#### **Conditional Probabilities**

$$P(A \mid B) = \frac{P(A \cap B)}{P(B)}$$

$$P(A \cap B) = P(A|B)P(B)$$

$$P(A \cap B) = P(B|A)P(A)$$

# Bayes and Naïve Bayes

$$P(S/1^{st}) = \frac{P(1st|S)P(S)}{P(1st)}$$

$$P(1st|\sim S)P(\sim S)$$

$$P(\sim S/1^{st}) = \frac{P(1st)}{P(1st)}$$

# Bayes and Naïve Bayes

$$P(1st \& Female | S)P(S)$$

$$P(S/1^{st} \& Female) = \frac{}{P(1st \& Female)}$$

$$P(1st \& Female/\sim S)P(\sim S)$$

$$P(\sim S/1 \text{st \& Female}) = \frac{}{P(1st \& Female)}$$

#### Naïve Bayes

$$P(S/1st\&Female) = P(1st\&Female|S)P(S) = \\ \frac{\text{Naive}}{P(1st/S)*p(Female|S)P(S)} \\ P(\sim S/1s\&Female) = P\left(1st\&\frac{Female}{\sim S}\right)P(\sim S) = \\ \frac{P(1st|\sim S)*P(Female/\sim S)P(\sim S)}{P(1st|\sim S)*P(Female/\sim S)P(\sim S)} \\ P(\sim S/1s\&Female) = P\left(1st\&\frac{Female}{\sim S}\right)P(\sim S) = \\ \frac{P(1st|\sim S)*P(Female/\sim S)P(\sim S)}{P(1st|\sim S)*P(Female/\sim S)P(\sim S)}$$

### Bayes and Naïve Bayes

Max of  $P(\Theta|S)P(S)$  Over all possible S

Max of  $P(\Theta 1|S)P(\Theta 2|S1)P(S)$ , Over all possible S