

程序代写代做 CS编程辅导

FIT2014 Theory of Computation



Lecture 7

Finite Automata
WeChat: cstutorcs

Assignment Project Exam Help
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Overview

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- ▶ Definition
- ▶ How they are used to define languages
- ▶ Representations
- ▶ Complement Languages
- ▶ Comparison with Regular Expressions

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Finite Automaton (FA)

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- ▶ Sometimes known as a **Deterministic Finite Automaton (DFA)**.
- ▶ Used for determining whether a word does or does not belong to a Regular Language.
- ▶ Used for defining a Regular Language.
- ▶ Used in Lexical Analysers.

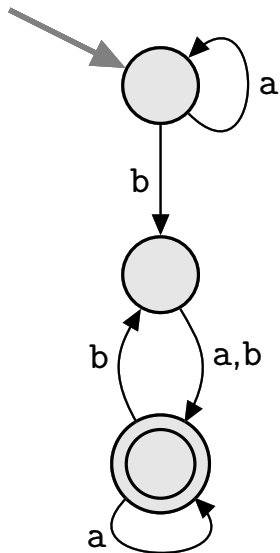
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state
represents vertices.
Specific



► Start State

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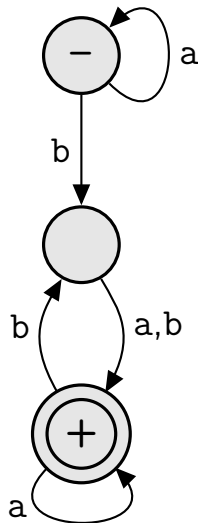
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transitions,
represented as directed edges,
labelled by letters

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Finite automaton: definition

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- ▶ A finite set of **states**
 - ▶ One called the Start State
 - ▶ Some (maybe none) called Final States
- ▶ An alphabet of possible input letters
- ▶ A finite set of **transitions**
 - ▶ that tell, for each state and each letter in the alphabet, which state to go to next.
 - ▶ There is a unique transition from any state for each letter in the alphabet.

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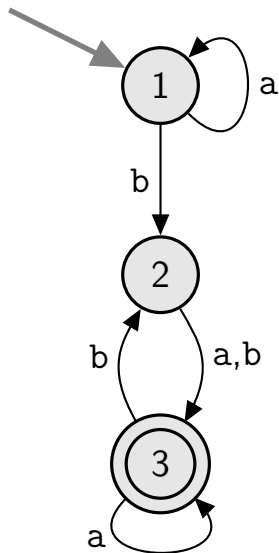
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Finite automaton: representations



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Finite automata

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Every string traces a unique path in the automaton, starting from the Start State and following the transitions, letter by letter.

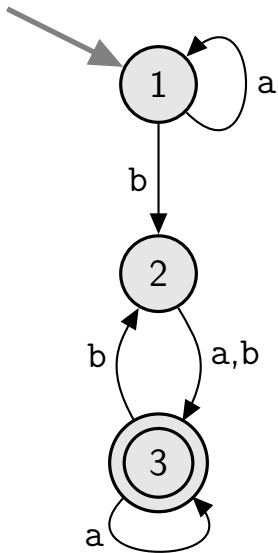
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		a	b
Start	1	1	2
	2	3	3
Final	3	3	2

Finite automata

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Algorithm 1: Execution of a Finite Automaton

Input: a string

Begin at the Start State.

while *there is another input letter* **do**

- | Read the next letter of the input string.
- | Move along the directed edge labelled by this letter.

if *you're in a Final State* **then**

- | Accept input string.

else

- | Reject input string.
-



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Finite automata

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Every string traces a unique path through an automaton, starting from the Start State and following the transitions, letter by letter.

Definitions

A string is **accepted** by a FA if its path ends on a Final State. Otherwise the string is **rejected**.

The **language recognised** by a FA is the set of all strings it accepts. We say the FA **recognises** the language, or **accepts** the language.

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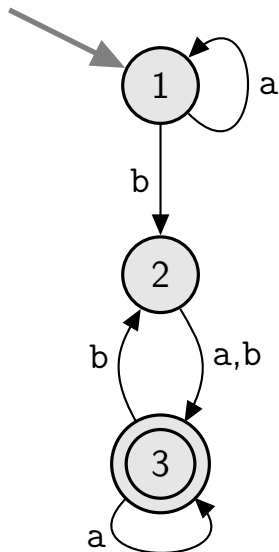
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Finite automata



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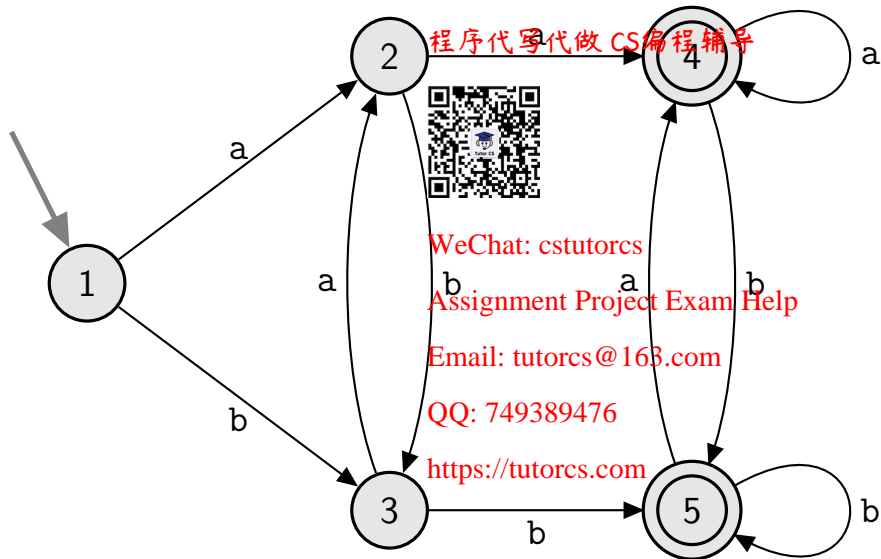
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		a	b
Start	1	2	3
	2	4	3
	3	2	5
Final	4	4	5
Final	5	4	5

Special Cases

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- ▶ All words accepted.
- ▶ No words accepted.
- ▶ Only the empty word accepted.
- ▶ Only non-empty words accepted.
- ▶ A single word accepted.

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Complements

If L is a language over an alphabet, then its **complement** \bar{L} is the set of words over the alphabet that are not in L .



$\Sigma^* \setminus L$

The complement of L is sometimes denoted by L' or L^c .

Examples

$$\bar{\emptyset} = \Sigma^*$$

$$\overline{\Sigma^*} = \emptyset$$

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$\overline{\{\text{words of } \leq 3 \text{ letters}\}} = \{\text{words of } \geq 4 \text{ letters}\}$

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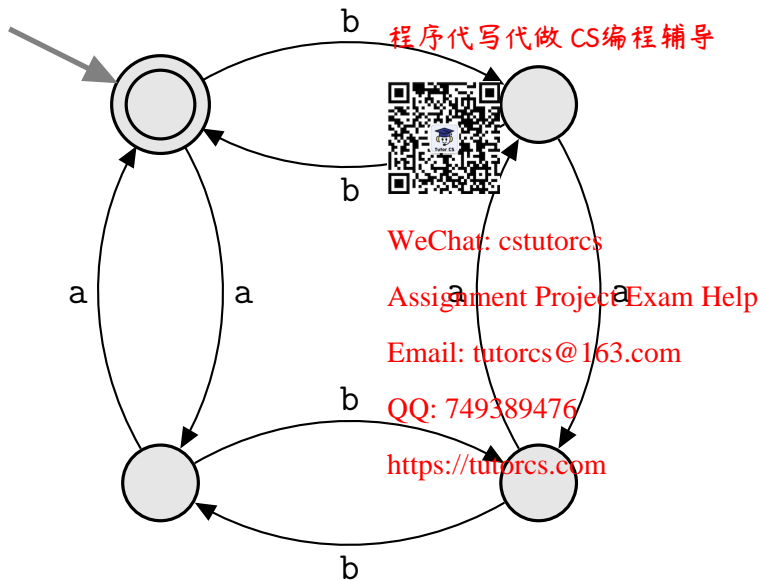
EVEN-EVEN $:=$ { strings that contain an **even** number of a's **and** an **even** number of b's }
 $=$ { ϵ , aa, bb, aaaa, aabb, abab, abba, baab, ... }.

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$\overline{\text{EVEN-EVEN}}$ $:=$ { strings which contain an **odd** number of a's **or** an **odd** number of b's }
 $=$ { a, b, ab, ba, aaa, aab, aba, abb, baa, ... }

EVEN-EVEN



Complement Finite Automaton (FA)

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Suppose some FA accepts the language L .



Change all the final states in the FA to non-final states,
and all the non-final states to final states.

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This new FA now accepts all the strings not accepted by the original FA
(i.e., all the words in \bar{L}),

and rejects all the words that the original accepted
(i.e., the words in L).

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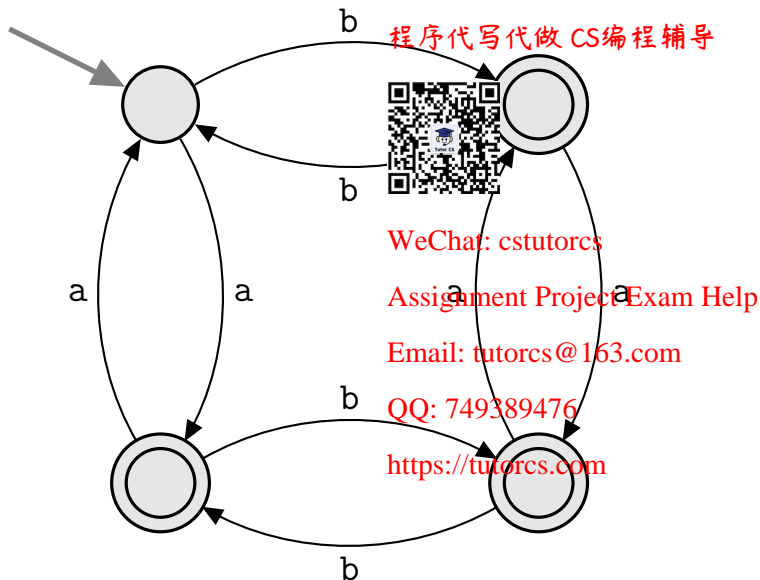
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So the new FA accepts \bar{L} .

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EVEN-EVEN



Comparison with Regular Expressions

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It is (usually) easier

to write down a **regular** **on** that defines a language
than

to design a **FA** to accept a language.



It is easier

to check whether a given string is accepted by a **FA**
than

to see whether it matches a **regular expression**.

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It is easier

to find complements using a **FA**

than

by using a **regular expression**.

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Some Generalizations of Finite Automata

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This week:

- ▶ It is *not* required that, for state and letter, there is a *unique* transition.
- ▶ It can change state *without* a letter.
- ▶ It can read *more than one* letter at a time.



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Next week:

- ▶ It can read strings which match *regular expressions*, not just single letters.

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Later:

- ▶ Each transition can produce *output letters* as well as changing state. (*transducer*)
- ▶ Transitions can *read and write* letters from some kind of *memory*.
- ▶ For a given state and letter, the next state is chosen *probabilistically*.

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Nondeterministic Finite Automaton (NFA)

NFA are defined like a Finite Automaton (FA) except for transitions.

Transitions

- ▶ For some states and letters, there may be a transition.
- ▶ The labels may include the empty word ϵ .



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So for a given letter and state there may be:

- ▶ No transition
- ▶ More than one transition

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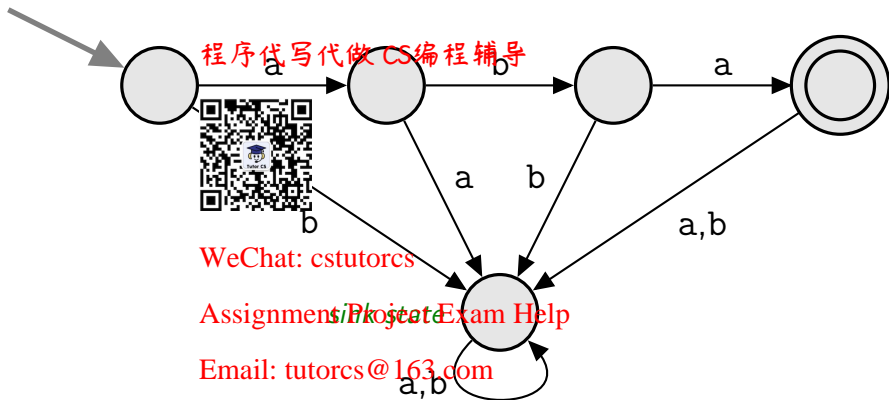
For a given string, the path it takes

- ▶ might not exist
- ▶ might not be unique

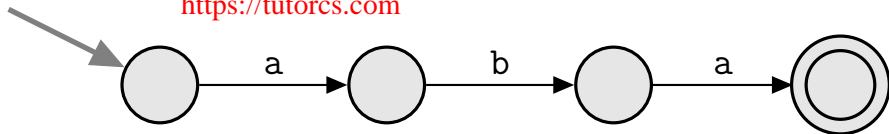
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aba

FA

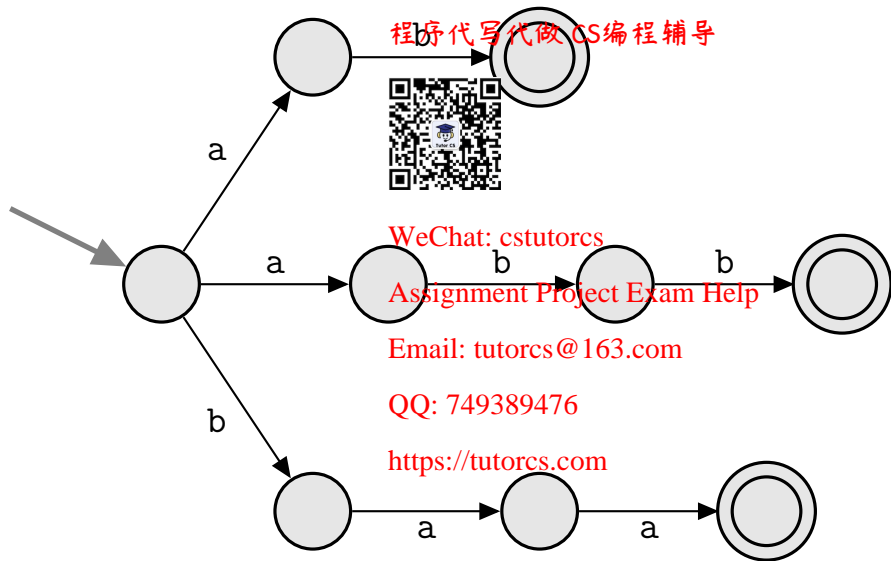


NFA

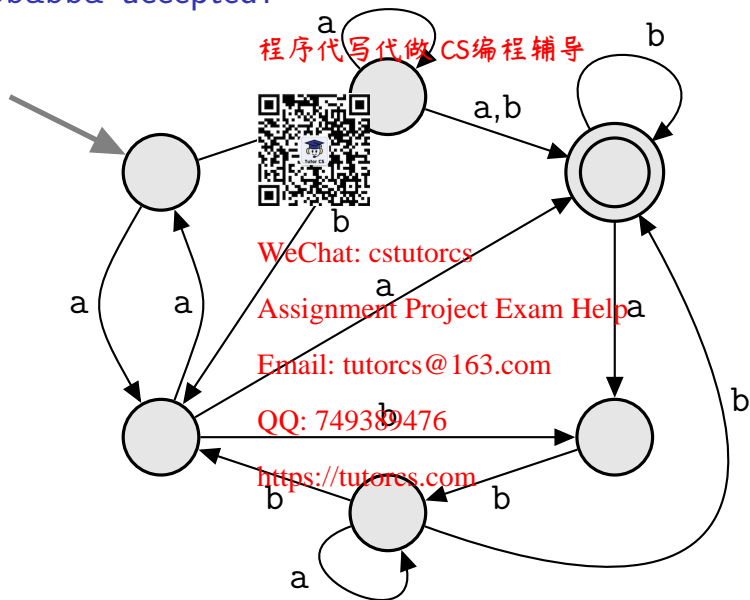


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$ab \cup abb \cup baa$



Is abbbabbbabba accepted?



Properties

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- ▶ If there is no transition for the next letter and state the machine crashes.
- ▶ Paths from the Start State to a Final State for a given input:
 - ▶ One
 - ▶ None
 - ▶ Several (Nondeterministic)
- ▶ **Accept** a string if there is **at least one** path from the Start State to a Final State.
- ▶ **Reject** a string if there are **no** paths from the Start State to a Final State.

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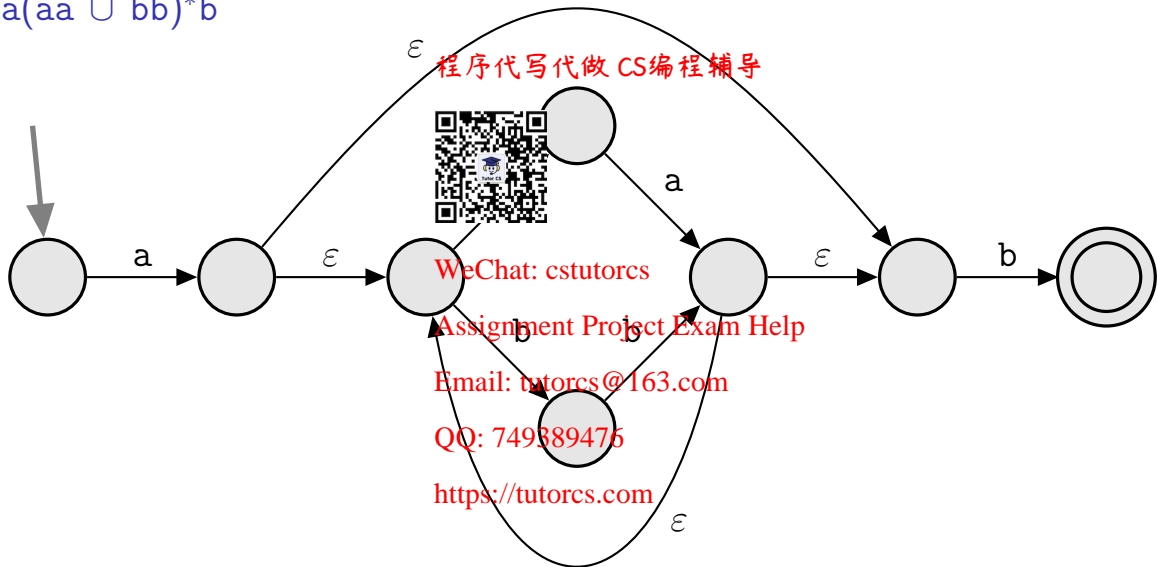
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$a(aa \cup bb)^*b$



Revision

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Finite Automata (FA)

- ▶ Definition. How to use them.
- ▶ How to construct a Finite Automaton to accept a language.



Complement Languages

- ▶ What they are. Designing FA to accept them.

Nondeterministic Finite Automata (NFA)

- ▶ Definition. How to use them.
- ▶ How to construct a Nondeterministic Finite Automaton to accept a language.

Reading: Sipser Ch 1.

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