### Logic and AI Programming:

## **Introduction to Logic Introduction to Prolog**

Assignment Project Exam Help

https://tutorcs.com

Weahatusstutgrerm

October – December

### Course Material

Course material will be available via CATE, including signment Project Exam Help

- ✓ Notes https://tutorcs.com
- ✓ Tutorial Extensises: cstutorcs
- ✓ Tutorial Exercise Solutions
- ✓ Coursework

### **CONTENTS**

#### Introduction to logic

### Propositional desirroject Exam Help

- Syntax
- · Semantique (Tsuth that let's cs.com
- Rules of inference (Natural Deduction)

#### Predicat We Ghat: cstutorcs

- Syntax
- Informal semantics
- Rules of inference (Natural Deduction)

#### Prolog programming

Time permitting: Probabilistic Prolog or Abductive Reasoniong



### **Books**

## background reading on logic

- Any book on logic will have useful examples.
- Richard Spencer-Smith, Logic and Prolog, Harvester Witeatsheafstuffneslibrary has a number of copies)
- Jim Woodcock and Martin Loomes, Software Engineering Mathematics", Pitman Publishing



## Books Prolog



• Ivan Bratko, "Prolog programming for Assignment Project Exam Help artificial intelligence", Addison-Wesley, Third Edition, 2001 and Third Edition, and Edition,

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### **Assessments and Examination**

- One Logic Coursework
- One Prolog Lab Assessment Project Exam Help
- One Examination in Way:

Paper M1 (Programat: Destritor and Logic) will have:

- two questions on Logic and
- two questions on Object-Oriented Design

# Relevance of this course to Spring Term Modules

- Logic-based Learning course

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  course
- Introduction to Artificial Intelligence
- System Veriff Chatigrestutores
- Argumentation and Multi-Agent Systems

#### and to a lesser extent

- Databases Assignment Project Exam Help
  - Database httpsiagetope.g.cenational calculus and some features of SQL vechat: estutores
  - Datalog: emerging e.g. in data integration, information extraction, network monitoring, security and cloud computing

## Logic has many applications in computing

#### For example:

• Basis of a farment of piece Farming languages, page Protones Cosp (Answer Set Programming).

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 Basis of verification tools to reason about C, Java and JavaScript programs, and algorithms for concurrency, e.g. using Separation Logic.

• Software engineering: Formal specifications and formal specifications and formal specifications.

How do you https://tutorcs.poogram is "correct"? WeChat: cstutorcs

Review, again and again and ....

- Review the spec
- Review the design description
- Review the code

### Test, again and again and ....

- Unit testing

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- Integratiohttestingtorcs.com
- Validation testing: cstutorcs

But that is not enough.

How many tests do you run to be sure the system is cortetne.//tutorcs.com

- ✓ Logic prov**WeChawaştut6pos**oving the system correct and
- ✓ this can be automated too.



# Logic is also useful more generally in life

- Clear thinking
- Judging validity of arguments and justification to the contraction of arguments and justification to the contraction of the c
- Spotting in Wordshatten stiets or cs
- Awareness and avoidance of ambiguities of natural language

# Which of the following arguments are valid?



- Advertisement for a computing book: If you don't use significate experient theled this book. But was a reason who uses computers. So you need this book.
- ➤ If you work hard you will succeed. So if you do not succeed you have not worked hard.

# Which of the following arguments are valid?

Heard in a radio interview with a well-known polishers. Arried Examples have come from thes Little osnothing good has resulted for us from our membership of the EU.

## More reasoning exercises

- 1. All the trees in the park are flowering trees.
- 2. Some of the trees in the park are dogwoods.
- 3. All dogwoods in the park are flowering trees.

Assignment Project Examine the first two statements are true, the third

statement is

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- A. true
- B. false
- C. uncertain



## More reasoning exercises

- 1. All the tales ignored Project Exam Help
- 2. All the roses in Zoe's garden are yellow.
- 3. All the flowers https://datatoresido.white or yellow

If the first two statement is

- A. true
- B. false
- C. uncertain

## More reasoning exercises

- Fact 1: All dogs like to run.
- Fact 2:
- Some dogs like to swim.
  Some dogs look like their owners.

  Project Exam Help Fact 3:

If these three statements are facts, which of the following statements must also be a lace? //tutorcs.com

- All dogs who like to swim look like their owners.

  Dogs who like to swim also like to run. I.
- II.
- III. Dogs who like to run do not look like their owners.
- Α. I only
- **B**. II only
- II and III only
- D None of the statements is a known fact.

# Some arguments – Are they valid?

- It has been proven that all heroin addicts smoked manipulated Frojere Fryouthel Therefore, smoking manipulated eadsoto heroin addiction. WeChat: cstutorcs
- ➤ We cannot win the war on poverty without spending money. So if we do spend money we will conquer poverty.

## Another argument – Is it valid?

> One of the old arguments of tobacco spokesmen against the glaim that smeking causes lying cancer: Lung cancer is more common among male smokers than the among female smokers. If smoking were the cause of lung cancer, this would not be true. The fact that lung cancer is more common among male smokers means that it is caused by something in the male make-up. If follows that lung cancer is not caused by smoking, but something in the male make-up.

## **Propositional Logic**

- A good place to start.
- It is the core of many logics.

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## Components of a logic

- Language:
  - alphabet symbols

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  - syntax : rultepfortptatingctogether the symbols to make grammatically correct sentences.
- Semantics: meaning of the symbols and the sentences.
- Inference rules

## The Propositional Language: Alphabet

Propositional symbols

```
e.g. use_conjunctst, heiert Fook, Help, r, s, p1
```

• Logical cohmectives:cs.com

```
A: and (conjunction) cs
```

v: (inclusive) or (disjunction)

 $\neg$ : not (negation)

sometimes denoted as ~

 $\rightarrow$ : implication (if-then)

### The Propositional Language: Syntax of a grammatically correct sentence

#### (well formed formula, wff)

- A propositional symbol is a wff.
- If W, Wasignam Project Fx and Help are

```
¬ (W) https://tutosometimes written as ~(W) (W1 \land W2) WeChat: cstutorcs (W1 \lor W2) (W2 \leftarrow W1) (W1 \leftrightarrow W2)
```

• There are no other wffs.

### **Examples**

Suppose p, q, r, s, t are propositions. Then: Assignment Project Exam Help  $(p \rightarrow q)$  $(r \wedge \lor t)$  https://tutorcs.com  $(p \rightarrow q)$  WeGhatioestutores  $((p \rightarrow q) \lor ((p \land r) \rightarrow \neg (s)))$ is a wff  $((p \rightarrow q) \lor ((p \land r) \rightarrow \neg(s)))$ Draw a parse tree.

## Examples

Passing the exams and the project implies passing Arignment Project Exam Help

```
(pass_exams \ hatps:p/tojorespann_MSc
```

You do not pass the MSc and you do not get a certificate if you do not pass the exams or you do not pass the project.

### Exercise

- Formulate the first two arguments from the beginning is the beginning in the beginning is the beginning in t
- Advertisemehttpsr/atutorqsuting book: If you don't use computers you don't need this book. But you are a person who uses computers. So you need this book.
- ➤ If you work hard you will succeed. So if you do not succeed you have not worked hard.

# Some notes on simplifying syntax

• To avoid ending up with a large number of brackets signment dropette come Halpst brackets. https://tutorcs.com

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#### Examples:

 $(p \rightarrow q)$  can be written as  $p \rightarrow q$  $((p \rightarrow q) \lor r)$  can be written as  $(p \rightarrow q) \lor r$ . • "— "binds more closely than the other connectives." This Projecte Exact Holdrop some brackets. https://tutorcs.com

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Example

$$(\neg (p) \land q) \rightarrow t$$
 can be written as  
 $(\neg p \land q) \rightarrow t$ 

 • A and ∨ bind more closely than → and ↔. This can be used itendropts Broje brackets. Help

```
Examples: https://tutorcs.com (\neg p \land q) \rightarrow t can be written as WeChat: cstutorcs \neg p \land q \rightarrow t.
```

$$(p \land q) \rightarrow (r \lor s)$$
 can be written as  $p \land q \rightarrow r \lor s$ .

## Binding Strength of the Connectives

To avoid having to use many brackets, there is a convention of the transfer transfer to the transfer transfer

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Also: WeChat: cstutorcs

- Order of precedence
- Binding priority

## Binding Strength of the Connectives

Strongest Assignment Project Exam Help

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 $\rightarrow$ 

Weakest

 $\longleftrightarrow$ 

## Binding conventions: Examples

- $p \vee q \wedge r$  is understood as  $p \vee (q \wedge r)$
- ¬p v q Assignment Project Exam Help | v q is understood as (¬p) v q
- $p \rightarrow q \leftrightarrow r$  is understood as  $(p \rightarrow q) \leftrightarrow r$

I prefer the first and third bracketed versions.

They are more clear, and having a few brackets is not much of a burden! Please don't write unreadable formulas like

$$p \lor \neg q \to \neg r \leftrightarrow \neg \neg s \land t \lor \neg u$$

# Use brackets to remove ambiguity

#### Example:

is ambiguous. https://tutorcs.com

In general WeChat: cstutorcs

$$P \rightarrow (Q \rightarrow R)$$

and

$$(P \rightarrow Q) \rightarrow R$$

are not equivalent (do not have the same meaning).

## **Binding conventions**

```
So p \rightarrow q \rightarrow r is a problem. Assignment Project Exam Help is a problem. It needs brackets to disamblguate it.

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But p \land q \land r and p \lor q \lor r are fine (to be discussed later).
```

### **Exercise:**

## Which of the following are wffs?

Assume

p, q, r, sad, happy, tall, rich, work hattps://tutorcs.com/steal, borrow, and possesses are propositional symbols.



- rich  $\rightarrow$  happy
- $(p \lor q) \land (r \to p)$  Project Exam Help
- $p \lor \rightarrow q$  https://tutorcs.com
- sad  $\rightarrow \neg happShat$ : cstutorcs
- $\neg$ happy  $\leftarrow$  sad

- rich  $\rightarrow \neg\neg$ happy
- rich 

  Assignment Project Exam Help

  (work hard ∨ steal)
- (steal  $\land \lor borrow) \rightarrow possess$
- (steal v borrowhat: cspussess
- steal  $\vee$  borrow  $\rightarrow$  possess

- $(p \land q \rightarrow r) \land (\neg p \rightarrow \neg q)$
- $p \rightarrow \neg p$ Assignment Project Exam Help
- https://tutorcs.com p ∧¬p

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#### We will look at

- Parse trees Assignment Project Exam Help
- >Principle https://www.cs.com
- Subformute Chat: cstutorcs

in the lecture.

# Notes on terminology

- $\neg$  is a **unary** operator.
- The other science raie ti Fary of the ators.
- $X \vee Y$  is hathed/theodisjunction of X and Y.
- X \ Y \ X and Y are disjuncts.
- $X \wedge Y$  is called the **conjunction of X and Y**.
- $X \wedge Y$  X and Y are conjuncts.
- $\neg X$  is called the **negation of X**.

# Notes on terminology cntd.

• A → B is called an implication.

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A is called the antecedent,

https://tutorgs.com/
B is called the consequent.

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A *Literal* is a proposition or the negation of a proposition.

## **Semantics**

#### **Provides**

- The meaning of the simple (atomic) units
- Rules for putting together the meaning of the atomic Whitshoo formothe meaning of the complex units (sentences).

Semantics specifies under what circumstances a sentence is *true* or *false*.

```
T (truth) and
F (falsity) Assignment Project Exam Help
are known as https://tutorcs.com
WeChat: cstutorcs
```

# Constructing Truth Tables for the connectives

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https://tute	orcs.com
T WeChat:	F
E	Т
$\Gamma$	1

A	В	$\mathbf{A} \wedge \mathbf{B}$	
<del> </del>	ent Project T ://tutorcs.c	Exam Help T	
•	hat: estuto:		
F	T	F	
F	F	F	

#### **Example**

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John is not happy;/butches.isocomfortable.

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Represent as  $-h \wedge c$ 

Four possible cases

Assignment Project Exam Help<sub>F</sub> WeChat: cstutorcs F F F

A	В	A∨B
Assignme	ent Project	Exam Help
	T://tutorcs.co	_
TweC	hat: Estuto	rcs T
F	T	T
F	F	F

A	В	$A \rightarrow B$	
T	nt Project F T //tutorcs.co	T	
WeCl	nat: cstutoro	es F	
F	T	T	
F	F	T	

# Compare $\land$ with $\rightarrow$

A	В	$A \wedge B$	A	В	$A \rightarrow B$
T	Assig T	nment I T	ject Exa T cs.com	ı <del>m Help</del> T	T
T	F	F WeChat:	T	F	F
F	T	F	F	T	T
F	F	F	F	F	T

A	В	A↔B
Assignmen	t Project Exan	n Help
	tutores.com	T
TweCh	at: cstutorcs	F
F	T	F
F	F	T

## Note

For any wffs A and B, " $A \leftrightarrow B$ " is true exactly wherighted Brief Ethers Hele truth values, i.e. when the water both true or both false.

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The truth value of a wff is uniquely determined by the truits that determined by the truits and determined by the truits and the component at the component of the component of

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#### **Example:**

The truth table for the wff  $(p \lor q) \land (r \rightarrow p)$  is as follows:

```
q r p \lor q r \to p   (p \lor q) \land (r \to p)
T T T Assignment Project Exam Help
           T https://tutorcs.com
   TF
  FT
           T WeGhat: cstutorcs
  FF
                             F
   TF
F
   FT
           F
                 F
                            F
   FF
```

#### **Exercise:**

How many rows will there be in a truth table for a wff contain/interpropositional symbols? WeChat: cstutorcs

 $2^n$ 



#### **Exercise:**

Recall we sassignment Engiect Exam Help

$$P \rightarrow (Q \rightarrow R)$$
 https://tutorcs.com

$$(P \rightarrow Q) \rightarrow R$$
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in general do not have the same meaning.

Under which interpretation(s) do the truth values of the two wffs differ?

### Notes

The connective "v" stands for *inclusive* or, i.e. p v q is Aistigrpneted Rectirect Whemelither proposition is true or both are. https://tutorcs.com

Often in English whentwestuser or" we intend exclusive or, e.g.

- I'll go shopping or I'll stay at home.
- We will meet at his house *or* at the club.

## Notes cntd.

In this propositional language there is no connective for exclusive or but we can still express the concept, e.g.

```
(goshopping vstayHome) \land
\neg (\textbf{yvethppiogutotay} Home)
In general "p exor q" can be represented as:
(p \lor q) \land \neg (p \land q)
```

#### **Exercise:**

Draw the truth table of the first wff above.

A	В	A∨B	$\neg (A \land B)$	A exor B
	Assignn	nent Pro	ject Exam	$HapB) \land \neg (A \land B)$
T	T http	s:// <b>T</b> utor	cs.com	F
T	F We	Chat: cs	tutores	T
F	T	T	Т	T
F	F	F	T	F

## Notes cntd.

- Law of excluded middle:
  - A proposition (anche Projecte Intlyna Livef) is either true or false there is no middle ground, no "unknown". https://tutorcs.com
- So propositional Ingicistate reglued logic.
- There are other logics, including 3-valued ones.
- SQL, for example, implements 3-valued logic, where comparisons with NULL, including that of another NULL gives *UNKNOWN*.

## Example NULL Values

Table T of people and their hair colours:

Name Hat Size Hair Colour

Assignment Project Exam Help
Helen NULL Brown

https://tutorcs.com
Medium Red

Large NULL

Large NULL

Select Name

From T

Where Hat Size=Large AND Hair Colour ≠ Brown

	A	В	$A \vee B$
	T	T	T
	T	F	T
٨	F	T	T
A	_	Project Ex F	F F
	https://t	utores.com	T
	WeChat	: cstytorcs	T
	F	U	U
	U	F	U
	U	U	U

• A proposition (and consequently a wff) cannot best othern Project felsen Help

https://tutorcs.com

**Exercise:** 

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Draw the truth table for  $A \land \neg A$ .

$\neg \mathbf{A}$	$A \wedge \neg A$
<del>ent Project</del> F	<del>Exam Help</del> F
://tutorcs.c	om
hat: Cstuto	rcs F
	://tutorcs.co

## Notes cntd.

- The interpretation of "→" may be unintuitive sometimes.
- The semanting of Project Exam Helple in logic. https://tutorcs.com
- A  $\rightarrow$  B is simply the same as  $\neg A \lor B$ .
- In English we use "if .. then" in many different ways, and sometimes quite confusingly.
- Don't read  $A \rightarrow B$  as "A causes B".

## Some definitions

#### **Definition:**

A wff whichseighnates Projectificanery Helperpretation of its constituent parts is called a tautology. https://tutorcs.com

Example WeChat: csautorcs

 $A \rightarrow A$ 

The two wffs above represent the **Law of excluded** middle.

A	$\neg \mathbf{A}$	$A \lor \neg A$
Assignme	ent Project	Exam Help
	F://tutorcs.c	
FWeC	hat: <b>Estuto</b>	rcs T

#### **Definition**

A wff which evaluates to false in every interpretation of interpre

Example  $A \land \neg A$ 

#### **Definition**

A wff which is neither a tautology, nor an inconsistent pis/autoretingency, or is said to be contingent. Chat: cstutores

## Exercise

For each of the following determine if it is a tautology signosist proper contingency by drawing the truth table.

- a.  $P \wedge (P \vee Q)^{https://tutorcs.com}$
- b.  $(P \vee Q) \wedge (Wellow)$ t: cstutorcs
- c.  $Q \land \neg P \land (P \lor (Q \rightarrow P))$
- d.  $(P \land (Q \lor P)) \leftrightarrow P$
- e.  $(P \rightarrow Q) \rightarrow (\neg P \lor Q)$
- f.  $((P \rightarrow Q) \land (R \rightarrow S) \land (P \lor R)) \rightarrow (Q \lor S)$

# Definition: Equivalence

Two wffs are equivalent iff their truth values are the same made Pevery Example lation.

https://tutorcs.com

A is equivale Mtd 6 h Bt is stepnes ented as

$$\mathbf{A} \equiv \mathbf{B}$$
.

"≡" is the metasymbol for equivalence.

### **Double Negation Rule**

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Implication Rechat: cstutorcs

$$A \rightarrow B \equiv \neg A \vee B$$

#### **Commutative Rules**

Associative Ringhat: cstutorcs

$$(A \wedge B) \wedge C \equiv A \wedge (B \wedge C)$$

$$(A \lor B) \lor C \equiv A \lor (B \lor C)$$

### **Idempotence**

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$$A \wedge A = A + A = A$$

#### **Distributive Rules**

A 
$$\wedge$$
 (B  $\wedge$  (B  $\wedge$  C)

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### De Morgan's Rules

$$\neg(A \lor B) \equiv \neg A \land \neg B$$
$$\neg(A \land B) \equiv \neg A \lor \neg B$$

```
A \leftrightarrow B \equiv
(A \rightarrow B) \land (B \rightarrow A)^{\text{Project Exam Help}}
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```

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$$A \wedge B \equiv B$$
 if ????

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$$A \wedge B \equiv B$$
  $H^{ttps://tutorcs.com}$  WeChat: cstutorcs

 $A \vee B \equiv B$  if ????

 $A \lor B \equiv B$  if A is an inconsistency

### Exercise



```
Show
```

A B Assignment Project Exam Help

https://tutorcs.com

Example WeChat

WeChat: cstutorcs

I get an MSc  $\rightarrow$  I get big salary  $\equiv$ 

 $\neg$ (I get an MSc  $\land \neg$  I get big salary)

### Exercises

Show

https://tutorcs.com

Show

WeChat: cstutorcs

$$A \leftrightarrow B \equiv \neg A \leftrightarrow \neg B$$

# Showing $A \leftrightarrow B \equiv \neg A \leftrightarrow \neg B$

LHS 
$$\equiv (A \rightarrow B) \land (B \rightarrow A)$$
  
RHS  $\equiv (A \rightarrow B) \land (B \rightarrow A)$   
 $\equiv (A \rightarrow B) \land (A \rightarrow B)$   
 $\Rightarrow (A \rightarrow B) \rightarrow (A \rightarrow B)$   
 $\Rightarrow (A \rightarrow B) \rightarrow$ 

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Compare LHS with RHS:

LHS 
$$\equiv (A \rightarrow B) \land (B \rightarrow A)$$
  
 $| \qquad | \qquad |$   
RHS  $\equiv (\neg B \rightarrow \neg A) \land (\neg A \rightarrow \neg B)$ 

And both correspondences are an instance of one equivareignment Project Exam Help

 $X \rightarrow Y \underline{\text{httpsy/tutorex.com}}$ 

So this equivalent enteriscemongh to prove LHS  $\equiv$  RHS.

Showing 
$$X \to Y \equiv \neg Y \to \neg X$$
 $X \to Y \equiv$ 

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 $\neg X \lor Y \equiv$ 

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rule

 $\neg X \lor \neg \neg Y \equiv$ 

WeChat: estators negation

 $\neg Y \lor \neg X \equiv$ 

commutativity of  $\lor$ 
 $\neg Y \to \neg X$ 

implication rule

### **Back to Exercise**

For each of the following determine if it is a tautology signosist proper continuency by drawing the truth table.

- a.  $P \wedge (P \vee Q)^{https://tutorcs.com}$
- b.  $(P \vee Q) \wedge (Wellow)$ t: cstutorcs
- c.  $Q \land \neg P \land (P \lor (Q \rightarrow P))$
- d.  $(P \land (Q \lor P)) \leftrightarrow P$
- e.  $(P \rightarrow Q) \rightarrow (\neg P \lor Q)$
- f.  $((P \rightarrow Q) \land (R \rightarrow S) \land (P \lor R)) \rightarrow (Q \lor S)$