

# 程序代写代做 CS编程辅导



CANDIDATE: please  
attach Student  
Support Unit sticker,  
if relevant

UNIVERSITY OF SUSSEX

10 YEAR EXAMINATION

10 YEAR EXAMINATION

LIMITS OF COMPUTATION

G5029

You can start this exam at a time of your choosing within a 24 hour window. Once started you will have a set exam duration in which to complete it (note: the assessment will close at end of the 24 hour window; start with sufficient time to complete).

If you have extra time due to Reasonable Adjustments this is additional to the exam duration below and has been added to your assessment on Canvas.

Email: [tutors@163.com](mailto:tutors@163.com)

Date: 18 May 2020  
24 Hour Window starts at: 09:30

Exam Duration: 3 hours (including time for scanning, collating, uploading)

QQ: 749389476

Candidates should answer TWO questions out of THREE.

If all three questions are attempted only the first two answers will be marked.

Each question is worth 50 marks.

<https://tutorcs.com>

Write or type your answers on A4 paper, scan and save as a single PDF file and upload to Canvas.

Please make sure that your submission includes the following:

Your candidate number (Do not put your name on your paper)

The title of the module and the module code.

Read Academic Integrity Statement

You MAY access online materials, notes etc. during this examination. You must complete this assessment on your own and in your own words. DO NOT discuss this assessment with others before the end of its 24 hour window. By submitting this assessment you confirm that your assessment includes no instances of academic misconduct, for example plagiarism or collusion. Any instance of academic misconduct will be thoroughly investigated in accordance with our academic misconduct regulations.

1. This question is about various notions of effective computability.

- (a) Why do we need to extend (change) the semantic function for the WHILE-language to interpret programs of the extended WHILE-language? [4 marks]
- (b) What does the extended WHILE-language provide? [4 marks]
- (c) Explain direct addressing used by the RAM computation model. Why is this needed at all? [5 marks]
- (d) What can you say about the relationship between RAM-decidable and WHILE-decidable problems about natural numbers? [4 marks]
- (e) Let the following WHILE-program `myprog` be as follows:

Assignment Project Exam Help

Email: [tutorcs@163.com](mailto:tutorcs@163.com)

QQ: 749389476

- i. Assuming that we start counting variables from 0, give the program-as-data representation of `myprog`. [12 marks]

- ii. Is this WHILE-program written in *code* WHILE or *extended* WHILE? [2 marks]

- iii. What is  $\llbracket \text{myprog} \rrbracket^{\text{WHILE}}(\ulcorner n \urcorner)$  for an arbitrary  $n \in \mathbb{N}$ ? Recall that  $\ulcorner n \urcorner$  the encoding of a natural number  $n$  as data. [3 marks]

- iv. What is  $\llbracket \text{myprog} \rrbracket^{\text{WHILE}}(d)$  for an arbitrary  $d \in \mathbb{D}$ ? [2 marks]

- (f) Assume  $c_1$  is a compiler from  $S$  to  $T$  written in  $L$ . Assume further  $c_2$  is a compiler from  $L$  to  $M$  written in  $C$ . What do we get if we compile  $c_1$  using  $c_2$ ? Be as precise as possible. [4 marks]
- (g) Can we add a new instruction to the instruction set of a standard Turing Machine, such that the resulting new Turing Machines, let's call them Turing Machines Plus, can decide more problems than the standard type of Turing Machines? Explain your answer. [5 marks]
- (h) Can we remove an instruction from the definition of standard Turing Machines, such that the resulting new Turing Machines, let's call them Turing Machines Minus, can decide fewer problems than the standard type of Turing Machines? Explain your answer. [5 marks]

2. This question is about decidability and semi-decidability, and self-referencing programs.



- (a) Let  $A$  (about binary trees). Assume there exists a WHILE-program  $P$  such that the following holds:

$\llbracket P \rrbracket d$  if, and only if,  $d \in A$ .

What can you deduce from the above for problem  $A$ ? [4 marks]

- (b) Which of the following problems are WHILE-decidable? (No explanation needed.)

- Halting problem
- Complement of the Halting problem
- Travelling Salesman problem
- Postman problem
- Tiling problem
- The problem whether a natural number is a prime number
- The problem whether a WHILE-program (as data) has the same behaviour as the WHILE-program `succ` (as given in lectures).

[7 marks]

- (c) Which of the following statements about closure properties of problems (considered as subsets of  $\mathbb{D}$ ) are always true (i.e. for any  $A, B, A_n$ , resp.)? (No explanation needed.)

- If  $A$  and  $B$  are both semi-decidable, their intersection,  $A \cap B$ , is also semi-decidable.
- If  $A$  and  $B$  are both decidable, their union,  $A \cup B$ , is also decidable.
- If  $A$  is semi-decidable, the complement of  $A$  is also semi-decidable.
- If  $A$  is decidable, the problem  $\{ \langle a.a \rangle \in \mathbb{D} \mid a \in A \}$  is also decidable.
- If  $A$  is semi-decidable, the problem  $\{ \ulcorner l \urcorner \in \mathbb{D} \mid l \text{ is a list that contains at least one element from } A \}$  is also semi-decidable. Recall that  $\ulcorner l \urcorner$  denotes the encoding of a list as data.
- If  $A_n$  is decidable for every  $n \in \mathbb{N}$ , the problem  $\{ d \in \mathbb{D} \mid d \in A_n \text{ for some } n \in \mathbb{N} \}$  is also decidable.

[6 marks]

- (d) Give a problem (set) that is semi-decidable but *not* decidable. [3 marks]

- (e) What proof technique (besides proof-by-contradiction) is used in the proof that the Halting Problem is undecidable? No explanation is required. [2 marks]

- (f) What proof technique (besides proof-by-contradiction) is used in the proof of Rice's Theorem? Explain what this technique is applied to. You don't have to explain the technique itself. [4 marks]

- (g) Explain for the following sets  $A \subseteq \text{WHILE-data}$  whether they are WHILE-decidable. If not, explain your answer. In cases where  $A$  is decidable, your answer should consist of a description of the decision procedure. Recall that  $\ulcorner p \urcorner$  denotes the encoding of a WHILE-program as data.



- i.  $A = \{ \ulcorner p \urcorner \mid \text{WHILE-program } p \text{ returns nil if its input encodes a WHILE-program that contains at least two assignment statements for the same variable} \}$  [4 marks]
- ii.  $A = \{ \ulcorner p \urcorner \mid \ulcorner p \urcorner \text{ contains at least two assignment statements for the same variable} \}$  [4 marks]
- iii.  $A = \{ \ulcorner p \urcorner \mid \text{WHILE-program } p \text{ returns nil for input nil} \}$  [4 marks]

- (h) Consider a WHILE-program  $p$  with the following property:

$$\llbracket p \rrbracket^{\text{WHILE}}(d) = \ulcorner p \urcorner \text{ for all } d \in \mathbb{D}$$

Recall that  $\ulcorner p \urcorner$  denotes the encoding of a WHILE-program  $p$  as data.

- i. What sort of program is  $p$  referring to the specific property above? [2 marks]
- ii. Explain carefully why programs with the above property are actually semantically well-defined, referencing results from the lectures. [6 marks]
- iii. Explain briefly how this is related to reflection and meta-programming. [4 marks]

<https://tutorcs.com>

3. This question is about complexity.

(a) Let program `prog` be defined as follows:

`prog`

`while`

`do`

`Y`

`write Y`



WeChat: cstutorcs

i. Is the WHILE-program `prog` above in  $\text{WHILE}^{\text{time}(8n+5)}$ ? Explain your answer carefully. [8 marks]

ii. Assume you have two WHILE-programs  $p \in \text{WHILE}^{\text{time}(n^2+18)}$  and  $q \in \text{WHILE}^{\text{time}(34n+12)}$  that have the same semantics. Under what conditions would it be better to use one or the other? [6 marks]

(b) The Travelling Salesman problem (TSP) is **NP**-complete.

i. Explain what is meant by this statement. As part of your answer explain also **NP**. [5 marks]

ii. Referring to TSP as specific example, explain to what extent approximation algorithms are a useful means to solve **NP**-complete problems (viewed as optimisation problems). [6 marks]

(c) Which of the following are true of the Cook-Levin Theorem? (No explanation required.)

- i. It says something about the Satisfiability Problem.
- ii. It is not a theorem but a thesis.
- iii. It says that for polynomial decidability it does not matter which programming language we are using, as long as it is as powerful as Turing machines.
- iv. It says the Travelling Salesman Problem is of exponential complexity.
- v. It says that a certain problem is **NP**-complete.

[5 marks]

(d) Which of the following problems are *known* to be **NP**-complete?

- i. 0-1 Knapsack problem
- ii. Complement of the Halting problem
- iii. Graph Colouring problem
- iv. Tiling problem
- v. Postman problem
- vi. Factorisation Problem

[6 marks]

- (e) In the following give a rough description of *how* you would prove the statement. You do not have to give a proof, but you are supposed to give a required plan, i.e. which activity you would need to carry out and which theorems you would use in which way. Be as precise as possible.



- i. For some fixed problem  $A$ : how would you establish that  $A$  is in  $LI$ ? [4 marks]
  - ii. For some fixed problem  $A$ : how would you establish that  $A$  can't possibly be in  $P^{WHILE}$  unless  $P^{WHILE} = NP^{WHILE}$ ? [5 marks]
- (f) Consider the statement  $BQP = NP$ .
- i. Explain what this statement means. [3 marks]
  - ii. What do we know about the validity of this statement? [2 marks]

WeChat: cstutorcs

Assignment Project Exam Help

Email: [tutorcs@163.com](mailto:tutorcs@163.com)

QQ: 749389476

<https://tutorcs.com>