Clayton School of Information Technology



### Assignment Project Exam Help

Email: tutorcs@163.com

Instructions:

10 minutes reading time.
3 hours writing Q: 749389476

No books, calculators or devices.

Total marks on https://tutorcs.com

Answers in blue.

Comments in green.



WeChat: cstutorcs

Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476

#### Question 1

# 程序代写代做 CS编程辅导(4 marks)

You are hunting a mouse in your wardrobe.

C: The moust

H: The mous

S: The moust

Use C, H and  $\blacksquare$  sition, in Conjunctive Normal Form, that is True precisely when the n  $\blacksquare$  set three locations: your coat, your hat or your shoe.

It's ok to have it in 3-CNF, which would have 7 clauses, provided done correctly. But the question does not stipulate 3-CNF.

Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476

Question 2 Suppose you have the digited tomper and the web Sanoting things:

computer(X): X is a computer. any Turing machine. utm(X):

cate logic with the meaning: (a) Write a universa

> "Everythin any Turing machine is a computer."

WeChat: cstutorcs Alternative:

# 

 $(X) \Rightarrow \mathtt{computer}(X)$ 

(b) What additional fact would you need to know, to be able to use this statement (and nothing else) to prove that the object myPhone is a computer? (Express this fact as an atomic sentence in prediction (2) tutores (a) 163.com

utm(myPhone)

QQ: 749389476

No need for full stop at the end, as this is predicate logic, not a Prolog fact.

Question 3
(a) Write down all strings first first Settler, the alphabeth, the regular the regular control of the control of th expression  $(((ab) \cup (ba))a)^*$ .

 $\varepsilon$ , aba, baa, aba a, baabaa.

(b) Give an NFA wi expression.

at recognises the language described by this regular

: cstutorcs

signment Project Exam Help

Email: tutorcs@163.com

Equivalent answers with extra enorgy Rensidons are ok.

Question 4

A language over alptaet 作的 such that a state of the the such that a state of the the such that a state of the the such that a state of the such t alphabet except for some finite number of strings. Prove that every cofinite language is regular.

A cofinite language Any finite language Regular languages a So any cofinite lang

plement.

plement of a regular language) is regular.

Alternative solution

Let L be any cofinite language.

Its complement,  $\overline{L}$ , is finite.

Therefore  $\overline{L}$  is regular to every fittle larger to represent the contraction of the contraction  $\overline{L}$  is regular to  $\overline{L}$  and  $\overline{L}$  is regular to  $\overline{L}$ .

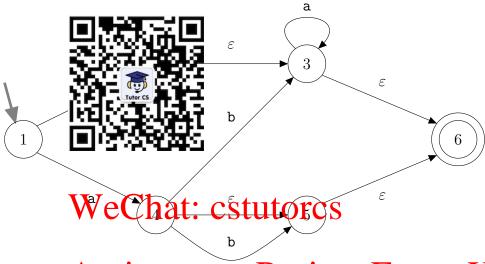
Therefore,  $\overline{L}$  is recognised by a Finite Automaton, by Kleene's Theorem.

If we change that FA so that every Final state becomes Non-Final, and every Non-Final state becomes Final, then we obtain an FA that pecepts precisel those strings met in  $\overline{L}$  in other words, this FA Supplement Project Exam Help Therefore L is regular, by Kleene's Theorem.

Email: tutorcs@163.com

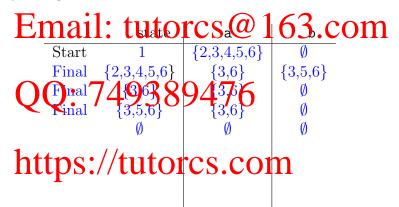
QQ: 749389476

Question 5
Given the following MA convertito Finite Attornators in the same language.



### Assignment Project Exam Help

Represent the FA by filling in the table below.



It's ok if the two states labelled  $\{3,6\}$  and  $\{3,5,6\}$  are merged. In fact, if the above FA is simplified using the state-minimisation algorithm, then those two states would be merged into one.

Question 6
Suppose you have, a Four Fishotal, Forthmitty converses to Regular Expressions and Regular Expressions to NFAs.

Explain how you would design and implement a lexical analyser to recognise tokens that match a particular result of the first section of the code come and implement a lexical analyser to recognise tokens that match a particular result of the code code, but do explain where the code come and the code code is a code of the code code.

Use one of the given Then use another gi Then convert the F ert the regular expression to an NFA to recognise it. nvert the NFA to an equivalent FA.

WeChat: cstutorcs

Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476

Use the Pumping Le福岛所依斯岛所有的大阪 CS编程辅导 (6 marks)

 $\{ \mathbf{a}^m \mathbf{b}^n : m < n \}$ 

is not regular.

Suppose that the gi

Then there is a FA

Let w be any string This certainly ensur L) is regular.

et N be the number of states of this FA.

ve need in order to apply the Pumping Lemma.

Then the Pumping Lemma for Regular Languages tells us that w = xyz where substrings  $x, y, z \text{ satisfy: } y \neq \varepsilon$  What  $z \in S$  for all  $i \in S$ 

It is not possible for y to include any of the letter b, since in that case xy would include every a, and there are m of them, so we would have |xy| > m. This, together with m > N(by construction of was signament Project for Xiamph Chpa).

So y falls entirely within the aa...a at the start. This means that pumping increases the number of as (using the fact that  $y \neq 0$ ) but not be number of by Sufficient pumping will yield more as than by, giving a non-member of  $\mathcal{L}$ , which contradicts the conclusion of the Pumping Lemma. Hence our assumption, that L is regular, is false.

#### QQ: 749389476

One variation might be to use  $w = a^m b^{m+1}$ , but still have m > N. This means that, as soon as you pump once, to get  $xy^2z$ , then you have at least as many as as bs, hence a non-member of L, hatetapstracture torcs.com



WeChat: cstutorcs

Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476

# Question 8 Give a Context-Free 程序がは馬頭旋の CS 编程 辅导<sup>(2 marks)</sup>

 $\{ \ {\tt a}^m {\tt b}^n \ : \ m>2n, \ n\geq 0 \ \}.$ 



The following would be fine if, in addition, the empty string were included in this language. But it does not satisfy the condition.

 $S \rightarrow \mathtt{aa}S\mathtt{b}$ 

 $S \rightarrow \mathrm{a} S$ 

 $S \rightarrow \varepsilon$ 

#### WeChat: cstutorcs

The following would be fine if the condition were modified to require n > 0 instead of  $n \ge 0$ .

The following would be fine if the condition were modified to require n > 0 instead of  $n \ge 0$ .

The following would be fine if the condition were modified to require n > 0 instead of  $n \ge 0$ .

 $S \ \to \ {\rm aa}X{\rm b}$ 

xEmail: tutorcs@163.com

 $X \rightarrow \varepsilon$ 

QQ: 749389476

# Question 9 Consider the followin程offst 作 写点,做 CS编程辅导 (6 marks)



$$S \rightarrow S \mathfrak{b}$$
 (2)

$$S \rightarrow \varepsilon$$
 (3)

Prove by induction generated by this gr

the form  $\mathbf{a}^m \mathbf{b}^n$ , where  $m \geq 0$  and  $n \geq 0$ , can be

We prove this by in (i.e., on m + n).

Inductive basis: if the length is 0, then the string is empty, and is generated by (3).

Inductive step: Supply the resultables of the stable of the step of the resultable of the step of the

Now suppose we have a string  $w = a^m b^n$  of length  $\ell$ .

Either the string starts with a, or ends with b, or both. (This uses  $\ell > 0$ .)

If it starts with a, than it can be written  $w = 10^{\prime}$  where  $w' = 10^{\prime}$  where  $w' = 10^{\prime}$  The fact that w' has length  $v' = 10^{\prime}$  and  $v' = 10^{\prime}$  where  $v' = 10^{\prime}$  and  $v' = 10^{\prime}$  where  $v' = 10^{\prime}$  and  $v' = 10^{\prime}$  and  $v' = 10^{\prime}$  where  $v' = 10^{\prime}$  and  $v' = 10^{\prime}$  and v'

#### Email: tutores@163.com

By prefixing each string in this derivation by a, we can form another derivation:

QQ: 749389476

Prepending this derivation with the production  $S \Rightarrow aS$  gives a derivation of w:

### https://tutores.com

So w is generated by the grammar.

A similar argument applies if the string w ends with b. This completes the inductive step.

The result follows, by the Principle of Mathematical Induction.



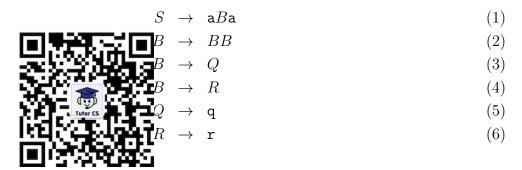
WeChat: cstutorcs

Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476

# Consider the followin程offet free 写响成的 CS编程辅导 (5 marks)



Give

- $\overset{\mathrm{(a)}}{\text{wechat: cstutorcs}}$
- (b) a parse tree,

for the string aqrqa, Abelling each step in the privation cashs light by the number of the rule used. Use the spaces below for your answers.

Email: tutorcs@163.com (a) Derivation:

by (2)

aBBBa by (2)

> aQRBa by (4)

> by (3) aQRQa

> aqRQa by (5)

by (6) aqrQa

by (5). aqrqa

Some variation in the order is possible.

Doesn't have to be leftmost or rightmost derivation.

(b) Parse tree:

### 程序代写代做 CS编程辅导



Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476

# Question 11 Given the following 程底存在写纸 CS编程辅导 (5 marks)



$$A \rightarrow AbA$$
 (2)

$$4 \rightarrow a \tag{3}$$

complete the following by the grammar.

a Pushdown Automaton for the language generated

$$\varepsilon, S \to A$$
  
 $a, A \to \varepsilon$ 

 $a, a \to \varepsilon$  is optional

WeChat: cstutorcs

Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476<sub>-,b</sub>

# Question 12 State two important states that can be roved until the Charles from the range of Context-Free Grammars.

1. The CYK algo was the string is generated by t

2. The Pumping v for any context-free language L and any sufficiently long string v for any context-free language L and any sufficiently empty, |vxy| is v for all v for al

WeChat: cstutorcs

Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476

Question 13
The 2's complement of Financian is followed by the complement of Financian is followed by the complement of Financian is followed by the complement of the complem

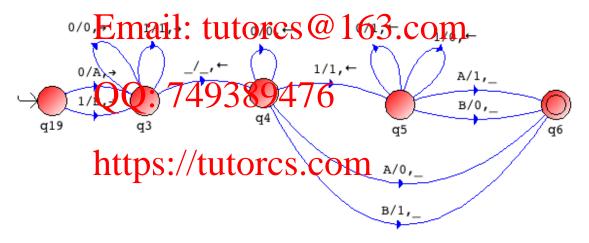
For example, if the etring is 0110100, then its 2's complement is 1001100.

Draw a Turing the 2's complement of any binary string.

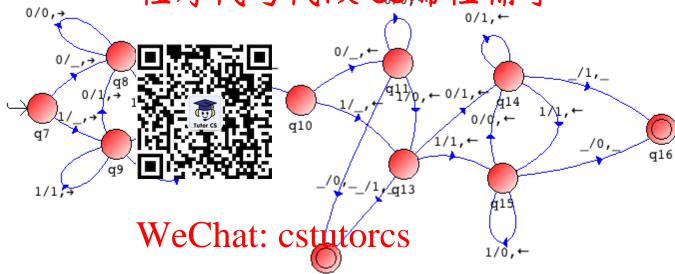


\* Allow any direction Assignment Project Exam Help

Here is the above in Tuatara, with some extra necessary arcs:



The following monstrous solution has the virtue of not introducing any extra characters into the tape alphabet, although that's not expected in this question:



Assignment Project Exam Help
Here is a solution working from the other end:

Email: tutores@163.com

# Question 14 (a) State the Church 程is 写代做 CS编程辅导 (4 marks)

Any function which can defined by an algorithm can be represented by a Turing Machine.

(b) Give two reason uring thesis is widely accepted.

Any two of the follo

• different approach and a substant approach approach and a substant approach approa

• long experience as programs, and therefore on Turing machines

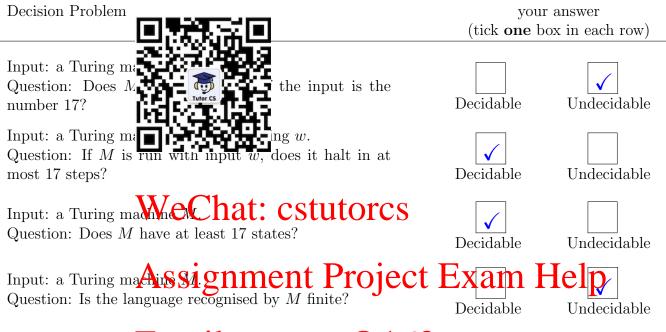
• no known counterexamples, i.e., no algorithms which seem to be unimplementable **CSTUTOTCS** 

### Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476

### Question 15 For each of the following decision troughts, tool the whether the city of the



Email: tutorcs@163.com

QQ: 749389476

Question 16 The Venn diagram of the next page tows several classes of the graves (a)-(j) in the list below, indicate which classes it belongs to, by placing its corresponding letter in the correct region of the diagram.

If a language do of these classes, then place its letter above the top of the diagram.

- (a)
- $\{\mathbf{a}^n\mathbf{b}^n:n>0\}$  $\{\mathbf{a}^n\mathbf{b}^n\mathbf{c}^n:n>$
- (c)
- (d) The set of all graphs containing a Hamiltonian circuit.
- The set of all gashes pthat no Cistutores (e)
- (f) The set of all correctly formed arithmetic expressions that only use positive integers and the symbols + and -. Assignment Project Exam Help (g) The set of all (encoding of) Turing machines that eventually halt, when given the
- selves as input.
- The set of all (Incodings pl) Tyring prochings (In) loof ever when given themselves (h) as input.
- (i) The set of all strings that have ever caused any real computer to eventually halt.
- The set of all Cottex-Free Gamma that defin an empty language. (j)



# Question 17 Prove that the follow 程序原纸 写纸 CS编程辅导 (7 marks)

Input: a Turing machine M, and a string x.

Question: If M is run on input x does it eventually accept x?

You may use the way was a ng Problem is undecidable.

Let M, x be any input of the problem, where we want to know whether or not M eventually halts where M is the problem.

From M, x, we constitute M program, which we call  $P_{M,x}$  (since we get a different program for even M, x) since M, x are hard-coded into the program):



If M halts for input A to symptometry, A in the property A with input A, and after that simulation halts (which it must, eventually, in this case), it will Accept.

On the other hand, it mail not tutorics @the 63, com get stuck in its simulation of M with input x, so it will never Accept.

So, M halts for input A f and only in  $P_{M,x}$ . (And this holds no matter what input is given to  $P_{M,x}$ .)

Therefore, if we have a decider, D, for the problem given in the question, then we can use it to construct a decider S for the literary S becomes as follows.

Suppose M, x is input to the halting problem. Compute the program  $P_{M,x}$ . (This is possible, as constructing the program  $P_{M,x}$  from M, x is computable.) Pick any input for  $P_{M,x}$  that you like. Use D to decide whether or not  $P_{M,x}$  accepts that input. If it does, then the answer to the halting problem is Yes; if it doesn't, the answer to the Halting Problem is No. So we have a decider for the halting problem.

This contradicts the undecidability of the Halting Problem. So the assumed decider, D, cannot exist. So the problem given in the question is undecidable.



WeChat: cstutorcs

Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476

Question 18
Let L be a recursive repulse (5) flagging. WS fine the first there is an enumerator that enumerates L. Here is an attempt at constructing an "enumerator" for L.

Let M be a Turing machine whose set of accepted strings is L. Construct another Turing machine E which do

```
For each string w = \underbrace{ }_{\text{Tubercs}} \underbrace{ }_{\text{turn (i.e., sequentially):}} \underbrace{ }_{\text{Input } w.} \underbrace{ }_{\text{Input } w.} \underbrace{ }_{\text{Continue to the next iteration.}} \underbrace{ }_{\text{turn (i.e., sequentially):}} \underbrace{ }_{\text{turn (i.e., sequentially):}}
```

### WeChat: cstutorcs

(a) What is wrong with this attempt at an enumerator?

It is quite possible that of some spainting and the problem has a problem of that iteration, and it never gets to examine any string w that comes later in the ordering of the strings. So those later strings can never be output by the enumerator of the sumerator cannot enumerate all strings in L (unless 113 bits). TULTORS of 163.COM

(b) Indicate briefly what would need to be done to fix it. (You don't need to say in detail how to fix it, but just indicate in general terms what to do.)

The simulated execution of M on each string w needs to be split up so that, in each main iteration, you just simulate one step of the execution of the machine on each of several strings w. By enlarging, at **a little Strict that OTC** of **Chilf** onsidered, you can ensure that all the required simulation is done eventually, in parallel.

Question 19
Suppose M is a Turner machine with time confidence of the computation in at most  $t^4$  steps.

(4 marks)

Turing Machine that can simulate any t-step Turing machine computation in at most  $t^4$  steps.

Find an upper  $\square$  tation and with proof, of the time taken by U to simulate the computation  $\square$  and  $\square$  input of size n.

Let x be an input st n is sufficiently large

r M. Then there is a constant c such that, provided of steps) taken by M for input x is  $\leq cn^3$ .

These steps can be simulated by U in  $\leq (cn^3)^4$  steps, i.e., in  $\leq c^4n^{12}$  steps. Since  $c^4$  is a constant, this means that the time taken by the simulation is  $O(n^{12})$ .

WeChat: cstutorcs

Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476

# 

Let L be a regular la Kleene's Theorem, there is a FA which recognises L. (or a computer program) that keeps track of which We can turn this int pending on that state, and what the next letter is, state the FA is in, TM (or program) looks at each letter of the input determines what the that letter — checking what it is and changing its string, in turn, and can be done in only a few steps (constant time record of the curren ormation is organised and managed). Multiply this or linear time, deper Hand you get an overall time complexity of quadratic by the number of le time or better. So it takes polynomial time, so L is in P. Hence every regular language is in P.

#### WeChat: cstutorcs Question 21

(2 marks)

Suppose that a particular decider has polynomial time complexity. When inputs are sufficiently large, what happens to its running time when the length of the input is doubled?

Choose one of the assignment beroject presidente Help

If more than one answer holds, you must choose the strongest (i.e., most precise) correct answer. Email: tutorcs@163.com

- (a) It is raised to at most a constant power.
- (b) It is increased by
- (c) It is increased by at most a constant amount.
- (d) It is at most doubled. //tutorcs.com It is at most squared.
- (e)
- (f) It increases by at most 2.
- (g) It doubles after two years, according to Moore's Law.

#### Question 22

## 程序代写代做 CS编程辑 字 1 marks)

Consider the language NO MONOCHROMATIC TRIANGLE, which consists of all graphs G such that we can assign colours to the edges of the graph so that (i) each edge is either Black or White G or G of length G in the graph which is G in the graph

(a) Prove that the l

CHROMATIC TRIANGLE is in NP.

Here is a verifier:

```
Input: graph C
Certificate: a 2 Certific
```

[This can be described in various ways. E.g., as an assignment of either Black or White to each edge of G, or a list of colours, Black/White, one colour for each edge, or a partition of the set of edges into two Arts still gnment Project Exam Help For each triangle of G:

```
if the three part he transcent sub-3 comment and Stop.

Accept and Stop.
```

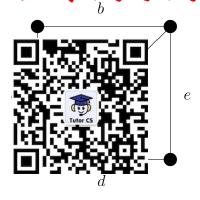
[If we reach this pint, exclution 389 bave of non-monochromatic.]

It should be clear from the construction of the verifier that it will accept if and only if the input graph belongs to NO MONOCHROMATIC TRIANGLE.

https://tutorcs.com

It remains to show that this verifier runs in polynomial time. To see this, observe that a graph on n vertices has  $O(n^3)$  triangles, so the number of outer-loop iterations is  $O(n^3)$ . For each such triangle, we must check that the three edges do not all receive the same colour. The exact amount of time taken by this depends on the details of the implementation (what data structure is used for the graph, etc.), but in any case takes polynomial time, and should take constant or linear time. Multiplying this by  $O(n^3)$  gives a total time which is polynomial in the input size. So the verifier is a polynomial-time verifier. So NO MONOCHROMATIC TRIANGLE has a polynomial-time verifier, hence it is in NP.

Now, let W be the following graph 代做 CS编程辅导



(b) Construct a Boolean expression  $E_W$  in Conjunctive Normal Form such that the satisfying truth assignments of  $E_W$  correspond to Johnson to the NO MONOCHROMATIC TRIANGLE problem on the above graph W (i.e., they correspond to colourings of the edges of W which have no monochromatic triangle).

Assignment Project Exam Help Using variables a, b, c, d, e, with True meaning Black and False meaning White (or the other

way round):

(a Email: tutores @el/63/com

An alternative approach is to use variables  $B_a, W_a, B_b, W_b, B_c, W_c, B_d, W_d, B_e, W_e$ , with the interpretation that lor any edge in the graph, O

 $B_x$  = True if edge x is Black, and False otherwise; What to True of the troise. Con the otherwise.

This is more cumbersome. The expression should then be:

$$(B_a \vee B_b \vee B_c) \wedge (W_a \vee W_b \vee W_c) \wedge (B_c \vee B_d \vee B_e) \wedge (W_c \vee W_d \vee W_e) \wedge (B_a \vee W_a) \wedge (\neg B_a \vee \neg W_a) \wedge (B_b \vee W_b) \wedge (\neg B_b \vee \neg W_b) \wedge (B_c \vee W_c) \wedge (\neg B_c \vee \neg W_c) \wedge (B_d \vee W_d) \wedge (\neg B_d \vee \neg W_d) \wedge (B_e \vee W_e) \wedge (\neg B_e \vee \neg W_e)$$

The first four clauses are clearly analogous to the four clauses of the earlier expression. The last ten clauses are to ensure that each edge gets precisely one colour.

### (c) Give a polynomial-time reduction from NO MONOCHROMATIC TRIANCLE to SAT-ISFIABILITY. 在了了一个文化的文化。

```
Input: Graph G.

For each edge of G, create a new variable.

For each triangle T

{

Let a,b,c be the create two new variable.

[Some might use that's fine if the content of the content of the create two new variable.

[Some might use that's fine if the content of th
```

Output: the conjunction of all the clauses created so far.

WeChat: cstutorcs

Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476

# (d) State the Cook-Levin Theorem 写代做 CS编程辅导

 ${\bf SATISFIABILITY} \ {\bf is} \ {\bf NP-complete}.$ 

MATIC TRIANGLE is NP-complete



(e) Given the facts what else, if anythi

question:
to prove, in order to show that NO MONOCHRO-

#### SAT SAT P NO MONOWPO (A hat: A statement of the stat

Reasoning, thoughts signaments broject Exam Help We know SAT is NP-complete, and we know NO MONOCHROMATIC TRIANGLE is in NP. So, if we show that SAT  $\leq_P$  NO MONOCHROMATIC TRIANGLE, then we have completed the proof than a MONOCHROMATIC TRIANGLE.

QQ: 749389476



WeChat: cstutorcs

Assignment Project Exam Help

Email: tutorcs@163.com

QQ: 749389476