程序代馬战 CS编程辅导

Faculty of Information Technology Semester 2, 2022

"IT2014 utorial 1 ges and Logic

ASSESSED PREP

You must provide a s campus classes), or su appropriate week in M on 6.

entire question at the start of your tutorial (for onfart of your tutorial using the class-specific link in the

- 1. Let ODD-ODD be the language of strings, over the alphabet $\{a,b\}$, that contain an odd number of a's and an odd number of bs. Let ODD-ODD be its complement. Prove that PALINDROMES \subseteq ODD-ODD.
- 2. Distributive Law Ar propisitional logicent Project Exam Help

 $P \lor (Q \land R)$ is logically equivalent to $(P \lor Q) \land (P \lor R)$.

(b) Prove that

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 $P \wedge (Q \vee R)$ is logically equivalent to $(P \wedge Q) \vee (P \wedge R)$,

using part (a) and a rule named after affrigate that have a friend of that is the same affrigate that the same affrigate that is the same affrication of the same affrication

3. Prove that

 $(P_1 \wedge \cdots \wedge P_n) \Rightarrow C$ is logically equivalent to $\neg P_1 \vee \cdots \vee \neg P_n \vee C$ **https://tutorcs.com**

4. A meeting about moon mission software is held at NASA in 1969. Participants may include Judith Cohen (electrical engineer), Margaret Hamilton (computer scientist), and Katherine Johnson (mathematician). Let Judith, Margaret and Katherine be propositions with the following meanings.

Judith Judith Cohen is in the meeting.

Margaret Hamilton is in the meeting.

Katherine Johnson is in the meeting.

For each of the following statements, write a proposition in Conjunctive Normal Form with the same meaning.

- (a) Judith and Margaret are not both in the meeting.
- (b) Either Judith or Margaret, but not both of them, is in the meeting. (This is the "exclusive-OR".)
- (c) At least one of Judith, Margaret and Katherine is in the meeting.
- (d) At most one of Judith, Margaret and Katherine is in the meeting.
- (e) Exactly one of Judith, Margaret and Katherine is in the meeting.
- (f) At least two of Judith, Margaret and Katherine are in the meeting.
- (g) At most two of Judith, Margaret and Katherine are in the meeting.

Exactly two of Julian, Margaret and Sthorin are in the meeting 程辅导

Exactly three of Judith, Margaret and Katherine are in the meeting.

None of Judith, Margaret and Katherine is in the meeting. (i)

Suppose we have if, Bipartite, Internal about a connected graph with at **5**. least two vertices, wit

Tree The grap! **Bipartite** The grap! Leaf

 ≥ 2 . (Such a vertex is sometimes called an *internal vertex*.) Internal The grap

Using these propositions, write a proposition in CNF with the following meaning:

If the graph is a tree, then it's bipartite and has a leaf, but if it's not a tree, then it has a vertex of degree 22 Chat: CSTUTOTCS

For each past or present Monash unit, we'll use its unit code to denote the proposition that you have passed the unit. SA if ABC1234 is a unit code, the we'll also use ALC1234 for a prolotical p with the following meaning.

Here is an edited extract from the Monash Handbook 2022, specifying the conditions under which you may enrol in FIT **O:** O: 749389476

Prerequisite:

• One of FIT1045, FIT1048, FIT1051, FIT1053, ENG1003, ENG1013 or (FIT1040 https://tutorcs.com

AND

• One of MAT1830, MTH1030, MTH1035, ENG1005

Prohibition:

- CSE2303
- (a) Using these rules and the propositions corresponding to all these unit codes, construct an expression in Conjunctive Normal Form that specifies the conditions under which you may enrol in FIT2014.

Now consider how you would construct an equivalent expression in <u>Disjunctive Normal Form</u>:

$$\underbrace{(\dots \wedge \dots \wedge \dots)}_{\text{disjunct}} \vee \underbrace{(\dots \wedge \dots \wedge \dots)}_{\text{disjunct}} \vee \dots \dots \vee \underbrace{(\dots \wedge \dots \wedge \dots)}_{\text{disjunct}}$$

(b) Give three of the disjuncts in such an expression.

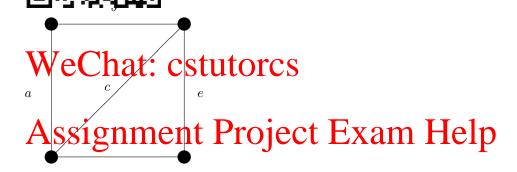
¹Thanks to FIT2014 tutor Ben Jones for detecting and reporting a small error in an earlier version of this question.

(c) How many disjute word such near the CS编程辅导

7. (mostly from FIT2014 Final Exam, 2015)

A **perfect match** subset X of the edge set of G that meets each vertex exactly once. In othe in X share a vertex, and each vertex of G is incident with exactly one edge

For example, in the latest section $\{a, e\}$ is a perfect matching. But $\{a, b, e\}$ is not a perfect matching (since some vertices a latest section $\{a, e\}$ is a perfect matching (since some vertices a latest section $\{a, e\}$ is not a perfect matching (since some vertices a latest section $\{a, e\}$ is not a perfect matching (since some vertices a latest section $\{a, e\}$ is not a perfect matching (since some vertices a latest section $\{a, e\}$ is not a perfect matching (since some vertices a latest section $\{a, e\}$ is not a perfect matching.



Let W be the abovernail: tutorcs@163.com

Construct a Boolean expression E_W in Conjunctive Normal Form such that the satisfying truth assignments for E_W correspond to perfect matchings in the above graph W.

When doing this, use Boolean variables a b c, d e which are each True if and only if the edge with the same name belongs to the perfect matching 4

- 8. Using the function symbol father, the predicate taller, and the constant symbols claire and max, convert the following sentences to Predicate Logic. Assume that taller(X,Y) means X is taller than Y and the miverse Conscourse is "all prope".
- ii. Max's father is taller than Max but not taller than Claire's father.
- ii. Someone is taller than Claire's father.
- iii. Everyone is taller than someone else.
- iv. Everyone who is taller than Claire is taller than Max.
- **9.** Suppose you have access to the following functions and relations:
 - |x| = the length of the string x
 - equality and inequality relations: $=, <, \le, >, \ge$
 - set membership, denoted by \in as usual.

Let L be a language.

- (a) Using quantifiers, write down a logical statement about L that is True if and only if L is finite.
- (b) Now write a statement about L that is True if and only if L is infinite.

Supplementar程底试写代做 CS编程辅导

10. Three boys, Adam Brian and Claude, are caught, suspected of breaking a glass winpolice: dow. When the

nocent'. Adam said:

Brian said: \mathbf{F} is Claude'.

lacksquare others did'. Claude said:

re telling the truth, and therefore concluded that The police believ Brian broke the didn't.

Using the following propositions statements of the boys and the police conclusion in propositional logic.

- A: Adam broke the Window Chat: cstutorcs
- B: Brian broke the window
- C: Claude broke the window.

Assuming that all the Assystatin the tentral tas Report ecits in Foxcay maid? Help

Recall the logical expression given near the end of Lecture 2 for your dinner party guest list: 11.

(Harry V Ron V Harris Adilly) tutores @ 163.com

- \land (¬Fred \lor George) \land (Fred \lor ¬George)
- $\begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \\ \end{array} \end{array} & \wedge \end{array} (\neg \text{Bellatrix} \lor \neg \text{Dolores}) \end{array}$ (¬Voldemort

How long would an equivalent DNF expression be? Specifically, how many disjuncts — smaller expressions combined using \vee to make the whole expression — would it have?

Leonard Book , Tellic Snith Arthur Son Cast Fill Diff used the pseudonym Blanche 12. Descartes for some of their writings. Each work by Blanche Descartes was written by some nonempty subset of the four. Let Leonard, Cedric, Arthur and Bill be propositions about one of Blanche Descartes's works with the following meanings.

> Leonard Leonard Books was one of the authors. Cedric Cedric Smith was one of the authors. Arthur Arthur Stone was one of the authors. Bill Bill Tutte was one of the authors.

Write a proposition in Conjunctive Normal Form meaning that exactly two of the four were authors of the work.

13. One-dimensional Go.

This question uses some concepts from the ancient east Asian board game known as Go in the West, Wéigí in China, Go or Igo in Japan, and Baduk in Korea. This game is over 2,000 years old,

 $^{^2}$ While they were still undergraduate students at Cambridge, these four wrote a paper which solved a famous open problem of recreational mathematics, helped create modern graph theory and influenced the course of history: R. L. Brooks, C. A. B. Smith, A. H. Stone, and W. T. Tutte, The dissection of rectangles into squares, Duke Mathematical Journal 7 (1940) 312-340.

and is generally regarded as harder that Chos. Indeed, until very recently, temputer programs for Go could not defeat human professionals (in contrast to Chess, where the best computer players have been stronger than human world champions since the late 1990s).

in 2016, with stunning performances by the program The situation char AlphaGo, created by his company began as a start-up in London in 2010 and was acquired by ctober 2015, it defeated the European champion Fan tp://www.nature.com/news/google-ai-algorithm-Hui in every game of masters-ancient-ga ■hen in March 2016 it defeated Lee Sedol of Korea, world in recent times: https://www.theatlantic. generally regarded as risible-opponent/475611/. The final score in that com/technology/arc five-game match was Go. In May 2017 it defeated the top-ranked player lacktriangledowntps://deepmind.com/research/alphago/ $\,$ or http: in the world, Ke Jie //361points.com/articles/thoughtsonalphago/.

Go is played on a graph, usually a square lattice (grid) of 19×19 vertices. But we will use much simpler graphs in this question manely path graphs with n vertices and n-1 edges, where $n \ge 1$. For example, with n = 10 we get the following path graph with n = 10 vertices and n = 10 edges.

Assignment Project Exam Help A position consists of a placement of black and white stones on some of the vertices of the graph.

A position consists of a placement of black and white stones on some of the vertices of the graph. Each vertex may have a black stone, or a white stone (but not both), or be uncoloured (i.e., vacant). A position is *legal* if every vertex with a stone can be linked to an uncoloured vertex by a path consisting entirely of vertices with stones of that same coloured vertex at the end of that path).

For example, the following position is legal, since each of its three "chains" of consecutive vertices of the same colour either starts or ends with an uncoloured vertex.

QQ: 749389476.

But the following position is illegal, since it has a chain of white vertices with black vertices at each end. (The position like the position illegal.) But it only takes one without an uncoloured neighbour to make the position illegal.)



We number the vertices on the path graph from 1 to n, from left to right. We say that a position on this path graph is almost legal if vertex n is coloured (i.e., has a stone) and its chain is not next to an uncoloured vertex, but every other chain is next to an uncoloured vertex. In other words, it is illegal, but the only chain making it illegal is the chain containing vertex n; all other chains are ok. The two positions given above are not almost legal: the first is legal (so it isn't almost legal), while the second is illegal but the illegality is not due to the last vertex (which in this case is uncoloured). The following position is almost legal. All its chains are ok except the last one on the right.



Let $V_{B,n}$, $V_{W,n}$, $V_{U,n}$, $L_{B,n}$, $L_{W,n}$, $L_{U,n}$, $A_{B,n}$, $A_{W,n}$ be the following propositions about a position on the *n*-vertex path graph.

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 $V_{W,n}$ Vertex n is White.

 V_{Un} Vertex n is Uncoloured.

L gal, and vertex n is Black. gal, and vertex n is White.

gal, and vertex n is Uncoloured.

most legal, and vertex n is Black. most legal, and vertex n is White.

(a) Use the proposition is a logical expression for the proposition of the proposition of

Now consider how legality and almost-legality on the *n*-vertex path graph are affected by extending the path to vertex n + 1.

- (b) If $L_{B,n}$ is true, when possible state [Black) White [tree] can vertex n+1 be in, if we want the position to be legal on the n+1-vertex path as well? Do the same for $L_{W,n}$ and $L_{U,n}$.
- (c) If $A_{B,n}$ is true, what possible states can extend P being if we want the position to be less p to the same for $A_{W,n}$.

Why is there no line for $A_{U,n}$ in the table?

(d) Construct a logical expless of the proposition of the proposition of the proposition of the proposition of the n-vertex path graph, and the V-propositions for vertex n+1.)

Do the same for $L_{W,n}$ 1, $A_{M,n}$ 1,

14. A vertex cover in a graph G is a set VC of vertices such that every edge of G is incident with some vertex in VC.

A clique in a graph is a set of vertices that are pairwise adjacent. (I.e., every pair of vertices in the clique is linked by a letter S://tutorcs.com

The *complement* of a graph G, written G, is defined as follows. It has the same vertex set of G, and its edge set consists of every pair of vertices that are *not* adjacent in G.

Let n denote the number of vertices of the graph under discussion.

Suppose we have a graph, and that **chosen** is a unary predicate that takes a vertex of our graph as its argument. This predicate therefore defines a subset of the vertex set of the graph (the "chosen vertices"). Suppose also that we have the following predicates, with the indicated meanings.

 $\mathbf{vertex}(\mathbf{X})$ \mathbf{X} is a vertex in our graph $\mathbf{edge}(\mathbf{X}, \mathbf{Y})$ there is an edge between vertices \mathbf{X} and \mathbf{Y}

- (a) Write a statement in predicate logic, using the predicates **vertex**, **edge** and **chosen**, to say that the chosen vertices form a vertex cover.
- (b) Write a statement in predicate logic, using the same predicates, to say that the chosen vertices form a clique.
- (c) Prove that, for any k, the number of vertex covers of size k in G equals the number of cliques of size n k in \overline{G} .
- (d) Give the relationship between the size of the smallest vertex cover in G and the size of the largest clique in \overline{G} .