Computer Vision (CS 419/619)
Spring 2024

Autoencoders

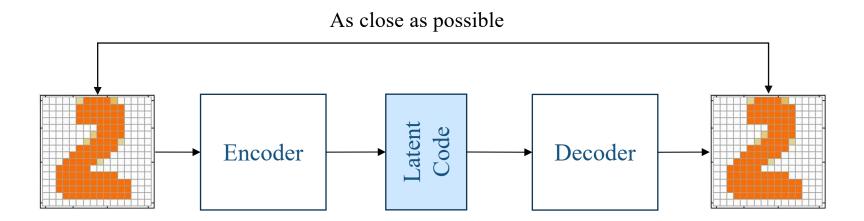


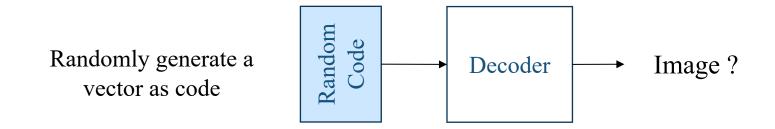
Myth of the Cave (*Plato's Allegory of the Cave*) [1]

• The aim of generative models is to learn or understand these latent variables, even when we are just given the observed variables/data.

- The story begins with prisoners who have lived their entire lives chained inside a cave.
- Behind the prisoners is a fire, and between the fire and the prisoners are people carrying puppets or other objects.
- These cast shadows on the opposite wall.
- The prisoners watch these shadows, believing this to be their reality as they have known nothing else.
- From the prisoners' perspective, the shadows are the "observed variables".
- These variables can be perceived and measured.
- Behind them are the true objects that are casting the shadow.
- From the prisoners' perspective, these objects are hidden from them.
- They are can termed as "latent variables".

1. https://www.studiobinder.com/blog/platos-allegory-of-the-cave/

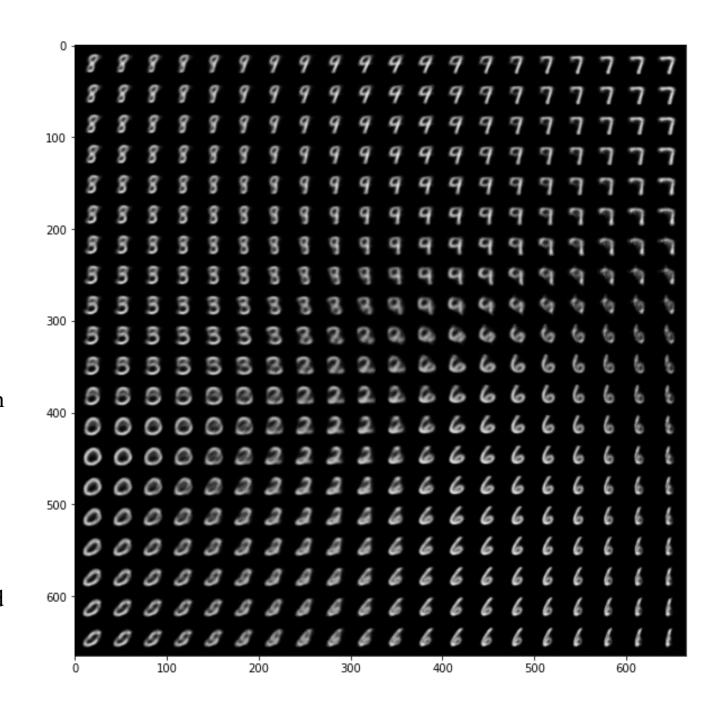


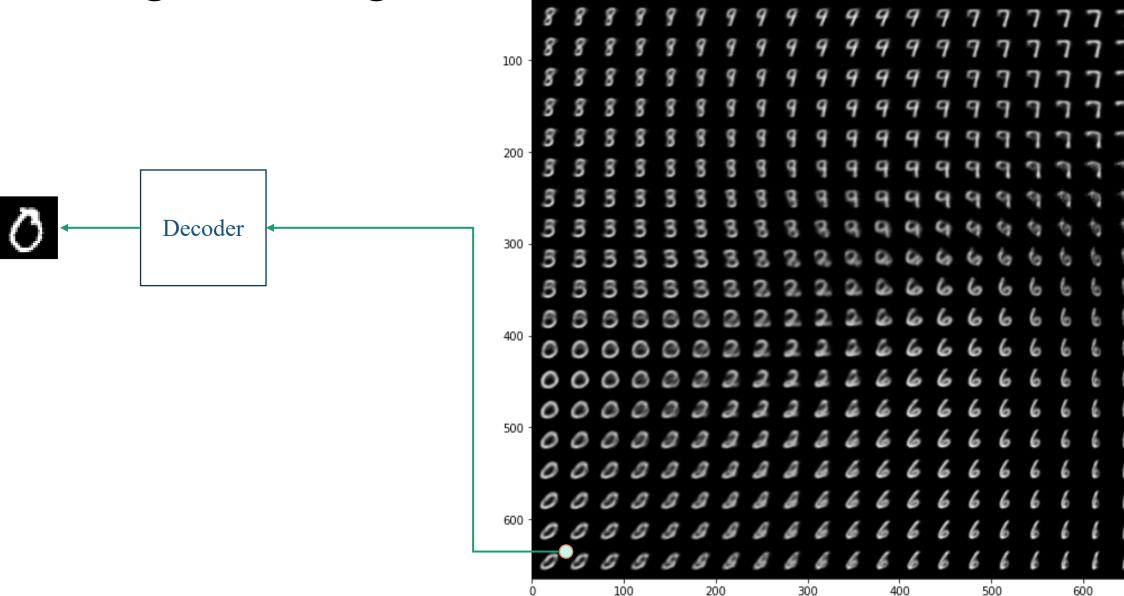


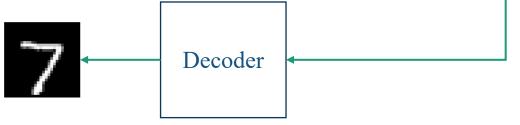
Notice the features along each axis:

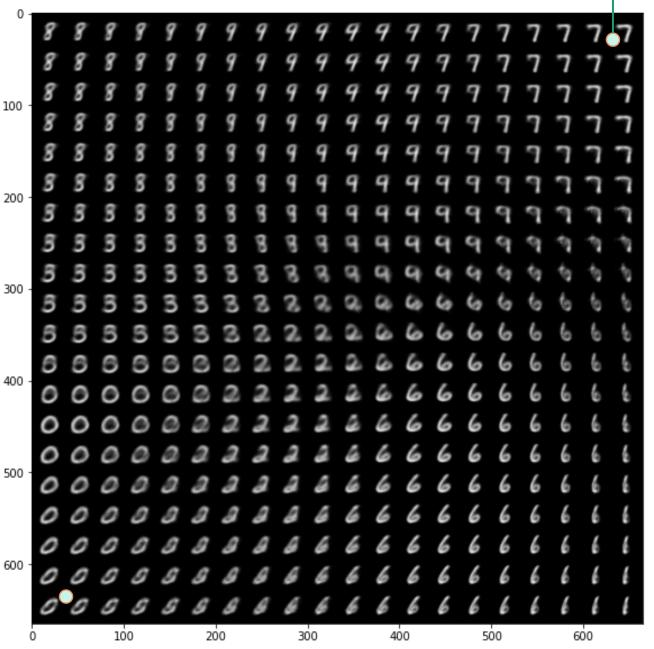
- Along the x-axis if move from 0 to 600.
 - There is a shift in feature
 - The images tend to go from circle to a straight line
- Along the y-axis
 - The above values tend (\sim 600) to show a loop on the top of the digit
 - The above values (\sim 0) tend to show a loop on the bottom of the digit.

- Grid of values in the latent space.
- The axes denotes the values in the latent vector.
- The images (*coordinates*) denote the reconstructed image from that vector.

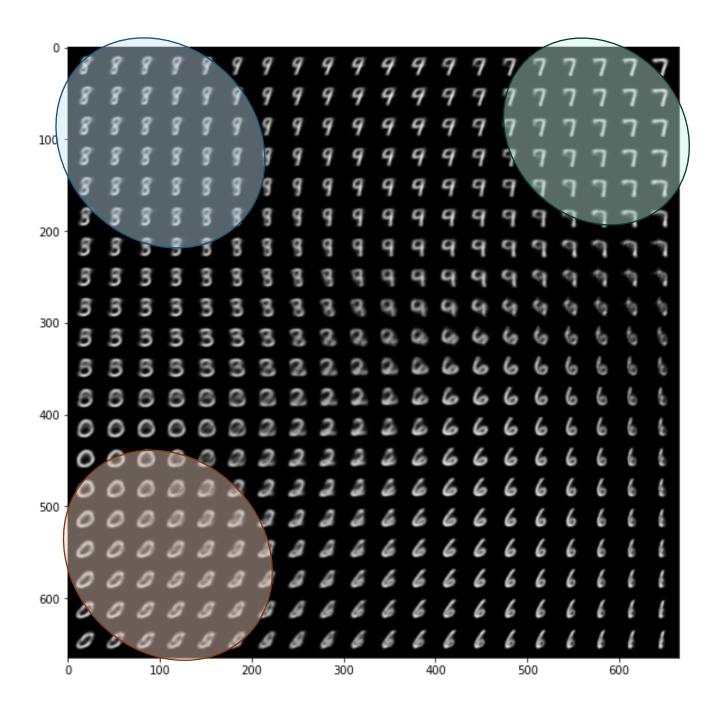








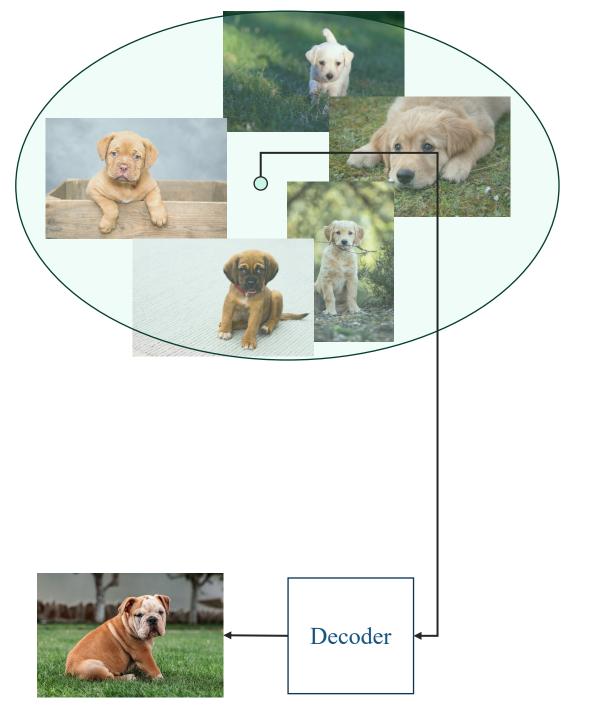
- Autoencoder tries to model the probability density of location of each class.
- Some 'special' types of autoencoder try to model only the parameters of probability distribution for each class.
- We will revisit the second point in a bit.

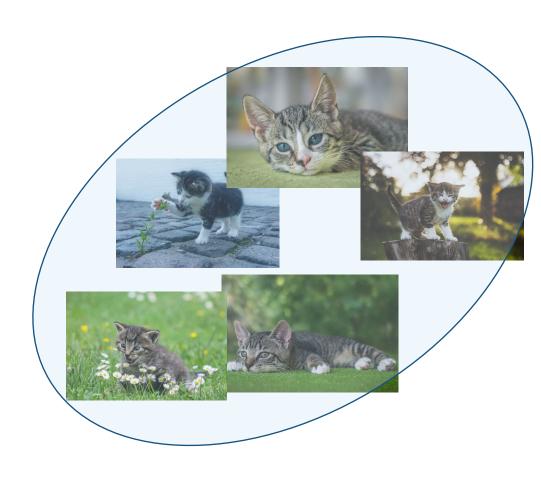


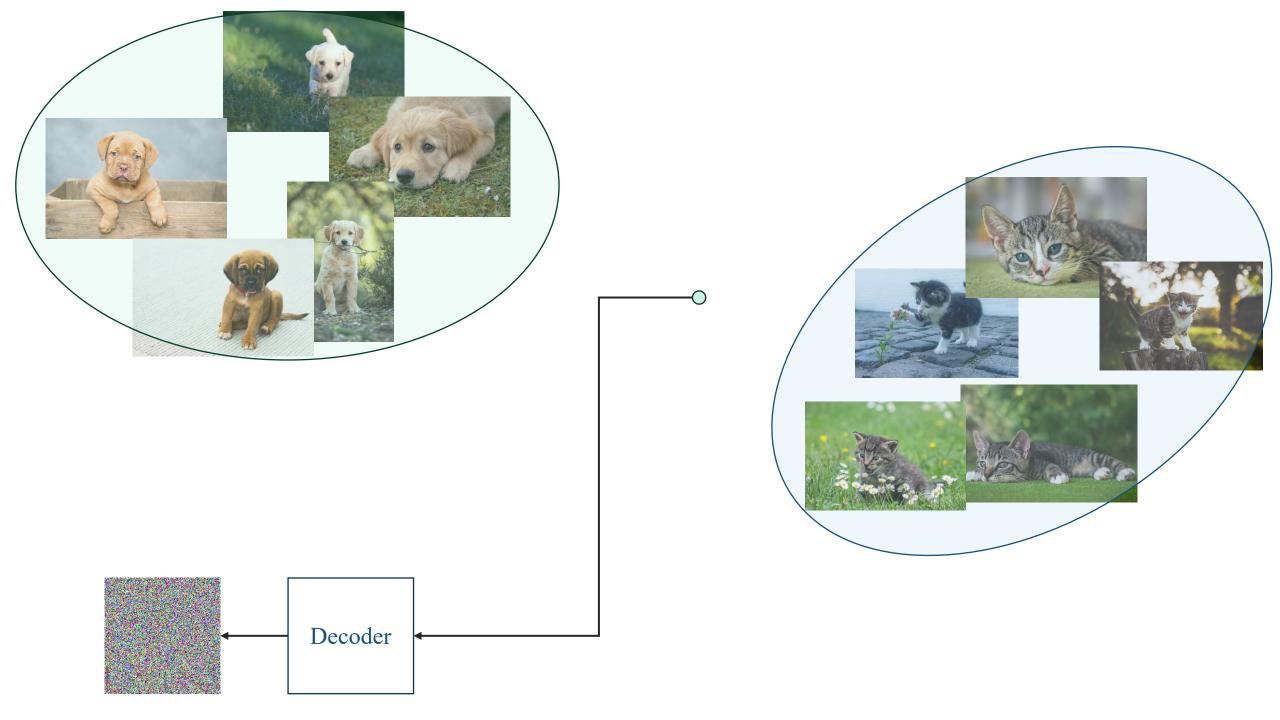


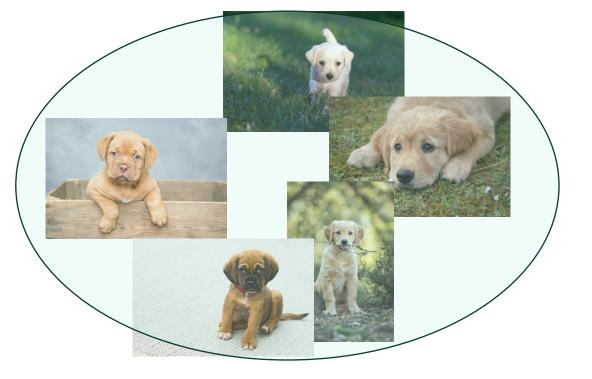




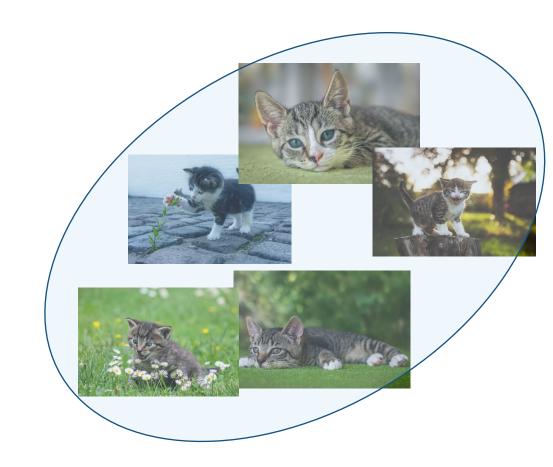




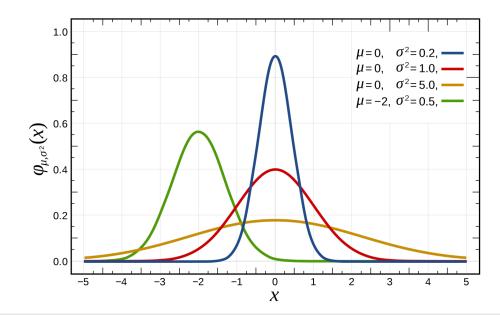




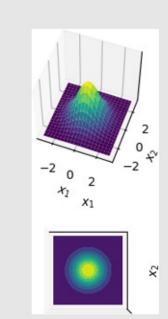
- The 'special' Autoencoder tries to learn the location of the 'clusters' instead of the vectors.
- Learning the clusters:
 - Center of the cluster (μ)
 - Spread of the cluster (\sum)

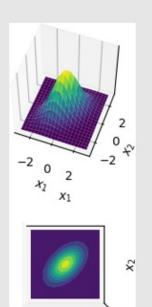


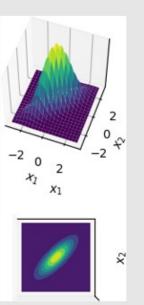
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$$\mu = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \Sigma = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \qquad \mu = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \Sigma = \begin{bmatrix} 1 & 0.5 \\ 0.5 & 1 \end{bmatrix} \quad \mu = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \Sigma = \begin{bmatrix} 1 & 0.8 \\ 0.8 & 1 \end{bmatrix}$$







1. Wikipedia,
https://en.wikipedia.org/wiki/G
aussian function

Reference and study material:

- 1. Deep Learning Part 1, Dr. Mitesh M. Khapra, NPTEL, https://archive.nptel.ac.in/noc/courses/noc19/SEM2/noc19-cs85/
- 2. Images are taken from Pixabay, https://pixabay.com/