

程序代写代做 CS编程辅导

Your Name:

- 1a. (5 points) Suppose  $A$  is an  $n \times n$  matrix with complex entries and  $A^* = A$ . Suppose  $V$  is a subspace of  $\mathbb{C}^n$  such that  $x \in V \Rightarrow Ax \in V$ . Show that  $A(V^\perp) \subset V^\perp$ .



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- 1b. (5 points) Suppose  $A$  is a real, symmetric,  $n \times n$  matrix. Show that  $e^A$  is positive definite.

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2a. (2 points) Write down the overdetermined linear system  $Ax = b$  whose least squares solution  $x = \begin{pmatrix} C \\ D \end{pmatrix}$  gives the best-fit line  $y(t) = C + Dt$  to the following points  $(t_i, b_i)$

$$\begin{array}{c|ccccc} t_i & -1/3 & 1 & 4 & 5 \\ \hline b_i & -13/4 & -1/4 & 9/4 & 13/4 \end{array}$$

in the sense that  $\|r\|_2$  is



2b. (5 points) Find the information  $H_1 = I - \tau_1 v_1 v_1^T$  that reflects the first column of the matrix from part 2a. (Find  $\tau_1$  and  $v_1$ , following the convention that  $(v_1)_1 = 1$ .)

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2c. (3 points) After applying  $H_1$  and computing and applying a second householder transformation, the above system becomes

$$\begin{pmatrix} -2 & -13/3 \\ 0 & -5 \\ 0 & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} C \\ D \end{pmatrix} = \begin{pmatrix} -1 \\ -5 \\ -0.3 \\ -0.4 \end{pmatrix}.$$

Compute  $C$ ,  $D$  and the norm  $\|r\|_2$  of the minimum residual.

3. (10 points) Let  $A = \begin{pmatrix} 6 & 8 \\ 4 & -3 \end{pmatrix}$ . Find all rank-1 matrices  $B$  such that  $\|A - B\|_2$  is minimized.

*Hint: if you can't figure out the SVD by inspection,  $AA^T$  is simpler than  $A^T A$  as a starting point to compute the SVD systematically.*

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4. (10 points) Compute the pseudo-inverse of

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$$A = \begin{pmatrix} 1 & 2 \\ -2 & 2 \\ 2 & -1 \end{pmatrix}$$

You can leave your answer as a product of 3 matrices if you wish, but compute each entry of each of those matrices.



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