

Third function:

$$y = z_1 \text{ OR } z_2$$

The truth table for function  $y$

$$y_{in} = z_1 v_1 + z_2 v_2$$

Assume the weights are initialized to

$$v_1 = v_2 = 1$$

$x_1$	$x_2$	$y$	$z_1$	$z_2$
0	0	0	0	0
0	1	1	0	1
1	0	1	1	0
1	1	0	0	0

Calculate the net inputs

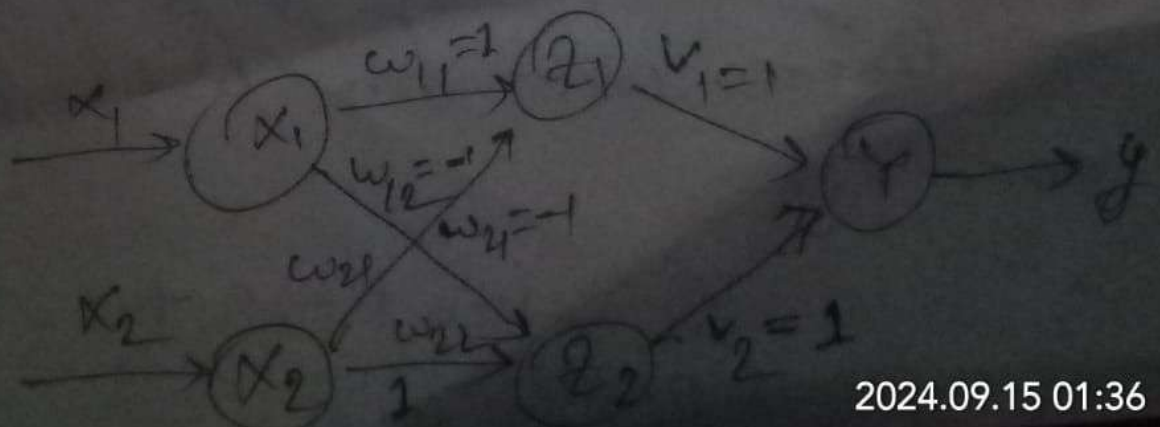
$$(0,0) \quad y_{in} = 0 \times 1 + 0 \times 1 = 0$$

$$(0,1) \quad y_{in} = 0 \times 0 + 1 \times 1 = 1$$

$$(1,0) \quad y_{in} = 1 \times 1 + 0 \times 1 = 1$$

$$(1,1) \quad y_{in} = 0 \times 1 + 0 \times 1 = 0$$

$$y = \begin{cases} 1 & \text{if } y_{in} \geq \theta \\ 0 & \text{if } y_{in} < \theta \end{cases}$$

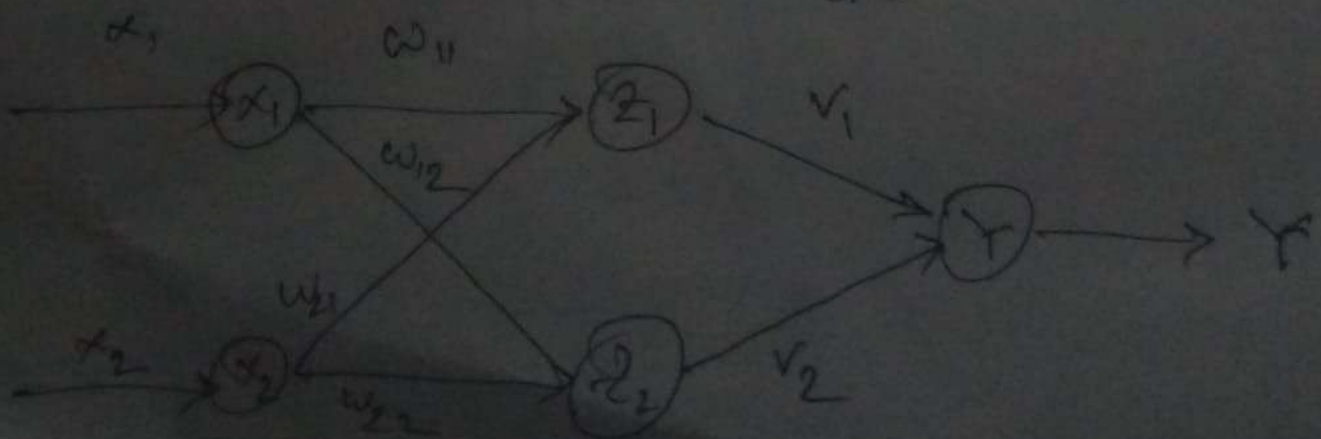


## lab-2 Implement XOR function using McCulloch-Pitts neuron.

- Consider the truth table for XOR function.
- The M-P neuron has no particular training algorithm.
- In M-P neuron, only analysis is being performed.
- XOR function cannot be represented by simple and single logic function; it is represented as

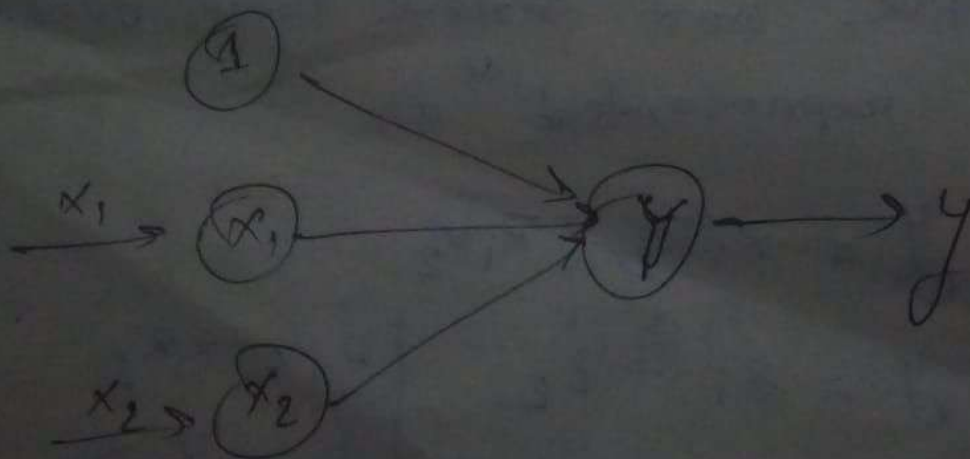
$$y = x_1 \bar{x}_2 + \bar{x}_1 x_2$$

$$\begin{aligned} y &= z_1 + z_2 \\ &= z_1 \text{ OR } z_2 \end{aligned} \quad \left| \begin{array}{l} z_1 = x_1 \bar{x}_2 \\ z_2 = \bar{x}_1 x_2 \end{array} \right.$$

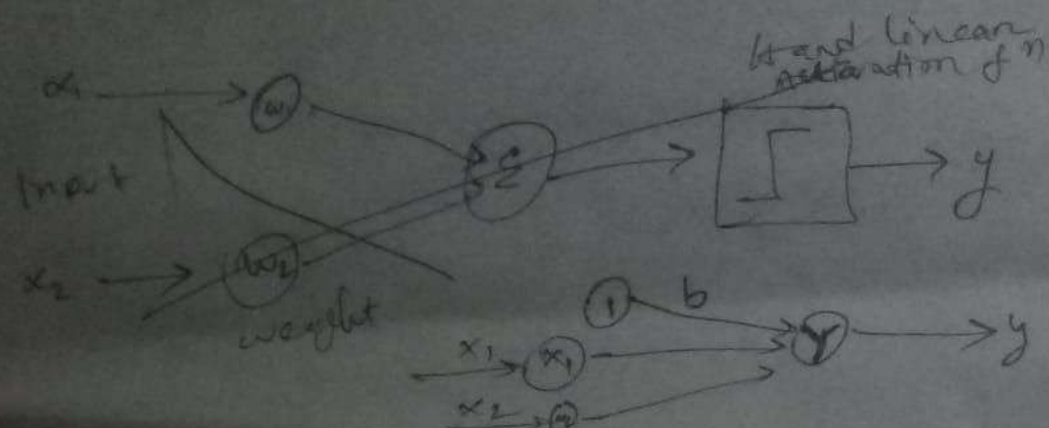


Epoch = 2

$x_1$	$x_2$	$b$	$y_{in}$	$y$	$\Delta w_1$	$\Delta w_2$	$b$	$w_1$	$w_2$	$w_3$
1	1	1	1	1	0	0	0	1	1	-1
1	-1	-1	-1	-1	0	0	0	1	1	-1
-1	1	-1	-1	-1	0	0	0	1	1	-1
-1	-1	-1	-1	-1	0	0	0	1	1	-1







### And Gate Perceptron

$$Y_{in} = b + x_1 w_1 + x_2 w_2$$

$$y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} > 0 \\ 0 & \text{if } y_{in} = 0 \\ -1 & \text{if } y_{in} < 0 \end{cases}$$

learning

$$\Delta w_1 = \alpha (t - y) x_1$$

input

target

$$y_{in} = b + \sum_{i=1}^n x_i w_i$$

$$\Delta w_2 = \alpha (t - y) x_2$$

$$\Delta b = \alpha (t - y)$$

$$\alpha = 1$$

if  $y \neq t$ , then

$$w(\text{new}) = w(\text{old}) + \alpha \Delta w$$

else  $w(\text{new}) = w(\text{old})$

input		target	Net input ( $y_{in}$ )	Calculated output ( $y$ )	Weight changes			Weights		
$x_1$	$x_2$				$\Delta w_1$	$\Delta w_2$	$\Delta b$	$w_1$	$w_2$	$b$
1	1	1	0	0	1	1	1	1	2	1
1	-1	-1	1	1	-1	1	-1	0	2	0
-1	1	-1	2	1	1	-1	-1	1	2	-1
-1	-1	-1	-3	-1	0	0	0	1	1	-1

If the  $\theta = 2$ , then the neuron fires

Hence  $w_{11} = 1$   $w_{21} = -1$

for  $z_2 = x_1 \times x_2$

consider  $w_{12} = w_{22} = 1$

calculate the net inputs

$$(0,0)_{zin} = 0 \times 1 + 0 \times 1 = 0$$

$$(0,1)_{zin} = 0 \times 1 + 1 \times 1 = 1$$

$$(1,0)_{zin} = 1 \times 1 + 0 \times 1 = 1$$

$$(1,1)_{zin} = 1 \times 1 + 1 \times 1 = 2$$

Hence, it is not possible to obtain function  $z_2$  using these weights

so we update the weight

$$w_{12} = -1, \quad w_{22} = 1$$

calculate the net inputs

$$(0,0)_{zin} = (0 \times -1) + 0 \times 1 = 0$$

$$(0,1)_{zin} = (0 \times -1) + 1 \times 1 = 1$$

$$(1,0)_{zin} = -1 + 0 = -1$$

$$(1,1)_{zin} = -1 + 1 = 0$$

$x_1$	$x_2$	$z_2$
0	0	0
0	1	1
1	0	0
1	1	0

$$f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} \geq \theta \\ 0 & \text{if } y_{in} < \theta \end{cases}$$

Hence

$$w_{12} = -1,$$

$$w_{22} = 1$$



Our target values are 0.01 and 0.99 our  $Y_1$  and  $Y_2$  value is not matched with our target values  $T_1$  and  $T_2$ . So find the error

$$\begin{aligned} E_{\text{total}} &= \sum \frac{1}{2} (\text{target} - \text{output})^2 \\ &= \frac{1}{2} (0.01 - 0.7513)^2 + \frac{1}{2} (0.99 - 0.7729)^2 \\ &= 0.2983711 \end{aligned}$$

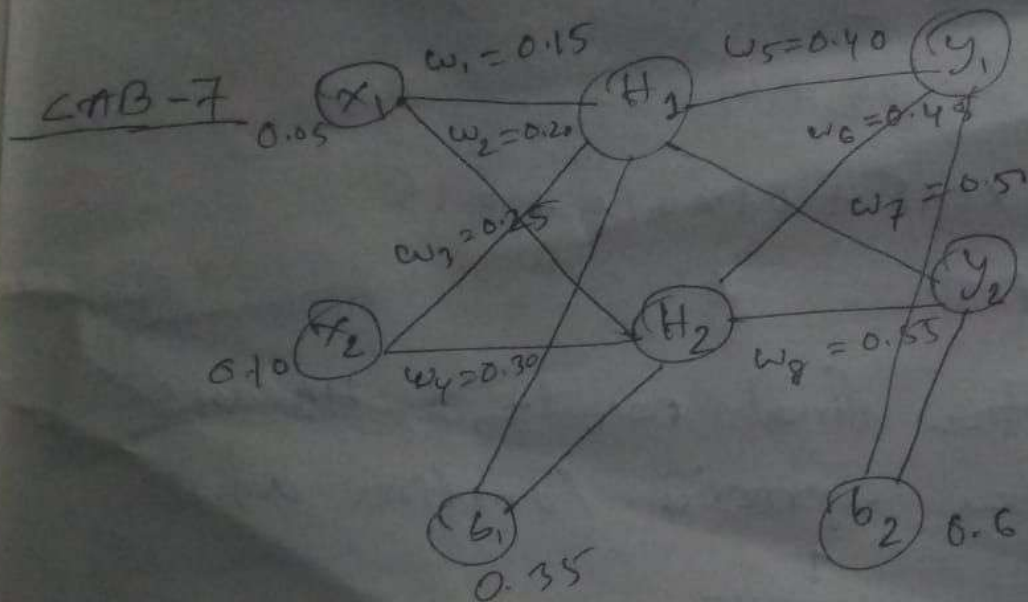
Backpass the output layer

$$\text{Error} = \frac{\partial E_{\text{total}}}{\partial w}$$

• We perform backward process to find  
Consider the last weight  $w_5$

Although there are many ways to define this error, one common measure is

$$E(\vec{a}) = \frac{1}{2} \sum_{d \in D} (f_d - o_d)^2$$



Here: Input values

$$x_1 = 0.05 \quad x_2 = 0.10$$

initial weight

$$\left\{ \begin{array}{ll} w_1 = 0.15 & w_5 = 0.40 \\ w_2 = 0.20 & w_6 = 0.45 \\ w_3 = 0.25 & w_7 = 0.50 \\ w_4 = 0.30 & w_8 = 0.55 \end{array} \right.$$

Bias values  $\rightarrow \tau_1 = 0.01$

$$\tau_2 = 0.99$$



অতিরিক্ত খাতা

পরীক্ষার্থী কর্তৃক পূরণীয়

কক্ষ পরিদর্শকের স্বাক্ষর ও তারিখ

পরীক্ষা

সাল

বিষয়/কোর্সের নাম :

Mr. Omar Faruk

সেমিস্টার/বর্ষ :

প্রশ্নপত্র কোড / বিষয় কোড :

পরীক্ষার তারিখ :

সকাল/বিকাল

(এ স্থান হতে উত্তর লেখা আরম্ভ করতে হবে)

Lab → 4

	Area	bedrooms	Price
1	2600	3	550000
2	3000	4	565000
3	3200	3	610000
4	3600	3	595000
5	4000	5	760000
6	4100	6	810000

machine learning model

$$= w_1 \times \text{area} + w_2 \times \text{bedrooms} + \text{bias}$$

$$w_1 = w_2 = b = 1$$

for first :  $\text{Price} = 1 \times 2600 + 3 \times 1 + 1$   
 $= 2604$

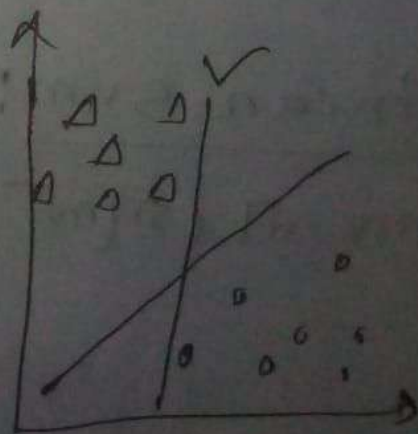
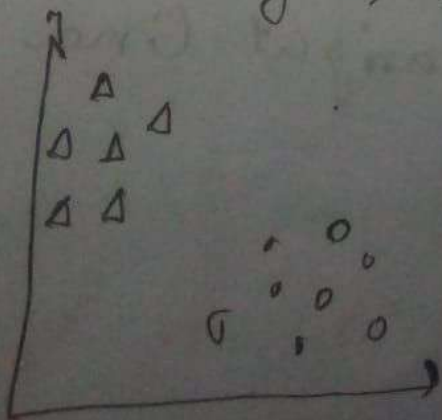
predict value is  $= 550000$

error =  $(\text{Price} - \text{predict}) = (2604 - 550000)$



Support Vector machine:- Support Vector machine or SVM is one of the most popular supervised learning algorithms, which is used for classification as well as regression problems.

- However, primarily, it is used for classification problems in ML.
- The goal of the SVM algorithm is to create the best line or decision boundary that can segregate  $n$ -dimensional space into classes so that we can easily put the new data point in the correct category in the future.
- The best boundary is known as the hyperplane of SVM.



• first function  $z_1 = x_1 \bar{x}_2$

• The Fourth table for function  $z_1$

Assume the weights are initialized to  
 $w_{11} = w_{21} = 1$

calculate the net inputs

$$(0,0) z_{in} = 0 \times 1 + 0 \times 1 = 0$$

$$(0,1) z_{in} = 0 \times 1 + 1 \times 1 = 1$$

$$(1,0) z_{in} = 1 \times 1 + 0 \times 1 = 1$$

$$(1,1) z_{in} = 1 \times 1 + 1 \times 1 = 2$$

$$f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} \geq \theta \\ 0 & \text{if } y_{in} < \theta \end{cases}$$

Activation function

Hence, it is not possible to obtain function  $z_1$  using these weight

we assign a new weight

$$w_{11} = 1 \quad ; \quad w_{21} = -1$$

$x_2$	$x_1$	$z_1$
0	0	0
0	1	0
1	0	1
1	1	0

Calculate the net inputs

$$(0,0) z_{in} = 0 \times 1 + 0 \times (-1) = 0$$

$$(0,1) z_{in} = 0 \times 1 + 1 \times (-1) = -1$$

$$(1,0) z_{in} = 1 \times 1 + 0 \times (-1) = 1$$

$$(1,1) z_{in} = 1 \times 1 + 1 \times (-1) = 0$$



Forward pass: Now, we first calculate the values  $H_1$  and  $H_2$  by a forward pass.

To find the value of  $H_1$  we first multiply the input value from the weight as

$$\begin{aligned} H_1 &= x_1 w_1 + x_2 w_2 + b_1 \\ &= 0.05 \times 0.15 + 0.1 \times 0.20 + 0.35 \\ &= 0.3775 \end{aligned}$$

To calculate the final result of  $H_1$ , we performed the sigmoid function as

$$\begin{aligned} H_{1 \text{ final}} &= \frac{1}{1 + \frac{1}{e^{H_1}}} \\ &= 0.593269992 \end{aligned}$$

We will calculate the value of  $H_2$  in the same way as  $H_1$

$$\begin{aligned} H_2 &= x_1 w_3 + x_2 w_4 + b_1 \\ &= 0.395 \end{aligned}$$

To calculate the final result of  $H_2$ , we performed the sigmoid function

$$\text{total error} = \text{error}_1 + \text{error}_2 + \dots + \text{error}_n$$

$$\text{Mean Squared Error} = \frac{\text{Total Error}}{n}$$

$$\text{error}_2 = (3005 - 56500)^2 = 3.1583838 \times 10^{11}$$

$$\text{error}_3 = (3204 - 61000)^2 = 3.682010956 \times 10^{11}$$

$$\text{error}_4 = (3604 - 59500)^2 = 3.497492288 \times 10^{11}$$

$$\text{error}_5 = (4006 - 76000)^2 = 5.71526928 \times 10^{11}$$

$$\text{error}_6 = (4106 - 81000)^2 = 6.494635792 \times 10^{11}$$

$$\text{Mean Squared Error (MSE)} = \frac{\text{Total Error}}{n}$$

$$= 3.75796575 \times 10^{11}$$

$$w_1 = w_1 - \text{learning rate} * \frac{\partial (\text{MSE})}{\partial w_1} = 1 - (-5) = 51$$

$$w_2 = w_2 - \text{learning rate} * \frac{\partial (\text{MSE})}{\partial w_2} = 1 - (-8) = 9$$

$$b = b - \text{learning rate} * \frac{\partial (\text{MSE})}{\partial b} = 1 - (20000) = 20001$$

22015 6m70-





# জাতীয় বিশ্ববিদ্যালয়

ক্রমিক নং : .....

02421218553

অতিরিক্ত উত্তরপত্র

- ১। পরীক্ষার নাম : .....
- ২। বিষয় : .....
- ৩। কোর্স/পত্র কোড : .....
- ৪। বিষয়ের শিরোনাম : .....
- ৫। তারিখ : .....
- ৬। ইনভিজিলেটরের স্বাক্ষর ও তারিখ : .....

(এ স্থান হতে উত্তর লেখা আরম্ভ করতে হবে)

Lab-1 এটি feedforward neural networks,  
এক বছর ২য় binary classification tasks. এটি  
এক বছর ২য় mode simple logic function.  
like AND function.

Perception model:- এক বা ততো অধিক input নিয়ে  
সহক weight for each input, summation function  
activation function and simple output.

Original input:-  $\{(-1, -1), (-1, 1), (1, -1), (1, 1)\}$   
target  $\{-1, -1, -1, 1\}$

$$H_2 = \frac{1}{1 + e^{1/H_2}}$$

$$= 0.576884378$$

Now calculate the values of  $Y_1$  and  $Y_2$  in the same way as we calculate the  $H_1$  and  $H_2$

$$Y_1 = H_1 * w_5 + H_2 * w_6 + b_2$$

$$= 1.10520597$$

~~We will calculate the value of  $Y_2$  in the same way as  $Y_1$~~   
calculate the final value of  $Y_1$

$$Y_1 = \frac{1}{1 + e^{-Y_1}} = 0.75136507$$

$$\text{Similarly } Y_2 = H_1 * Y_7 + H_2 * Y_8 + b_2$$

$$= 1.2249214$$

$$Y_2 \text{ final} = \frac{1}{1 + \frac{1}{e^{Y_2}}} = 0.772928465$$





# জাতীয় বিশ্ববিদ্যালয়

ক্রমিক নং : D2421218533

অতিরিক্ত উত্তরপত্র

- ১। পরীক্ষার নাম : .....
- ২। বিষয় : .....
- ৩। কোর্স/পত্র কোড : .....
- ৪। বিষয়ের শিরোনাম : .....
- ৫। তারিখ : .....
- ৬। ইনভিজিলেটরের স্বাক্ষর ও তারিখ : .....

(এ স্থান হতে উত্তর লেখা আরম্ভ করতে হবে)

Lab-1 এটি feedforward neural networks,  
এবং এছাড়াও binary classification tasks. এটি  
ব্যবহার করে mode simple logic function.  
like AND function.

Perception model :- এক বা ততো অধিক input নিয়ে  
এক weight for each input, summation function,  
activation function and simple output.

Perceptron input :-  $\{(-1, -1), (-1, 1), (1, -1), (1, 1)\}$   
target  $\{-1, -1, -1, 1\}$

The dimensions of the hyperplane depend on the features present in the dataset which means if there are 2 features (shown in the image) then hyperplane will be a straight line.

- And if there are 3 features, then hyperplane will be a 2-dimension plane.
- We always create a hyperplane that has a ~~max~~ maximum margin, which means the maximum distance between the data points.

Linear SVM: straight line for

(not for non-linear)

non-linear SVM: straight line for

(not for linear)