程序代屬优數 CS编程辅导

Faculty of Information Technology $2^{nd} \ {\rm Semester} \ 2022$



Attempt all quest

ASSESSED PREPARATION: Question 6.

You must submit a serious attempt at the entire question or CS

Assignment Project Exam Help

- (a) Find a Context-Free Grammar for the language
- (b) Prove, by induction of the string length, that every string of the form $\mathbf{a}^n \mathbf{b}^i \mathbf{c}^{2n}$ can be generated by your grammar.
 - (c) Find a Pushdown Automaton that recognises this language.

QQ: 749389476

2.

Consider the following four statements, which we call W, X, Y and Z.

- W: Every contemporary deligious com
- X: Every context-free language is finite.
- Y: There exists an infinite context-free language.
- Z: There exists a finite context-free language.

(a)

- (i). Which of X, Y, Z is the logical negation of W?
- (ii). Which of W, X, Y, Z is true?
- (b) Define the predicates **CFL** and **Infinite** to have the following meanings.

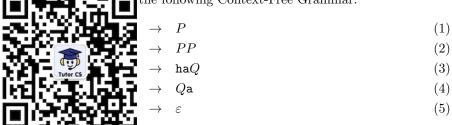
 $\mathbf{CFL}(L)$ L is context-free $\mathbf{Infinite}(L)$ L is infinite

The universe of discourse is all languages.

- (i). Write statements W, X, Y, Z in predicate logic, using these two predicates.
- (ii). Use the properties of quantifiers, and laws of propositional logic as needed, to derive an existential statement equivalent to $\neg W$.

(iii). Which of X, Y, Z程序优写版 CS编程辅导

3. Let LOL be the the following Context-Free Grammar.



- (a) Warm-up:
 - (i). What is the shortest string in LOL? Give a derivation for it.
- (ii). Is the above grammer Egularhat: CStutorcs
- (iii). Is LOL a regular language? If so, give a regular expression for it. If not, prove it.
- (iv). Is the above grammar in Chomsky Normal Form Pf so, why: if not, take why not. Help
- (b) Here is an attempted proof that LOL is infinite. Comment on what is correct and incorrect in this proof.

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- 1. Let x be some string in LOL.
- 2. The string x must have a derivation, using the above grammar.
- 3. The only rule in the granmar that opey not have a nonterminal symbol on its right-hand side is the last one, (5).
- 4. So any derivation of x must finish with an application of (5).
- 5. Therefore the string just before x in the derivation of x must have a Q.
 6. Therefore the derivation of x has the form

$$S \Longrightarrow \cdots \Longrightarrow x_{\text{left}} Q x_{\text{right}} \stackrel{(5)}{\Longrightarrow} x_{\text{left}} x_{\text{right}} = x,$$

where x_{left} denotes the portion of x before Q, and x_{right} denotes the portion of x after Q.

7. So, instead of applying rule (5) to this last occurrence of Q, we could apply rule (4) followed by rule (5), giving

$$S \Longrightarrow \cdots \Longrightarrow x_{\text{left}}Qx_{\text{right}} \stackrel{(4)}{\Longrightarrow} x_{\text{left}}Qax_{\text{right}} \stackrel{(5)}{\Longrightarrow} x_{\text{left}}ax_{\text{right}}.$$

This new string is also in LOL and is one letter longer than x. Call it y.

- 8. We can apply this argument again to y, to get a string in LOL that is one letter longer than y, and then we can get strings that are even longer than that, and so on, indefinitely.
- 9. So we can generate infinitely many strings. Therefore LOL is infinite.

(c) Prove by induction 程, for all 人, 与 language 也, CS编辑 輔 是 and a seast n.

- (d) Here is an attempted proof by contradiction that LOL is infinite. It uses, in the middle, the and bad about this proof. proof given in (c). Co
 - 1. Assume, by hat LOL is finite.
 - 2. \(Insert he d on (c), that LOL has arbitrarily long strings. \rangle
 - 3. This contra nat LOL is finite.
 - 4. Therefore 1
- (e) Construct a correct proof by contradiction that LOL is infinite, using the following approach:

WeChat: cstutorcs 1. Start by assuming LOL is finite, as in (c) step 1.

- 2. Show that LOL contains a nonempty string. (No need to use the assumed finiteness of LOL just vet.)
- 3. Among all Anssignment, Porojecty Exvann yhlelp choose it?
- 4. Show how to construct a string in LOL that is longer than x.
- Email: tutorcs@163.com
- 6. Therefore LOL is infinite
- This question is 0.000 to 0.000 0.000 0.000 0.000 0.000 0.000 0.0004.
- (a) Review Tute 4, Q6, reflecting on the discussion of it in your tutorial, and correcting your attempt at the question.
- (b) Use the Pumping Land $\{a, b, c\}$ is not context-free.
- (c) Hence prove that the language of binary string representations of adjacency matrices of graphs is not context-free.

You may assume that the intersection of a context-free language with a regular language is context-free. (Challenge: prove this.) Note that, unlike regular languages, the class of context-free languages is not closed under intersection. (Can you prove this?)

Recall the **Pumping Games** of Tute 4. An expansion pack has now been released, called **5**. Double Pumping Games.

You can play a Double Pumping Game for any language. The players are Con and Noni. First, the players are given a language L (which may or may not be context-free). Con moves first, then Noni moves, then Con moves, then Noni moves. The rules for their moves are as follows.

- Con first chooses a number $k \in \mathbb{N}$.
- Then Noni chooses a string $w \in L$ with $|w| > 2^{k-1}$.
- Then Con divides w up into substrings u, v, x, y, z such that $vy \neq \varepsilon$ and $|vxy| \leq 2^k$.

· Then Noni choose 程序代码 CS编程辅导

The result of the game is that:

- if $uv^i x y^i z \in L$,
- (a) Play the game
- (b) Using quantifie rtion that Con has a winning strategy.
- rtion that Noni has a winning strategy. (c) Using quantifie
- (d) What does the CFLs tell us about circumstances in which winning strategies exist?

, and (ii) $\{a^n b^n a^n : n \ge 0\}$.

6.

A Stock Exchange publishes daily information on the share price of a company as a 5-tuple of at: cstutores numbers

 $(p, c, s, p_{\max}, p_{\min})$

where

the price peaks il grammeraity Posta read of Lexan Help

the difference between p and the published price for the previous trading day;

the number of shares sold during the day;

the maximum share price for this company during the most recent 52 weeks (including this week); the minimum share price for this company during the most recent 52 weeks (including this week). p_{max}

 p_{\min}

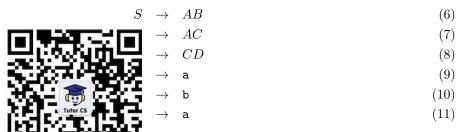
The language SHA EPHICLINFO SPI, over the even-symbol alphabet $\{0,1,-,+,(,),\,,\}$, consists of all numerically valid 5-tuples of binary numbers that could (hypothetically, allowing arbitrarily high prices and arbitrary trading volumes) represent information on the share price according to the above description. We require:

- p, p_{\min} and p_{\max} can be some point white self-energy equirement that p lies between p_{\min} and p_{\max} inclusive
- c can be any integer whose value is consistent with the above definitions of all the five numbers. If it is negative, it is prefixed by a minus sign; if it is positive, it is prefixed by a plus sign; and if it is zero, no sign is given.
- s can be any nonnegative integer. Its sole constraint is that if s=0 then c=0 too, since if no shares are traded then the price cannot change (since it is trading in the sharemarket that determines the price).
- Binary numbers must have no leading zeros, except that the number 0 itself is represented as a single 0.

Is the language SPI context-free? If so, give a Context-Free Grammar for it. If not, prove that it is not, using the Pumping Lemma for Context-Free Languages.

¹These definitions contain some simplifications for the purposes of the assignment. In practice, Australian share prices are usually quoted in dollars, with cents given after the decimal point. But increases or decreases in share prices are indeed typically given in cents, as here.

7. Let G be the following 原代写代做 CS编程辅导



Use the Cocke-Young G ithm to determine whether or not the string abbba is generated by G.

- 8.
- (a) Convert the CFG in Q5 into a Chomsky Normal Form grammar for LOL.
- (b) Using this Chomsky Volume Ford Tammar Solly 11eO (Talsorithm to the string hahaa.

Assignment Project Exam Help

Supplementary exercises

- 9. Find Regular Grund for the following regular Engels in 63.com
- i) $(a \cup b)^*(aa \cup bb)$
- ii) $((a \cup b)(a \cup b))^*$
- iii) $(aa \cup bb)^*$ QQ: 749389476
- iv) $(ab)^*aa(ba)^*$
- $^{\mathrm{v)}\;(ab\cup ba)(aa\cup bb)}$ https://tutorcs.com
- 10. Describe PDAs for each of the Regular Grammars you found in the previous question.
- 11. You have seen how to construct a grammar for any regular language, using an NFA for the language. But suppose we wanted to construct a grammar for a regular language directly from a regular expression, and without constructing an NFA first. How would you do it? (The grammar need not be regular.)

12.

Let k be a fixed positive integer. A k-limited Pushdown Automaton is a Pushdown Automaton whose stack can store at most k symbols (regardless of the length of the input string).

- (a) Explain how a k-limited Pushdown Automaton can be simulated by a NFA.
- (b) Deduce that a language is recognised by a k-limited PDA if and only if it is regular.
- 13. In Australian Rules Football, a team gains *points* by kicking *goals* and *behinds*. A goal is worth 6 points, and a behind is worth one point. The winner is the team with the greatest number of points at the end of the game.

A team's score is given as a triple a numbers (y, b, p), where g is the number of behinds, and p is the number of points. These numbers must be nonnegative and satisfy 6g + b = p. For example, (1, 2, 8) is a valid score, since $6 \times 1 + 2 = 8$.

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e scores.

1111) \in FootyScore.

In this language, ther

(a) Is the language Fc

(b) Is the language Formula (b

14. Prove by induction that the CYK algorithm correctly determines whether or not a given string x is generated by a given context-free grammar G.

More specifically: WeChat: cstutorcs

- 1. Prove by induction on n that, for every substring y of x, where |y| = n, the algorithm correctly finds all nonterminals in G that can generate y.
- 2. Explain briefly how is with a thin of the line of the control of the whether x can be generated by G.

The idea of the proof is given in Lecture 16, slide 18. Your task is to avoid the gap in that sketch proof ("Continue, in this way...") and produce a correct proof by marcine.

15. A finite sequence $(x_1, x_2, ..., x_n)$ of positive integers is *strictly increasing* if, for all i such that $1 \le i \le n-1$, we have $x_i < x_{i+1}$.

In this question, sequences are represented as binary numbers separated by #. For example, the sequence (1, 2, 5, 14, 42) consisting of the first five Cataran numbers², is represented as

1#10#101#1110#101010

Let SIS be the language towards three-letter alphabet {0.1 #}, consisting of all strictly increasing sequences of positive integers with each sequence represented as described above.

Prove that SIS is not context-free.

16. In the game of Cricket, a bowler "bowls" a cricket ball at a batsman. Each time this is done, the batsman tries to hit the ball, and might score some number of runs, or the bowler might take the wicket of the batsman (in which case the batsman has to leave, and is replaced by another batsman). A bowler bowls the ball six times, making up an over, and then makes way for another bowler to have their turn.

In cricket statistics, a bowler's activity is summarised by four integers: O, M, R, W, where

- O is the total number of **overs** bowled by that bowler,
- *M* is the number of **maiden overs** by that bowler: these are those overs in which no run was scored by batsmen,
- R is the number of **runs** scored from the bowling of that bowler,

 $^{^2}$ The n-th Catalan number counts the number of members of the Dyck language that have n pairs of matching parentheses. The Catalan number sequence has links to a wide range of topics in Computer Science and "occurs in connection with so many recursive algorithms" (Donald E. Knuth, *The Art of Computer Programming, Vol. 3, Sorting and Searching, Addison-Wesley, Reading, Ma., 1973, p. 296.*)

· W is the number 程底线 馬拉姆 CS编程辅导

We assume: 3

• A batsman can s a each ball bowled, making up to 36 runs from an over.

• At most one wice the state of the state of

We also use the fact the fact the fact that the fact that

- $(111\cdots 11,1111,1111\cdots 11,11)$ \in CricketBowlingFigures. It represents the bowling figures (27,4,72,2). 5 WeChat: cstutorcs
- $(11, 1, \overbrace{111 \cdots 11}, 1111111111111) \in \text{CricketBowlingFigures}$. It represents the bowling figures (2, 1, 36, 12).
- (,,,) \in CricketBowingFigure. It represents the bowing figures (0,0,0,0) of a bowler who does not get a turn at bowling.
- (1,11,111,1111) CricketBowlingFigures. The bowling figures (1,2,3,4) are impossible, since O < M.
- $(11,1,\overline{111\cdots 11},1111111111111) \notin \text{CricketBowlingFigures}$. The bowling figures (2,1,36,13) are impossible, since $\sqrt[6.7]{49389476}$
- (a) Is the language CricketBowlingFigures regular? Prove or disprove.
- (b) Is the language Crack BOSEF grants to the Free Special Properties of the Special Properties

 $^{^3}$ Cricket experts might notice some simplifying assumptions here . . .

 $^{^4}$ In unary representation, a number n is represented as a string of n 1s. For example, in unary, the number 5 is represented by 11111, and 0 is represented by the empty string.

⁵Question for cricket tragics: what is the significance of these bowling figures, in the history of Test Cricket?