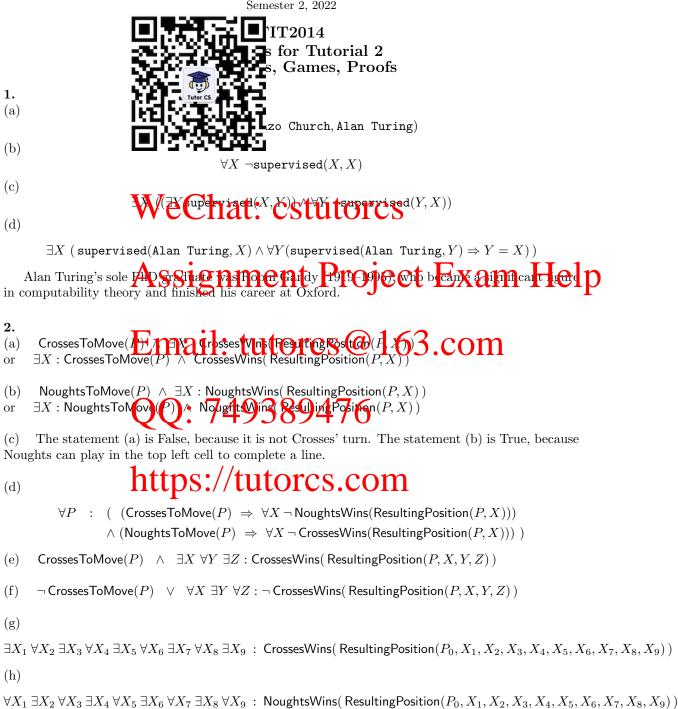
程序代屬优數 CS编程辅导

Faculty of Information Technology Semester 2, 2022



 $[\]forall X_1 \ \exists X_2 \ \forall X_3 \ \exists X_4 \ \forall X_5 \ \exists X_6 \ \forall X_7 \ \exists X_8 \ : \ \mathsf{NoughtsWins}(\ \mathsf{ResultingPosition}(P_0, X_1, X_2, X_3, X_4, X_5, X_6, X_7, X_8))$

The following is also correct (why?):¹

Thanks to FIT2014 tutor Zhi Hao Tan for spotting an error in an earlier version of (h)&(i) and helping correct it.

程序代写代做 CS编程辅导 (i)

 $(\exists X_1 \ \forall X_2 \ \exists X_3 \ \forall X_4 \ \exists X_5 \ \forall X_6 \ \exists X_7 \ \forall X_8 \ \exists X_9 \ :$ \neg NoughtsWins(ResultingPosition $(P_0, X_1, X_2, X_3, X_4, X_5, X_6, X_7, X_8, X_9)))$

 $(\forall X_1 \exists X_2 \forall X_3 \exists X_4 \forall X_5 \exists X$ rossesWins(ResultingPosition $(P_0, X_1, X_2, X_3, X_4, X_5, X_6, X_7, X_8, X_9))$

In fact, using some ba above solution is suffice

me, it's possible to show that the second part of the

 $\forall X_1 \exists X_2 \forall X_3 \exists X_4 \forall X_5 \exists X_6$

tesWins(ResultingPosition $(P_0, X_1, X_2, X_3, X_4, X_5, X_6, X_7, X_8, X_9)$)

Why is that?

(j)

 $\exists X_1 \ \exists X_2 \ \exists X_3 \ \exists X_4 \ \exists X_5 \ \bigvee_6 \ \bigoplus \ \exists X_8 \ \biguplus_{1} \ \vdots \ \mathsf{NogStWild}(\mathsf{ReslingSosition}(P_0,X_1,X_2,X_3,X_4,X_5,X_6,X_7,X_8,X_9))$

In fact, if Noughts wins at all, then it must win on the eighth move (i.e., Noughts's fourth move), because the last move (X_9) is by Crosses and that move cannot undo a line of Noughts already formed. So an alternative splitting in ment Project Exam Help $\exists X_1 \exists X_2 \exists X_3 \exists X_4 \exists X_5 \exists X_6 \exists X_7 \exists X_8 : \text{NoughtsWins}(\text{ResultingPosition}(P_0, X_1, X_2, X_3, X_4, X_5, X_6, X_7, X_8))$

Furthermore, for Noughts to win frem P_0 , it is sufficient to erecate a line of three Noughts while no line of three crosses is created and also they lim little the conglets in part of a pa three Crosses such that those Crosses are not in a line. Therefore, it is possible for Noughts to win if and only if it is possible for Noughts to win within six moves (i.e., three moves each). Therefore another correct solution is:

 $\exists X_1 \; \exists X_2 \; \exists X_3 \; \exists X_4 \; \mathsf{Q}_5 \\ \mathsf{X}_6 \; : \; \mathsf{NoughtsWins}(\mathsf{ResultingPosition}(P_0, X_1, X_2, X_3, X_4, X_5, X_6))$

The justification for six-move solution makes use of some more detailed properties of Noughts and Crosses. The justification for the eight-move solution only uses the property that it is never a disadvantage to move in this game. (In other words, it would felter be advantageous to pass, if that were allowed.) The nine-move solution uses no specific properties of the game at all, other than that it finishes in at most nine moves. It was all we were looking for in this question, as the focus is on predicate logic, quantifiers, and the relationship between quantifiers and assertions about moves in games.

3. Assume, by way of contradiction, that there exists a nonempty hereditary language that does not contain the empty string. Let L be such a language.

Since L is nonempty, it contains at least one string, and therefore it contains a shortest string. Let x be a shortest string in L. Since L does not contain the empty string (by assumption), x cannot be empty. So it has length ≥ 1 , and therefore contains some letters.

Since L is hereditary, some string x^- obtained from x by deleting one letter of x must also belong to L. But this gives a member of L which is shorter than the shortest possible string in L. This is a contradiction. So our assumption, that there exists a nonempty hereditary language that does not contain the empty string, must be wrong. Therefore every nonempty hereditary language contains the empty string.

²Thanks to FIT204 tutor Nathan Companez for spotting and correcting an error in an earlier version of this note to the solution of part (i).

³Thanks to FIT2014 tutor Nhan Bao Ho for this observation and the next one.

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- (a) k-th odd number = 2k 1
- (b) Inductive basis 1^2 , so 1^2 to 1^2 of the first k odd numbers is just the first odd number, 1, which equals 1^2 , so

(c)

4.

Sum c Tutor cs — mber

- = **Tradit George T**h odd number)
- = (sum of the first k odd numbers) + ((k + 1)-th odd number)
- = (sum of the first k odd numbers) + 2(k+1) 1

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(d) Continuing from above,

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(e) Continuing from above,

Email: tutorcs@163.com = $(k+1)^2$.

This completes the Incurrence tep Te 4 going in 8 to 4 k 7 to

- (f) So, by the Principle of Mathematical Induction, it is true for all k that the sum of the first k odd numbers is k^2 .
- 5. Base case: $n = \frac{\text{https://tutorcs.com}}{\text{total}}$

The tree with one vertex has zero edges, which is 1-1, so the claim is true for n=1.

Inductive step:

Suppose $k \geq 1$, and that any tree with k vertices has k-1 edges.

Let T be any tree with k+1 vertices.

Now, every tree with ≥ 2 vertices has a leaf, and removing any leaf from a tree gives another tree with one fewer vertex and one fewer edge.

So, remove a leaf from T. Let T^- be the smaller tree so obtained. It has k vertices, so we can apply the Inductive Hypothesis to it. This tells us that T^- has k-1 edges. Since we only deleted one edge when we deleted the leaf, this implies that T has (k-1)+1 edges, i.e., k edges. This is one fewer than its number of vertices. This completes the inductive step.

Therefore, by Mathematical Induction, it is true that, for all n, every tree on n vertices has n-1 edges.

6.

Base case: n = 3:

3! = 6, while $(3-1)^3 = 2^3 = 8$, so the inequality is true for n = 3.

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Suppose that $n! \leq (n-1)^n$ is true for a particular number n, where $n \geq 3$. Let's look at what happens at n+1.

```
(n+1)! = ( ess it in terms of a smaller case)

\leq ( y the Inductive Hypothesis, i.e., n! \leq (n-1)^n)

= ( a slight rearrangement ...)

\leq (a little high-school algebra ...)

\leq n^{n+1}

= ((n+1)-1)^{n+1}.
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This last line is just to make clear latter expression to of the required form.

So, by Mathematical Induction, it is true for all $n \geq 3$ that $n! \leq (n-1)^n$.

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7. Inductive basis (n = 1): P_1 is just x_1 , so if $x_1 = F$, then P_1 is immediately False. So the statement holds in this case.

Inductive step: Let $k \ge 1$. Assume the fifth $x_1 = F$ then by Figure 1. Assume the first $x_1 = F$ then we have

$$\begin{array}{ll} P_{k+1} &= P_k \wedge x_{k+1} & \text{(as noted in the question)} \\ \textbf{https://x/tutores.demonstrates} \\ F, \end{array}$$

which completes the inductive step.

Therefore the statement holds for all n, by Mathematical Induction.

8. (a) (b)

Inductive basis:

Inductive Step:

Suppose $n \leq 100$. Applying wc to standard output of this length gives a one-line standard output stating the numbers of lines, words and characters, with the number of characters being n. This output has 1 line, 3 (or 4?) words and some small number of characters consisting of the digit 1, the digit 3, a couple of digits (at most) for n, and some number of spaces (say, 21 altogether, but the analysis is much the same if this number is different). Applying wc again gives one line with these numbers in it: 1, 3, 25, again alongside 21 spaces. Another application of wc gives the same result. So the claim is true for $n \leq 99$.

Inductive step:

Now suppose the claim is true when the file/string has $\leq k$ characters, where $k \geq 100$. Suppose we are given a file/string of k+1 characters. Applying wc gives a one-line standard output, giving

numbers of lines, words程序优秀。另位体系CS编辑编号

l w k+1

For any number x, where x is a sum of digits in x. Our one-line output has some number x of spaces, same x is a sum of non-space characters is

 $\operatorname{rits}(w) + \operatorname{digits}(k+1).$

Now, $l \le k+1$ and $w \le s+3 \cdot \operatorname{digits}(k+1)$

e number of characters in the one-line output above is fk is large enough.

To see this, first try $\kappa = 100$. Then

 $s + 3 \cdot \operatorname{digits}(k+1) = 21 + 3 \cdot \operatorname{digits}(100 + 1)$

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= 30,

which is indeed $\leq k$. (Only minor changes are needed here if the actual value of s is not 21; it will not be *much* different from the property k indeeds k indeeds k (Figure 1), digit k (k k) with a state k the same or increases by k. But it only increases rarely, when k+1 becomes 100, then when it becomes 1000, and so on. So, given that s+3 digits $(k+1) \leq k$ for k=100 (and by a good margin), this inequality continues to hold for all higher k.

Since this is now set the part of the Hypothesis fells is an eventually give constant output.

Therefore the result follows for all n, by the Principle of Mathematical Induction.

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⁴In fact, $w \le (k+1)/2$, since every consecutive pair of words must have at least one space between them. But we don't need this better upper bound on w.

⁵Thanks to FIT2014 tutor Nathan Companez for part of this argument.