程序們爲微微US编程辅导

Due: February 27 2023

Instructions:

- Show your wold be given if you can show some program and the show some program and the show on. If you can't solve a problem in full generality, try to solve some special cases.
- You may work in groups and consult outside resources (textbooks, web sites, etc.). However, you should ckpoyledge any assistance received from other people or outside resources. If working in a group, please list the names of your group members.
- Submitted solutions should either be typed, preferably using LaTeX, or neatly handwritten.
 Assignment Project Exam Help
- Solutions should be submitted as PDF documents through Canvas. If submitting scanned images, please assemble all pages into a single PDF document prior to uploading to Canvas.

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- 1.) Suppose that X is a first random match which takes virus the fellowing probabilities. $\mathbb{P}(X=-2)=\mathbb{P}(X=2)=2/5$ and $\mathbb{P}(X=1)=1/10$. Calculate the following quantities:
 - (a) $\mathbb{E}[X]$;
 - (b) Var(X);



iable with probability mass function

$$\mathbf{WeChat:}^{p_Z(n) = \begin{cases} Cn^{-2} & \text{if } n \neq 0 \\ \mathbf{0} & \text{stutorcs} \end{cases}$$

- (a) Find the value of the normalizing constant C.
- (b) Calculate the probability of the event "Z is even." Assignment Project Exam Help
 (c) Calculate the expected value of Z.
- 3.) Suppose that X and let $W = \frac{X}{X + Y + 1}$.
 - (a) Find the probability mass function of W (b) Calculate $\mathbb{E}[W]$. (a) Find the probability mass function of W 49389476
- 4.) Suppose that N is interpolar full transfer on N=k, let X be uniformly distributed on the integers $\{0,1,\cdots,k\}$
 - (a) Find the probability mass function of X.
 - (b) Calculate $\mathbb{E}[N|X=k]$ for $k=0,\cdots,n$.
- 5.) Suppose that X and Y are independent integer-valued random variables with probability mass functions p_X and p_Y and let Z = X + Y.
 - (a) Find an expression for the probability mass function p_Z in terms of p_X and p_Y .
 - (b) Use your result from (a) to show that if X and Y are independent binomial random variables with parameters (n_1, p) and (n_2, p) , then their sum Z = X + Y is Binomial with parameters $(n_1 + n_2, p)$.

- 6.) Suppose that five bell ar sampled will replace that from an in the contents were balls, 10 blue balls, 5 green talks and 5 yellow balls and let R, D, C and Y, Tespectively, lenote the numbers of red, blue, green or yellow balls in the sample.
 - ion of (R, B, G, Y). (a) Find the joint p
 - (b) Find the probab of B and of R + G.
 - (c) Calculate $\mathbb{E}[G]$



ve integer-valued random variable with distribution

$$\mathbb{P}(X=k) = \frac{k^{-s}}{\xi(s)}, \quad k = 1, 2, 3, \cdots$$

where

WeChat: cstutorcs $\xi(s) \equiv \sum_{n=1}^{\infty} n^{-s}$.

$$\xi(s) \equiv \sum_{n=1} n^{-s}.$$

(a) Let p_1, p_2, \cdots be an enumeration of the prime numbers and define $E_{p_i} = \{X \equiv 0 \text{ m}\}$

- to be the event that X is divisible by p_i . Show that the events E_{p_1}, E_{p_2}, \cdots are independent.

(b) Use the result from (a) to prove that tutores @ 163.com $\frac{1}{\xi(s)} = \prod_{i=1}^{n} (1 - p_i^{-s}).$

$$\frac{1}{\xi(s)} = \prod_{i=1}^{\infty} (1 - p_i^{-s})$$

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- 8.) Suppose that X, Y and Z are discrete real-valued random variables.
 - (a) Show that $\mathbb{E}[X \text{ https://tutorcs.com}]$ (b) Calculate $\mathbb{E}[g(X)|X]$, where $g: \mathcal{R} \to \mathcal{R}$ is a real-valued function.

 - (c) Calculate $\mathbb{E}[X|Y]$ assuming that X is independent of Y.
- 9.) Suppose that Z_0, Z_1, \cdots is a sequence of independent, identically-distributed random variables with distribution $\mathbb{P}(Z_i = 1) = \mathbb{P}(Z_i = -1) = 1/2$ and define the sequence X_0, X_1, \cdots recursively by setting $X_0 = 0$ and $X_{n+1} = X_n + Z_n$ for each $n \ge 1$. Calculate $\mathbb{E}[X_{n+m}|X_n]$ for $n, m \geq 0$.
- 10.) Although the sex ratio at birth is close to 1:1 in human populations, biased sex ratios are found in many other species. This is true of many parasitoids, which lay their eggs on another host organism; when the eggs hatch, the young enter into the still living host and consume it from within, often taking care to avoid eating essential organs. In many of these species, mating occurs within the host organism between siblings.

- (a) Find a formula formula formula for the expected number of inseminated females that emerge from each formula formul
- (b) For each s, find μ_{ESS} have this expected value. This is said to be the optimal sex ratio, ϕ_{ESS} .
- (c) Explain the relationship between the survival probability s and the optimal sex ratio. **CSTULOTCS**

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