

# 程序代写代做 CS编程辅导

Take-Home Final Exam for ISy 7406

This is an open-book take-home final exam. You are free to use any resources including textbooks, notes, computers and internet, but **no collaborations are allowed**, particularly you cannot communicate, *online* or *oral* (in person or via Zoom, etc.) with anyone about this midterm (except the TAs or instructor via piazza if you have an account). **This must be individual work.** See Canvas for the data sets and some useful information.

**Overview:** In probability and statistics, it is important to understand the mean and variance for any random variables. When the distribution of a random variable  $Y$  depends on two independent variables  $X_1$  and  $X_2$ , it is straightforward to simulate the random variable  $Y$ 's, but it is often highly non-trivial to characterize the exact distribution of  $Y = Y(X_1, X_2)$  including deriving the explicit formula for the mean and variance of  $Y = Y(X_1, X_2)$  explicitly as a function of  $X_1$  and  $X_2$ .

**Objective:** In this exam, suppose that  $Y = Y(X_1, X_2)$  is a random variable whose distribution depends on two independent variables  $X_1$  and  $X_2$ , and the objective is to estimate two deterministic functions of  $X_1$  and  $X_2$ : one is the mean  $\mu(X_1, X_2) = \mathbf{E}(Y)$  and the other is the variance  $V(X_1, X_2) = \text{Var}(Y)$ .

For that purpose, you are provided the observed 200 realizations of the  $Y$ 's values for some given pairs  $(X_1, X_2)$ 's. You are asked to use data mining or machine learning methods that allow us to conveniently predict or approximate the mean and variance of  $Y = Y(X_1, X_2)$  as a function of  $X_1$  and  $X_2$ . That is, your task is to predict or approximate two values for those given pairs  $(X_1, X_2)$  in the testing data set: one for the mean  $\mu(X_1, X_2) = \mathbf{E}(Y(X_1, X_2))$  and the other for the variance  $V(X_1, X_2) = \text{Var}(Y(X_1, X_2))$ .

**Training data set:** In order to help you to develop a reasonable estimation of the mean and variance of  $Y = Y(X_1, X_2)$  as deterministic functions of  $X_1$  and  $X_2$ , we provide a training data set that is generated as follows. We first choose the uniform design points when  $0 \leq X_1 \leq 1$  and  $0 \leq X_2 \leq 1$ , that is,  $x_{1i} = 0.01 * i$  for  $i = 0, 1, 2, \dots, 99$ , and  $x_{2j} = 0.01 * j$  for  $j = 0, 1, 2, \dots, 99$ . Thus there are a total of  $100 * 100 = 10^4$  combinations of  $(x_{1i}, x_{2j})$ 's, and for each of these  $10^4$  combinations, we generate 200 independent realizations of the  $Y$  variables, denoted by  $Y_{ijk}$  for  $k = 1, \dots, 200$ .

The corresponding training data, `7406train.csv`, is available from Canvas. Note that this training data set is a  $10^4 \times 202$  table. Each row corresponds to one of  $100 * 100 = 10^4$  combinations of  $(X_1, X_2)$ 's. The first and second columns are the  $X_1$  and  $X_2$  values, respectively, whereas the remaining 200 columns are the corresponding 200 independent realizations of  $Y$ 's.

Based on the training data, you are asked to develop an accurate estimation of the functions  $\mu(X_1, X_2) = \mathbf{E}(Y)$  and  $V(X_1, X_2) = \text{Var}(Y)$ , as deterministic functions of  $X_1$  and  $X_2$  when  $0 \leq X_1 \leq 1$  and  $0 \leq X_2 \leq 1$ .

To assist you, a limited empirical data analysis (EDA) on the training data is provided in the appendix by using R. Please feel free to modify to other language such as Python, Matlab, etc.

**Testing data set:** For the purpose of evaluating your proposed estimation models and methods, we choose 50 random design points for  $X_1$  and 50 random design points for  $X_2$ . Thus there are a total of  $50 * 50 = 2500$  combinations of  $(X_1, X_2)$  in the testing data set. You are asked to use your formula to predict  $\mu(X_1, X_2) = \mathbf{E}(Y)$  and  $V(X_1, X_2) = \text{Var}(Y)$  for  $Y = Y(X_1, X_2)$  for the  $50 * 50 = 2500$  combination of  $(X_1, X_2)$  in the testing data (please keep the six digits for your answers).

The exact values of the  $(X_1, X_2)$ 's in the testing data set are included in the file `7406test.csv`, which is available from Canvas. You are asked to use your formula to predict  $\mu(X_1, X_2) = \mathbf{E}(Y)$  and  $V(X_1, X_2) = \text{Var}(Y)$  for the  $50 * 50 = 2500$  combination of  $(X_1, X_2)$  in the testing data (please keep (at least) six digits for your answers).

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**Estimation Evaluation Criterion.** In order to evaluate your estimation or prediction, we obtain “true” values  $\mu(X_1, X_2) = \mathbf{E}(Y)$  and  $V(X_1, X_2) = \text{Var}(Y)$  for each combination of  $(X_1, X_2)$  in the testing data set, based on the following Monte Carlo simulations (we will not release these true values!).

We first generated 200 independent realizations of  $Y$ 's for each combination of  $(X_1, X_2)$  in the testing data set, but we will not release these realizations for the testing data. Next, for each given combination of  $(X_1, X_2)$ , we have 200 realizations of  $Y$ 's, denoted by  $Y_1, \dots, Y_{200}$ , and then we compute the “true” values

$$\mu_{true}^* = \bar{Y} \quad \text{and} \quad V_{true}^* = \hat{\text{Var}}(Y) = \frac{1}{200-1} \sum_{i=1}^{200} (Y_i - \bar{Y})^2.$$

Your predicted mean or variance functions, say,  $\hat{\mu}(X_1, X_2)$  and  $\hat{V}(X_1, X_2)$ , will then be evaluated as compared to these true values,  $\mu_{true}^*(X_1, X_2)$  and  $V_{true}^*(X_1, X_2)$ :

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$$MSE_{\mu} = \frac{1}{IJ} \sum_{i=1}^I \sum_{j=1}^J (\hat{\mu}(x_{1i}, x_{2j}) - \mu_{true}^*(x_{1i}, x_{2j}))^2$$
$$MSE_V = \frac{1}{IJ} \sum_{i=1}^I \sum_{j=1}^J (\hat{V}(x_{1i}, x_{2j}) - V_{true}^*(x_{1i}, x_{2j}))^2, \quad (1)$$

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where  $(I, J) = (50, 50)$  for the testing data.

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**Your tasks:** as your solution set to this exam, you are required to submit two files to Canvas before the deadline:

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- (a) A .csv file on the required prediction that includes your predicted values for  $\mu(X_1, X_2) = \mathbf{E}(Y)$  and  $V(X_1, X_2) = \text{Var}(Y)$  for the testing data (in 6 digits). Please name your file as “1.YourLastName.YourFirst.Name.csv”, e.g., “1.Mei.Yajun.csv” for the name of the instructor. I think students in our class have a unique combination of last/first name, and thus there is no need to include the middle name.

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- The submitted csv file in excel must be  $2500 \times 4$  column, and the first two columns must be the exact same as the provided testing data file “7406test.csv”. The third column should be your estimated mean  $\hat{\mu}(X_1, X_2)$ , and the fourth column is your estimated variance  $\hat{V}(X_1, X_2)$ .
  - If you want, please round your numerical answers to the six decimal places, e.g., report your estimations as the form of 30.xxxxxx, but this is optional: in our evaluation process we will use the round function to round your answers to the six decimal before computing MSE.
  - Please save your predictions as a  $2500 \times 4$  data matrix in this .csv file, e.g., **without headers or row/column labels/names**. We will use the computer to auto-read your .csv file and then auto-compute the MSE values in equation (1) for all students, based on the alphabet order of the last/first name, and thus it is important for you to follow this guideline, e.g., without headers or extra columns/rows in the .csv file and name your .csv file as the above form.
- (b) A (pdf or docx) file that explains the methods used for the prediction. Please name your file as “2.YourLastName.YourFirst.Name”, e.g., “2.Mei.Yajun.pdf” or “2.Mei.Yajun.docx” for the name of the instructor.

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Your written report should be like good journal papers that thoroughly explain and justify your proposed models and methods, also see the guidelines on the final report of our course project. Please feel free to use any methods — this is an open-ended problem, and you can either use any standard method from the class, or develop your estimation by a completely new approach.



### Remark:

- If you upload your files at Canvas, the file names might be renamed automatically by Canvas to "FirstName.csv-1" or similar. If this occurs, please do not worry, as we will find it and correct for you.
- This final exam essentially asks you to build two different models: one is to predict  $\hat{\mu}$  and the other is to predict  $\hat{V}$ . For each model, there are  $p = 2$  independent variables ( $X_1, X_2$ ), although both  $\hat{\mu}(X_1, X_2)$  and  $\hat{V}(X_1, X_2)$  functions are likely needed to be nonlinear in order to receive good predict performance. To be more specific, you might want to look beyond the multiple linear regression model of  $\beta_0 + \beta_1 X_1 + \beta_2 X_2$ , and investigate some nonlinear models such as polynomial regressions, local smoothing, generalized additive models, random forests, boosting, support vector machine with suitable kernels, neural networks, etc. Then you need to decide which (nonlinear) models should be used for predictions in the testing dataset. Hopefully this high-level viewpoint allows you easily develop models for prediction.
- After your submission, please double check your submitted .csv file at Canvas to see whether it has exactly 2500 rows and 4 columns or not, whether it has "NA" or missing values or not. In the past, there were three typical small mistakes that will severely affect predictions: (i) having 5 or more columns (e.g., one unnecessary column to label observations); (ii) having more than 2500 rows (e.g., predictions on the training data instead of the testing data, or having predictions from multiple models); and (iii) having "NA" values in the .csv files (e.g., some models will generate a prediction of "NA" if the data in the testing dataset is outside the range of the training dataset). Thus it is crucial to assure that your .csv file has the required 2500 rows and 4 columns that reports the desired prediction values.

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**Grading Policies:** The total point of this take-home final exam is 25 points, which will be graded by the TAs and instructor. There are three components:

- **Prediction accuracy on mean:** 10 points. The smaller  $MSE_{\mu}$  in (1) the better. Tentatively, we plan to assign "10" if  $MSE_{\mu} \leq 1.20$ , "9" if  $(1.20, 1.40]$ , "8" if  $(1.40, 1.60]$ , "7" if  $(1.60, 1.80]$ , "6" if  $(1.80, 2.00]$ , "5" if  $(2.00, 3]$ , "4" if  $(3, 10]$ , "3" if  $(10, 20]$ , "2" if  $(20, 30]$ , etc. For your information, in the past semesters, the percentages of students who received "10", "9", and "8" are 43%, 35%, 16%, resp. For the students who received low grades, they often did not realize that they made small mistakes/errors here or there, or did not tune the hyper-parameters appropriately, etc. In general, we feel that our grading is very generous, and will keep the right to adjust the grading schedule to be more generous if needed.
- **Prediction accuracy on variance:** 10 points. The smaller  $MSE_V$  in (1) the better. Note that predicting variance is a much harder question as compared to predicting mean, and thus we expect that MSE to be much larger. Tentatively, we plan to assign "10" if  $MSE_V \leq 550$ , "9" if  $(550, 570]$ , "8" if  $(570, 590]$ , "7" if  $(590, 610]$ , "6" if  $(610, 630]$ , "5" if  $(630, 650]$ , "4" if  $(650, 700]$ , "3" if  $(700, 1000]$ , "2" if  $(1000, 5000]$ , etc. In the past semesters, 60% students received "10", and more than "90%" received at least "8". Thus we feel the grading should be generous, and will keep the right to adjust the grading schedule to be more generous if needed.

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- **Written Report:** 15 points. There are no specific guidelines on the written report, and please feel free to use the commonsense. With that said, we will look at the following aspects. Is the report well-written or easy to read? Is it easy to find the final chosen model or method? Does the report clearly explain how to choose the final chosen method? Does the report discuss how to suitably choose the final chosen model? We plan to assign the grades of this component as follows: “A” - 5, “B” - 4, “C” - 3, “D” - 2, “F” - 1, “Not submitted” - 0):

The TAs and instructors will best to give fair technical grades to all reasonable answers, e.g., even if your prediction is not as good as other students, we keep the right to increase your prediction accuracy if your written report has a solid justification of your proposed models/methods/results. We acknowledge that ultimately this is a subjective decision.

If needed, please feel free to leave a public or private message at Piazza. Good luck to your final exam!

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**Appendix:** Some useful R codes for (A) training dataset, (B) testing dataset, and (C) our auto-grading program.

(A) Empirical Data Analysis of training dataset, which might be useful to inspire you to develop suitable methods for



```
#####  
### Read Training  
## Assume you save data in the folder "C:/temp" in your local laptop  
traindata <- read.csv("C:/temp/7406train.csv", sep=",");  
dim(traindata);  
## dim=10000*202  
## The first two columns are X1 and X2 values, and the last 200 columns are the Y values
```

### Some example plots for exploratory data analysis

### please feel free to add more exploratory analysis

```
X1 <- traindata[,1];
```

```
X2 <- traindata[,2];
```

```
## compute the empirical estimation of muhat = E(Y) and Vhat = Var(Y)
```

```
muhat <- apply(traindata[,3:202], 1, mean);
```

```
Vhat <- apply(traindata[,3:202], 1, var);
```

```
## You can construct a dataframe in R that includes all crucial
```

```
## information for our exam
```

```
data0 = data.frame(X1 = X1, X2=X2, muhat = muhat, Vhat = Vhat);
```

```
## we can plot 4 graphs in a single plot
```

```
par(mfrow = c(2, 2));
```

```
plot(X1, muhat);
```

```
plot(X2, muhat);
```

```
plot(X1, Vhat);
```

```
plot(X2, Vhat);
```

```
## Or you can first create an initial plot of one line
```

```
## and then iteratively add the lines
```

```
##
```

```
## below is an example to plot X1 vs. muhat for different X2 values
```

```
##
```

```
## let us reset the plot
```

```
dev.off()
```

```
##
```

```
## now plot the lines one by one for each fixed X2
```

```
##
```

```
flag <- which(data0$X2 == 0);
```

```
plot(data0[flag,1], data0[flag, 3], type="l",
```

```
      xlim=range(data0$X1), ylim=range(data0$muhat), xlab="X1", ylab="muhat");
```

```
for (j in 1:99){
```

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```
flag <- which(data0$X2 == (1.01*J))
lines(data0[flag,1], data0[flag, 3]);
}
```

## You can also plot  $\hat{\mu}$  for fixed  $X_1$  or for  $V$ hat

### You are essentially asked to build two models based on "data0":  
### one is to predict  $\hat{\mu}$  on  $(X_1, X_2)$ ; and  
### the other is to predict  $\hat{V}$  based on  $(X_1, X_2)$ .



(B) Read the testing data and write your prediction on the testing data:

```
## Testing Data: first read testing X variables
testX <- read.table(file = "C:/temp/7406test.csv", sep=",");
dim(testX)
## This should be a 2500*2 matrix
```

## Next, based on your models, you predict  $\hat{\mu}$  and  $\hat{V}$  for  $(X_1, X_2)$  in testX.

```
## Suppose that will lead you to have a new data.frame
## "testdata" with 4 columns, "X1", "X2", "muhat", "Vhat"
## Then you can write them in the csv file as follows:
## (please use your own Last Name and First Name)
write.table(testdata, file="C:/temp/1.LastName.FirstName.csv",
  sep=",", col.names=F, row.names=F)
```

```
## Then you can upload the .csv file to the Canvas
## Note that in your final answers, you essentially add two columns for your estimation of
##  $\hat{\mu}(X_1, X_2) = E(Y)$  and  $\hat{V}(X_1, X_2) = \text{Var}(Y)$ 
## to the testing X data file "7406test.csv".
## Please double check whether your predictions are saved as a 2500*4 data matrix
## in a .csv file "without" headers or extra columns/rows.
```

(C) Our auto-grading program on your prediction (this does not affect your prediction, and it is only for those interested students). Also if somehow the auto-grading program failed (e.g., due to inconsistent file names), we will manually compute your prediction, as we want to make sure to have a fair grading to everyone.

```
##### In the auto-grading, we run loops, one loop for each student
##### In each loop, we first generate the filename as name1 = "1.LastName.FirstName.csv",
##### Next, we compare your answers with those Monte Carlo based values,
##### "muhatestMC" and "VhatestMC", which were computed as mentioned in the exam
##### and held out by the instructor (sorry that we would not release them
##### since otherwise students can simply copy and paste to get perfect predictions).
#####
```

## 程序代写代做 CS编程辅导

```
resulttmp <- read.table(file = "name1", sep = ",");  
muhatmp <- round(resulttmp[,3], 6); ## Your predicted values for \mu in 6 digits  
Vhatmp <- round(resulttmp[,4], 6); ## Your predicted value of Vhat in 6 digits  
MSEmu <- mean((resulttmp[,3] - muhatmp)^2);  
MSEV <- mean((resulttmp[,4] - Vhatmp)^2);  
##### Your technique is based on MSEmu and MSEV values  
##### In general, the smaller the value, the better.  
##### However, the answer on how small is small.  
##### Also it is more accurate prediction on Variance than on Mean  
##### END #####
```

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