



MONASH University

Information Technology

程序代写代做 CS编程辅导

FIT1006



Business Information Analysis

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Lecture 14

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Theoretical Sampling Distributions

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Topics covered:

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■ Theoretical Sampling Distributions

- Introduction to sampling.
- The Central Limit Theorem.
- The sampling distribution of the mean and proportion.



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Course outline: ^{程序代写代做 CS编程辅导} Progress report



Applications

Describing
Data

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Probability

Being
Certain

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Modelling

Reporting

Update: Being certain

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- Two samples are drawn from two different populations, or the same population? What factors would affect your decision?



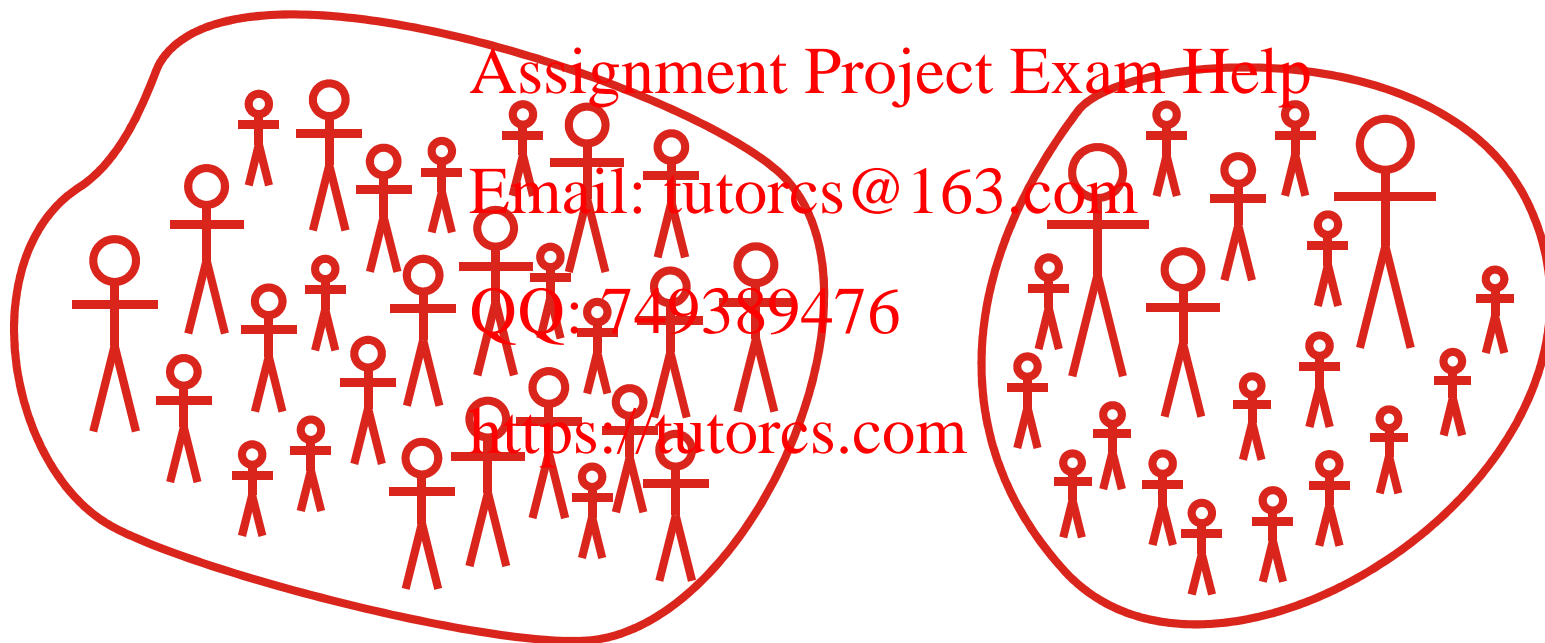
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Estimating a population parameter



- The usual method of estimating a population parameter is to take a sample, and using the sample statistics make an inference about the population parameter.
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- We are frequently interested in the mean of a population, or the proportion of a population exhibiting a certain characteristic.
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- We look at how we determine the accuracy of our estimate of these parameters, based on the value of the parameter in question and the sample size.
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Estimation

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- Part 1. The behavior of samples



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Populations and Samples

- We want to use a sample to make an inference about a population.



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Populations and Samples

- Taking different samples of the same size from a population may yield different means.



- Thus, the sample mean is itself a random variable having its own distribution.

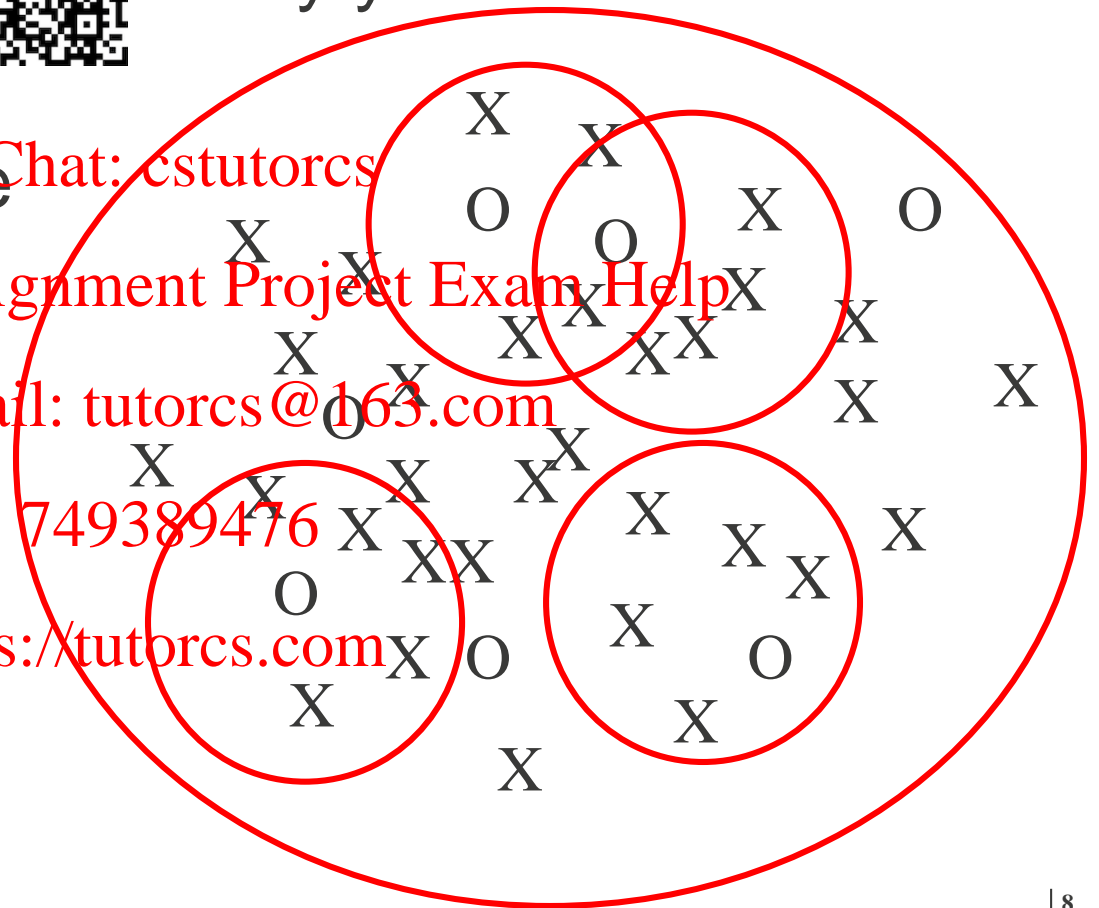
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CLTProject.exe

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- This application take multiple samples from a population and (the variability in the samples as a function of sample size). (We will do this in Tutorial 8)



Random Samples: Exploring the Central Limit Theorem

Parent Distribution: 1, 2, 3, 4, 5, 6

Sample Size: 8

Number of Samples: 10

Sample Means: 2.1250, 4.1250, 4.1250, 4.3750, 4.3750, 2.6250, 3.3750, 3.0000, 4.2500, 3.6250

Last Sample: 3, 1, 5, 6, 5, 2, 5, 4

Buttons: Copy Input, Make Samples, Copy Sample Means, Copy Last Sample

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A Binomial distribution problem



- The following slide shows 1000 samples taken from a population where, for example, $p = 0.9$
- 0 = right handed ($p = 0.9$)
- 1 = left handed ($p = 0.1$)
- Samples of size 1, 2, 5, 10, 100, 1000 are taken and the means calculated.
- 1000 samples were taken with replacement. (*That means each sample was chosen observed and put back into the population*)

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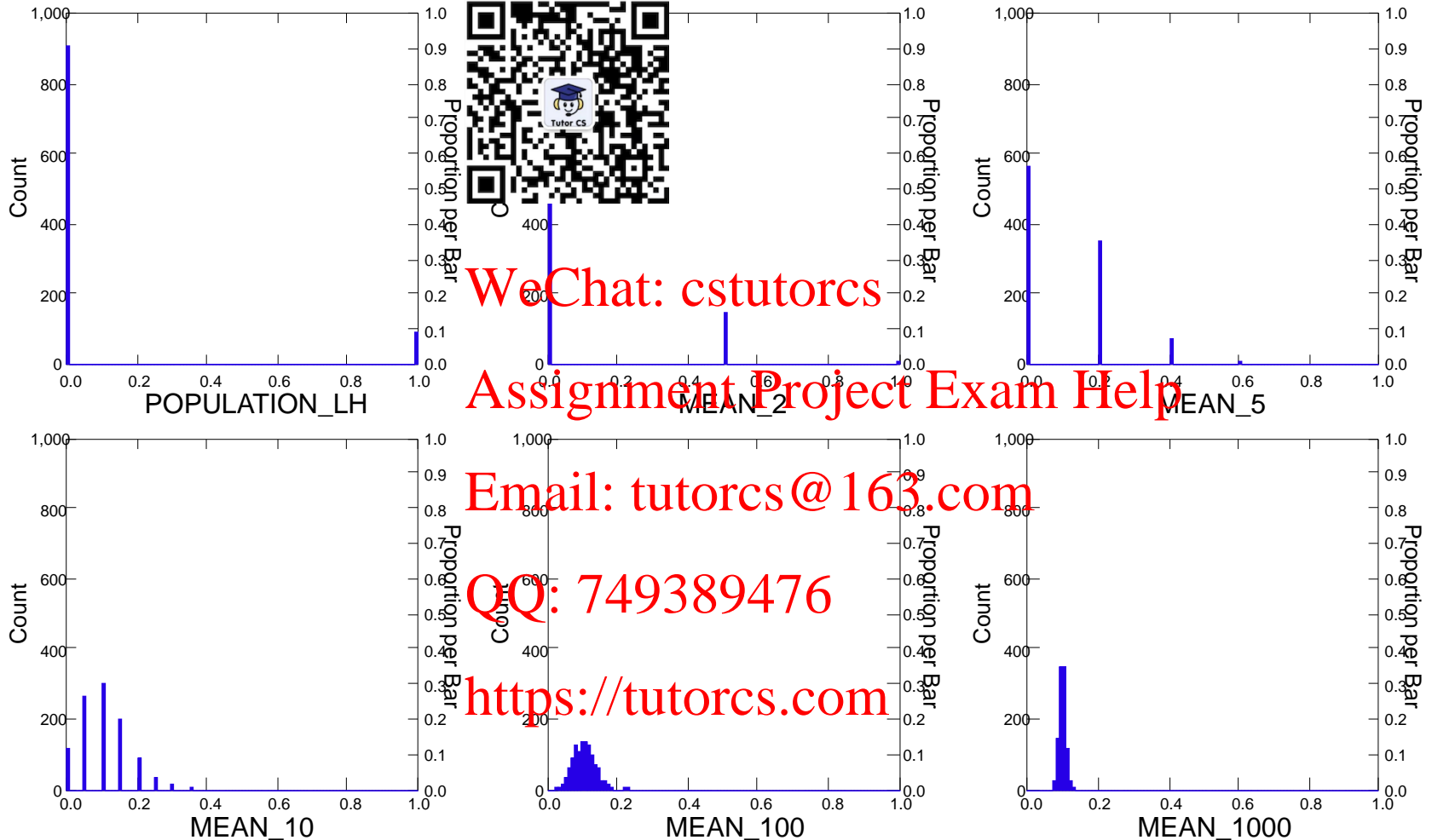
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Effect of sample size



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Observations

- As sample size larger, 3 things happen:
 - 1 Histogram goes from having a Binomial distribution to approaching a Normal distribution.
 - 2 Sample mean converges to the population mean.
 - 3 Variance of the sample mean decreases – inversely proportional to sample size.

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- Part 2. The Central Limit Theorem



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The Central Limit Theorem



- The Central Limit Theorem is fundamental to inferential statistics.
- The main idea is that if we take large enough sample from a population, we find that *regardless of the distribution of the parent population*, the sample mean is:
 - 1. Normally distributed around the population mean.
 - 2. The variance of the sample mean is the population variance divided by the size of the sample.

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Conditions for the CLT to hold



- 1 Samples must be sufficiently large ($n \geq 30$).
- 2 Samples must be of equal size.
- 3 Sampling must be carried out with replacement.

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- *In practice we usually only take and analyse one sample from a population. The conditions above are used to establish the validity of the CLT.*

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CLT demonstration



- 10000 uniformly distributed random numbers were generated using S. A histogram of them appears below.

- Data generated using: WeChat: cstutorcs

Utilities > Basic >

BASIC

NEW

REPEAT=10000

LET a=URN

SAVE d:\Random_10000_Uniform

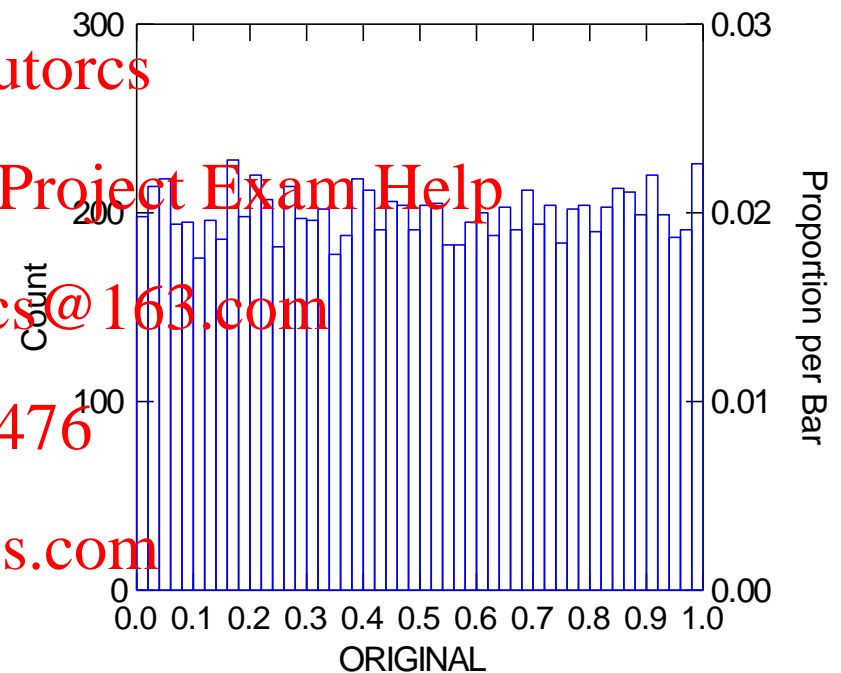
RUN

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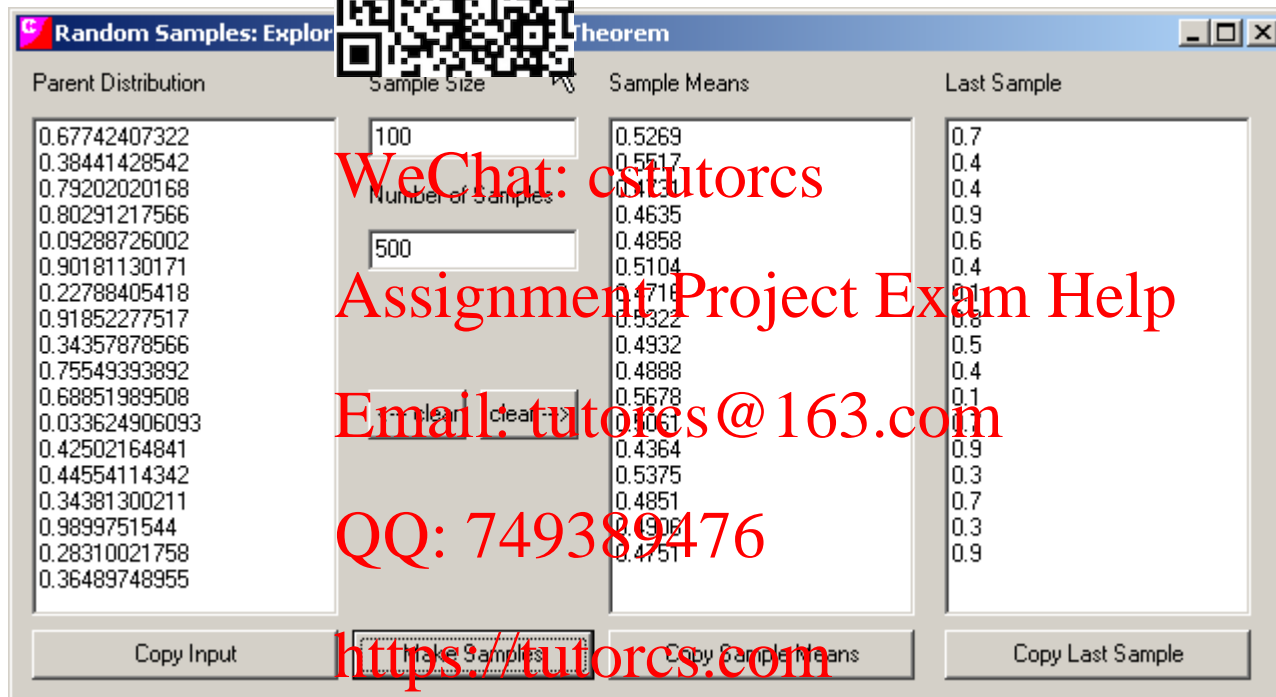
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- CLTProject.exe 计算 500 个样本的均值，每个样本大小为 100

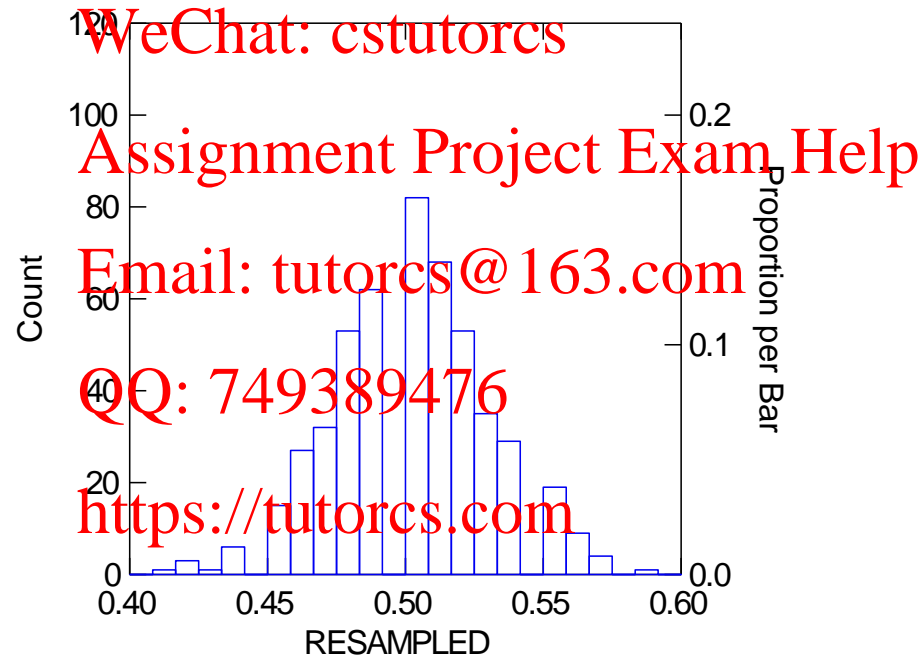


- File: FIT1006 Lecture 17 CLT.syz

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- The randomly generated data was saved as text, copied and pasted into C:\Program Files\Microsoft Research\MSR\ct.exe. 500 samples of size 100 were taken and the means calculated. A histogram of the means is below.



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- Comparing the descriptive statistics for both the original data and 500 samples of size 100.



	ORIGINAL	RESAMPLED
N of cases	10000	500
Minimum	0.000	0.410
Maximum	1.000	0.590
Median	0.499	0.500
Mean	0.501	0.501*
Standard Dev	0.290	0.028*
N 1 of 4	0.247	0.480
N 2 of 4	0.499	0.500
N 3 of 4	0.754	0.520

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- Part 3. The sampling distribution of means and proportions



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Notation, main characters:

Parameter

Mean

Standard Deviation

Proportion



Population

Sample

\bar{x}

s

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$\sigma_{\bar{x}}$ = standard error of the sample mean

σ_p = standard error of the sample proportion

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The sample values are used to estimate the unknown population parameters; taking into account variability introduced by sampling.

The Sampling Distribution of the Mean



From the CLT, take a sample of size n ,

From a population with mean μ and variance σ^2

Then, as n increases:

The sample mean, $\bar{x} \rightarrow \mu$, and variance $(\bar{x}) \rightarrow \frac{\sigma^2}{n}$

thus $\bar{x} = \mu$ and $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$ for n large.

sample standard dev.
(standard error)

<https://flux.qa> (Feed code: 3J6KGV)

Question 1



If a sample of 100 counts is taken from a population, with $\mu = \$2000$ and standard deviation \$500; the distribution of the sample mean is:

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A. Normal(mean = 20, stdev = 5)

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B. Normal(mean = 20, stdev = 50)

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C. Normal(mean = 2000, stdev = 5)

✓ D. Normal(mean = 2000, stdev = 50)

Example 1

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- A sample of 100 accounts were taken from a population of accounts with mean \$2000 and standard deviation \$500. What is the probability that the sample mean will be less than 2050?

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From the population, $\mu = 2000$, $\sigma = 500$

For the sample, $\bar{x} = 2000$, $n = 100$

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z	0.00	0.01
0.0	0.5000	0.5040
0.1	0.5398	0.5438
0.2	0.5793	0.5832
0.3	0.6179	0.6217
0.4	0.6554	0.6591
0.5	0.6915	0.6950
0.6	0.7257	0.7291
0.7	0.7580	0.7611
0.8	0.7881	0.7910
0.9	0.8159	0.8186
1.0	0.8413	0.8438
1.1	0.8643	0.8665
1.2	0.8849	0.8869

$$\text{thus } \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{500}{\sqrt{100}} = 50$$

and $\bar{x} \approx N(2000, 50^2)$

$$P(\bar{x} < 2050) = P\left(z < \frac{2050 - 2000}{50}\right)$$

$$= P(z < 1), \quad z \approx N(0, 1^2) = 0.8413$$

The Sampling Distribution of a Proportion

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If we take a sample of size n ,

From a population with proportion p of interest

Then, from the CLT, as n increases:

Sample proportion, $p \rightarrow \rho$, variance(p) $\rightarrow \frac{\rho(1 - \rho)}{n}$

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Thus $p = \rho$, $S_p = \sqrt{\frac{\rho(1 - \rho)}{n}}$ for n large,

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$np, n(1-p) \geq 5$

Standard error of proportion

Example 2

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z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157
0.6	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517

- It is thought that the proportion of left handed people in the population is 10%. What is the probability that a sample of 100 people taken at random would have a proportion of left handers less than 0.12?

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$$\frac{\pi(1-\pi)}{n}$$

$$\pi = 0.1, n = 100$$

$$E(p) = 0.1, \text{Var}(p) = \frac{0.1 \times 0.9}{100} = 0.03^2$$

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$$\text{thus } p \sim N(0.1, 0.03^2)$$

$$P(p < 0.12) = P\left(z < \frac{0.12 - 0.1}{0.03}\right)$$

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$$= P(z < 0.67), z \sim N(0, 1^2) = 0.7486$$

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Reading/Questions (Selvanathan)



- Sampling inference and sampling distributions.
 - Reading: 7th Ed. Chapter 9.
 - Questions: 7th Ed. 9.4, 9.12, 9.13, 9.18, 9.24, 9.25

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