

Estimating and Interpreting Psychological Networks in R

Jens Lange and Janis Zickfeld

Sep 11, 2022

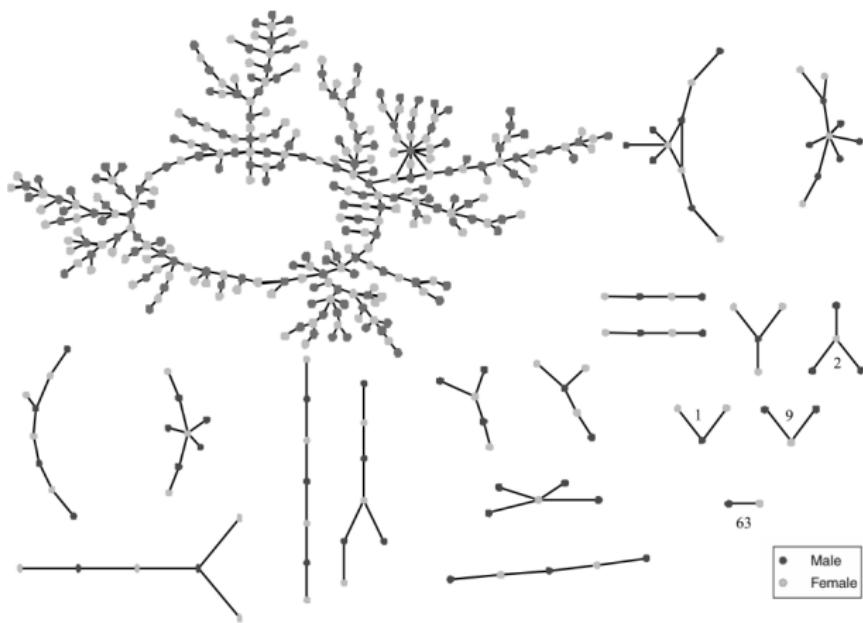
Introduction to Complex Networks

Complexity Science

- ▶ *complex systems* entail parts that interact with each other to produce system behavior



Complex Networks - Examples



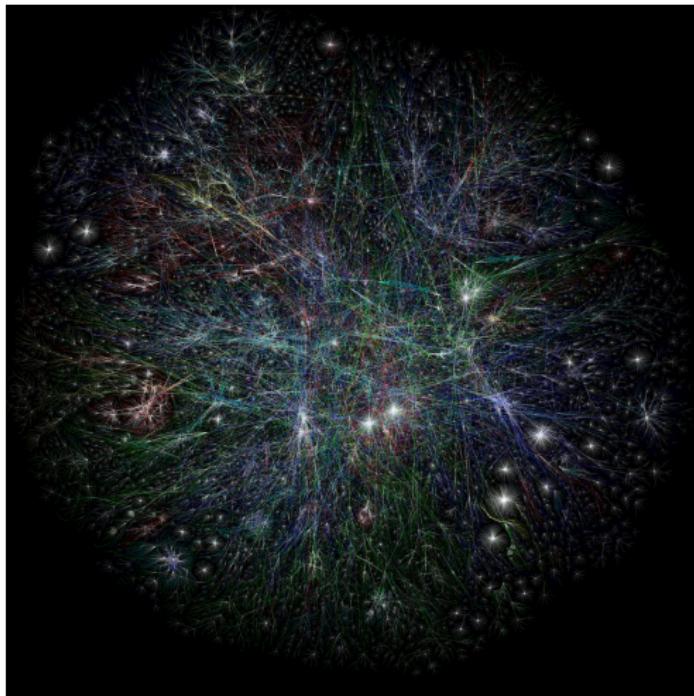
Bearman et al. (2004, AJS)

Complex Networks - Examples



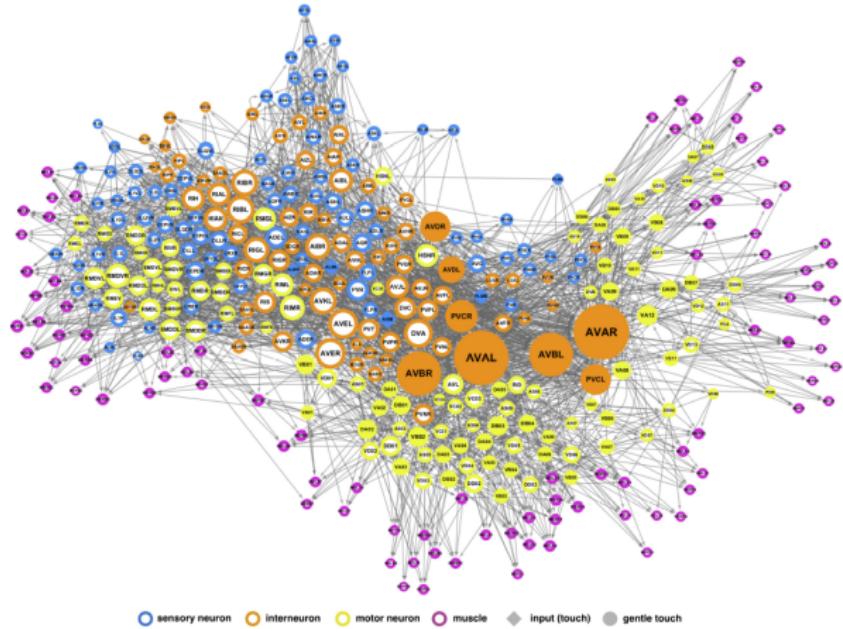
Xiaoqian et al. (2017, CJA)

Complex Networks - Examples



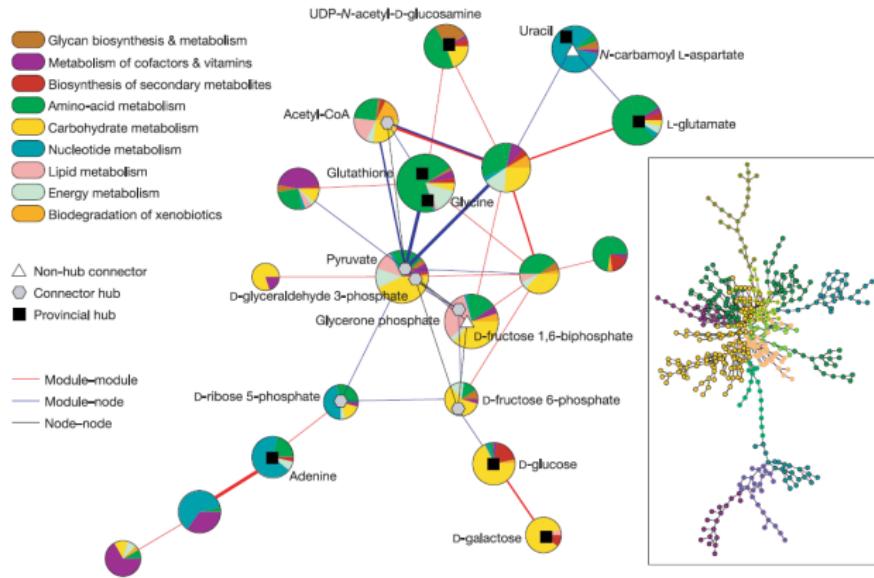
Albert et al. (1999, Nature)

Complex Networks - Examples



Yan et al. (2017, Nature)

Complex Networks - Examples



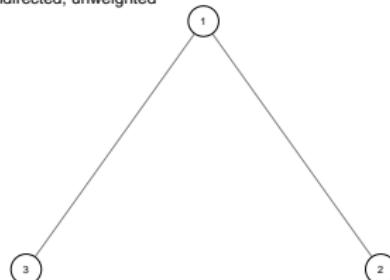
Guimerà & Amaral (2005, Nature)

Complex Networks - Definitions

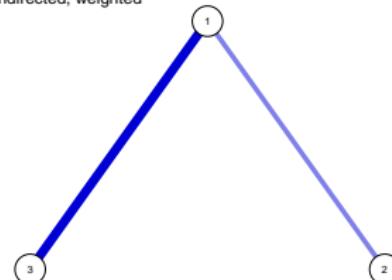
- ▶ network: *nodes* that are connected via *edges*
- ▶ nodes can be...
 - ▶ people
 - ▶ neurons
 - ▶ psychological variables
 - ▶ ...
- ▶ edges can be...
 - ▶ friendships
 - ▶ synapses
 - ▶ causal connections
 - ▶ ...

Complex Networks - Definitions

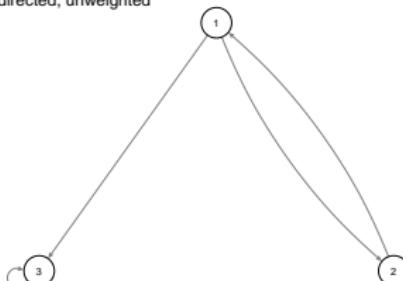
undirected, unweighted



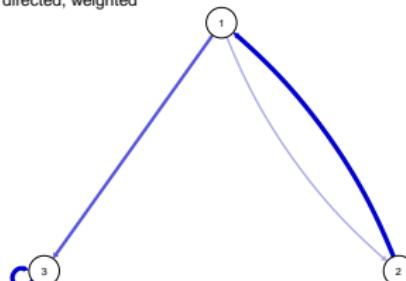
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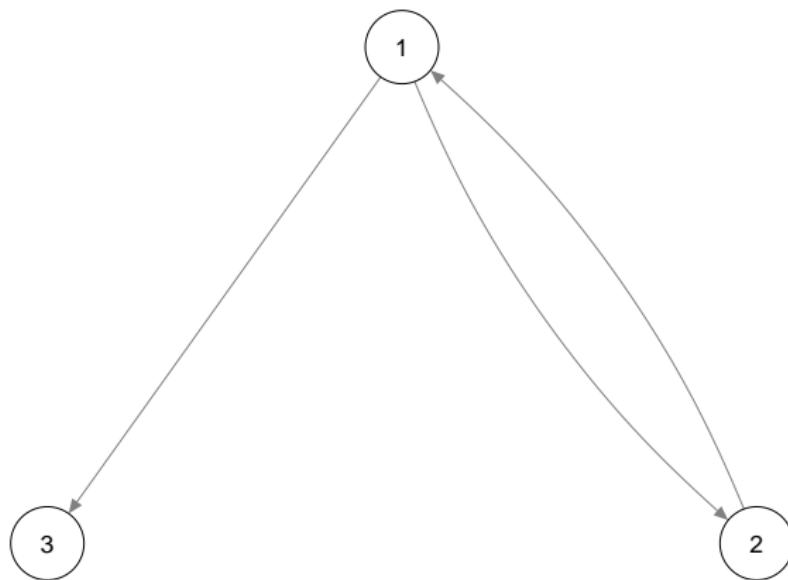


directed, weighted



Complex Networks - Mathematical Notation

- ▶ a Graph G entails sets of nodes N and edges E
 - ▶ $G = \{N, E\}$
 - ▶ $N = \{1, 2, 3\}$
 - ▶ $E = \{(1, 2), (1, 3), (2, 1)\}$

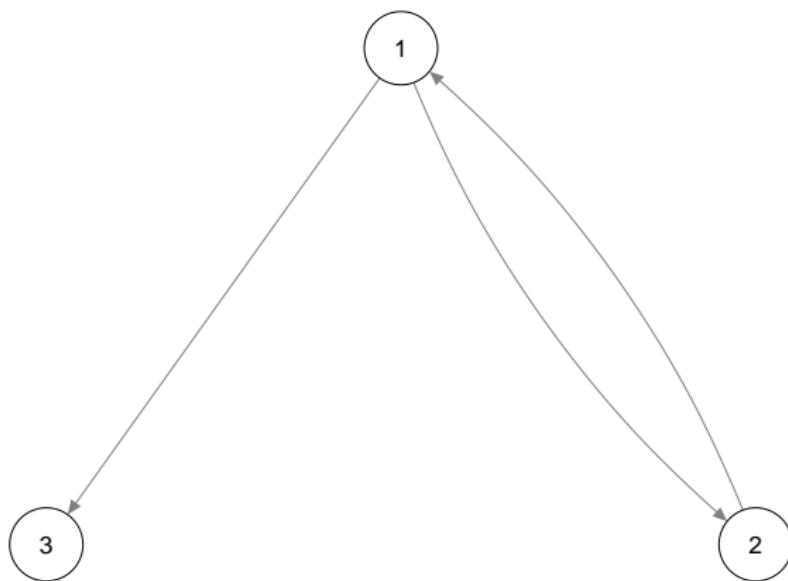


Complex Networks - Adjacency/Weights Matrix

- ▶ *adjacency matrix*: $N \times N$ matrix, with elements 0 or 1
 - ▶ 1 in row i and column j : edge from node i to j
 - ▶ undirected network has symmetric adjacency matrix
- ▶ *weights matrix* has the same form but with weights

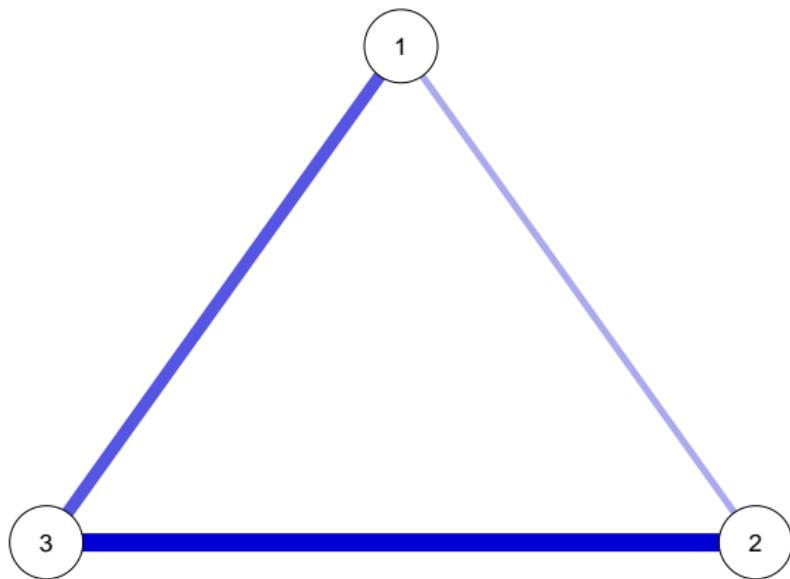
Complex Networks - Adjacency/Weights Matrix

$$\mathbf{A} = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$



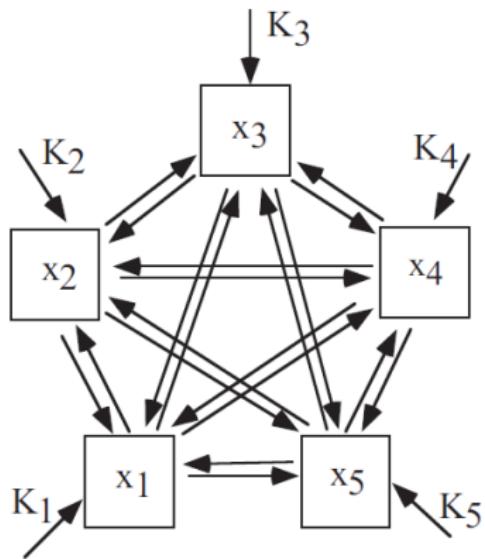
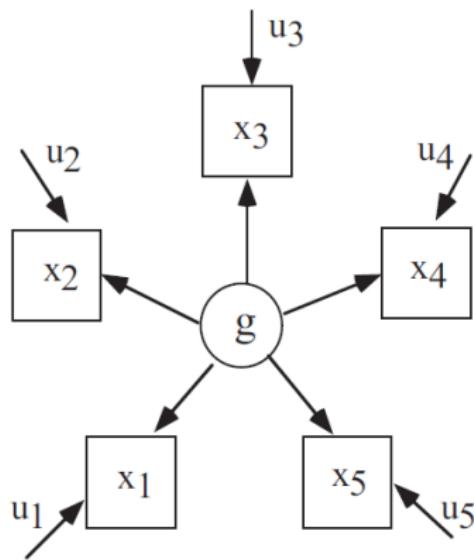
Complex Networks - Adjacency/Weights Matrix

$$\mathbf{W} = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 0 & 3 \\ 2 & 3 & 0 \end{bmatrix}$$



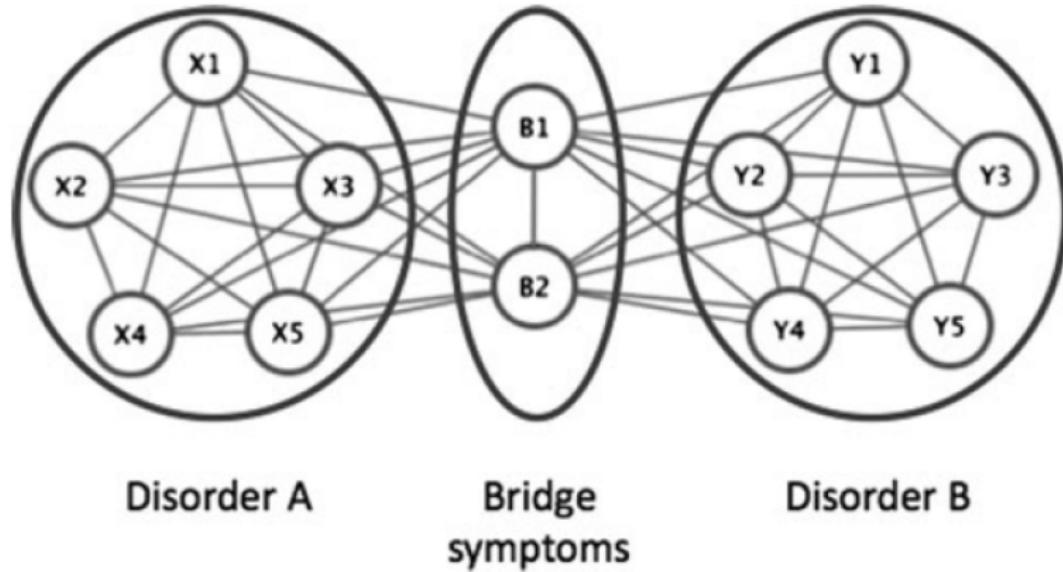
Psychological Networks

Psychological Networks - Intelligence



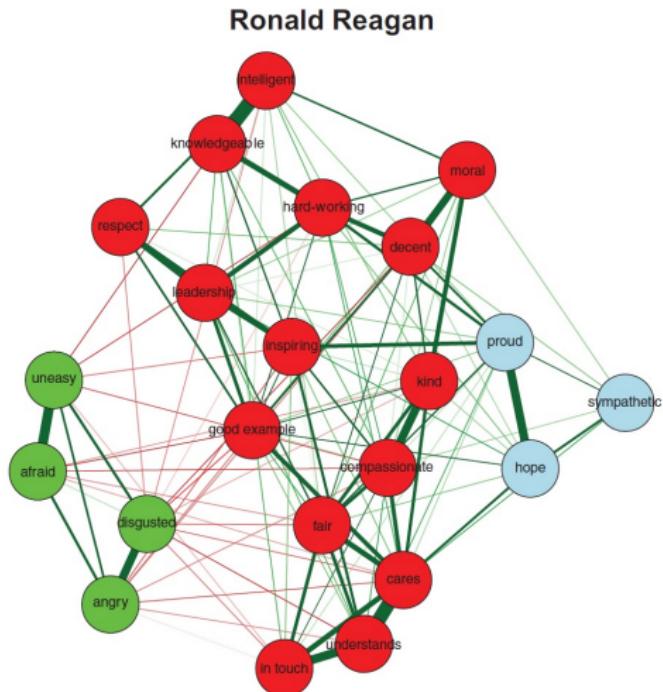
Van der Maas et al. (2006, Psych Review)

Psychological Networks - Psychological Disorders



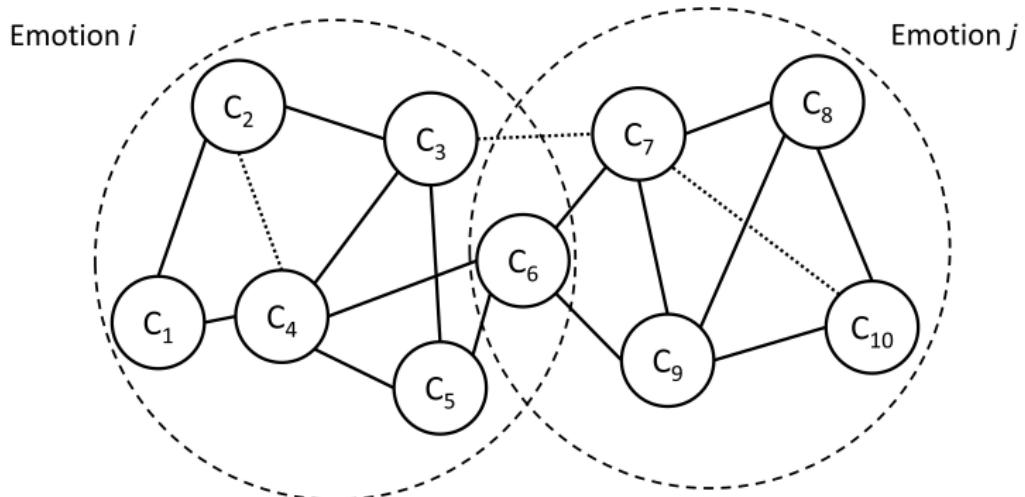
Cramer et al. (2010, BBS)

Psychological Networks - Attitudes



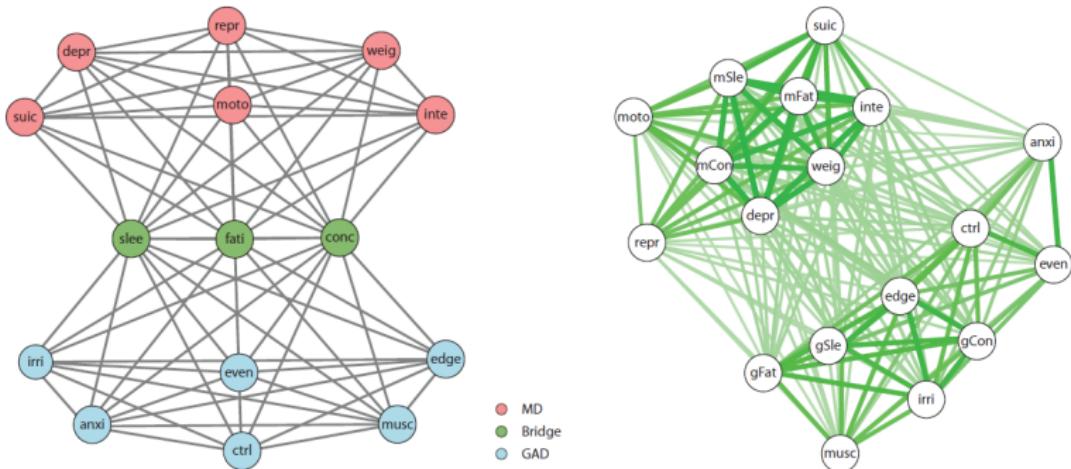
Dalege et al. (2016, PsychRev)

Psychological Networks - Emotions



Lange et al. (2020, PPS); Lange & Zickfeld (2021, ER)

Psychological Networks - Network Analysis



Borsboom et al. (2021, NRMP)

Summary for Introduction

Summary

- ▶ networks are versatile approach to complex systems
- ▶ networks entail sets of nodes and edges
- ▶ in psychological networks...
 - ▶ nodes: indicators of a psychological construct
 - ▶ edges: causal connections between indicators
- ▶ network analysis as methodological tool to estimate causal networks

Estimating Cross-sectional Psychological Networks

Data Structure

- ▶ Person X Node-Rating Matrix

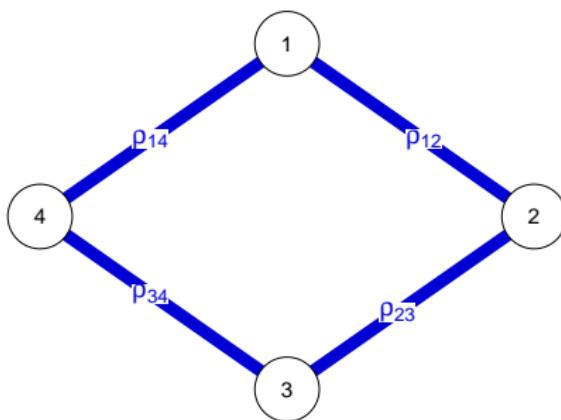
```
#>   Subject Node1 Node2 Node3 Node4  
#> 1      1     3     2     5     1  
#> 2      2     2     1     6     2  
#> 3      3     1     1     4     2  
#> 4      ...   ...   ...   ...   ...  
#> 5      n     3     3     5     4
```

pairwise Markov Random Field Model (pMRF)

- ▶ unique relationships of two nodes

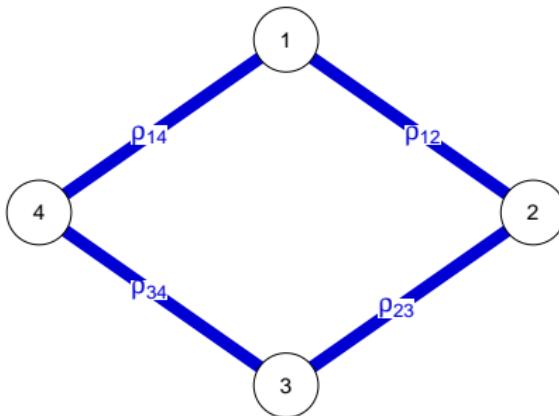
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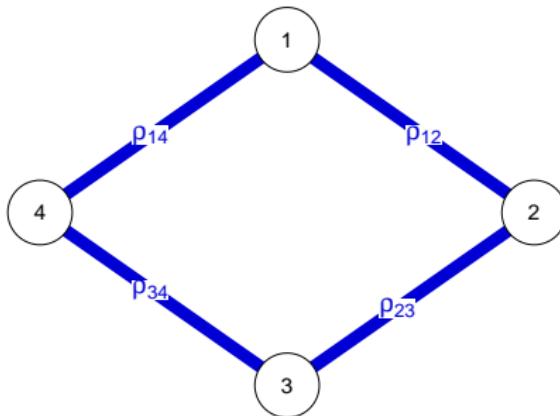
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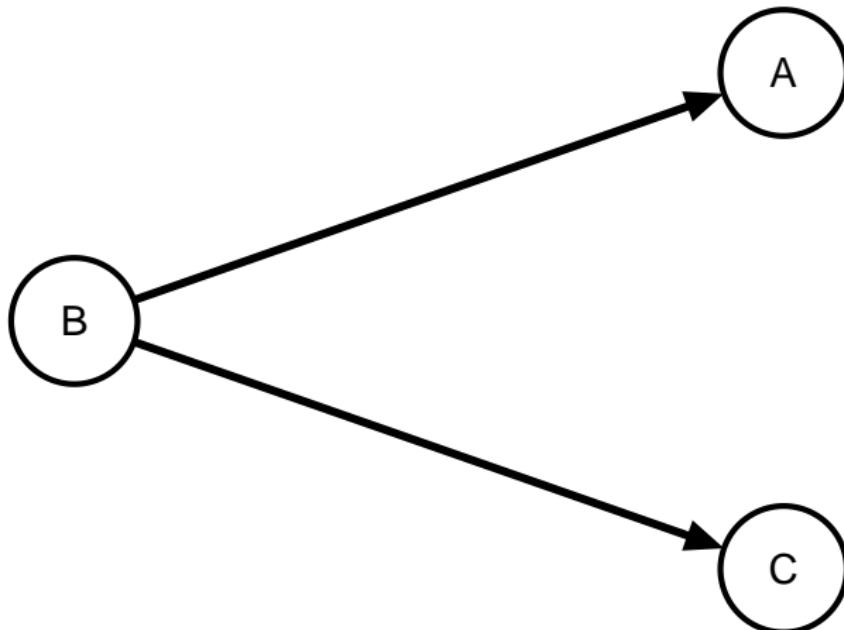
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 - ▶ no edge: e.g. $\text{Node1} \perp\!\!\!\perp \text{Node3} \mid \text{Node2}, \text{Node4}$



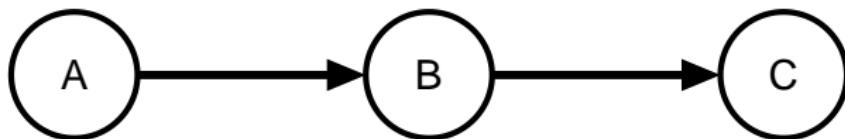
pairwise Markov Random Field Model (pMRF)

- ▶ conditional (in)dependencies imply causal structure
- ▶ three cases → *common cause*
 - ▶ $r(A, C) > 0$ and $A \perp\!\!\!\perp C | B$



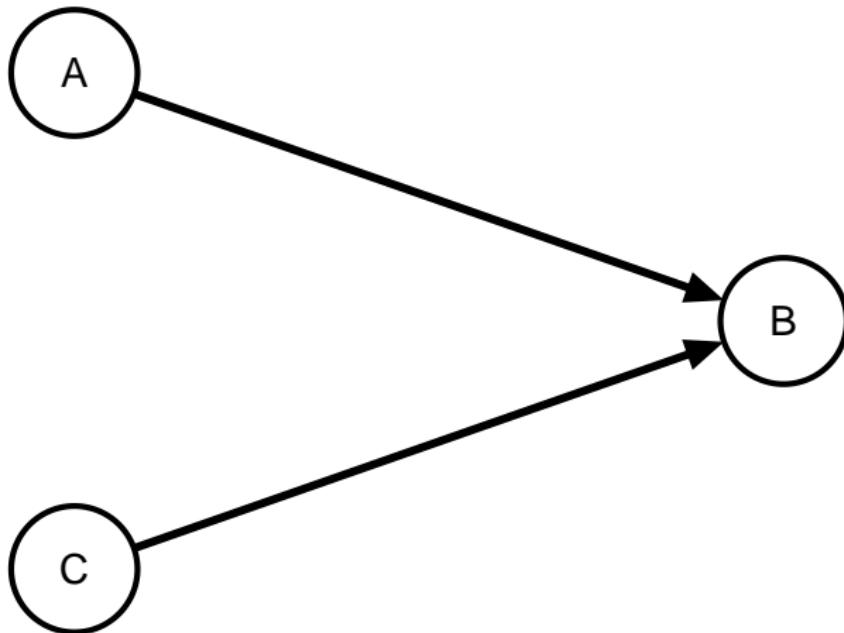
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pairwise Markov Random Field Model (pMRF)

- ▶ conditional (in)dependencies imply causal structure
- ▶ three cases → *collider*
 - ▶ $r(A, C) = 0$ and $A \not\perp\!\!\!\perp C \mid B$



Gaussian Graphical Model

- ▶ pMRF for continuous data

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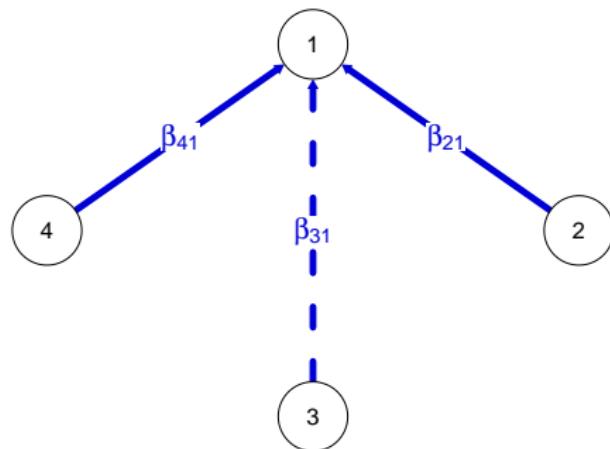
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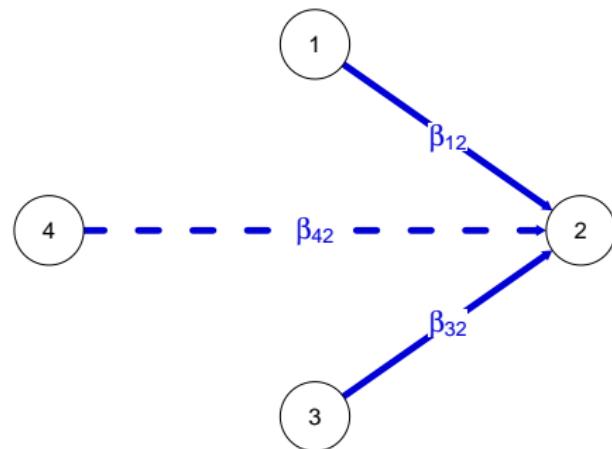
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 3. apply AND or OR rule to determine edge weights

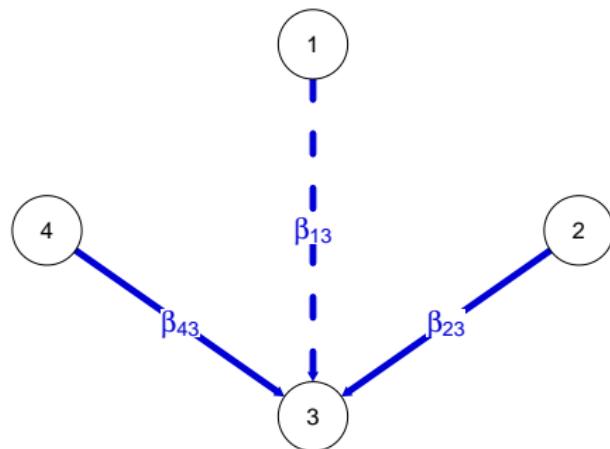
Gaussian Graphical Model – Node-wise Regression



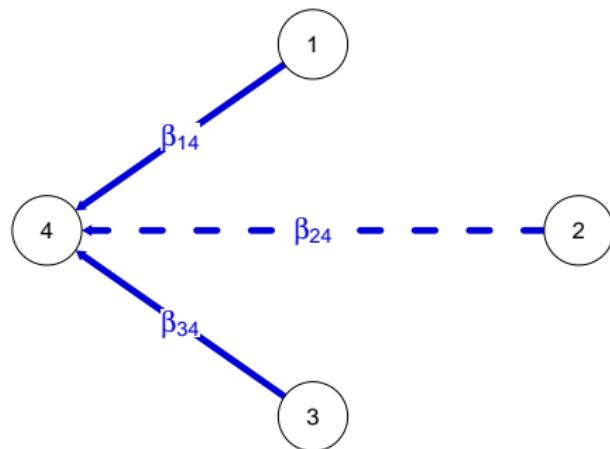
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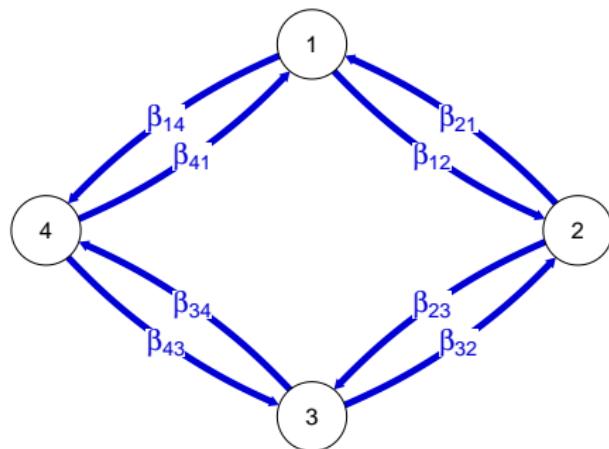
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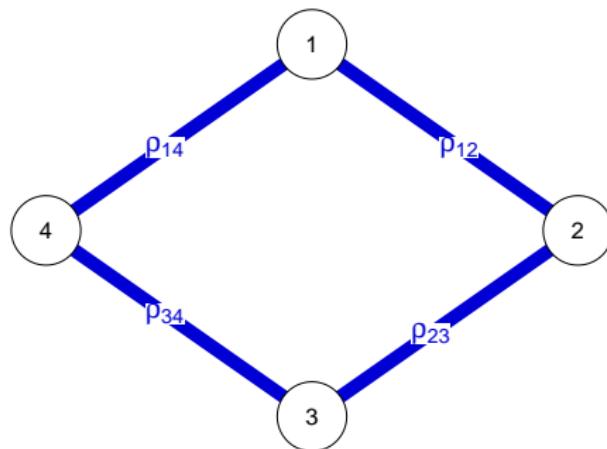
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Model Selection - Regularization

- ▶ method: Least Absolute Shrinkage and Selection Operator (LASSO)

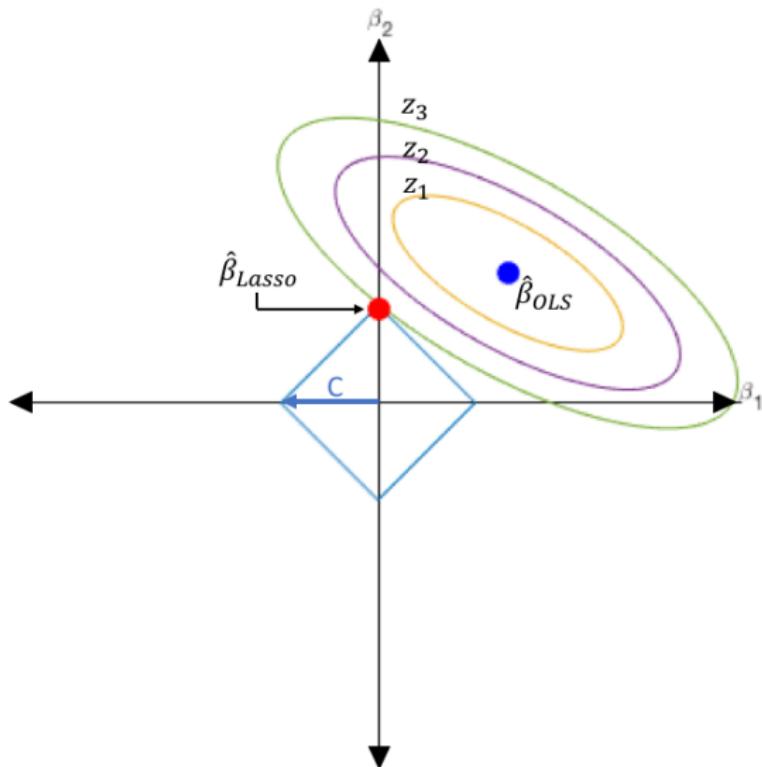
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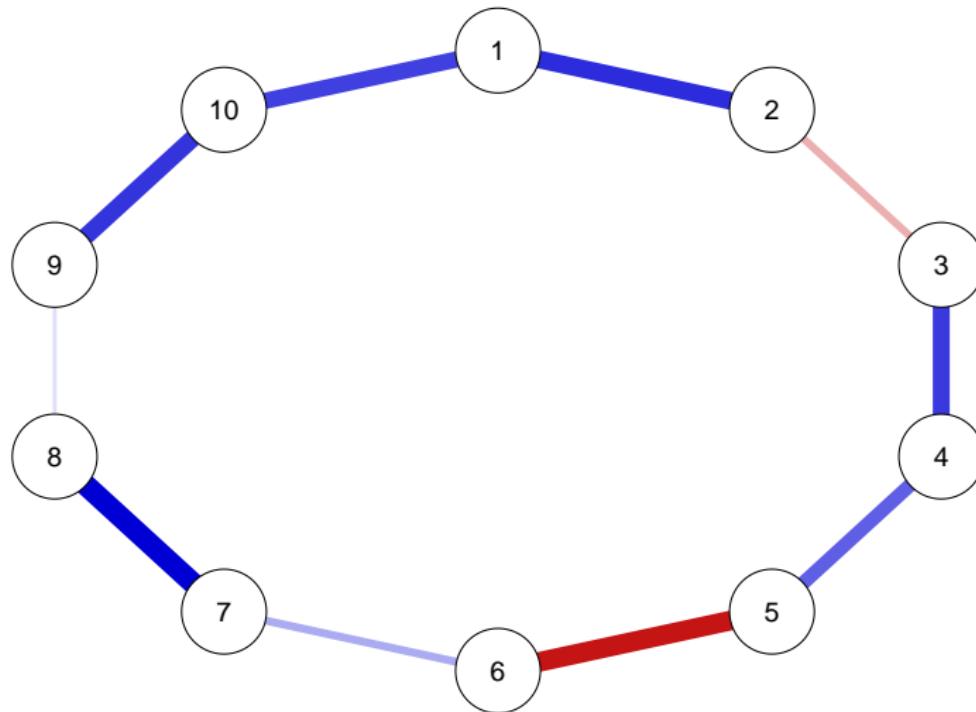
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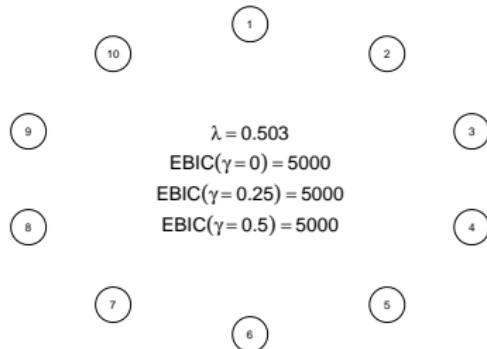
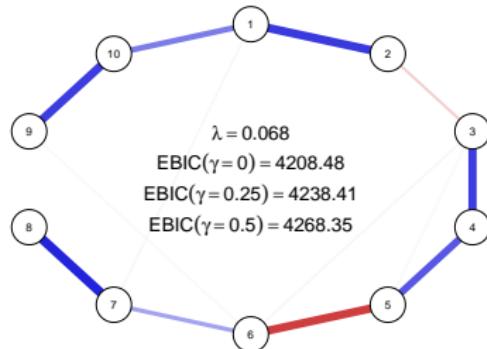
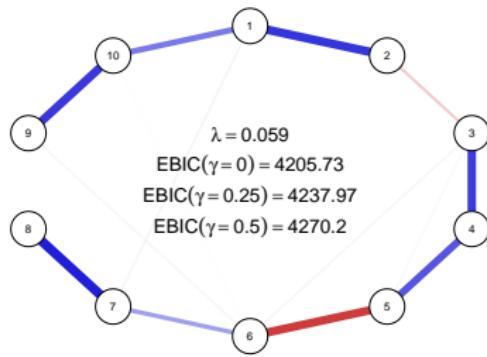
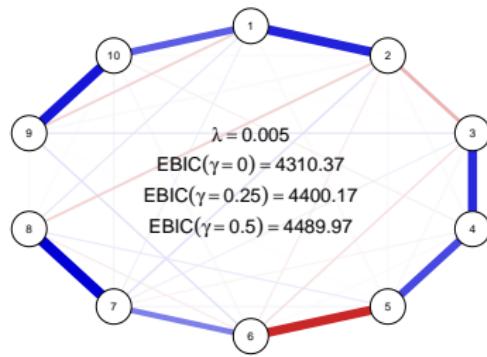
Model Selection - Regularization

- ▶ method: Least Absolute Shrinkage and Selection Operator (LASSO)
 - ▶ limits the size of all edges
 - ▶ sets small edges to exactly zero
 - ▶ varying tuning parameter λ changes sparsity (100 networks)
 - ▶ minimize Extended Bayesian Information Criterion (EBIC)
 - ▶ hyperparameter γ controls EBIC
 - ▶ 0: err on the side of discovery
 - ▶ 0.5: err on the side of caution
 - ▶ typically set 0.25 or 0.5
- ▶ LASSO for partial correlations (gLASSO) and node-wise regression (eLASSO)

Model Selection - Regularization (Example)



Model Selection - Regularization (Example)



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- ▶ disadvantages
 - ▶ poor performance in large sample sizes
 - ▶ relies on assumption of sparsity

Model Selection - Regularization

- ▶ advantages
 - ▶ very fast
 - ▶ high sensitivity
 - ▶ receives network structure also with low sample size
 - ▶ clearer pictures by setting edges to zero
- ▶ disadvantages
 - ▶ poor performance in large sample sizes
 - ▶ relies on assumption of sparsity
 - ▶ leads to biased estimates

Model Selection - What to Choose?

- ▶ no idea
- ▶ check Isvoranu & Epskamp (in press, PM)
- ▶ consider, what you want to do
- ▶ regularization (EBICglasso) is most common

Ising Model

- ▶ pMRF for binary data

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 - ▶ logistic regression

Ising Model

- ▶ pMRF for binary data
- ▶ estimation via node-wise regression
 - ▶ logistic regression
 - ▶ regularization via eLASSO

Network Analysis in R

OSF Files

<https://osf.io/8akru/>

Get Started

- ▶ set working directory

```
setwd("...")
```

- ▶ load packages

```
#R version 4.2.1
## #packages
library(qgraph)           #plotting networks; version 1.9.2
library(bootnet)          #estimating networks; version 1.5
library(psych)             #psych statistics; version 2.2.5
library(CliquePercolation) #network structure and data set; version 0.3.0
library(psychonetrics)     #(confirmatory) network modeling; version 0.10
library(dplyr)              #helpful function; version 1.0.10
```

Load Data

```
#load data - ratings of Obama
data(Obama)
data <- Obama

###Items
##Beliefs - scale from 1 to 5
#Mor - "Is moral"
#Led - "Would provide strong leadership"
#Car - "Really cares about people like you"
#Kno - "Is knowledgeable"
#Int - "Is intelligent"
#Hns - "Is honest"
##Feelings - scale from 1 to 5
#Ang - "Angry"
#Hop - "Hopeful"
#Afr - "Afraid of him"
#Prd - "Proud"
```

Descriptive Statistics

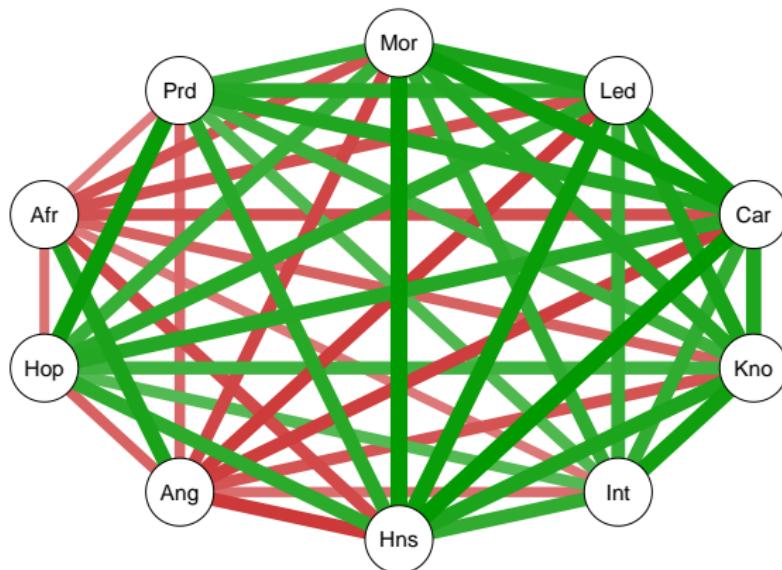
```
describe(data)
#-> several missing values
#-> no obvious skewness or kurtosis
```

Zero-order correlations

```
#compute correlations
correlations <- cor(data, use = "pairwise.complete.obs")
correlations
```

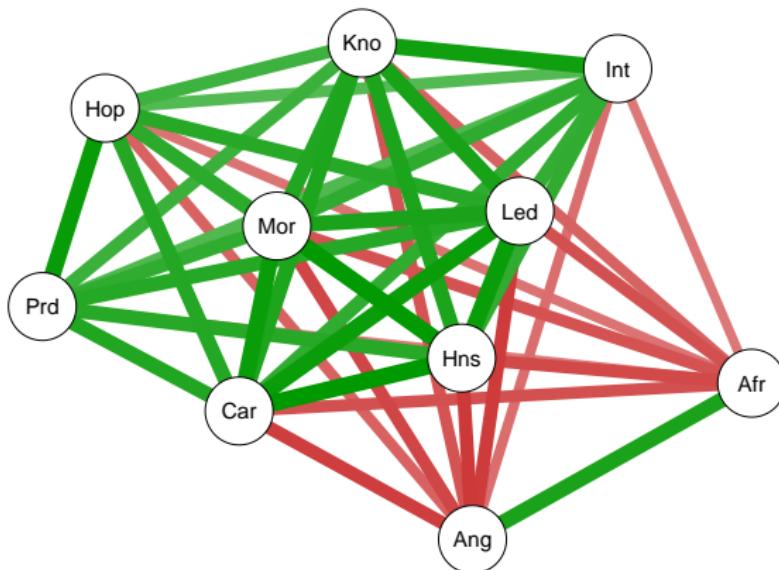
Plotting Correlations with qgraph

```
#plotting correlations with qgraph  
cor_graph <- qgraph(correlations)
```



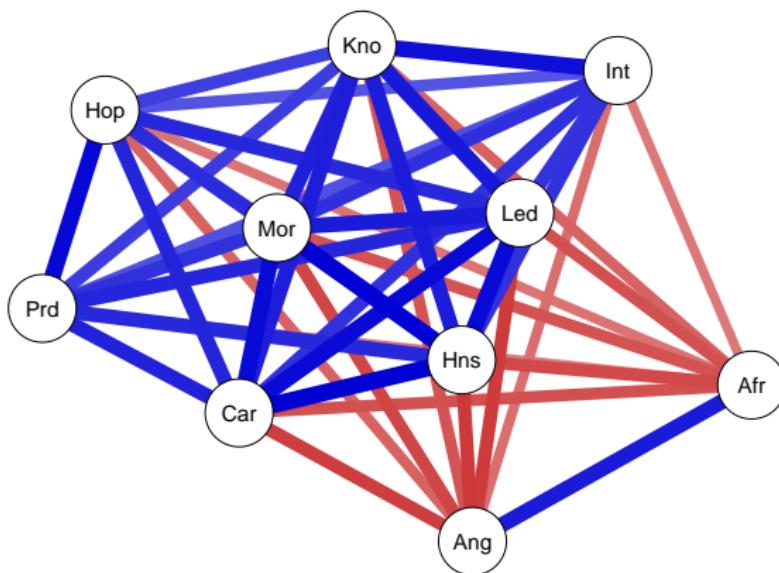
Plotting Correlations with qgraph

```
#+ using Fruchterman-Reingold  
cor_graph <- qgraph(correlations, layout = "spring")
```



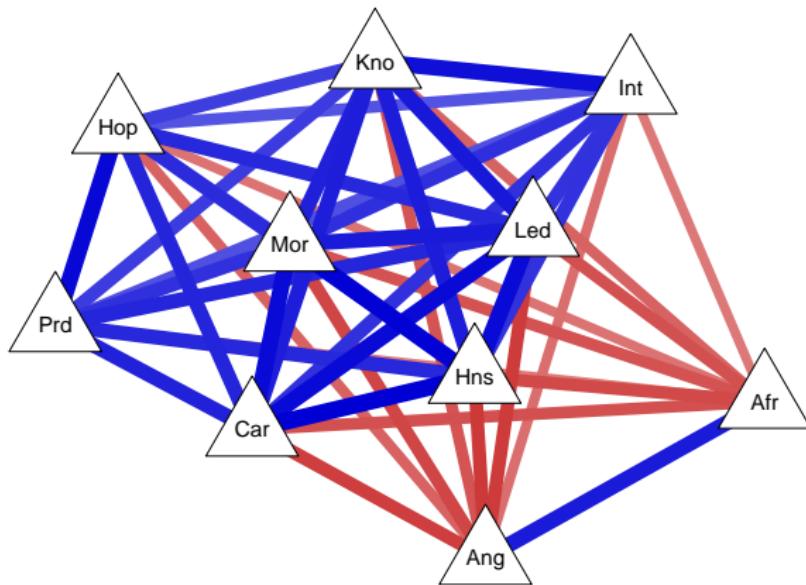
Plotting Correlations with qgraph

```
#+ change for color-blind people  
cor_graph <- qgraph(correlations, layout = "spring",  
                     theme = "colorblind")
```



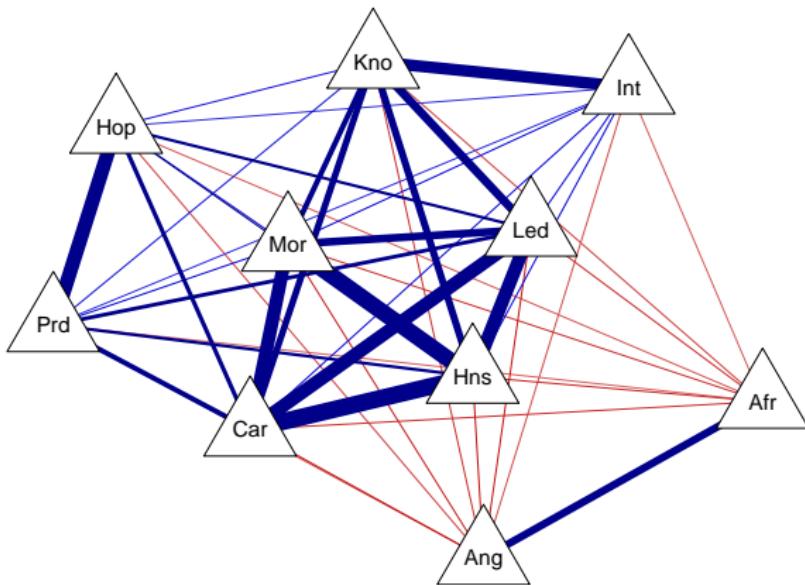
Plotting Correlations with qgraph

```
#+ change shape of nodes  
cor_graph <- qgraph(correlations, layout = "spring",  
                      theme = "colorblind", shape = "triangle")
```



Plotting Correlations with qgraph

```
#+ make correlations with absolute value < .70 less important  
cor_graph <- qgraph(correlations, layout = "spring", theme = "colorblind",  
shape = "triangle", cut = .7)
```



Plotting Correlations with qgraph

```
#for list of features see options in qgraph help page  
?qgraph
```

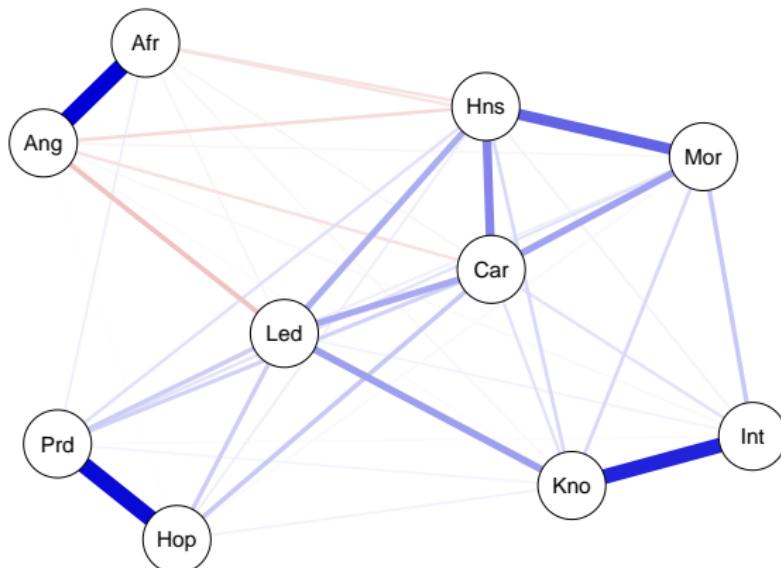
Estimating the Gaussian Graphical Model

```
#estimate regularized partial correlation network
#EBICglasso (gLASSO with EBIC model selection)
#correlations determined via cor
#pairwise deletion of missing values
GGM_net <- estimateNetwork(data, default = "EBICglasso", corMethod = "cor",
                             missing = "pairwise")

#> Warning in EBICglassoCore(S = S, n = n, gamma = gamma, penalize.diagonal =
#> penalize.diagonal, : A dense regularized network was selected (lambda < 0.1 *
#> lambda.max). Recent work indicates a possible drop in specificity. Interpret the
#> presence of the smallest edges with care. Setting threshold = TRUE will enforce
#> higher specificity, at the cost of sensitivity.
```

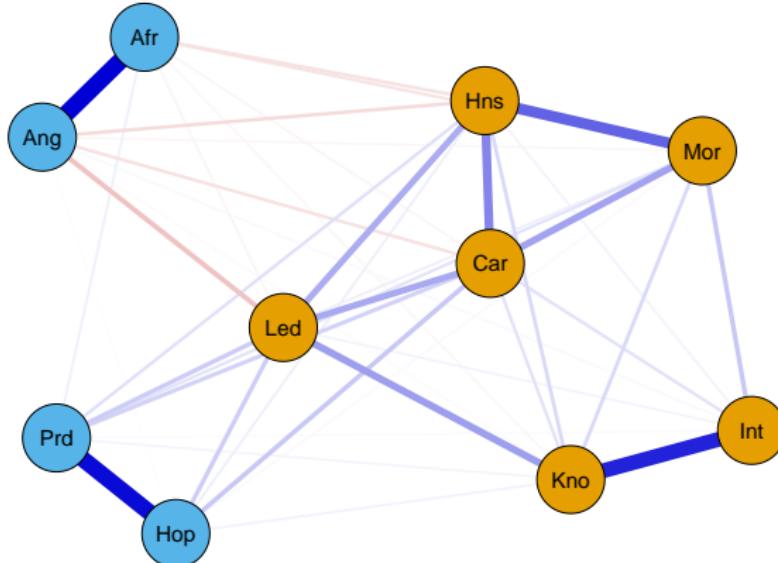
Plotting the Gaussian Graphical Model

```
#plot network with qgraph  
GGM_graph <- plot(GGM_net)
```



Plotting the Gaussian Graphical Model

```
###declare beliefs and feelings separate groups  
groups <- c(rep("Beliefs",6), rep("Feelings",4))  
  
#plot network with groups; no legend  
GGM_graph <- plot(GGM_net, layout = "spring", theme = "colorblind",  
                   groups = groups, legend = FALSE)
```



Information about Gaussian Graphical Model

```
#save layout of the graph  
layout <- GGM_graph$layout  
  
#get weights matrix  
Wmat_GGM <- getWmat(GGM_graph)  
Wmat_GGM
```

Node Centrality

- ▶ (potentially) information about how important a node is

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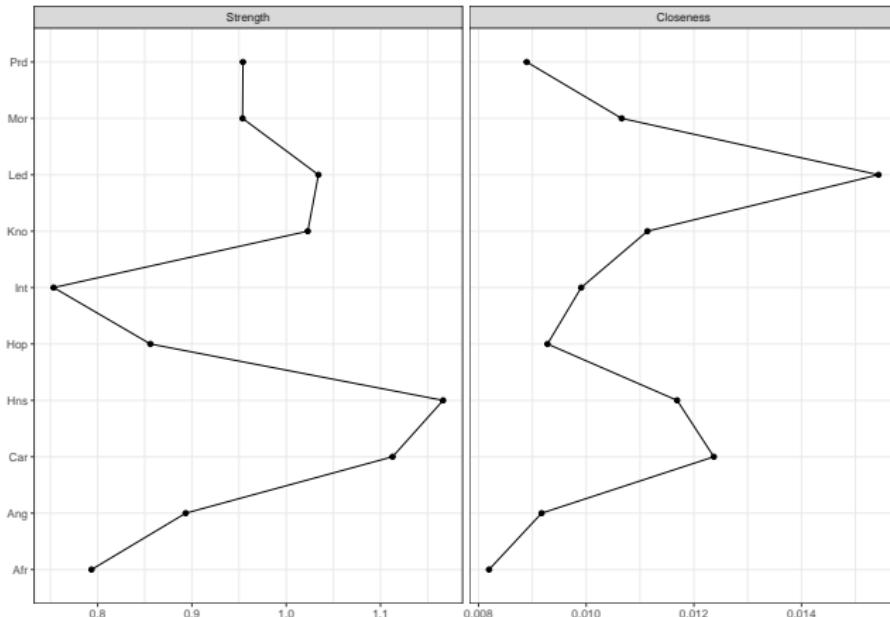
- ▶ (potentially) information about how important a node is
 - ▶ *strength (degree)*: sum of all edge weights
 - ▶ *closeness*: inverse of average shortest path length
 - ▶ ...

Node Centrality

```
#determine values  
cent <- centrality(GGM_net)  
  
#get values  
cent$OutDegree  
cent$Closeness
```

Node Centrality

```
#plot values  
centralityPlot(GGM_net, scale = "raw",  
                include = c("Strength", "Closeness"))
```



Network Stability and Difference Tests

- ▶ edges in regularized networks are significant

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 - ▶ case-dropping bootstrap: successively drop cases; check parameter consistency
 - ▶ for centrality indices

Network Stability and Difference Tests

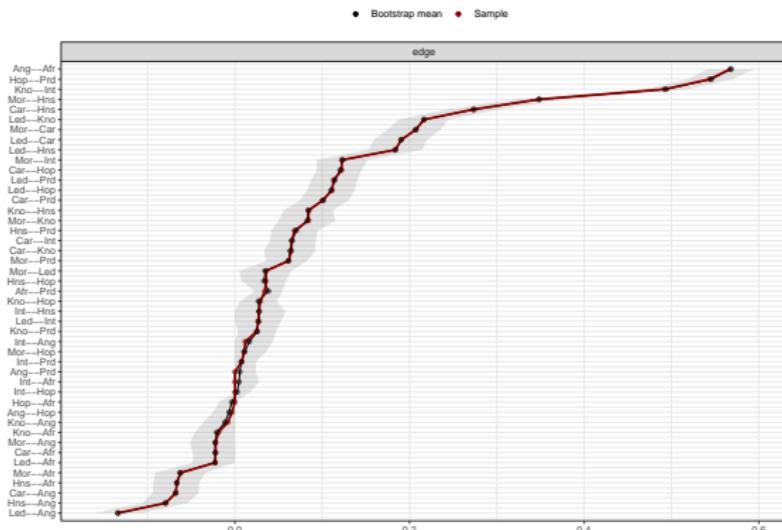
```
#non-parametric bootstrap
#-> for edge stability and edge as well as centrality difference tests
#run bootstrap
set.seed(4186)
boot1 <- bootnet(GGM_net, statistics = c("edge","Strength","Closeness"),
                  nboots = 1000, nCores = 2, type = "nonparametric")
save(boot1, file = "boot_edges.RData") #save results

#case-dropping bootstrap
#-> for centrality stability
#run bootstrap
set.seed(4186)
boot2 <- bootnet(GGM_net, statistics = c("Strength","Closeness"),
                  nboots = 1000, nCores = 2, type = "case")
save(boot2, file = "boot_centrality.RData") #save results
```

Network Stability and Difference Tests

```
load("boot_edges.RData")
load("boot_centrality.RData")

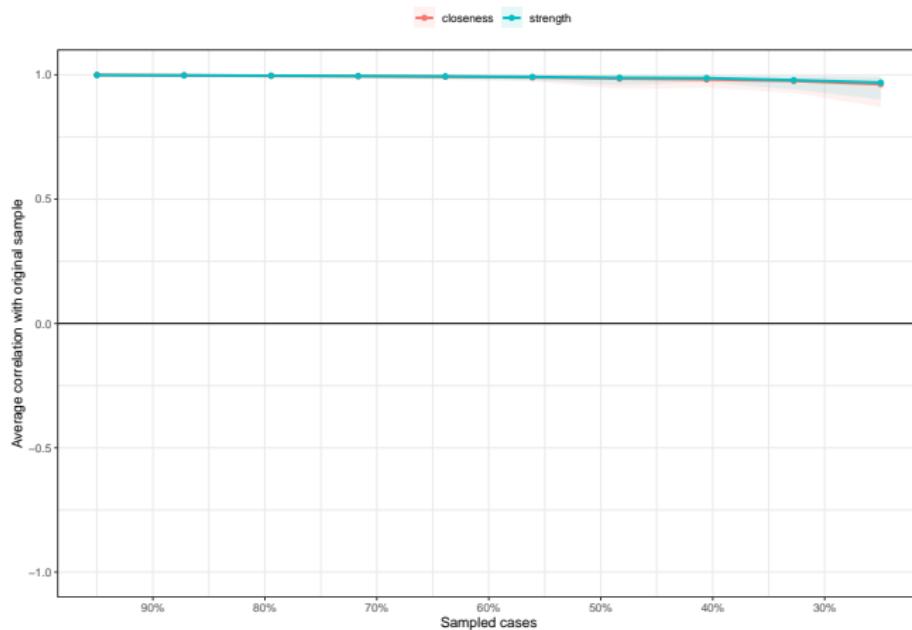
#plot edge CIs
plot(boot1, statistics = "edge", labels = TRUE, order = "sample")
```



```
#plot edge CIs + make labels visible by creating large pdf
# pdf("edge_stability.pdf", height = 10)
# plot(boot1, statistics = "edge", labels = TRUE, order = "sample")
# dev.off()
```

Network Stability and Difference Tests

```
#plot centrality stability  
plot(boot2, statistics = c("Strength","Closeness"))
```



Network Stability and Difference Tests

```
#check stability of centrality indices  
corStability(boot2)
```

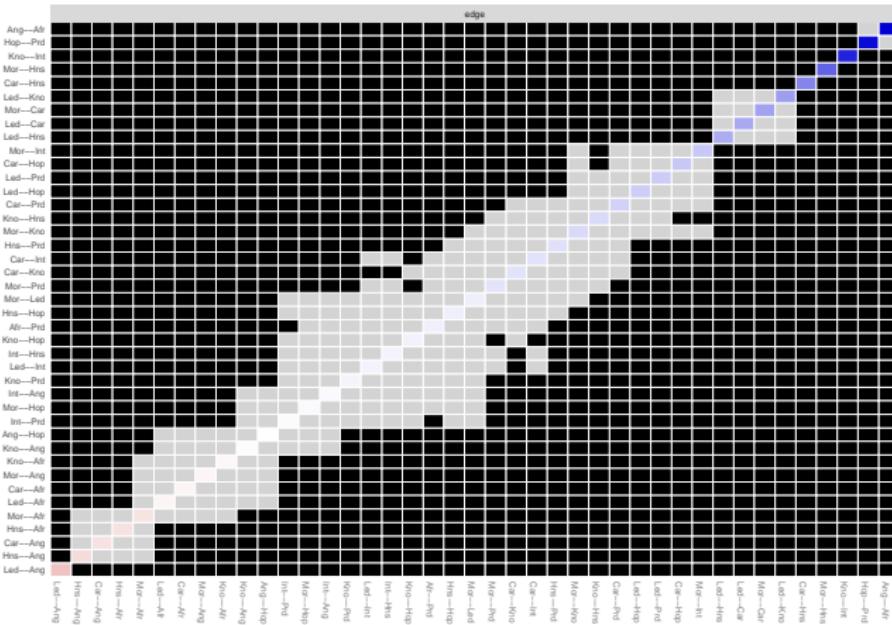
```
#> === Correlation Stability Analysis ===  
#>  
#> Sampling levels tested:  
#>   nPerson Drop%  n  
#> 1    1478  75.0 104  
#> 2    1938  67.2  95  
#> 3    2398  59.5 114  
#> 4    2858  51.7 102  
#> 5    3318  43.9  86  
#> 6    3778  36.1 111  
#> 7    4238  28.3  93  
#> 8    4698  20.6  96  
#> 9    5158  12.8 102  
#> 10   5618   5.0  97  
#>  
#> Maximum drop proportions to retain correlation of 0.7 in at least 95% of the samples:  
#>  
#> closeness: 0.75 (CS-coefficient is highest level tested)  
#>   - For more accuracy, run bootnet(..., caseMin = 0.672, caseMax = 1)  
#>  
#> strength: 0.75 (CS-coefficient is highest level tested)  
#>   - For more accuracy, run bootnet(..., caseMin = 0.672, caseMax = 1)  
#>  
#> Accuracy can also be increased by increasing both 'nBoots' and 'caseN'.
```

```
#-> strength and closeness can be interpreted
```

Network Stability and Difference Tests

```
#plot edge weights difference test
plot(boot1, statistics = "edge", plot = "difference",
      onlyNonZero = TRUE, order = "sample")
```

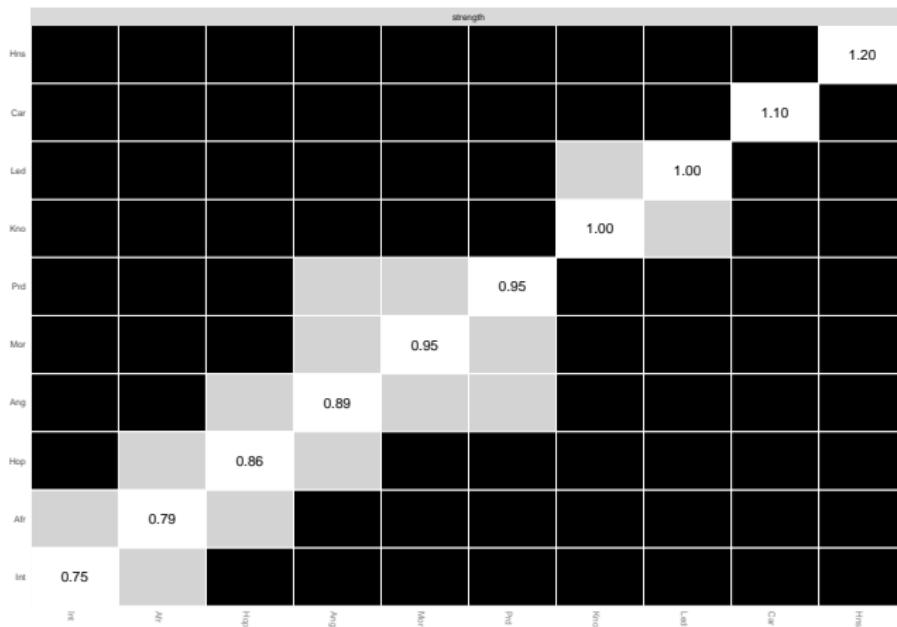
```
#> Expected significance level given number of bootstrap samples is approximately: 0.05
```



Network Stability and Difference Tests

```
#plot strength difference test
plot(boot1, statistics = "strength", plot = "difference",
      order = "sample")
```

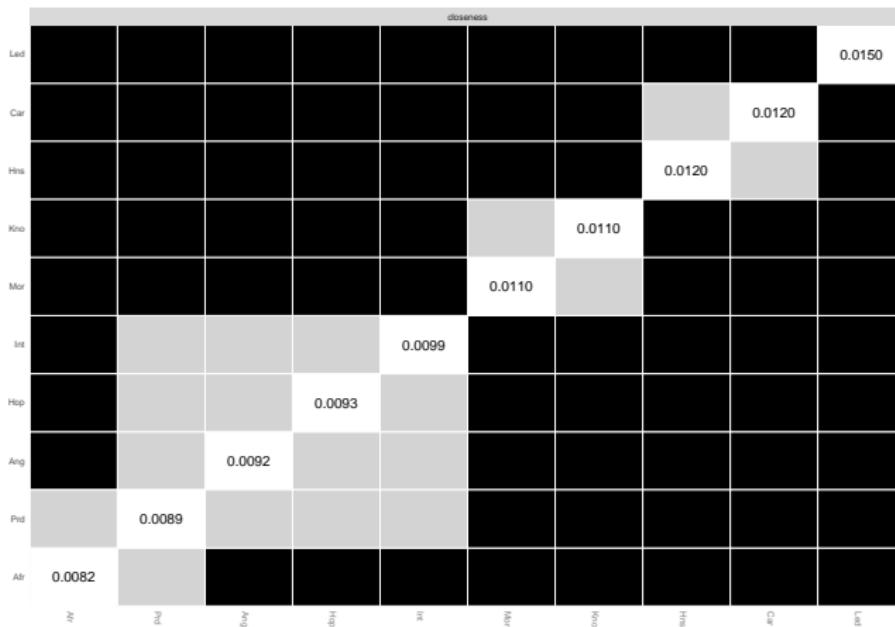
```
#> Expected significance level given number of bootstrap samples is approximately: 0.05
```



Network Stability and Difference Tests

```
#plot closeness difference test
plot(boot1, statistics = "closeness", plot = "difference",
      order = "sample")
```

```
#> Expected significance level given number of bootstrap samples is approximately: 0.05
```



Estimating the Ising Model

```
#can be estimated via estimateNetwork
#variables automatically binarized at median
#here, feeling variables better binarized at 2 because 1 indicates "no, I never felt this"
split <- describe(data)$median
split[which(groups == "Feelings")] <- 2

#estimate regularized logistic node-wise regression network
#define where to binarize variables
#eLASSO (LASSO with EBIC model selection)
#listwise deletion of missing values (pairwise not possible for regressions)
Ising_net <- estimateNetwork(data, default = "IsingFit", split = split,
                               missing = "listwise", rule = "OR")

##> Estimating Network. Using package::function:
##>   - IsingFit::IsingFit for network computation
##>   - Using glmnet::glmnet

##> Warning in bootnet::binarize(data, split = split, verbose = verbose): Splitting
##> data by 3Splitting data by 3Splitting data by 3Splitting data by 4Splitting data
##> by 4Splitting data by 3Splitting data by 2Splitting data by 2Splitting data by
##> 2Splitting data by 2
```

Information about the Ising Model

```
#extract thresholds
thresholds <- Ising_net$intercepts
thresholds

#extract weights matrix
Wmat_Ising <- getWmat(Ising_net)
Wmat_Ising
```

Comparing the Gaussian Graphical Model and Ising Model

```
#correlating weights matrices
cor.test(Wmat_GGM[upper.tri(Wmat_GGM)], Wmat_Ising[upper.tri(Wmat_Ising)])
```



```
#>
#> Pearson's product-moment correlation
#>
#> data: Wmat_GGM[upper.tri(Wmat_GGM)] and Wmat_Ising[upper.tri(Wmat_Ising)]
#> t = 16.579, df = 43, p-value < 2.2e-16
#> alternative hypothesis: true correlation is not equal to 0
#> 95 percent confidence interval:
#> 0.8752870 0.9610981
#> sample estimates:
#> cor
#> 0.929904
```

Other model selection

```
####thresholding with significance (bootnet)
GGM_net_thres <- estimateNetwork(data, default = "pcor",
                                    threshold = "sig", alpha = .01)
```

```
#> Estimating Network. Using package::function:
#>   - qgraph::qgraph(..., graph = 'pcor') for network computation
#>   - psych::corr.p for significance thresholding
```

```
plot(GGM_net_thres, layout = layout)
```

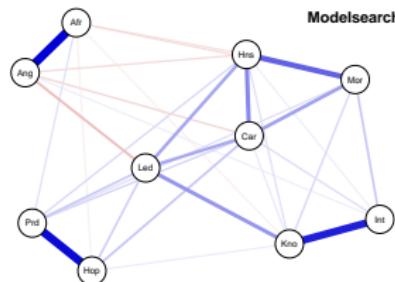
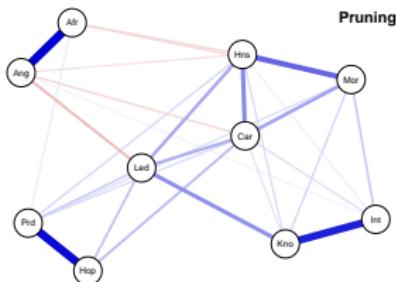
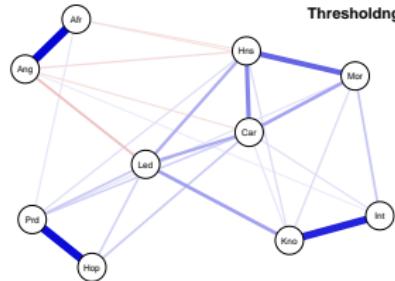
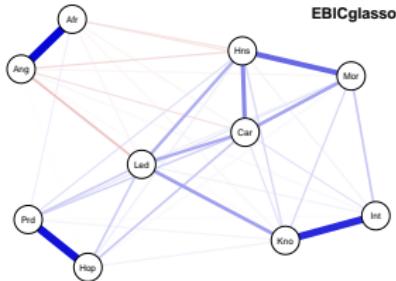
```
####pruning (psychonetrics)
GGM_net_prune <- ggm(data) %>% runmodel %>% prune(alpha = .01)
Wmat_GGM_prune <- getmatrix(GGM_net_prune, "omega")
qgraph(Wmat_GGM_prune, theme = "colorblind",
       layout = layout, labels = names(data))
```

```
####model search with modelsearch (psychonetrics)
GGM_net_modelsearch <- ggm(data) %>% runmodel %>% prune %>% modelsearch
Wmat_GGM_modelsearch <- getmatrix(GGM_net_modelsearch, "omega")
qgraph(Wmat_GGM_modelsearch, theme = "colorblind",
       layout = layout, labels = names(data))
```

Other model selection

```
####compare networks
#-> get maximum edge across all networks
Wmat_GGM_thres <- getWmat(GGM_net_thres)
max_edge <- max(Wmat_GGM, Wmat_GGM_thres,
                  Wmat_GGM_prune, Wmat_GGM_modelsearch)
#-> plot networks next to each other
layout(matrix(c(1,2,
               3,4), nrow = 2, ncol = 2, byrow = TRUE))
plot(GGM_net, maximum = max_edge)
title("EBICglasso", adj = 1)
plot(GGM_net_thres, layout = layout, maximum = max_edge)
title("Thresholdng", adj = 1)
qgraph(Wmat_GGM_prune, theme = "colorblind",
       layout = layout, labels = names(data),
       maximum = max_edge)
title("Pruning", adj = 1)
qgraph(Wmat_GGM_modelsearch, theme = "colorblind",
       layout = layout, labels = names(data),
       maximum = max_edge)
title("Modelsearch", adj = 1)
```

Other model selection



Other developments in network analysis in R

See also...

- ▶ categorical variables (*mgm*; Haslbeck & Waldorp, 2020, JSS)
- ▶ time-series data (idiosyncratic and group-level; Epskamp et al., 2018, MBR)
- ▶ latent variables in networks (Epskamp et al., 2017, Psychometrika)
- ▶ moderated network models (Haslbeck et al., 2021, MBR)
- ▶ network comparison (*NCT*; Van Borkulo et al., in press, PM)
- ▶ interpretable plots (Jones et al., 2018, Frontiers)
- ▶ Bayesian estimation (Williams, 2021, MBR)
- ▶ confirmatory network modeling (Kan et al., 2020, JI)
- ▶ networks for panel data (Epskamp, 2020, P)
- ▶ model selection recommendations (Isvoranu & Epskamp, in press, PM)
- ▶ ...

Summary for Network Analysis

Summary

- ▶ psychological networks can be estimated via pairwise Markov Random Field Models
 - ▶ continuous data: Gaussian Graphical Model
 - ▶ binary data: Ising Model
- ▶ estimation via model selection
- ▶ central nodes can be structurally important
- ▶ stability of network parameters should be checked
- ▶ *bootnet*, *qgraph*, or *psychonetrics* can estimate and plot networks in R

Thank you very much for your attention!