## 程序代馬式做 CS编程辅导

Faculty of Information Technology Semester 2, 2022



ASSESSED PREP

You must provide a ser classes), or submit it

ire question at the start of your tutorial (for on-campus ial begins (for online classes).

1. (mostly from FIT2014 Final Exam, 2018)

The predicate supervised has two treuments both of which are people. The meaning of supervised(X, Y) is that person X supervised the PLP of person Y.

Express each of the following three sentences in predicate logic.

- (a) Alonzo Church was the PhD supervisor of Alan Turpe oject Exam Help
- (b) No person supervised their own PhD.
- (c) Not every PhD supervisor had a PhD supervisor.

  Note. This on this pewritten is an expected selection of the company of th
- (d) Alan Turing supervised only one person's PhD.

2. This question is about the game Noughts-and-Crosses (known as Tic-Tac-Toe in the US). This game is played using a 3 × 3 grid, usually drawn in the manner of Figure 1(a). Two players, Crosses and Noughts, each take turns to place X and O, respectively, in one cell of the grid. Once a cell is occupied by helphayers its entry connect be charged, and neither player can play there again. A player wins when help have three of their symbols in a line, horizontally, vertically, or diagonally, there being eight possible lines altogether; when that happens, the game stops. If all cells are occupied (five by Crosses and four by Noughts) and none of the eight three-cell lines have three identical symbols, then the game stops and is a Draw. (For simplicity, we forbid resignations and agreed draws.)

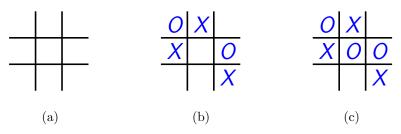


Figure 1: Some positions in Noughts-and-Crosses

The variable P always stands for a position in Noughts-and-Crosses, which represents the state of the array after the players have played some number of moves. A position thus corresponds to a  $3 \times 3$  array with some subset of the cells occupied, in which the number of Crosses either equals, or

exceeds by one, the number of Youghts In the former case, then the fifty player to hove must be Crosses; in the latter case, the next player to move must be Noughts. The diagram in Figure 1(a) shows the position before anyone has moved; the next player to move is Crosses. The diagram in Figure 1(b) shows a property of the next player to move its crosses. The diagram in Figure 1(b) shows a property of the next player to move turns and Noughts has had two turns; the next player to move turns are the next player to move turns and Noughts has had two turns; the next player to move must be Noughts.

A move can be specified to the larger whose turn it is and specifying the cell into which they place their symbol to the position of Figure 1(b), the move "Noughts: centre cell" gives the position of the position of Figure 1(b).

A winning move is the first line of three identical symbols at wins immediately, i.e., that completes the first line of three identical symbols at wins immediately, i.e., that completes the first line of three identical symbols are at wins immediately, i.e., that completes the first line of three identical symbols are at wins immediately, i.e., that completes the first line of three identical symbols are at wins immediately, i.e., that completes the first line of three identical symbols are at wins immediately.

We use the followi

- The predicate CrossesWins(P) is True if, in position P, there is a line of three Crosses and no line of three Noughts.
- The predicate Noughts Wis (P) is True if in position P, there is a line of three Noughts and no line of three Crosses.
- The predicate  $\mathsf{CrossesToMove}(P)$  is True if, in position P, it is the turn of Crosses to move (in other words, the numbers of Crosses and Noughts are equal, and no-one has won yet).
- The predicate Noughts Town (P) is True if, in position 1, it is the turn of Noughts to move (in other words, the number of Crosses is one greater than the number of Noughts, and no-one has won yet).
- The function Resulting Position P,  $X_1 \sqcup Y_1 \sqcup Y_2 \sqcup Y_3 \sqcup Y_4 \sqcup Y$

Using quantifiers and the variables, predicates and function described above, write statements in predicate logic with each of the following meanings.

- (a) Crosses has a winning move in position P.
- (b) Noughts has a winning move in position P.
- (c) For each of the statements you wrote for (a) and (b), determine whether the statement is True or False when P is the following position.



By analogy with the definition of "winning move" given above, we could define a *losing move* to be a move that gives a position that is a win for the opponent, i.e., where there is a line of three of the opponent's symbols that did not exist in the game before. In Noughts-and-Crosses, this never happens. (Why?)

# (d) Write a predicate 是所有的 CS 编辑 辅导

- (e) Crosses has a straight of the first moves from position P (where the three moves are one by Crosses, or the first moves from position P).
- (f) Crosses does not be a find a finding within three moves from position P. For this question, you gical negation occurs immediately in front of any quantifier.
- (g) Crosses has a winning strategy from the initial position  $P_0$ .
- (h) Noughts has a white crate value the istalt state & S
- (i) With best possible play from both sides from the initial position  $P_0$ , the game ends in a Draw.
- (j) It is possible for Austria Paroject Exam Help
- 3. A language L is called **hereditary** if it has the following property:

  For every nonempty string x in L, there is a character in x which can be defected from x to give another string in L.

Prove by contradiction that every nonempty hereditary language contains the empty string. 749389476

4. Prove the following statement, by mathematical induction:

#### $(*https://tutoircs:ddcumprequals k^2.$

- (a) First, give a simple expression for the k-th odd number.
- (b) Inductive basis: now prove the statement (\*) for k = 1.

**Assume** the statement (\*) true for a specific value k. This is our **Inductive Hypothesis**.

(c) Express the sum of the first k+1 odd numbers ...

$$1+3+\cdots+((k+1)-\text{th odd number})$$

- $\dots$  in terms of the sum of the first k odd numbers, plus something else.
  - (d) Use the inductive hypothesis to replace the sum of the first k odd numbers by something else.
  - (e) Now simplify your expression. What do you notice?
- (f) When drawing your final conclusion, don't forget to briefly state that you are using the Principle of Mathematical Induction!

### 5. Prove, by inductiffen final for all of the CS fine has a fine of the State of the final final final final final final fine of the control of the final final

- (b) [Challenge] Can you use a similar  $\leq (n-2)^n$ ? What assumptions do you need to make about n? How far can you push this: what if 2 is replaced by a larger number? What is the best upper bound of the form  $f(n)^n$  that you can find, where f(n) is some function of n?

#### WeChat: cstutorcs

### Assignment Project Exam Help

#### Supplementary exercises

- 7. Let  $P_n$  be the proposition  $x \wedge x$  is equivalent to  $P_{n-1} \wedge x_n$ .
  - Prove by induction on n that, if  $x_1 = F$ , then  $P_n$  is False.
- 8. This question is pased of Lab 0. Section Express 1. Let program be any program that can be run in Linux and produces standard output. Suppose we do program | wc as above, followed by a sequence of further applications of | wc.

```
$ program | wc https://tutorcs.com
$ program | wc | wc
...
$ program | wc | wc | wc
...
$ program | wc | wc | wc
...
:
```

- (a) Determine how many pipes are required before the output ceases to change, and what that output will be.
- (b) Prove by induction that, whatever *program* is (as long as it produces some standard output), continued application of | wc eventually produces this same fixed output.

This is probably best done by proving, by induction on n, that if | wc is applied repeatedly to a file of  $\leq n$  characters, it will eventually produce the fixed output you found in part (a).