



# FIT2093 INTRODUCTION TO CYBER SECURITY

Assignment Project Exam Help

**Week 2 Lecture**

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**Cryptography I:**

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**Symmetric Key Encryption**

**Part 1**

**Principles for CONFIDENTIALITY**



# Outline

Symmetric Cryptography

## Part 1: Basic Concepts

- CONFidentiality problem
- Cryptography: big picture
- Encryption: Classical Ciphers
- Encryption: Modern Cipher principles

## Part 2: Modern Encryption Algorithms

- Block ciphers
  - Design requirements
  - Case study I: Data Encryption Standard (DES)
  - Case study II: Advanced Encryption Standard (AES)
- Block Cipher Modes: How to use block ciphers for encryption
  - ECB, CBC, CTR

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# CONFidentiality Problem

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# The CONF Problem: Insecure Channel vs Secrecy

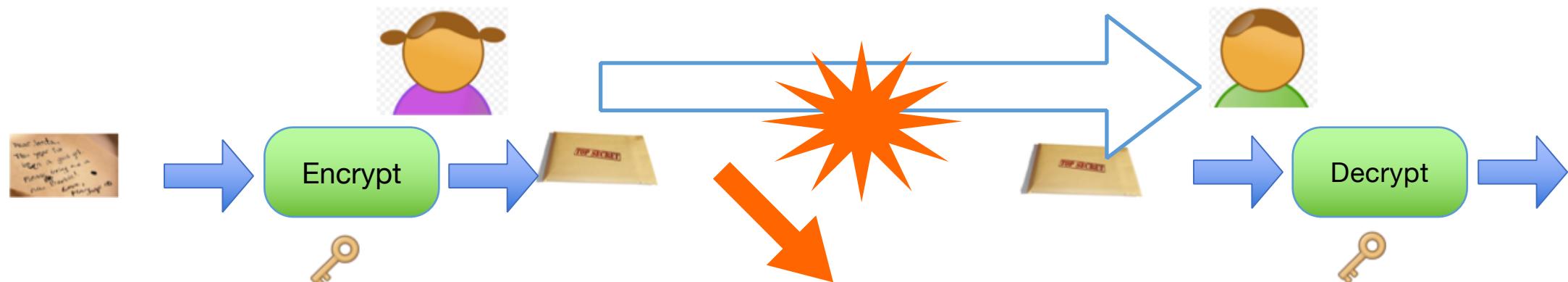
- Aim: vs **Insecure** channel / storage
- **Strategy**
  - *accept* fact: channel **insecure**  
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  - whatever sent, could be **intercepted** (eavesdropping)  
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- no control over channel

## CONFidentiality : How?

- Aim: reveal nothing: secrecy / confidentiality (CONF)
  - Strategy
    - accept fact: whatever sent, could be intercepted (eavesdropping)
    - prevent
      - even if intercepted, not reveal secret info
      - scramble info before send, s.t. only Rx can descramble (encrypt) WeChat: cstutorcs (decrypt)
      - use secret (key) s.t. only Rx can decrypt





# CONFidentiality: How?

Symmetric Crypto

- Goal: secret data remains CONFidential  
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- Means:
  - not all can access <https://tutorcs.com>
  - only some can access WeChat: cstutorcs
- Q: how to enforce?
  - access control: check who, & grant access
  - encryption:
    - lock, only some have key
    - scramble / mix up, only some can undo

- State **what can't** be solved/avoided, aim for **next best**
  - e.g. channel insecure, cannot avoid **interceptions**  
so next best: **don't** let intercepted things **reveal** info
- *change* means: “**Assignment Project Exam Help**” “**wrap it up**” →
  - (physically secure the channel)
  - (secure the sent info)
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- be fluid: the **means** could be varied , as long as same **goal** achieved eventually
  - x prevent **interception**, that's ok
  - so prevent **revelation** of info



# CONFidentiality: How?

Symmetric Crypto

- Goal: secret data remains CONFidential
- Means:
  - not all can access, only some can access
- How?
  - encryption: cannot access anymore
  - decryption: to access again, undo the encryption
    - only some can decrypt (*restricted reversal*)
    - how?
      - keep algorithms secret
      - use extra (secret) input (the key)



# CONFidentiality: via Obscurity?

Symmetric Crypto

- ... only **some** can decrypt ...

- How?

- keep algorithms **secret**

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# CONFidentiality: Kerckhoffs' Principle

Symmetric Crypto

- ... only **some** can decrypt ...
- How?
  - use extra (secret) **input** (called the **key**)  
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https://tutorcs.com](https://tutorcs.com)

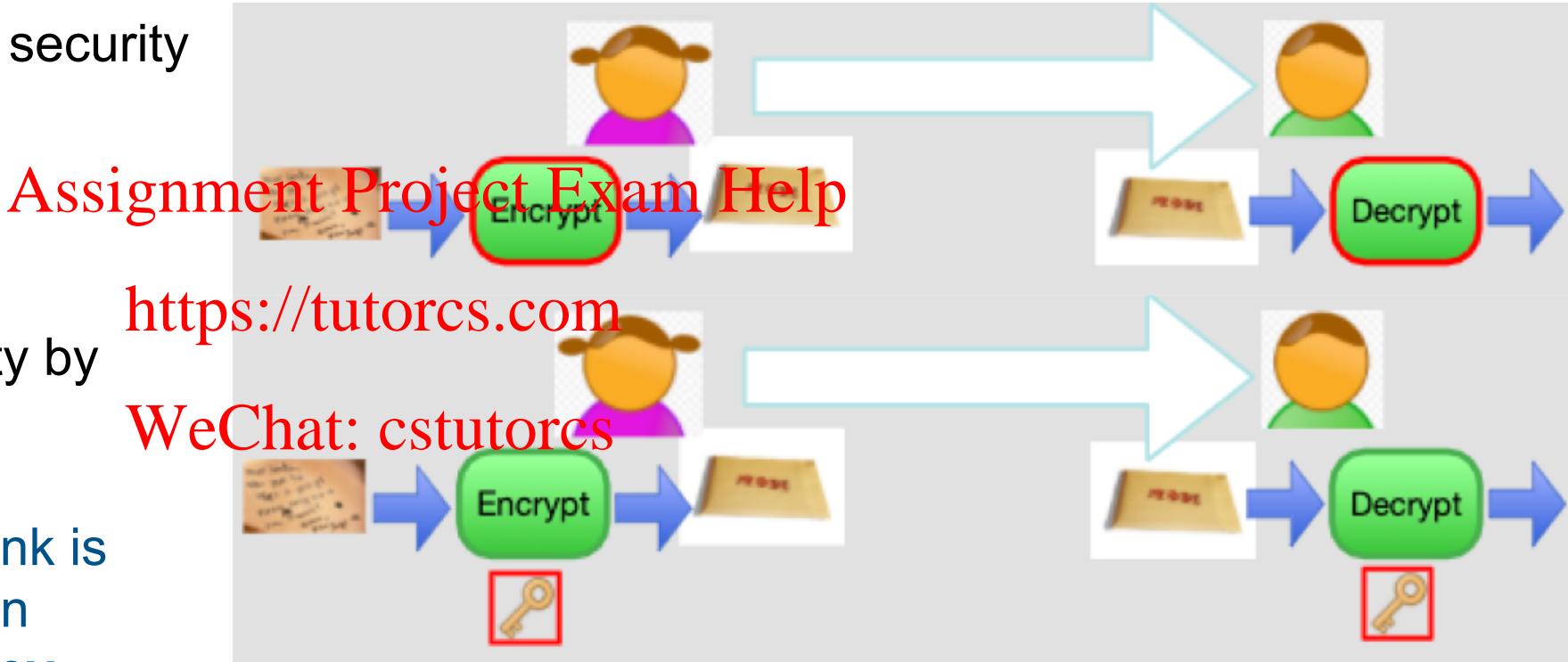




# CONFidentiality

## Symmetric Crypto

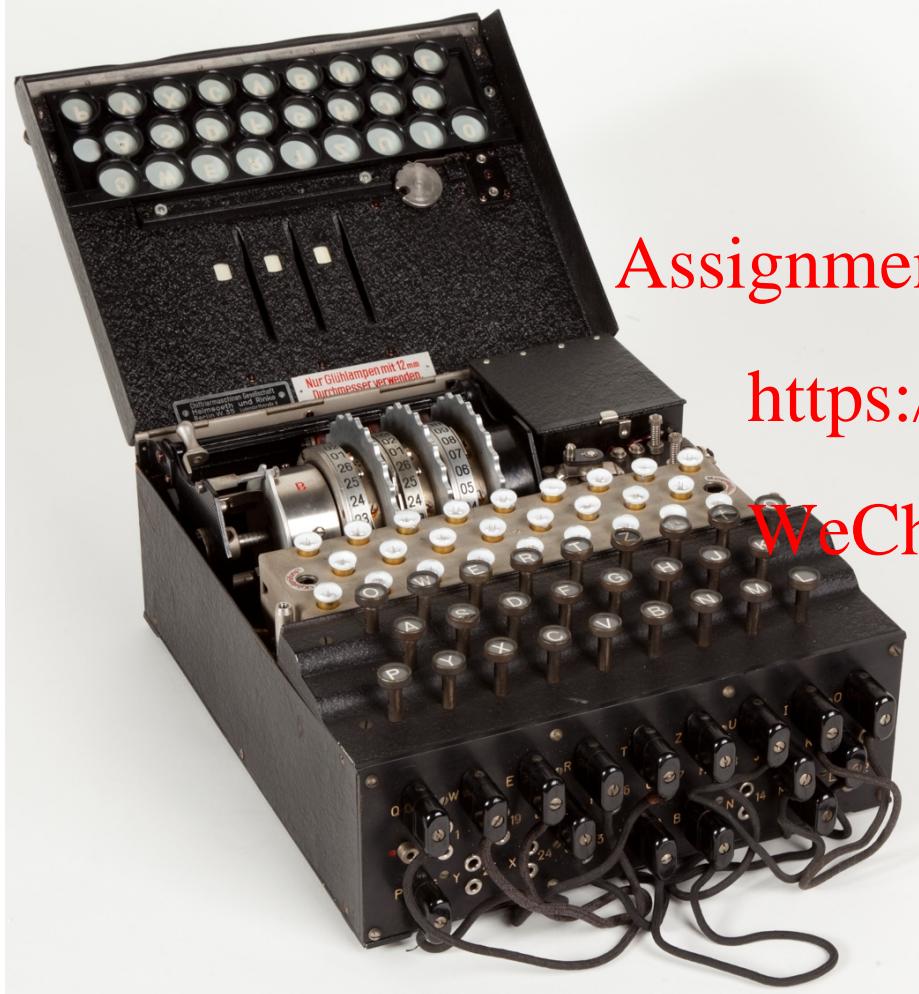
- keep algorithms secret: security by obscurity
- keep key secret: security by Kerckhoffs' principle
- Q: which one do you think is harder to do: Keeping an **algorithm** secret or a **key** secret? Why?



### Activity (5 mins)

- 1) Click the latest link in the Zoom chat
- 2) Add your question response to the Ed forum

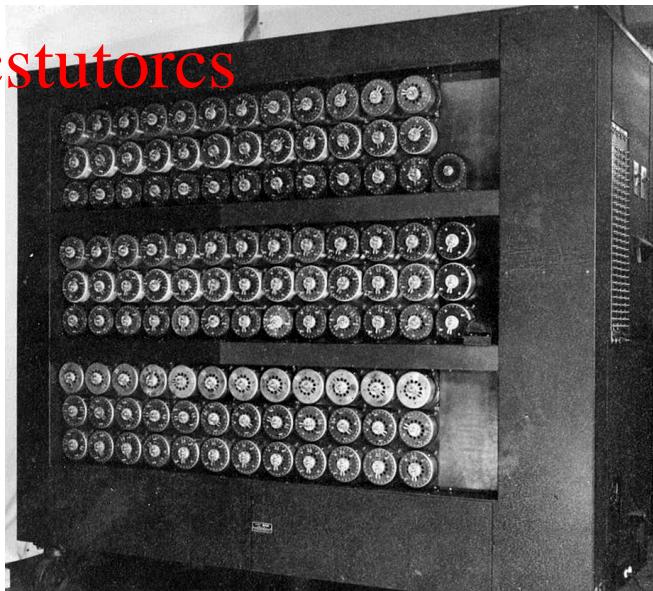
# A hint from history...



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# Cryptography: Big Picture

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# Cryptography: Big Picture

## Symmetric Crypto

- **CONFidentiality**: achieved via Encryption (weeks 2-4)
  - Two types of encryption:
    - Symmetric key (week 5)
    - Public Key (weeks 6-7) <https://tutorcs.com>
- **INTegrity** achieved via (week 5)
  - Message Authentication Code (MAC) – symmetric key
  - Digital Signatures – public key
- **AUTHentication** achieved via (week 5)
  - Digital Signatures – public key



# Cryptography: Big Picture

## Symmetric Crypto



### Cryptography - Terminology

- plaintext  $p \rightarrow$  Encryption  $\rightarrow$  ciphertext  $c$
- message  $m \rightarrow$  MAC  $\rightarrow$  tag  $\tau$
- message  $m \rightarrow$  DigitalSignature  $\rightarrow$  signature  $s$
- ...
- Cryptography:
  - techniques that transform the input (message) such that output allows to achieve CONF, INT, AUTH, ...
  - History
    - from Greek words kryptos (hidden) & graphein (writing)
    - initially: study of message **secrecy** (hidden writing) aka CONF, now covers many other security goals

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# Cryptography vs Cryptanalysis

Symmetric Crypto

## Cryptography - Terminology

- Cryptography: by cryptographer
    - how to design to achieve security
  - Cryptanalysis: by cryptanalyst
    - how to break / analyse security
    - offers security assurance to others about your design
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# Encryption: Classical Ciphers

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# Cryptography: Classical

## Symmetric Crypto

- Mostly about encryption
  - e.g. Caesar Cipher [during Julius Caesar's time]
  - Enigma [by Germany during World War II]
- Classical Ciphers: two types
  - Substitution
  - Transposition

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# Cryptography: Classical

# Symmetric Crypto



- **Substitution**  
Systematically **substitute** (group of) letters with other (group of) letters ...  
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  - *Example:* change each letter with another letter that is two positions down in the English alphabet  
sequence: “message” => “oguuucig”  
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  - **Transposition**  
**Rearrange** the **position** of the letters in the message according to the **key** (not depend on value of letter(s))
  - *Example:* Move each letter in the message by 1 position:  
“message” => “emessag”



# Classical Example: Caesar Cipher

Symmetric Crypto



- Caesar cipher:
  - a **substitution** cipher, named after Julius Caesar  
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- How it works:  
each letter is substituted with the letter *a fixed number of positions* after it in the alphabet table  
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- The **number of positions** is the **key** both for encryption and decryption:  
should not let others know how many number of positions



# Classical Example: Caesar Cipher

Symmetric Crypto



- $K=3 \dots$  Shifted by three characters



# Classical Example: Caesar Cipher

Symmetric Crypto



- Caesar Cipher can be viewed as modulo operation
- **Encryption:** Assignment Project Exam Help
  - Let  $x$  be the position of plaintext letter to be replaced,  $n$  be number of positions to be shifted to <https://tutorcs.com> (ciphertext) letter i.e the key is the value of  $n$  WeChat: cstutorcs
  - $E_n(x) = (x+n) \bmod 26$  & substitute that character in that position
- **Decryption:**
  - $D_n(x) = (x-n) \bmod 26$

# Classical Example: Caesar Cipher

Symmetric Crypto



- for a key  $K = 3$ ,
  - plaintext letter: ABCDEFG...PQRSTUVWXYZ
  - ciphertext letter: DEFGHI...STUVWXYZABC

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e.g.      **TREATY IMPOSSIBLE**      WeChat: cstutorcs  
is translated into  
**WUHDWB LPSRVVLEOH**

- Play with the online Caesar cipher here:

<https://cryptii.com/pipes/caesar-cipher>

# Caesar Cipher: Attack

Symmetric Crypto



- Q: How to **attack** the Caesar Cipher?
- A: by brute force exhaustive search for the key
  - Q: what is the key? [Assignment Project Exam Help](https://tutorcs.com) <https://tutorcs.com>
- Attack time complexity is very low
  - can be easily broken
  - Q: how many possible keys?
  - Q: how to check a guess for key?
  - Q: how long would it take?

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- Activity (5 mins)
- 1) Click the latest link in the Zoom chat
  - 2) Add your question response to the Ed forum

# Caesar Cipher: Attack example

## BRUTE FORCE ATTACK ON CAESAR CIPHER

LET'S SAY WE ARE USING CAESAR TO ENCRYPT THE NAME "ALICE",  
THERE WILL BE ONLY 26 POSSIBILITIES:

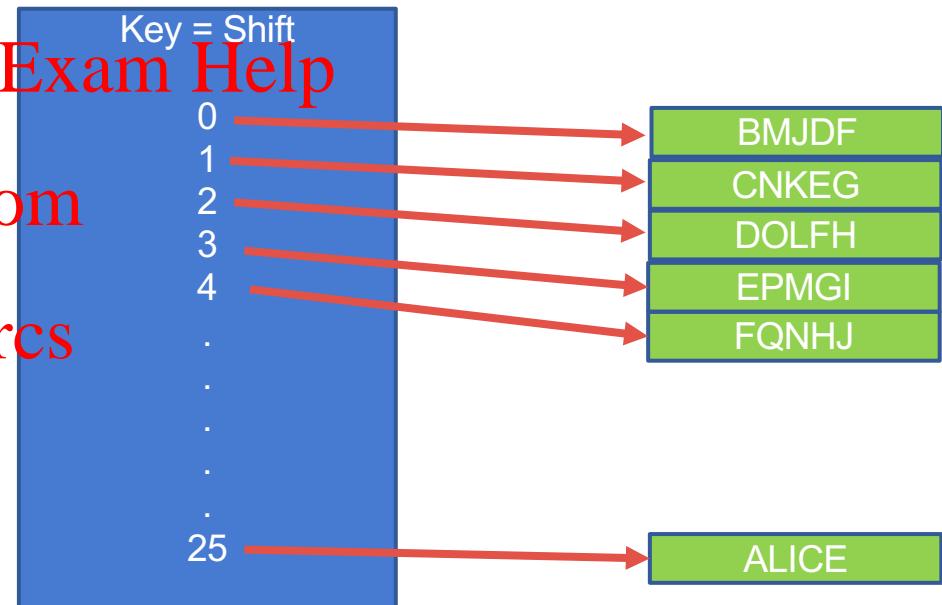
ONLY ONE OF THE 26 POSSIBLE DECRYPTIONS WILL TYPICALLY  
MAKE SENSE

E.G. BRUTE FORCE ATTACK ON CIPHERTEXT = "BMJDF"

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# Caesar Cipher: Attack

Symmetric Crypto



- Security of the Caesar Cipher
  - insecure against **brute force exhaustive key search**  
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- Attack complexity
  - how many guesses?
    - how many possible shifts = ~~WeChat 26 (too slow!!)~~
  - effort to check each guess
    - see if it's English

# Example II: Monoalphabetic Substitution Cipher

Symmetric Crypto

- Build a (mapping) table that **maps** a character with the replacement character

Q: How is this cipher different from Caesar cipher?  
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- Need this **table** (in fact column 2) to encode/decode messages
  - *assuming the alphabets in column 1 is in a known sequence, else column 1 also needed*
- Different people can use different tables

A	D
B	A
C	I
D	B
E	J
F	C
G	H
H	K
...	...
Z	F

# Example II: Monoalphabetic Substitution Cipher

Symmetric Crypto

- Build a (mapping) table that **maps** a character with the replacement character
- Q: What property(ies) does this table need to satisfy?  
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<https://tutorcs.com>  
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- Q: How many such mapping tables are possible for 26 upper-case English alphabets?
  - 26! Mapping tables. Why?

A	D
B	A
C	I
D	B
E	J
F	C
G	H
H	K
...	...
Z	F

# Monoalphabetic Substitution Cipher: Security

Symmetric Crypto

- Alphabet substitution (mapping) table
  - can be thought of as a key:  
[Assignment](#) [Project](#) [Exam](#) [Help](#)
  - Number of possible keys  $N = 26! \sim 4 \times 10^{26}$
  - Brute force key search ~~is feasible after millions of years~~

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Q: Assume each key guess takes  $1 \text{ ns} = 10^{-9} \text{ sec}$  to check.

How long would brute force key search take?

Activity (5 mins)

Add your question response to the Ed forum

A	D
B	A
C	I
D	B
E	J
F	C
G	H
H	K
...	...
Z	F

# Monoalphabetic Substitution Cipher: Security

## Symmetric Crypto

- But, is Monoalphabetic cipher secure against **other cryptanalysis attacks?**
  - No, an efficient **statistical frequency analysis** attack:
    - Observation: **Assignment Project Exam Help**
      - each plaintext letter always encrypts to **same ciphertext letter**
      - so: **<https://tutorcs.com>**
      - letter repeat in plaintext letter  
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→ repeat in ciphertext !
      - **cipher weakness:** ciphertext letter frequencies are equal to corresponding plaintext letter frequencies
    - **Fact:** letter frequency in English gives lots of info on letter
      - use fact with above weakness to break the cipher!

A	D
B	A
C	I
D	B
E	J
F	C
G	H
H	K
...	...
Z	F

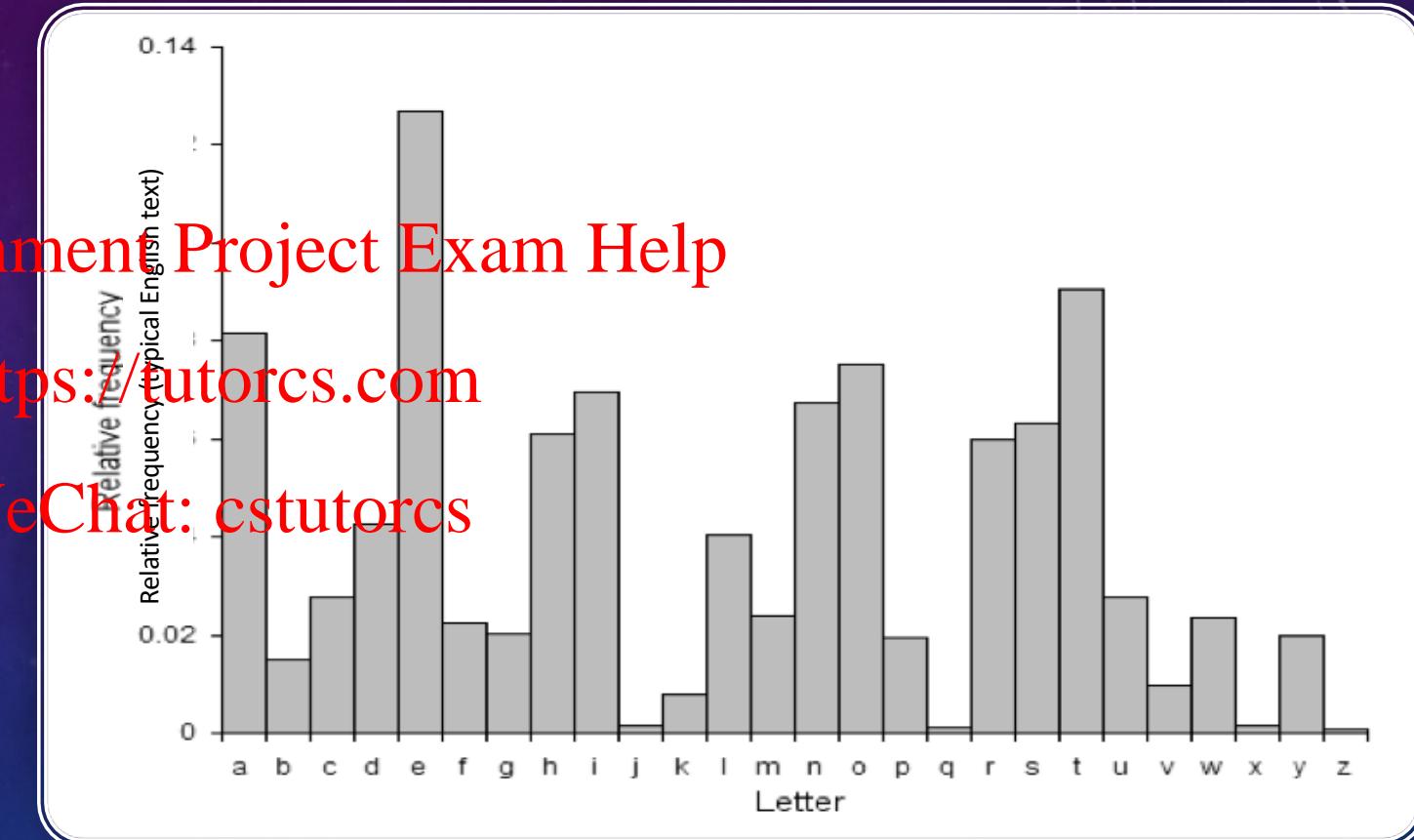
## CRACKING THE MONOALPHABETIC SUBSTITUTION CIPHER: FREQUENCY ANALYSIS ATTACK

- By using frequency analysis with following **assumptions**:
    - Messages are in English form
    - The message is long enough to see the repetitive patterns
- as we'll see, they don't have to be too long!*

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# FREQUENCY ANALYSIS ATTACK: EXAMPLE

Given the ciphertext:

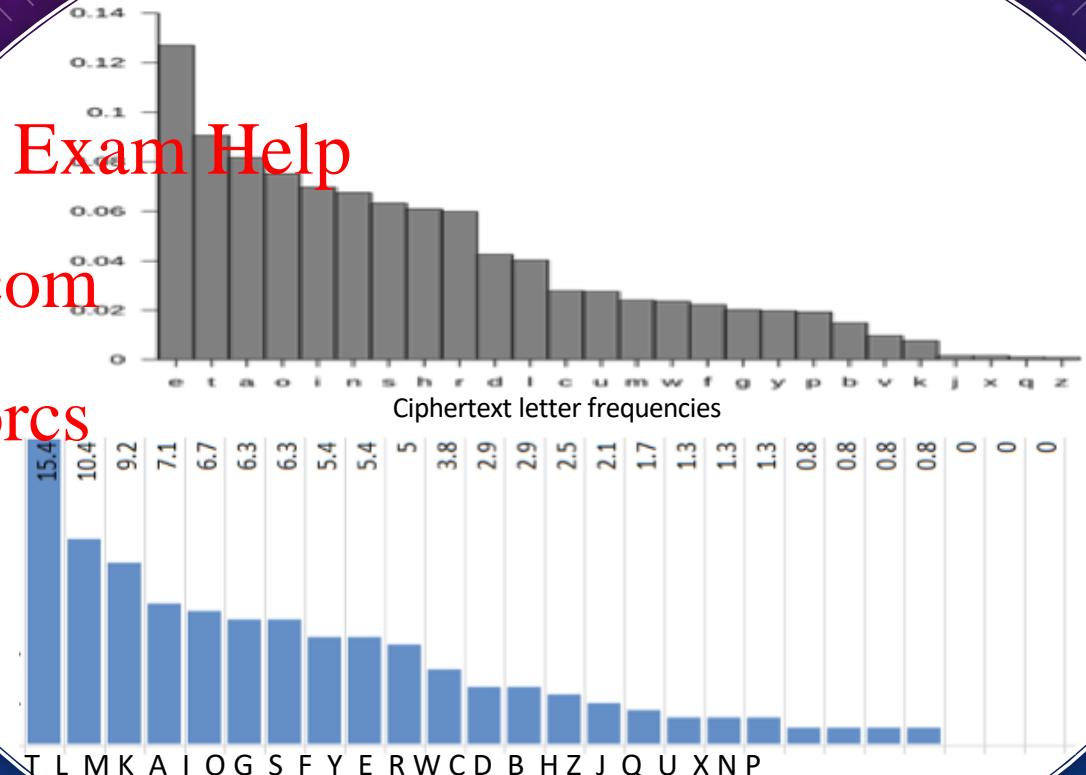
STUTFR LIASS LHTAQ GY LAEKOYOET AM  
CGKSRL TFR MIT CQFR LAOSL GXTK MIT  
CAMTKL LWKYAET JWOTMSB ZWM LWKTSB  
TXTF OY MIT DGKKGC OL ZAKKTF GY  
HKGDOLTL FGMIOFU LIASS YGKTILMASS DB  
KTMWKF MG ZTEGDT MIT RTC MIAM  
JWTFEITL MIT SAFR MG LHAKT MIT  
LAFRL MIT LTAL MIT LQOTL O GYYTK  
MITT MIOL LOSTFM LAEKOYOET

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English Letter Frequencies



# FREQUENCY ANALYSIS ATTACK: EXAMPLE

1. See the frequency table, replace T with E, because normally the letters with highest frequencies will match

```
SEUEFR LIASS LHEAQ GY LAEKYOEE AM  
CGKSRL EFR MIE COFR LAOSL GXEK MIE  
CAMEKL LWKYAEE JWOEMS ZWM LWKESB  
EXEF OY MIE DGKKGC OL ZAKKEF GY  
HKGDOLEL FGMIOFU LIASS YGKEFLMASS DB  
KEMWKF MG ZEEGDE MIE REC MIAM  
JWEFEIEL MIE SAFR MG LHAK E MIE  
LAFRL MIE LEAL MIE LQOEL O GYYEK  
MIE MIOL LOS E FM LAEKYOEE
```

2. See the replaced ciphertext, any short & repeated words? One short word that ends with E is THE. Update the table.

```
SEUEFR LHASS LHEAQ GY LAEKYOEE AT  
CGKSRL EFR THE COFR LAOSL GXEK THE  
CATEKL LWKYAEE JWOETSB ZWT LWKESB  
EXEF OY THE DGKKGC OL ZAKKEF GY  
HKGDOLEL FGTHOFU LHASS YGKELTASS DB  
KETWKF TG ZEEGDE THE REC THAT  
JWEFEHEL THE SAFR TG LHAK E THE  
LAFRL THE LEAL THE LQOEL O GYYEK  
THEE THOL LOSEFT LAEKYOEE
```

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Ciphertext	Frequency	Plaintext
T	15.4	E
L	10.4	T
M	9.2	A
K	7.1	O
A	6.7	I
P	6.3	N
O	6.3	S
G	5.4	H
S	5.4	R
F	5	D
Y	3.8	L
E	2.9	C
R	2.9	U
W	2.5	M
C	2.1	W
D	1.7	F
B	1.3	G
H	1.3	Y
Z	1.3	P
J	0.8	B
Q	0.8	V
U	0.8	K
X	0.8	J
N	0	X
P	0	Q
V	0	Z

# FREQUENCY ANALYSIS ATTACK: EXAMPLE

3. There are still short words e.g. "I", "but", can be guessed from current ciphertext.

Replace Z with B, W with U, O with I.

```
SEUEFR LHASS LHEAQ GY LAEKIYIEE AT  
CGKSRL EFR THE CIFR LAISL GXEK THE  
CATEKL LUKYAAE JUIETSB BUT LUKESSB  
EXEF IY THE DGKKGC IL BAKKEF GY  
HKGDILEL FGTHIFU LHASS YGKELTASS DB  
KETUKF TG BEEGDE THE REC THAT  
JUEFEHEL THE SAFR TG LHAKE THE  
LAFRL THE LEAL THE LQIEL I GYYEK  
THEE THIL LISEFT LAEKIYIEE
```

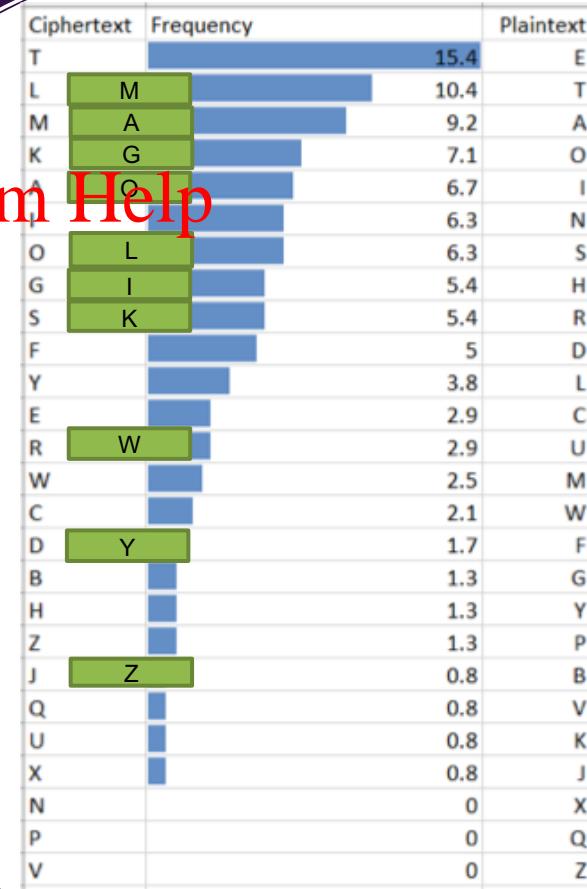
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4. With the replaced ciphertext, we can discover even more short words, such as "that", "to", "if" and "this". Notice that the plaintext of A is A too, which is not shown in the frequency analysis because the sample text is not long enough.

```
SEUEFR SHASS SHEAQ OF SAERIFIIEE AT  
CORSRS EFR THE CIFR SAISS CXER THE  
CATERS SURFAEE JUIETSB BUT SURESSB  
EXEF IF THE DORROC IS BARREF OF  
HRODISES FOTHIFU SHASS FORESTASS DB  
RETURF TO BEECODE THE REC THAT  
JUEFEHES THE SAFR TO SHARE THE  
SAFRS THE SEAS THE SQIES I OFFER  
THEE THIS SISEFT SAERIFIIEE
```



# FREQUENCY ANALYSIS ATTACK: EXAMPLE

5. Looking back to the frequency table we have, replace E with C.

SEUEFR	SHASS	SHEAQ	OF	SACRIFICE	AT	
CORSRS	EFR	THE	CIFR	SAISS	OXER	THE
CATERS	SURFACE	JUIETSB	BUT	SURESB		
EXEF	IF	THE	DORROC	IS	BARREF	OF
HRODISES	FOTHIFU	SHASS	FORESTASS	DB		
RETURF	TO	BECODE	THE	REC	THAT	
JUEFCHE	THE	SAFR	TO	SHARE	THE	
SAFRS	THE	SEAS	THE	SQIES	I	OFFER
THEE	THIS	SISEFT	SACRIFICE			

6. Continue with the table, skipping the letters that are already being replaced, replace C with W

SEUEFR	SHASS	SHEAQ	OF	SACRIFICE	AT	
WORSRS	EFR	THE	WIFR	SAISS	OXER	THE
WATERS	SURFACE	JUIETSB	BUT	SURESB		
EXEF	IF	THE	DORROW	IS	BARREF	OF
HRODISES	FOTHIFU	SHASS	FORESTASS	DB		
RETURF	TO	BECODE	THE	REW	THAT	
JUEFCHE	THE	SAFR	TO	SHARE	THE	
SAFRS	THE	SEAS	THE	SQIES	I	OFFER
THEE	THIS	SISEFT	SACRIFICE			

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Ciphertext	Frequency	Plaintext
T	15.4	E
L	10.4	T
M	9.2	A
K	7.1	O
A	6.7	I
P	6.3	N
O	6.3	S
G	5.4	H
S	5.4	R
F	5	D
Y	3.8	L
E	2.9	C
R	2.9	U
W	2.5	M
C	2.1	W
D	1.7	F
B	1.3	G
H	1.3	Y
Z	1.3	P
J	0.8	B
Q	0.8	V
U	0.8	K
X	0.8	J
N	0	X
P	0	Q
V	0	Z

# FREQUENCY ANALYSIS ATTACK: EXAMPLE

7. Ciphertext letter B has two possible plaintext letters, which is G and Y. Looking at the current text, the words containing B makes more sense if replacing with Y, thus replace B with Y.

SEUEFR	SHASS	SHEAQ	OF	SACRIFICE	AT	
WORSRS	EFR	THE	WIFR	SAISS	OXER	THE
WATERS	SURFACE	JUIETSY	BUT	SURESY		
EXEF	IF	THE	DORROW	IS	BARREF	OF
HRODISES	FOTHIFU	SHASS	FORESTASS	DY		
RETURF	TO	BECODE	THE	REW	THAT	
JUEFCHE	THE	SAFR	TO	SHARE	THE	
SAFRS	THE	SEAS	THE	SKIES	I	OFFER
THEE	THIS	SISEFT	SACRIFICE			

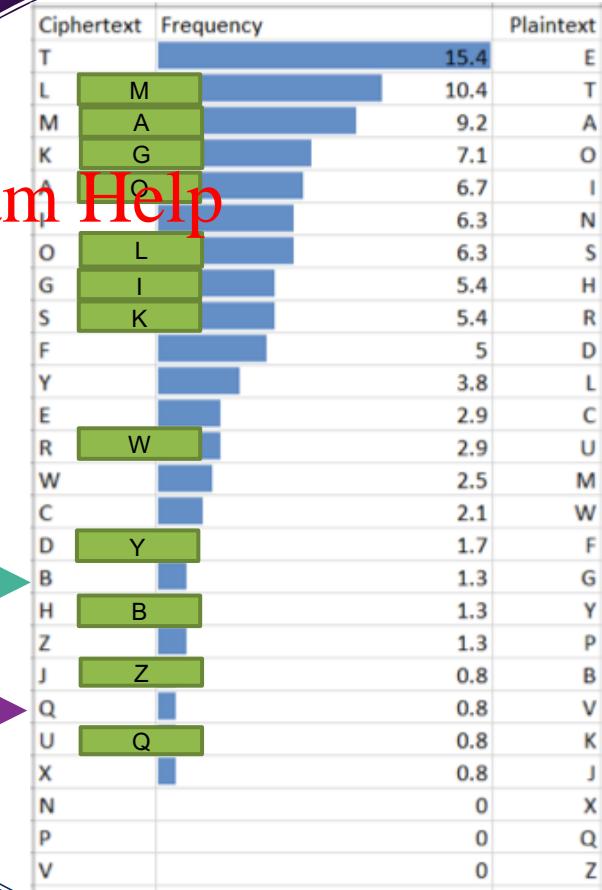
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8. Using the same method as in Step 7, replace Q with K instead of V and J.

SEUEFR	SHASS	SHEAK	OF	SACRIFICE	AT	
WORSRS	EFR	THE	WIFR	SAISS	OXER	THE
WATERS	SURFACE	JUIETSY	BUT	SURESY		
EXEF	IF	THE	DORROW	IS	BARREF	OF
HRODISES	FOTHIFU	SHASS	FORESTASS	DY		
RETURF	TO	BECODE	THE	REW	THAT	
JUEFCHE	THE	SAFR	TO	SHARE	THE	
SAFRS	THE	SEAS	THE	SKIES	I	OFFER
THEE	THIS	SISEFT	SACRIFICE			



# FREQUENCY ANALYSIS ATTACK: EXAMPLE

9. We can tell "shall", "forestall", "over", "even", "morrow", replacing S with L, X with V, F with N, D with M respectively.

LEUENR SHALL SHEAK OF SACRIFICE AT  
WORLRS ENR THE WINR SAILS OVER THE  
WATERS SURFACE JUIETLY BUT SURELY  
EVEN IF THE MORROW IS BARREN OF  
HROMISES NOTHINU SHALL FORESTALL MY  
RETURN TO BECOME THE REW THAT  
JUENCHES THE LANR TO SHARE THE  
SANRS THE SEAS THE SKIES I OFFER  
THEE THIS SILENT SACRIFICE

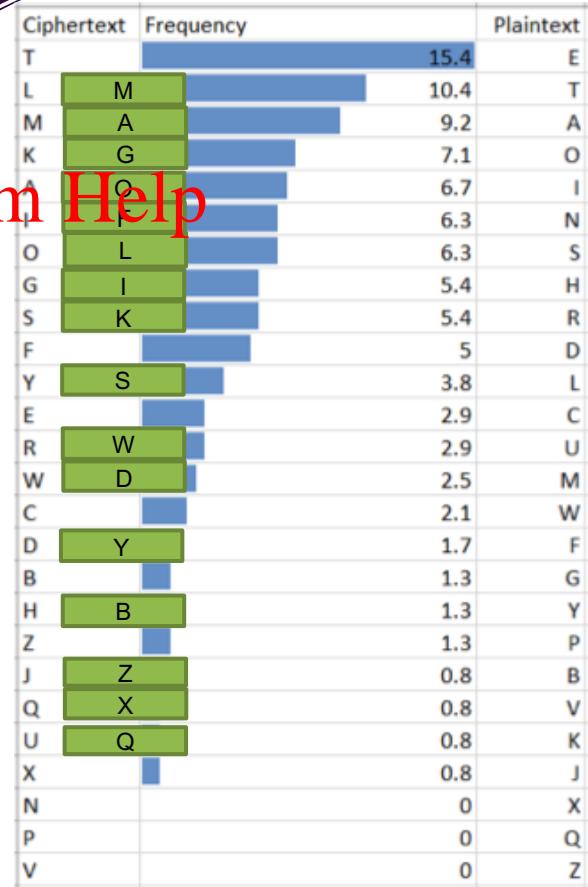
8. Using same method as in Step 9, replace R with D, H with P, U with G...and the rest of the letters accordingly.

LEGEND SHALL SPEAK OF SACRIFICE AT  
WORLDS END THE WIND SAILS OVER THE  
WATERS SURFACE QUIETLY BUT SURELY  
EVEN IF THE MORROW IS BARREN OF  
PROMISES NOTHING SHALL FORESTALL MY  
RETURN TO BECOME THE DEW THAT  
QUENCHES THE LAND TO SPARE THE  
SANDS THE SEAS THE SKIES I OFFER  
THEE THIS SILENT SACRIFICE

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## FAILED ATTEMPT TO FIX THE MONOALPHABETIC STATISTICAL WEAKNESS

How about a more complex **two-step cipher**:

1. Encrypt message M with monoalphabetic key K1 to get ciphertext C1  
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2. Encrypt C1 again with monoalphabetic cipher with a different key K2 to get ciphertext C2  
<https://tutorcs.com>



Q: Is the two-step more secure than one-step monoalphabetic cipher?

A: No. Why?

**Activity (5 mins)**

- 1) Click the latest link in the Zoom chat
- 2) Add your question response to the Ed forum

# Example III: Transposition Cipher: Rail Fence Cipher

Symmetric Crypto

- an example transposition cipher
- letters placed in multiple number of lines,  
from line 1 position 1 to line 2 position 2, then line 3 position 3, line 2 position 4,  
line 1 position 5, etc      **Assignment Project Exam Help**
- e.g. the plaintext “**WE ARE DISCOVERED FLEE AT ONCE**”  
**W . . . E . . . C . . . R . . . L . . . T . . . E** <https://tutorcs.com>  
. E . R . D . S . O . E . E . F . E . A . O . C .  
. . A . . . I . . . V . . . D . . . E . . . N . . .  
WeChat: cstutorcs
- ciphertext: **wecrlte erdsoeefeaoc aivden**
- Q: What is the key for this example of rail fence cipher?
- Rail fence of depth 3

# Example III: Transposition Cipher: General

Symmetric Crypto

- Decide on a block size L (say  $L = 10$  letters)
- Fix a permutation of  $(0, 1, 2, 3, \dots, 9)$  i.e. the key K:
  - e.g.  $K = (5, 3, 1, 4, 6, 8, 2, 0, 9, 7)$
  - Transpose every block of L successive message letters according to K,  
e.g.:  $0123456789 \quad 0123456789$   
**WeChat: cstutorcs**
  - Message = **HELLO THERE** HOWARETHEY
  - Cipher = **TLEOHRLHEE EAORTEEWHY**
- Secure?
  - No – Statistical patterns (letter frequencies) remain in ciphertext!

# Encryption: Modern Cipher principles

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# Modern Ciphers = Product Ciphers

Symmetric Crypto

- Substitution & Transposition
  - each contributes own strength to encryption
- Q: does combining a monoalphabetic substitution & transposition cipher give a
  - Monoalphabetic substitution cipher?
  - A transposition cipher?
- No! product is more complex than either one individually!
  - Number of possible product keys is (likely to be) the product of number of keys of individual methods

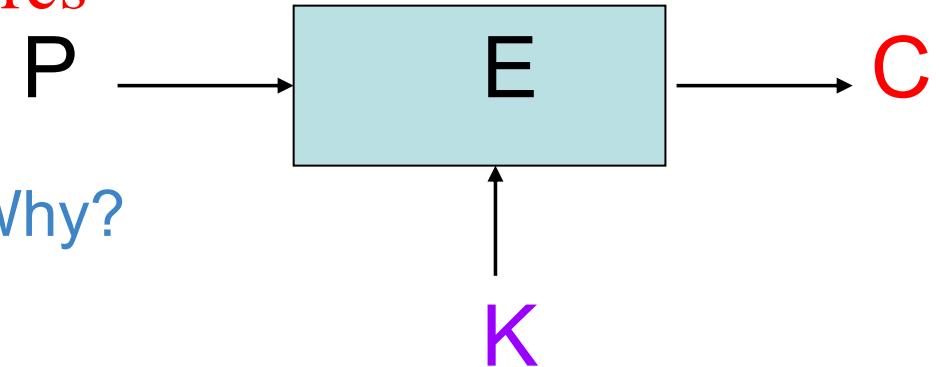
# Cipher Properties (I)

Symmetric Crypto

- **Confusion**

- make the **relationship** between ciphertext C & encryption key K as **complex as possible**  
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  - otherwise observing C statistics would leak info on K
- achieved by **complex substitution**
- Hard to get K by observing C  
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Q: Does Caesar cipher have confusion? Why?



# Cipher Properties (II)

Symmetric Crypto

- **Diffusion**

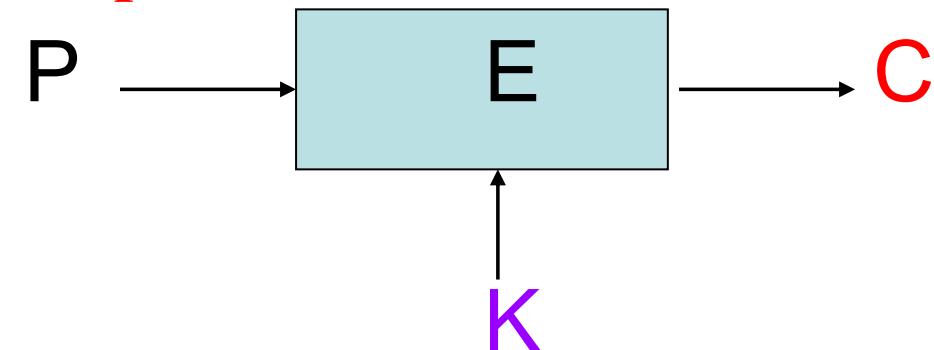
- should **spread** the information from P so that (eventually) each P digit affects many C digits
- achieved by complex **transposition**
- patterns in P can no longer be observed in C

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- Q: If some cipher encrypts  $P = "HELPME"$  to  $C = "GQWCKW"$
- and encrypts  $P = "HE\textcolor{red}{M}PME"$  to  $C = "GQADKW"$
- Does this cipher achieve Diffusion? Why/why not?



Activity (5 mins)

Add your question response to the Ed forum

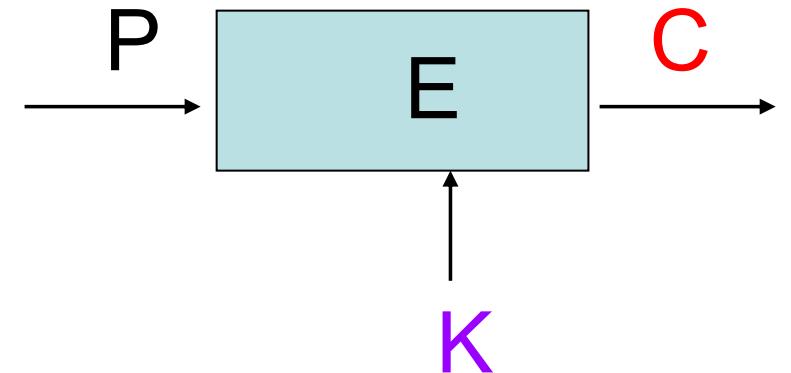
# Cipher Properties (III)

## Symmetric Crypto

- **Avalanche effect (diffusion for changes in either P or K)**
  - Small change in either **plaintext P** or **key K** produces a **significant** change in the **ciphertext C**
  - E.g. change in one bit of P or one bit of K should produce a change in **many bits** of C

- E.g.
- $P=11000000, K = 01101101 \rightarrow C = 10101011$
- $P=11000000, K = 01111101 \rightarrow C = 11011101$

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# Unconditional vs Computational Security

Symmetric Crypto

- Two kinds of encryption security requirements
- Unconditional security

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- even if attacker has infinite computational power,  
<https://tutorcs.com>
- cannot get information on plaintext from ciphertext

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- Computational security
  - if attacker has limited computational power,
    - cannot get information on plaintext from ciphertext
    - time needed for attack > useful age of info
    - cost of breaking > value of info



# The One-Time Pad

Symmetric Crypto

- Q: Is unconditionally secure encryption possible?
- A: Yes - One-Time Pad Encryption
  - start with the Caesar substitution cipher [Assignment Project Exam Help](#)
  - but use an independent random alphabet shift for each plaintext letter: <https://tutorcs.com>

e.g.       $K = (2, 9, 13, 20, 4)$  WeChat:cstutorcs

M = H E L L O

C = J N Y F P

- Claim: It is not possible to break this cipher by brute force exhaustive search. Q: Why?



## EXAMPLE OF DECRYPTING ONE-TIME PAD BY USING RANDOM KEY

Given a ciphertext “EQNVZ”. Assume we already obtained the random key, which is also the same length “XMCKL”, how do we decrypt the message?

E	Q	N	V	Z
4	16	13	21	25
X	M	C	WeChat: cstutorcs	
23	12	2	10	11
<hr/>				
7	4	11	11	14
H	E	L	L	O

1. Convert the letters into numbers, where A = 0, B = 1...Z  
 $- 25$
2. Subtract the value of random key from the ciphertext
3. If the result is a negative number, calculate how much it needs to reach 26. In this case,  $-19 - 7 = -26$ . Thus 7.
4. Convert the number back into alphabets, which is the message in plaintext

# ONE-TIME PAD USING RANDOM KEY

IMPOSSIBLE TO APPLY BRUTE FORCE ATTACK!

Why is brute force attack impossible on a one-time pad?

Reason is NOT the complexity of brute force!

e.g. a short plaintext "Alice", we will have  $26 \times 26 \times 26 \times 26 \times 26 = 11,881,376$  possibilities, which is easy to search through in a fraction of a second on any computer today

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However if we are using random key for each of the alphabet, this is like rolling a 26-sided die for each encrypted letter



# REASON FOR IMPOSSIBILITY TO BRUTE FORCE THE ONE-TIME PAD: ALL POSSIBLE DECRYPTIONS ARE EQUALLY LIKELY

It is possible to brute force the number of possibilities in previous slide.

However, since each possible key is **equally likely**, it is impossible to know which decryption is the correct one, i.e.

All possible English words with the same length as the ciphertexts are possible decryptions!

E.g. Ciphertext = "DAPRC"  
and 3 different possible keys:

Key 1: WWEGO

Key 2: QACPE

Key 3: DPHPY

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D	A	P	R	C
15	17			2

D	P	H	P	Y
3	15	7	15	25

0	11	8	2	4
A	L	I	C	E

# One-Time Pad: Why not popular?

Symmetric Crypto

- **Big Problem:** Key is as long as the message...
  - leads to impractical key exchange problem for most (large) messages

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- However, still used for very high security applications
  - e.g. (famous historical example): White-House to Kremlin nuclear emergency “hotline” (red telephone). ~~WeChat: estutoros~~ keying tapes physically delivered via embassy



# Security in practice: Computational security

## Symmetric Crypto

- via Substitution-Transposition Product Cipher
- Substitution: Assignment Project Exam Help
  - need to exchange & remember the substitution table
  - table can be big, if alphabet size is large
- Transposition/Permutation: WeChat: cstutorcs
  - plaintext is rearranged i.e. permutation
- Design principles
  - Need to avoid large substitution tables, but still need a method to substitute characters (or bits)
  - Need efficient permutation/transposition method

