程序代写代做 CS编程辅导

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Financial Econometrics

torial 4 solutions

1. Estimating MA

Consider an invertibe $\mathbf{E} = \mathbf{E} = \mathbf{E} + \mathbf{E}_t + \mathbf{E$

Using the MA(1) eq we find

$$\varepsilon_1 = y_1 - \mu - \theta_1 \varepsilon_0 \; ,$$

$$\varepsilon_2 = y_2 - \mu - \theta_1 \varepsilon_1$$
 be $(\mu h^{\theta})_1$ restrictors

$$\varepsilon_3 = y_3 - \mu - \theta_1 \varepsilon_2 = y_3 - \mu - \theta_1 [y_2 - \mu - \theta_1 (y_1 - \mu - \theta_1 \varepsilon_0)],$$

which are *non-linear* Aunctions of the presenters ($t_1\theta_1$). Obvious t, the same call-leading for $t=4,5,\ldots$ The shock ε_t is interpreted as the 1-step ahead forecast error. Hence, the "least squares" principle here is to choose the values of (μ,θ_1) to minimise the sum of squared 1-step ahead forecast errors: SSE $(\mu,\theta_1)=\varepsilon_1^2+\varepsilon_2^2+\varepsilon_3^2$. Note that the SSE is a *non-linear* function of (μ,θ_1) and its minimisation is carried out by numerical search algorithms in practice. For a long series of y_t , kay D=3000, the above applies straightforwardly. We note that the expression of ε_3 involves the term $\theta_1^3\varepsilon_0$. In general, the expression of ε_t involves the term $\theta_1^t\varepsilon_0$. For large t the least of the present t is a point of the present t increases as long as the MA is invertible (where t in the large t increases as long as the MA is invertible (where t increases t increases as long as the MA is invertible (where t increases t increases as long as the MA is invertible (where t increases t increa

MLE is based on maximizing the likelihood of observing y_t . An important technical caveat here: the probability to observe the exact values y_t is zero (separately of jointly) because we deal with continuous random variable. The likelihood is proportional to the joint probability that in each time the random variable will fall within the range $y_t \pm \delta$, where δ is a very (infinitesimally) small positive number, the joint probability is

$$P(y_1 - \delta < Y_1 < y_1 + \delta \text{ and } y_2 - \delta < Y_2 < y_2 + \delta \text{ and } ... \ y_T - \delta < Y_T < y_T + \delta) = CDF(y_1 + \delta, y_2 + \delta, ..., y_T + \delta) - CDF(y_1 - \delta, y_2 - \delta, ..., y_T - \delta)$$

The same small δ is used in the definition of the derivative:

$$\lim_{\delta \to 0} \frac{CDF(y_1 + \delta, y_2 + \delta, \dots, y_T + \delta) - CDF(y_1 - \delta, y_2 - \delta, \dots, y_T - \delta)}{2\delta} = f(y_1, y_2, \dots, y_T),$$

where $f(y_1, y_2, ..., y_n)$ the positive of the CDF CS 编程辅导 Hence for small positive δ:

$$P(y_1 - \delta < Y_1 < y) = (y_1 + \delta, \dots, y_T - \delta < Y_T < y_T + \delta) \approx 2\delta f(y_1, y_2, \dots, y_T)$$

Therefore, maximize the first to maximizing f() because $\delta > 0$.

Obviously you do not be to derive the part above, but hopefully it helps with understanding. So, i consistency of maximise the probability that any random sample (a collection of random variables) falls as close as possible to the observed realization of the random sample by choosing the parameters which therefore the specific family of distributions (we typically use Normal with just two parameters). The parameters of the distribution are related to the parameters of the model for a given model. If there is no such relation the parameters of the model are not identified.

Coming back from this illuminating digression the joint pdf is given by $f(y_3, y_2, y_1)$. We can factorise it: Email: tutorcs@163.com

$$f(y_3, y_2, y_1) = f(y_3, y_2 | \Omega_1) f(y_1) = f(y_3 | \Omega_2) f(y_2 | \Omega_1) f(y_1)$$

So
$$y_t = \mu + \varepsilon_t + \theta_1 \varepsilon_{t-1}$$
 and $\varepsilon_t \sim iid$ WN $N(0, \sigma^2)$. Hence

The conditional (and unconditional) distribution of y_t is Normal because y_t is just a linear combination of ε_t , ε_{t-1} which are Normally distributed by assumption. Find the mean and the variance of y_t -s and write down the pdfs.

$$y_1 \sim N(\mu, (1 + \theta_1^2)\sigma^2); f(y_1) = (2\pi(1 + \theta_1^2)\sigma^2)^{-1/2} exp\{-\frac{(y_1 - \mu)^2}{2(1 + \theta_1^2)\sigma^2}\}$$

$$y_2|\Omega_1 \sim N(\mu + \theta_1 \varepsilon_1, \sigma^2); f(y_2|\Omega_1) = (2\pi\sigma^2)^{-1/2} exp\{-\frac{(y_2 - \mu - \theta_1 \varepsilon_1)^2}{2\sigma^2}\}$$

$$y_3 | \Omega_2 \sim N(\mu + \theta_1 \varepsilon_2, \sigma^2); f(y_3 | \Omega_2) = (2\pi\sigma^2)^{-\frac{1}{2}} exp\{-\frac{(y_3 - \mu - \theta_1 \varepsilon_2)^2}{2\sigma^2}\}$$

程序代写代做 CS编程辅导 Note that when computing y₁ we treated ε₀ as a random variable. In fact this causes a

tely identified from the data). Therefore it is ε_0 and ε_1 (each of the important to conditi **T**e of ε_0 *[it can be integrated out of the likelihood if $\boldsymbol{\varepsilon}_0$, but the integration is not simple]. we want to assume j

So, we will maximiz

$$y_1|\varepsilon_0 \sim N(\mu + \theta_1\varepsilon_0, \sigma^2); f(y_1|\varepsilon_0) = (2\pi\sigma^2)^{-1/2} exp\{-\frac{(y_1 - \mu - \theta_1\varepsilon_0)^2}{2\sigma^2}\}$$

Now as we move forward ε_1 can be identified. In fact, we can rewrite all three densities as:

$$\ln f(y_3, y_2, y_1 | \varepsilon_0) = \ln f(y_3 | y_2, y_1, \varepsilon_0) f(y_2 | y_1 | \varepsilon_0) f(y_2 | \varepsilon_0) + \ln f(y_1 | \varepsilon_0) \int_{-\infty}^{\infty} \frac{1}{2} \left[\frac{2\pi \sigma^2}{2} \right]_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{1}{2} \left[\frac{(2\pi \sigma^2)^{\frac{1}{2}}}{(\varepsilon_1^2 + \varepsilon_2^2 + \varepsilon_3^2)^{\frac{1}{2}}} \right] \int_{-\infty}^{\infty} \frac{1}{2} \left[\frac{(2\pi \sigma^2)^{\frac{1}{2}}}{(\varepsilon_1^2 + \varepsilon_2^2 + \varepsilon_3^2)^{\frac{1}{2}}} \right] \int_{-\infty}^{\infty} \frac{1}{2} \left[\frac{(2\pi \sigma^2)^{\frac{1}{2}}}{(\varepsilon_1^2 + \varepsilon_2^2 + \varepsilon_3^2)^{\frac{1}{2}}} \right] \int_{-\infty}^{\infty} \frac{1}{2} \int_{-\infty}^{\infty} \frac{1}{2} \left[\frac{1}{2} \frac{1}{2}$$

Note that in this case in $f(y_2|y_1, \varepsilon_0)$ we do not have to condition on ε_1 , it can be discovered if we know y_1, ε_0 (using the equations in the beginning of this question). Similarly ε_2^2 and ε_3^2 , are defined already.

Note that in terms of estimating (μ, θ_1) minimizing SSE is equivalent to maximizing ln likelihood (conditional on ε_0).

3. Find the unconditional variance of ARMA(1,1) model

$$y_t = \mu + \theta_1 \varepsilon_{t-1} + \varphi y_{t-1} + \varepsilon_t, \ \varepsilon_t \sim iid \ \mathrm{WN}(0, \sigma^2)$$

Using stationarity and taking into account dependence between ε_{t-1} and y_{t-1}

$$var(y_t) = \theta_1^2 \sigma^2 + \varphi^2 var(y_t) + 2\theta_1 \varphi cov(\varepsilon_t, y_t) + \sigma^2$$

 $cov(\varepsilon_t, y_t) = \sigma^2$ which can be found from $cov(\varepsilon_t, \mu + \theta_1 \varepsilon_{t-1} + \varphi y_{t-1} + \varepsilon_t) =$

$$E(\varepsilon_t(\mu+\theta_1\varepsilon_{t-1}+\varphi y_{t-1}+\varepsilon_t))-E(\varepsilon_t)E(y_t)=0+0+0+\sigma^2-0=\sigma^2$$

The zeros are due to the fact that $E(\varepsilon_t) = 0$, $E(\varepsilon_t \varepsilon_{t-1}) = 0$ (white noise property), $E(\varepsilon_t y_{t-1}) = 0$ (white noise property) and $E(\varepsilon_t \varepsilon_t) = \sigma^2$.

DETOUR: Note that white noise property does NOT $E(\varepsilon_{t-1}y_t) = (\theta_1 + \varphi)\sigma^2$ is this example.

Hence,
$$var(y_t) = \frac{\sigma^2(1+\theta)}{1} \frac{\sigma^2(1+\theta)}{1-\varphi^2} = \sigma^2\left(1+\frac{(\theta_1+\varphi)^2}{1-\varphi^2}\right)$$

- 4. [Box-Jenkins methodology]
- The time series plot of INF shows that the inflation was on average lower after 1990 than (a) before 1990. You may use the unit-root test with or without a time trend (by selecting or not selecting Trend and intercept in the unit root test pop-up menu). From the testing results below, the null of a NF cal Corega dell as a stytionary (or trade 1) unit root is rejected (ver small b Qaluel) stationary) time series.



Null Hypothesis: INF has a unit root Exogenous: Constant Lag Length: 1 (Automatic based on SIC, MAXLAG=12)				Null Hypothesis: INF has a unit root Exogenous: Constant, Linear Trend Lag Length: 1 (Automatic based on SIC, MAXLAG=12)		
		t-Statistic	Prob.*			t-Statis
Augmented Dickey-Fuller test statistic		-3.910993	0.0027	Augmented Dickey-Fuller test statistic -4		-4.6745
Test critical values:	1% level	-3.489117		Test critical values:	1% level	-4.0412
	5% level	-2.887190			5% level	-3.4500
	10% level	-2.580525			10% level	-3.1503
*MacKinnon (1996) one-sided p-values.			*MacKinnon (1996) one-sided p-values.			

Augmented Dickey-Fuller Unit Root Test on INF

Visually, the correlogram of INF shows a PAC cutoff at lag j = 2 with exponential decaying AC, which fits the cutoff pattern of an AR(2) model. On the other hand, the PAC

Augmented Dickey-Fuller Unit Root Test on INF

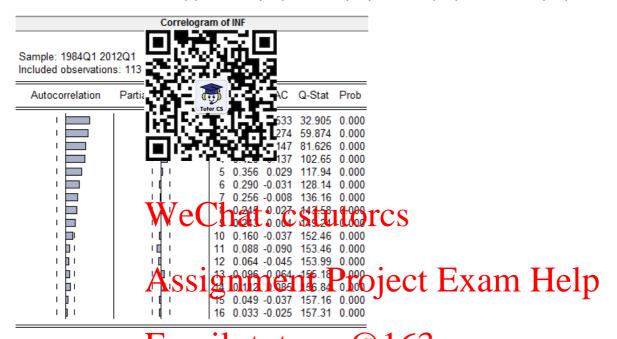
t-Statistic

4.674579

-4.041280 -3.450073 -3.150336 Prob.*

0.0013

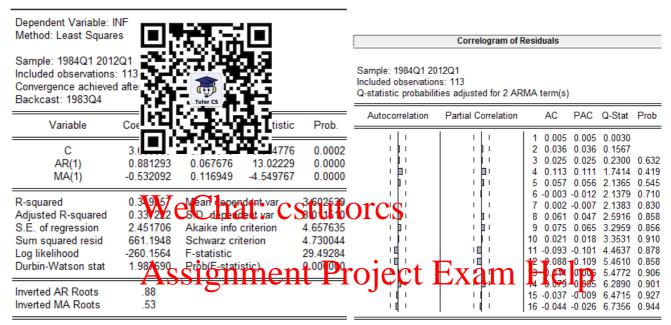
may also be interpreted as an exponential decay. For this reason, we consider the following models as candidates: AR(2), ARMA(1,1), ARMA(2,1), ARMA(1,2) and ARMA(2,2).



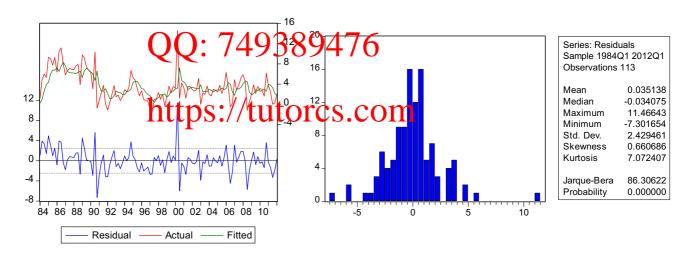
(c) The AIC and SIC values for the models considered in (b) are listed in the table below. Clearly, both AIC and SIC select ARMA(1,1).

ARMA(p,q)	ARMA(2,0)	ARMA(1,1)	ARMA(2,1)	ARMA(1,2)	ARMA(2,2)
AIC	4.675253	<mark>4,657635</mark>	4.668168 S.COM	4.673624	4.683174
SIC	4.747661	4.730044	4.764713	4.770169	4.803855

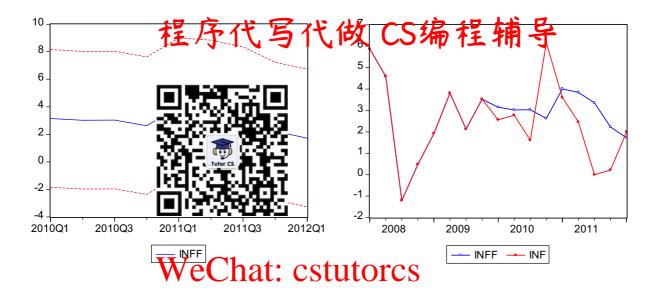
(d) The estimation output of ARMA(1,1) indicates that the roots of the AR polynomial and the MA polynomial are outside the unit circle (note that EViews reports inverted roots). There is no common root. The estimated ARMA coefficients are all statistically and economically significant. The residual-actual-fitted plot shows that the model fits the data quite well (also $\bar{R}^2 = 0.337$), although a few residual points are beyond the 2-standard deviation bands. The key of an ARMA model is to capture the dependence structure in the time series. The residual from an adequate model should not exhibit autocorrelation. The residual correlogram of the ARMA(1,1) confirm that there are no autocorrelations in the residuals (large p-values, which are adjusted for the degrees of freedom lost in estimating the ARMA parameters). Further the histogram of the residual indicates that the normality is strongly rejected, which explains why a few residual points are outside the 2-se bands in the



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(e) For the forecast exercise, you should be able to see the graphs below, where INFF (blue curve) stands for the 1-step ahead forecasts from the ARMA(1,1) model and INF (red curve) is the actual. The second graph is from the command "**plot inff inf**". The first graph is from the **Forecast** menu, which includes the 2-se bands (dashed red lines). By comparison, the interval forecasts (2-se bands) in fact covered the actuals.



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