### Assignment et Exaginelp

https://tutorcs.com

WeChat: cstutorcs Fariba Sadri

### **Example: MSc regulations**

Passing the exams and the project implies passing Arisignment Project Exam Help

https://tutorcs.com

You do not washthe Misocand you do not get a certificate if you do not pass the exams or you do not pass the project.

## Let us take the following propositions for formulating the MStoject Example 19

https://tutorcs.com

pe: passeexamsstutores

pp: pass project

pm: pass MSc

gc: get certificate

In propositional logic:

pe App Assignment Project Exam Help

¬pe∨¬pp -https:ptutoxcs.cgm

WeChat: cstutorcs

Not expressive enough if we want to consider individual students, to check who has passed the MSc, and who has not, for example.

### Example

#### John:

passes the signment Project Example

but not the examps://tutorcs.com

Mary: WeChat: cstutorcs

passes the exams

passes the project

Who passes the MSc?

### Example

# For all individuals X: (pe(X) $\land$ Pp(X) $\rightarrow$ pm(X) https://tutorcs.com

For all individuals 
$$X$$
:

 $(\neg pe(X) \lor \neg pp(X) \rightarrow \neg pm(X) \land \neg gc(X))$ 

### Increase the expressive power of the Propositional Proposi

- Predicates: https://dktorasgraments (extending propositions)eChat: cstutorcs
- Parameters: as arguments of the predicates
- Variables: as arguments of the predicates
- Quantification

# More formal expression of the MSc regulations

```
\forall X (pe(X) \land pp(X) \rightarrow pm(X))
Assignment Project Exam Help
```

$$\forall X(\neg pe(X)) \xrightarrow{\text{https://tutores.com}} WeChat: cstutore(X) \land \neg gc(X))$$

**∀**: Universal Quantifier

```
Now given:

pe(mary) Assignment Project Exam Help

pp(mary)

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help

to positive the project Exam Help

<math>to positive the project Exam Help

to positive the project Exam Help
```

 $pe(mary) \land pp(mary) \rightarrow pm(mary)$ 

We can conclude:

pm(mary)

```
Also given:
pp(john)
¬pe(john)
            Assignment Project Exam Help
Using
\forall X(\neg pe(X)) \rightarrow (tXt) \rightarrow s.copm(X) \land \neg gc(X)
With instance Tiphnsinforcs
\neg \mathbf{pe}(\mathsf{john}) \vee \neg \mathbf{pp}(\mathsf{john}) \rightarrow
                       \neg pm(john) \land \neg gc(john)
We can conclude:
\neg pm(john) \land \neg gc(john)
```

### Another example

Every student has a tutor.

for all X Assignment Project Exam Help

(if X is a student then

there is WY Satelf that Y's is tutor of X)

 $\forall X (student(X) \rightarrow \exists Y tutor(Y,X))$ 

**∃**: Existential Quantifier

# The Predicate Logic Language Alphabet:

- Logical connectives (same as propositional logic): Assignment Project Exam Help
- Predicate symbols (as opposed to propositional symbols):a set of symbols each with an associated arity hat: cstutores
- A set of constant symbols.
   E.g. mary, john, 101, 10a, peter\_jones
- Quantifiers  $\forall$ ,  $\exists$
- A set of variable symbols. E.g. X, Y, X1, YZ.

#### Arity

```
In the previous examples:

Predicate Symbol Arity

student https://tutorcs.com

tutor WeChat: cstutorcs

pm 1

pp 1
```

A predicate symbol with

arity = 0 Assignment Project Exam Help is called a **nullary predicate** (it is a proposition;://tutorcs.com

arity = 1 is Waltacumarys predicate,

arity = 2 is called a binary predicate.

A predicate symbol with arity=n (usually n>2) is called an **n-ary** predicate.

#### **Definition:**

A Term is any constant or variable symbol.

https://tutorcs.com

WeChat: cstutorcs

# Syntax of a grammatically correct sentence (wff) in predicate logic

- p(t<sub>1</sub>,..., t<sub>n</sub>) is a wff if p is an n-ary predicate symbol and the transfer sems Exam Help
- If W, W1, and W2 are wffs then so are the following: https://tutorcs.com

```
\neg W \qquad \text{WeCMatric Mutorcs} \qquad W1 \lor W2
W1 \to W2 \qquad W1 \leftrightarrow W2
\forall X(W) \qquad \exists X(W)
where X is a variable symbol.
```

• There are no other wffs.

From the description above you can see that propositional logic is a special case of predicate logic.

Asignment Project Exam Help

n-ary, n>0, and we have terms and
quantifiers

WeChat: cstutorcs
Propositional Logic:
all the predicates are
nullary

#### Convention used in most places in these notes:

Assignment Project Exam Help

- Predicate and apps//antosymbols start with lower case letters.

  WeChat: cstutorcs
- Variable symbols start with upper case letters.

#### **Examples**

The following are wffs:

1. — martisignment Project Exam Help

https://tutorcs.com

2.  $\forall X (alive(X) \land adult human(X) \land \\ \neg married(X) \rightarrow \\ single(X) \lor divorced(X) \lor widowed(X))$ 

3.  $\exists X (bird(X) \land \neg fly(X))$ 

#### The following are not wffs:

4 – X Assignment Project Exam Help

https://tutorcs.com

5. single(X) We Chat: cstutorcs

6.  $\forall \exists X \text{ (bird}(X) \rightarrow \text{feathered}(X))$ 

# Exercise which of the following are wffs?

- 1.  $\forall X p(X)$
- 2.  $\forall X p(\hat{Y})$  Signment Project Example 2.
- 3.  $\forall X \exists Y p(Y)$  https://tutorcs.com
- 4. q(X,Y,Z) WeChat: cstutorcs
- 5.  $p(a) \rightarrow \exists q(a,X,b)$
- 6.  $p(a) \vee p(a,b)$

- 7.  $\neg \neg \forall X r(X)$
- 8.  $\exists X \ \exists Y \ p(X,Y)$  Project Exam Help
- 9.  $\exists X, Y p(X, Y)$ ://tutorcs.com
- 10.  $\forall X (\neg \exists Y) e Chat: cstutorcs$
- 11.  $\forall x (\neg \exists Y p(x,Y))$



#### Exercise

Formalise the following in predicate logic using the fight with grain that the fight with their more or less to by ious reaconing):

lecTheatre/1, weffre/1 cstortains/2, lecturer/1, has/2, same/2, phd/1, supervises/2, happy/1, completePhd/1.

- 1. 311 is a lecture theatre and 447 is an office. Assignment Project Exam Help
- 2. Every lectutestheators contains a projector.
- 3. Every offitecontains to telephone and either a desktop or a laptop computer.
- 4. Every lecturer has at least one office.
- 5. No lecturer has more than one office.

- 6. No lecturers share offices with anyone.
- 7. Some Accitances is Reprevised Phi Districted and some do not so
- 8. Each PhD student has an office, but all PhD students share their office with at least one other PhD student.

- 9. A lecturer is happy if the PhD students he/she<sup>Assipervisets</sup>Projectessfully Elmplete their PhD.https://tutorcs.com
- 10. Not all PhD students complete their PhD.

#### Note:

Assignment Project Exam Help states that there is at least one X such that phythetic tup fress.com

WeChat: cstutorcs

E.g. **3X** father(**X**, john)

says John has **at least** one father (assuming *father(X,Y)* is to be read as X is father of Y).

#### Exercise

Assuming a predicate same(X, Y) that expresses in a predicate same(X, Y) that expression individual, expression statement that John has exactly one father. You may also assume a binary predicate "father" as above.