

1 Introduction

Definition 1.1

Let $\Sigma = \{0, \dots, \sigma - 1\}$ be a finite, ordered set. The elements of Σ are called *characters* or *symbols* and Σ is called an *alphabet* of size σ .

Definition 1.2

A *string* S is a sequence of characters from an alphabet Σ .

- We usually use $n = |S|$ to be the length of the string.
- The i -th character of S is $S[i]$. Indices are 0-based.
- The substring from the i -th to the j -th character is $S[i..j]$.
- A substring with $i = 0$ is called *prefix*. A substring with $j = n - 1$ is called *suffix*.
- The i -th *suffix* is $S[i..n - 1]$.

1.1 Tries

Definition 1.3

Let $S = \{S_0, S_1, \dots, S_{N-1}\}$ be a set of strings over an alphabet Σ . A *trie* is a tree, where each node represents a different prefix in the set S . The root represents the empty prefix ϵ . Vertex u representing prefix Y is a child of vertex v representing prefix X , if and only if $Y = Xc$ for some character $c \in \Sigma$. The edge (v, u) is then labeled c .

If S is the set of all suffixes of a string T , the trie is called *suffix trie*.

Example 1.4

Figure 1.1 shows the suffix trie for the string `banana$`: The dollar sign `$` is a sentinel that does not appear elsewhere in the text. This guarantees, that no suffix is a prefix of another suffix and the suffix trie therefore has $n + 1$ leaves.

