1}) + cov(\varepsilon_{t}, y_{t-1}) = 0 + b_{t} var(y_{t}) + 0$$

The last zero follows because of the assumption of white noise for  $\varepsilon_{t}$  . This implies that  $\mathcal{E}_t$  uncorrelated with all past  $\mathcal{E}_{t-i}$  and hence past  $y_{t-i}$ . Note that all future  $y_{t+i}$  are correlated with  $\varepsilon_t$ . The shock lives in the AR model infinitely.

Also note that you could derive the expression for covariance using the ask definition of the covariance. The expression would be more redical, but the result would be the same.



What is the (optimal) forecast of  $y_{t+i}$ , for i = 1,2 on the basis of time t information? (b)

$$E(y_{t+1} \mid \Omega_t) = \alpha + by_t$$

$$E(y_{t+1} \mid \Omega_t) = \alpha + by_t$$

 $E(y_{t+2} \mid \Omega_t) = \alpha + b_1(\alpha + by_t)$  Assignment Project Exam HelpCalculate conditional variance  $var(y_{t+1} \mid \Omega_t)$  and form confidence interval for forecast.

(c)

$$\operatorname{var}(y_{t+1} \mid \Omega_t) = \sigma^2 \text{ as } \alpha + b_t y_t \text{ is a constant under } \Omega$$
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CI:  $\alpha + by_t \pm s\sigma$ , where s depends on the confidence level s=1.96 at 95% confidence.

Is  $y_t$  a white nois process 749389476(d)

 $y_t$  is white noise when  $b_1 = 0$ , but typically it is not a white noise process.

https://tutorcs.com When  $y_t$  is a covariance stationary process?

(e)

 $y_t$  is covariance stationary  $|b_t| < 1$ 

(f) Think about an economic example where AR(1) is relevant?

Many economic aggregates like unemployment or GDP are AR(1).

Question 2. Suppose that a researcher estimated the lag 1 autocorrelation coefficient using a series of T=100 observations and found at to be equally 0.75 Is the autocorrelation coefficient significantly different from 0.75 pecify the null hypothesis, the alternative, test statistics, null distribution and decision criterion.

In case of two sided t

Ho:  $\rho_1 = 0$ . Ha:  $\rho_1 = 0$ 

 $\frac{1}{T}$ ), Test stat =  $\frac{0.15}{1/\sqrt{100}} = 1.5$ 

**autocorrelations** 

Need to specify signided becision: fail to reject different from 0.

ically 5%. Decision rule: -1.96 < Test stat< 1.96 e of the autocorrelation coefficient is not significantly

Question 4.

Let  $f_{t+h|t}$  be the forecast of Parametric Interest on of elements in  $\Omega_t$ . Which  $f_{t+h|t}$  minimises the mean square forecast error (MSFE)?

 $MSFE = E[(y_{t+h} - f_{t+h|t})^{2} | \Omega_{t}].$  Assignment Project Exam HelpConditional mean  $E[y_{t+h} | \Omega_{t}]$  is the best forecast in terms of the MSFE criterion

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\*Formal proof

Option 1. Explicitly write down the definition of the integral

$$MSFE = E[(y_{t+h} - f_{t+h})^{2} | \Omega_{t}] = \int y_{t+h}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} - 2 \int y_{t+h} f_{t+h|t} g(y_{t+h} | \Omega_{t}) dy_{t+h} + \int f_{t+h|t}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} = \int y_{t+h}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} - 2 \int y_{t+h} f_{t+h|t} g(y_{t+h} | \Omega_{t}) dy_{t+h} + \int f_{t+h|t}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} = \int y_{t+h}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} - 2 \int f_{t+h|t} E(y_{t+h} | \Omega_{t}) + \int f_{t+h|t}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} = \int y_{t+h}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} - 2 \int f_{t+h|t} E(y_{t+h} | \Omega_{t}) + \int f_{t+h|t}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} = \int y_{t+h}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} - 2 \int f_{t+h|t} E(y_{t+h} | \Omega_{t}) dy_{t+h} + \int f_{t+h|t}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} = \int y_{t+h}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} - 2 \int f_{t+h|t} E(y_{t+h} | \Omega_{t}) dy_{t+h} + \int f_{t+h|t}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} = \int y_{t+h}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} - 2 \int f_{t+h|t} E(y_{t+h} | \Omega_{t}) dy_{t+h} + \int f_{t+h|t}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} = \int y_{t+h}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} - 2 \int f_{t+h|t} E(y_{t+h} | \Omega_{t}) dy_{t+h} + \int f_{t+h|t}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} = \int y_{t+h}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} + \int f_{t+h|t}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} + \int f_{t+h|t}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} = \int y_{t+h}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} + \int f_{t+h|t}^{2} g(y_{t+h} | \Omega_{t}) dy_{t+h} + \int f_{t+h|t}^{2$$

Note we took out f outside of integral because it is not a function of  $y_{t+h}$ . We also used the fact that proper (conditional) density g integrates toward one and the definition of the conditional expectation.

FOC:

$$\frac{\partial MSFE}{\partial f_{t+h|t}} = -2E(y_{t+h} \mid \Omega_t) + 2f_{t+h|t} \equiv 0 \rightarrow f_{t+h|t}^* = E(y_{t+h} \mid \Omega_t)$$

SOC:

$$\frac{\partial^2 MSFE}{\partial f_{t+h|t}^2} = 2 > 0 \rightarrow \text{true minimum}$$

Option 2. Subtract and add the correct answer in the squared term.

$$MSFE = E[(y_{t+h} - f_{t+h|t}) | \Omega_t] + E[(y_{t+h} - E(y_{t+h} | \Omega_t)) + E(y_{t+h} | \Omega_t) + E(y_{t+h} | \Omega_$$

The first term of the 1 hand not a function of f and the third term if quadratic in f. Hence, if we show the show the state of the

$$E[(y_{t+h} - E(y_{t+h} \mid \Omega_t) - f_{t+h|t}) E[(y_{t+h} - E(y_{t+h} \mid \Omega_t)) \mid \Omega_t] = 0$$

$$E(y_{t+h} \mid \Omega_t) - f_{t+h|t} \text{ is just a constant under } \Omega_t \text{ and can be taken outside of the conditional}$$
expectation. Then, we just apply the expectation operator sequentially.

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Email: tutorcs@163.com

QQ: 749389476

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### **QUESTION**

Consider the



AR(1) model:

$$\alpha + b_1 y_{t-1} + \epsilon_t$$

To find the OI imize the sum of squared residuals:

$$SSR = \sum_{t=1}^{T} (y_t - \alpha - b_1 y_{t-1})^2$$
 (1)

WeChat: 
$$\underbrace{cstutorcs}_{\partial \hat{\alpha}} = -2\sum_{t}^{t} (y_{t} - \hat{\alpha} - \hat{b}_{1}y_{t-1}) = 0$$
 (2)

## Assignmenta Project Exam Help

# Email: $tuter{\hat{o}rcs} = \hat{e}^2 \hat{f}_{t}^T \hat{e}_{3}^T \hat{e}_{3}^T \hat{e}_{5}^T \hat{e}_{5}^T$

$$\sum_{t}^{T} y_{t-1} y_{t} - \hat{\alpha} \sum_{t} y_{t-1} - \hat{b}_{1} \sum_{t} y_{t-1}^{2} = 0$$

$$\mathbf{QQ: 749389476}$$
(5)

After substituting  $\hat{\alpha}$  and solving for  $b_1$ 

$$= \frac{\frac{1}{T} \sum_{t} y_{t-1} y_{t} - \frac{1}{T^{2}} \sum_{t} y_{t} \sum_{t} y_{t-1}}{\frac{1}{T} \sum_{t} y_{t-1}^{2} - \frac{1}{T^{2}} (\sum_{t} y_{t-1})^{2}}$$
(7)

$$\to \frac{E(y_{t-1}y_t) - E^2(y_t)}{E(y_t^2) - E^2(y_t)} \tag{8}$$

Now let us check the properties of this estimator in terms of bias and consistency.

$$\hat{b}_1 = \frac{\sum_t y_{t-1}(\alpha + b_1 y_{t-1} + \epsilon_t) - \frac{1}{T} \sum_t (\alpha + b_1 y_{t-1} + \epsilon_t) \sum_t y_{t-1}}{\sum_t y_{t-1}^2 - \frac{1}{T} (\sum_t y_{t-1})^2}$$
(9)

$$\hat{b}_1 = b_1 + \frac{\sum_{t=2}^T y_{t-1} \epsilon_t - \frac{1}{T} \cdot \sum_{t=2}^T \epsilon_t \sum_{t=2}^T y_{t-1}}{\sum_{t=2}^T y_{t-1}^2 - \frac{1}{T} (\sum_{t=2}^T y_{t-1})^2}$$
(10)

Taking unconditional expectation:

$$E\left(\hat{b}_{1}\right) = b_{1} + E\left[\frac{\sum_{t=2}^{T} y_{t-1} \epsilon_{t} - \frac{1}{T} \cdot \sum_{t=2}^{T} \epsilon_{t} \sum_{t=2}^{T} y_{t-1}}{\sum_{t=2}^{T} y_{t-1}^{2} - \frac{1}{T} (\sum_{t=2}^{T} y_{t-1})^{2}}\right]$$

$$= b_{1} + E\left[\frac{\sum_{t=2}^{T} y_{t-1} \epsilon_{t}}{\sum_{t=2}^{T} y_{t-1}^{2} - \frac{1}{T} (\sum_{t=2}^{T} y_{t-1})^{2}}\right] - \frac{1}{T} E\left[\frac{(\sum_{t=2}^{T} \epsilon_{t})(\sum_{t=2}^{T} y_{t-1})}{\sum_{t=2}^{T} y_{t-1}^{2} - \frac{1}{T} (\sum_{t=2}^{T} y_{t-1})^{2}}\right]$$

$$(11)$$

Now, even with  $E(\epsilon_t|y_{t-1})=0$ , we cannot write that  $E\left(\sum_{t=2}^T \epsilon_t\right)(\sum_{t=2}^T y_{t-1})=0$ , because  $\epsilon_t$  and  $E(\epsilon_t|y_{t-1})=0$ . We cannot write that  $E(y_t|y_t)=0$ . We product of the two sums and use the fact that  $E(E(\epsilon_t|y_{t-1}))=0$ .

$$E\left(\sum_{t=2}^{T} \epsilon_{t}\right)\left(\sum_{t=2}^{T} y_{t-1}\right) \neq E\left(\sum_{t=2}^{T} E(\epsilon_{t}|y_{t-1})\left(\sum_{t=2}^{T} y_{t-1}\right)\right)$$

For the first expectation, we have the same issue, even if  $\epsilon_t$  and  $y_{t-1}$  are independent,  $\epsilon_t$  is not independent from the numerator  $\sum_{t=2}^T y_{t-1}^2 - \frac{1}{T}(\sum_{t=2}^T y_{t-1})^2$ , therefore, we cannot separate the two expressions in the fraction:

$$E\begin{bmatrix} \underbrace{\sum_{t=2}^{T} y_{t-1} \epsilon_{t}}_{\sum_{t=2}^{T} y_{t-1}^{2} - \frac{1}{T} (\sum_{t=2}^{T} y_{t-1})^{2}} = E \begin{bmatrix} \underbrace{\sum_{t=2}^{T} y_{t-1}}_{\sum_{t=2}^{T} y_{t-1}^{2} - \frac{1}{T} (\sum_{t=2}^{T} y_{t-1})^{2}} \epsilon_{t} \end{bmatrix} (12)$$

$$Email: tutorcs \begin{bmatrix} \underbrace{\underbrace{\sum_{t=2}^{T} y_{t-1}^{2} - \frac{1}{T} (\sum_{t=2}^{T} y_{t-1})^{2}}} \\ \underbrace{\underbrace{\underbrace{\sum_{t=2}^{T} y_{t-1}^{2} - \frac{1}{T} (\sum_{t=2}^{T} y_{t-1})^{2}}} \end{bmatrix} E(\epsilon_{t}|y_{t-1}) \end{bmatrix}$$

OLS is BIASIDA the AR (40 and 8 pm ) moles

In this question, to show asymptotic normality, we do not need unbiased estimator. We can use the LLN and CLT.

The LLN give T is the solution of averages, so every sum term is divided by T:

$$\begin{aligned}
\text{plim } \left(\hat{b}_{1}\right) &= b_{1} + \text{plim } \left[\frac{\sum_{t=2}^{T} y_{t-1} \epsilon_{t} - \frac{1}{T} \cdot \sum_{t=2}^{T} \epsilon_{t} \sum_{t=2}^{T} y_{t-1}}{\sum_{t=2}^{T} y_{t-1}^{2} - \frac{1}{T} (\sum_{t=2}^{T} y_{t-1})^{2}}\right] & (13) \\
&= b_{1} + \text{plim } \left[\frac{\sum_{t=2}^{T} y_{t-1} \epsilon_{t} / T}{\sum_{t=2}^{T} y_{t-1}^{2} / T - \frac{1}{T^{2}} (\sum_{t=2}^{T} y_{t-1})^{2}}\right] & (14) \\
&- \text{plim } \left[\frac{(\sum_{t=2}^{T} \epsilon_{t} / T) (\sum_{t=2}^{T} y_{t-1} / T)}{\sum_{t=2}^{T} y_{t-1}^{2} / T - \frac{1}{T^{2}} (\sum_{t=2}^{T} y_{t-1})^{2}}\right]
\end{aligned}$$

By the LLN, each average converges to the expected value of its argument:

$$p\lim_{t=2}^{T} \epsilon_t / T = E(\epsilon_T) = 0, \tag{15}$$

$$\operatorname{plim} \sum_{t=2}^{T} y_{t-1} \epsilon_t / T = E(y_{t-1} \epsilon_t) = E(y_{t-1} E(\epsilon_t | y_{t-1})) = 0$$
 (16)

We get the result: plim  $\hat{b}_1 = b_1$  which is equal to zero under the null hyporthesis

in the question how asymptotic normality, we use the CLT:

plim 
$$\left(\sum_{t=2}^{T} y_{t-1} \epsilon_t / \sqrt{T}\right)$$

$$\left(\sum_{t=2}^{T} y_{t-1}^2 / T - \frac{1}{T^2} (\sum_{t=2}^{T} y_{t-1})^2\right)$$

$$\left[\sum_{t=2}^{T} \epsilon_t / \sqrt{T}\right) (\text{plim } \sum_{t=2}^{T} y_{t-1} / T)$$

$$\text{plim } \left(\sum_{t=2}^{T} y_{t-1}^2 / T - \frac{1}{T^2} (\sum_{t=2}^{T} y_{t-1})^2\right)$$

For simplicity, let us call  $Q = \text{plim} \left(\sum_{t=2}^{t} y_{t-1}/T \leq \frac{1}{T^2} (\sum_{t=2}^{T} y_{t-1})^2\right)$  and assume that it exists. Which will because  $Q = V(y_{t-1})$  and stationarity it should be finite. We also assume that  $\mu = \text{plim} \sum_{t=1}^{T} y_{t-1}^2 / T = E(y_{t-1})$  exists and finite (under stationarity). Significantly  $P = \text{plim} \sum_{t=1}^{T} y_{t-1}^2 / T = E(y_{t-1})$  exists and finite p

Email:=
$$tu \frac{\int_{t=0}^{\text{plim}} \left(\sum_{t=0}^{T} y_{t-1} \epsilon_t / \sqrt{T}\right)}{torcs} com$$
(18)

QQ: 749  $\left[389476\right]$ 

By CLT, we know that if  $Z_t$  is  $N(0,\sigma^2)$ , then  $\frac{\sum_t Z_t}{\sqrt{T}}$  is approximately normal  $N(0,\sigma^2)$ . The articles://tutores.com

$$\sum_{t=2}^{T} y_{t-1} \epsilon_t / \sqrt{T} \sim N\left(0, \sigma^2 \text{plim } \frac{\sum_t y_{t-1}^2}{T}\right)$$
 (19)

$$\sum_{t=2}^{T} \epsilon_t / \sqrt{T} \sim N(0, \sigma^2)$$
 (20)

Using properties of normally distributed random variables: for any constant c, and X that is N(a, b), cX is  $N(a, c^2b)$ .

$$\sqrt{T}\hat{b}_1 \sim \frac{1}{Q} N\left(0, \sigma^2 \operatorname{plim} \frac{\sum_t y_{t-1}^2}{T}\right) - \frac{E(y_{t-1})}{Q} N(0, \sigma^2)$$
 (21)

$$\sim N(0, \sigma^2 V) \tag{22}$$

$$V = \left( \text{plim} \frac{\sum_{t} y_{t-1}^{2}}{T} - E(y_{t-1})^{2} \right) / Q^{2} = 1/Q = 1/V(y_{t})$$
 (23)

$$V(y_t) = \sigma^2/(1 - b_1^2) (24)$$

$$V = (1 - b_1^2)/\sigma^2 (25)$$

Therefore,  $\sqrt{T}\hat{b}_1 \sim N(0,(1-b_1^2))$ . Under the null hypothesis of  $b_1=0$ , we have  $\sqrt{T}\hat{b}_1 \sim N(0,1)$ , which means that we can approximate the distribution of  $\hat{b}_1$  with N(0,1/T).

CAPMGEGO
une 24, 2021

1 Calculate t market eturns of T-Bill, gold, GE stock and

```
[92]: import pandas as pd
     import numpy as new chat: cstutorcs
[93]: data = pd.read_csv("C:\\Users\\rluck\\OneDrive\\capm.csv", header=[4])
                                               Project Exam Help
[93]:
                  DATE
                                  S&P500
                           Gold
                                   87.12 6.40
            12/08/1975
                         166.05
                                                 0.9218
     1
            13/08/1975
                         163 59
                                                0 9936
            14/08/1975
     3
            15/08/1975
                         163.50
                                   86.36
                                          6.42
                                                 0.9244
                                   86.20
            18/08/1975
                         163.50
                                                 0.9348
     10432
             6/08/2015
                        1090.15
                                 2083.56
                                          0.04
                       1096.85
                                          0.06
     10433
             7/08/2015
                                 2077.57
                                                25.7900
            10/08/2015 1103.35
                                 2104.18 0.12
                                                26.2400
     10434
     10435
            11/08/2015 11(19.) $ 2081 07 (0.11) $5 (710) []
            12/08/2015 1123.85
     10436
                                 2086.05 0.10
     [10437 rows x 5 columns]
     #Computing log returns: R_gold = 100*ln(P_g/P_{g-1})
     Rf = 100/360*ln(1+rf)
[94]: data['R gold']=100*np.log(data['Gold']/data['Gold'].shift(1))
     data['R f'] = 100/360*np.log(1+data['Rf']/100)
     data['R GE'] = 100*np.log(data['GE']/data['GE'].shift(1))
     data['R_m'] = 100*np.log(data['S\&P500']/data['S\&P500'].shift(1))
     print(data.head())
              DATE
                      Gold S&P500
                                     Rf
                                             GE
                                                   R_{gold}
                                                                         R_GE \
                                                                R_f
     0 12/08/1975
                   166.05
                             87.12 6.40
                                         0.9218
                                                      {\tt NaN}
                                                           0.017232
                                                                          NaN
     1 13/08/1975 163.50
                                   6.45 0.9036 -1.547596 0.017363 -1.994150
                             85.97
     2 14/08/1975 163.50
                             85.60 6.45 0.9036 0.000000 0.017363 0.000000
```

```
R_m
0 NaN
1 -1.328808
2 -0.431312
3 0.883932
4 -0.185443
```

### Calculating Fig. 5 for gold and GE

```
[95]: data['R_p']= data['R_m']- data['R_f']
data['R_ge']= data['R_GE']-data['R_f']
data['R_go']= data['R_GE']-data['R_f']
data['R_go']= data['R_GE']-data['R_f']
```

```
R_gq1d
[95]:
                            Gold
                                   S&P500
                   DATE
                          186.050
                                   BM221140
                                                  ONDIBECT INVOINGE
      0
             12/08/1975
                          163.50
                                                  0.9036 - 1.547596
             13/08/1975
      1
                                    85.97
                                           6.45
                                                                    0.017363
      2
             14/08/1975
                          163.50
                                    85.60
                                           6.45
                                                  0.9036
                                                          0.000000
                                                                    0.017363
      3
             15/08/1975
                         163.50
                                    86.36
                                                           0.000000
                                                                     0.017284
                                   .86Lbd L6/42
                                                          000000 00.017284
      4
             18/08/1975
                                  2083.56 0.04
                                                 26.0300
      10432
              6/08/2015 1090.15
                                                          0.415484 0.000111
      10433
             7/08/2015
                         1096 85
                                                          0.612713
                                                                     0.000167
                         1103.35
      10434
             10/08/2015
                                  2104.18
                                                          0.590857
                                                                     0.000333
      10435
             11/08/2015
                         1109.67
                                  2084.07
                                           0.10
                                                 25.7100
                                                          0.571167
                                                                     0.000278
      10436
             12/08/2015
                         1123.85
                                  2086.05
                                           0.10
                                                 25.8600
                                                          1.269762 0.000278
                 R GE
      0
                  {\tt NaN}
                            NaN
                                      {\tt NaN}
                                                NaN
                                                          NaN
      1
            -1.994150 -1.328808 -1.346171 -2.011512 -1.564958
      2
             0.000000 -0.431312 -0.448674 -0.017363 -0.017363
      3
             2.275809 0.883932 0.866648
                                          2.258525 -0.017284
             1.118772 -0.185443 -0.202727
                                           1.101488 -0.017284
      10432 -0.268560 -0.778318 -0.778429 -0.268671
                                                     0.415373
      10433 -0.926290 -0.287903 -0.288069 -0.926457
                                                     0.612547
      10434 1.729814 1.272690 1.272357
                                           1.729481
                                                     0.590524
      10435 -2.040494 -0.960313 -0.960591 -2.040772
                                                     0.570889
      10436 0.581735 0.094961 0.094684 0.581458
                                                     1.269484
```

[10437 rows x 12 columns]

```
Data: Remove N
                                                                               代做 CS编程辅导
[96]: data = data.dropna(subset
           data.to_csv("C:\\Users
                                                            luck\\OneDrive\\capm1.csv")
           data.head()
[96]:
                            DATE
                                                                                        GE
                                                                                                   R_{gold}
                                                                                                                            R_f
                                                                                                                                             R_GE \
           1 13/08/1975
                                                                                0.9036 -1.547596 0.017363 -1.994150
           2 14/08/1975
                                                                                               0.000000 0.017363 0.000000
           3 15/08/1975
                                                                                               0.000000 0.017284 2.275809
           4 18/08/1975
                                                                                               0.000000 0.017284 1.118772
           5 19/08/1975
                                                                                0.9218
                                                                                               0.000000 0.017415 -1.400432
                                             R_p
                          R m
                                                               R_ge
                                                                                  R go
           1 -1.328808 -1.3461717 -2 011512 -1.564958
           2 -0.431312 -0.448 COLDER CONTROL OF STUTORCS
           3 0.883932 0.866648
                                                       2.258525 -0.017284
           4 -0.185443 -0.202727
                                                       1.101488 -0.017284
           5 -1.460733 -1.478 48 -4
                                                                         nent Project Exam Help
[97]: !pip install sklearn
            !pip install statsmodels
          Requirement already
          packages (0.0)
          Requirement already satisfied: scikit-learn in
          c:\users\rluck\anatoma3\lib\site=\ackges\from sklearn) (0.24.1)
          Requirement already satisfied: scipy>=0.19.1 in
          c:\users\rluck\anaconda3\lib\site-packages (from scikit-learn->sklearn) (1.6.2)
          Requirement already satisfied:, joblib>=0.11 in
          c:\users\rluck\ana \data \data \sigma \data \dat
          Requirement already satisfied: numpy>=1.13.3 in
          c:\users\rluck\anaconda3\lib\site-packages (from scikit-learn->sklearn) (1.20.1)
          Requirement already satisfied: threadpoolct1>=2.0.0 in
          c:\users\rluck\anaconda3\lib\site-packages (from scikit-learn->sklearn) (2.1.0)
          Requirement already satisfied: statsmodels in c:\users\rluck\anaconda3\lib\site-
          packages (0.12.2)
          Requirement already satisfied: numpy>=1.15 in c:\users\rluck\anaconda3\lib\site-
          packages (from statsmodels) (1.20.1)
          Requirement already satisfied: scipy>=1.1 in c:\users\rluck\anaconda3\lib\site-
          packages (from statsmodels) (1.6.2)
          Requirement already satisfied: pandas>=0.21 in
          c:\users\rluck\anaconda3\lib\site-packages (from statsmodels) (1.2.4)
          Requirement already satisfied: patsy>=0.5 in c:\users\rluck\anaconda3\lib\site-
          packages (from statsmodels) (0.5.1)
          Requirement already satisfied: python-dateutil>=2.7.3 in
          c:\users\rluck\anaconda3\lib\site-packages (from pandas>=0.21->statsmodels)
          (2.8.1)
```

```
Requirement already satisfied: pytz>=2017.3 in c:\users\rluck\anacorda3\frac{1}{12}\stackages from panacorda3\lib\site-packages (2021.1)

Requirement already satisfied: six in c:\users\rluck\anaconda3\lib\site-packages (from patsy>=0.5->

"matplotlib inlin import statsmodel import statsmodel from sklearn import import matplotlib

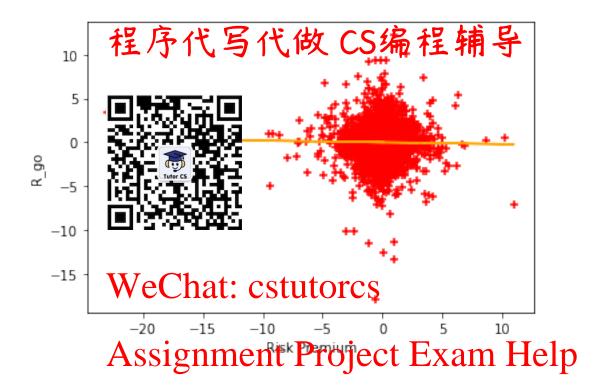
"Totor cs | mf
```

### 4 I. Plotting Gold excess returns with market excess returns

```
[99]: #Regressing excess with the last the state of the s
```

[100]: [<matplotlib.lines.Line2D at 0x18397b4e220>]

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```
[101]: #model with interEmail: tutores@163.com
     X= sm.add_constant(X)
```

model = sm.OLS(y1,X).fit() predictions = model predict 749389476 j= (model.summary())

-0.0201

print(j)

R\_p

https://tutores.com

===========	=====;	=======		=====	=========		
Dep. Variable:	R_go			R-squ	ared:	0.000	
Model:	OLS			Adj. R-squared:			0.000
Method:	Least Squares			F-statistic:			3.181
Date:	Thu, 24 Jun 2021			Prob (F-statistic):			0.0745
Time:	13:42:13			Log-Likelihood:			-16959.
No. Observations:	10436			AIC:			3.392e+04
Df Residuals:	10434			BIC:		3.394e+04	
Df Model:			1				
Covariance Type:	nonrol	oust					
============	======			=====	========		
	coef	std err		t	P> t	[0.025	0.975]
const 0.	0057	0.012	0	.473	0.637	-0.018	0.029

Omnibus: 2812.110 Durbin-Watson: 2.071

-1.784

0.011

0.075

-0.042

0.002

Prob(Omnibus):

Skew:

Kurtosis:

程序代的第代的 CS编程辅导 0.00

\_\_\_\_\_\_

Notes:

[1] Standard Error specified.

DW-stats of 2.071 is

Yet, the p-value of the level and the R-square

covariance matrix of the errors is correctly

that there is no serial correlation.

icates that it is slightly significant at 7.5% significance in low explanatory power of the model.

5 Residuals plot for gold

Chat: cstutorcs

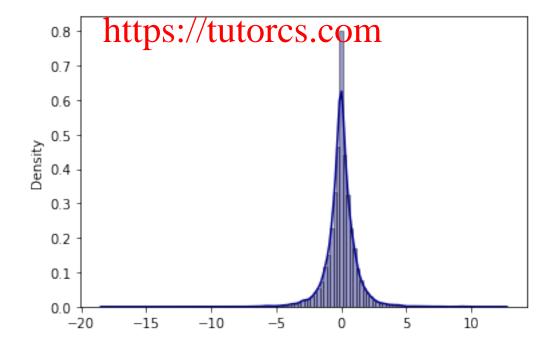
[102]: residuals\_go = model.resid

import seaborn as sns

C:\Users\rluck\anaconda3\lib\site-packages\seaborn\distributions.py:2557:
FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Plashabblyout blot use ther Displot a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

warnings.warn(ms) Futurewarn4re 389476

[102]: <AxesSubplot:ylabel='Density'>



[103]: from scipy import stats

JB\_go= stats.jarque bera(residuals go)

JB\_go

[103]: Jarque\_beraResult 42195044507, pvalue=0.0)

The plot and JB test of normality. It is clearly a non-normal distribution of normality.

### 6 Cusum Test for Gold

[104]: # endog = data.R\_go WeChat: cstutorcs

Rp = data.R\_p WeChat: cstutorcs

endog = data.R\_go

exog = sm.add\_constant(Rp)

mod = sm.RecursiveLS(endog,exog)

res\_1 = mod.fit() ASSIgnment Project Exam Help

fig = res\_1.plot\_cusum(figsize=(10,6));

C:\Users\rluck\anatonda3\lib\sitepackages\statsmode\s\130\da1\ts\1\ts\1\ts\100\formula \ts\2000\da1\

warnings.warn('An unsupported index was provided and will be'



7 White Test of Heteroskedasticity for Gold

[106]: [('Lagrange Multiplier statistic:', 36.866651106570274), ("LM test's p-valoe: \$\frac{1}{2}\$\fra

LM test statistic is 36 87 m ail or equation for a com

F-stats = 18.49 and the corresponding p-value is 0

Since the p-value of the both LM and Estate is despithan 0.05, we reject the null hypothesis that there is no heterosked society in the residual. It interes that the heterosked asticity exists and the standard errors need to be corrected.

### 8 Breusch-Go<mark>afrepsM/testtorGslcOM</mark>

```
[107]: import statsmodels.stats.diagnostic as dg
print (dg.acorr_breusch_godfrey(model, nlags= 2))
```

(14.058774886495657, 0.0008854740175917412, 7.036171882380294, 0.0008836668869260258)

T-statistic of Chi-squared is 14.0588 and the corresponding p-value is 0.0009

F-statistic is 7.0362 and the corresponding p-value is 0.0009

Since p-value is less than 0.05, we reject the null hypothesis, thus inferring there is some autocorrelation at order less than or equal to 2.0

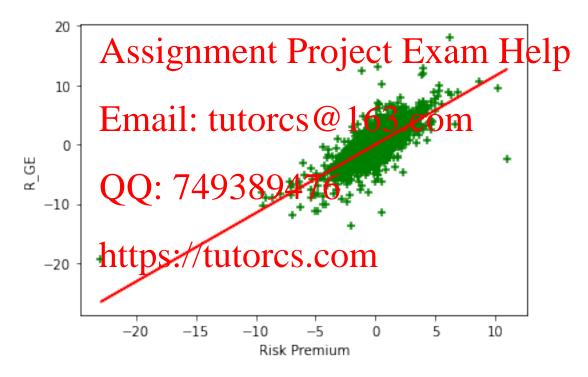
9 II. Plotting GE excess returns with market excess returns

```
[108]: %matplotlib inline
    reg = linear_model.LinearRegression()
    X = data[['R_p']]
    y = data['R_ge']
    reg.fit(X,y)

[108]: LinearRegression()

[109]: plt.xlabel('Risk)
    plt.ylabel('R_GE')
    plt.scatter(data.R_p,data.R_GE,color='green',marker='+')
    plt.plot(data.R_p,reg.predict(data[['R_p']]), color='red')
```

[109]: [<matplotlib.lines In a tag of Station CS



### 10 Regressing GE excess return with market excess return

```
[110]: #model with intercept
X =sm.add_constant(X)
model_1 = sm.OLS(y,X).fit()
predictions = model_1.predict(X)
j = (model_1.summary())
```

### print(j)

## 程序代写代做CS编程辅导

\_\_\_\_\_\_

Dep. Variable:
Model:
Method:
Date:

Time:

No. Observations: Df Residuals: Df Model:

Covariance Type:

R-squared: 0.564
Adj. R-squared: 0.564
F-statistic: 1.351e+04
Prob (F-statistic): 0.00
Log-Likelihood: -15682.
AIC: 3.137e+04
BIC: 3.138e+04

**L.** 

	crefy e	(therrat	:-cstut	P> t  O1CS	[0.025	0.975]
const	-0.0012	0.011	-0.114	0.909	-0.022	0.020
R_p	1.1569	0.010	116.224	0.000	1.137	1.176
========	:============	73-75-75	;;;;;;; <u>;</u> ;;;;;;;;;;;;;;;;;;;;;;;;;;;;			========

Omnibus: Assignment Project Exam Help

 Prob(Omnibus):
 0.000 Jarque-Bera (JB):
 109234.319

 Skew:
 0.109 Prob(JB):
 0.00

 Kurtosis:
 -15.845 Oronds (a) 163 com
 1.07

Notes.

[1] Standard Error assume that the jover succe matrix of the errors is correctly specified.

DW-stats of 1.995 is close to 2.0, implying that there is no serial correlation.

Since p-value of the bath control is less than 1.65 Sec Court null hypothesis that beta is zero.

The CAPM equation for GE can be written as follows:

$$R_q e = 1.1569 * R_p + Rf$$

where  $R_g e$  is the return from GE stock,  $R_p = Rm - Rf$  is the market risk premium and Rf is the risk free rate of return

If we want to replicate the returns from GE, we can rearrange the above equation:

$$R_q e = 1.1569 * Rm + (1 - 1.1569) * Rf$$

 $\Rightarrow$  We can buy 1.1569 of market portfolio (i.e. S&P500 index fund) and then short 0.1569 T-Bill.

### 11 Residual Plots for GE 程序代写代做 CS编程辅导

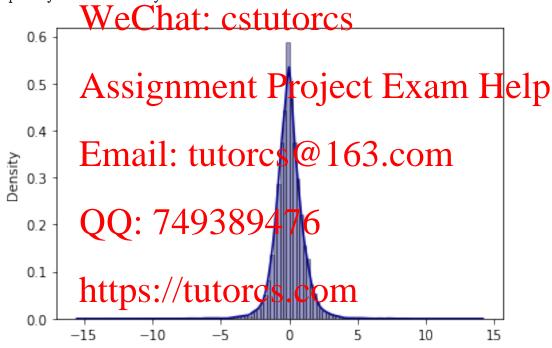
[111]: residuals = model\_1.resid import seaborn as sns sns.distplot(residuals hist=True | bde=True, bins=int(120), color=u →'darkblue',hist | black'})

C:\Users\rluck\ana
FutureWarning: `di
future version. Pl
function with simi
histograms).

warnings.warn(msg, FutureWarning)

ckages\seaborn\distributions.py:2557:
cated function and will be removed in a
de to use either `displot` (a figure-level
or `histplot` (an axes-level function for

[111]: <AxesSubplot:ylabel='Density'>



```
[112]: from scipy import stats

JB_GE= stats.jarque_bera(residuals)

JB_GE
```

[112]: Jarque\_beraResult(statistic=109234.31887176927, pvalue=0.0)

The plot and JB test (p-value <0.05) rejects the null hypothesis of normality. It is clearly a non-normal distribution.

```
[113]: endog = data.R_ge
Rp = data.R_p
```

```
exog = sm.add_constant(Bp)
mod = sm. Recursive 经邮货,成写代做 CS编程辅导
res_1 = mod.fit()
fig = res_1.plot_cusum(figsize=(10,6));
C:\Users\rluck\ana
                               del.py:578: ValueWarning: An unsupported
packages\statsmode
index was provided
                              red when e.g. forecasting.
 warnings.warn('A
                               x was provided and will be'
     200
                     Chat: cstutorcs
     100
      0
    -100
               Email: tutorcs@163.com
    -200
    -300
```

## https://tutorcs.com

Cusum test of stability for GE shows stability of beta as it is within the 5% significance level band.

### 12 White Test of Heteroskedasticity for GE

('F-statistic:', 318.60924780728743),

### ("F-test's p-value:", 49073934719673876e-135)] CS编程辅导 LM test statistic is 600.72 and the corresponding p-value is 0

F-stats = 318.61 and the corresponding p-value is 0

Since the p-value of t at six is less than 0.05, we reject the null hypothesis that there is no heterosked at the standard errors need at the

[115]: print (dg.acorr\_b: [115] = el\_1, nlags= 2))

(5.174836714176367

T-statistic of Chi-squared = 5.1748 and the corresponding p-value = 0.075.

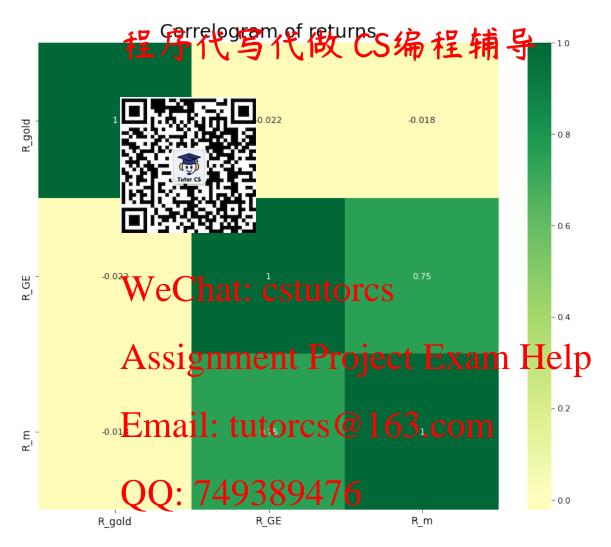
F-statistics = 2.5877 and the corresponding p-value = 0.075

Since p-value exceeds (10), we fail the lect the Shirth Colors. Sthus inferring there is no autocorrelation at order less than or equal to 2.0

[]:

## Assignment Project Exam Help

13 Extra: Correlation matrix between returns of gold, GE and market Email: tutorcs@163.com



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