# **Differential Equations**

#### **Table of Contents**

Introduction	- ]
Having No Independent Variable.	1
Initial Value Problems	2
Plotting a solution.	2
Compound Example	3
An Example with Variables	3

### Introduction

Matlab is quite powerful when it comes to solving differential equations. The standard command is dsolve (think Differential Solve) and has the format dsolve('equation', 'variable'). Here equation is a differential equation in the form of a string and variable is the independent variable. For example suppose we wished to solve y'=2y+x.

We type this into Matlab as:

Note that Dy represents the derivative of the variable y. Also we should note here that you may get a differently numbered constant C1, C2, etc. depending upon how many constants that have shown up in Matlab for you. Don't worry for now about how they're numbered.

### Having No Independent Variable.

Consider the differential equation y' = 3y. If you do this in Matlab:

You see the solution is given as a function of t. Why t? The answer is that first, the differential equation has no independent variable so Matlab doesn't know what y is supposed to be a function of. Second, t is pretty normal since often differential equations are used for functions of time. If you want another variable you can tell Matlab:

We can use higher derivatives like D2y and D3y too. For example we can solve y'' = 2y treating y as a function of z by typing:

#### **Initial Value Problems**

We can also state initial conditions using the form dsolve('equation','initial condition','variable') where initial condition is also a string. For example:

And higher order with multiple initial conditions:

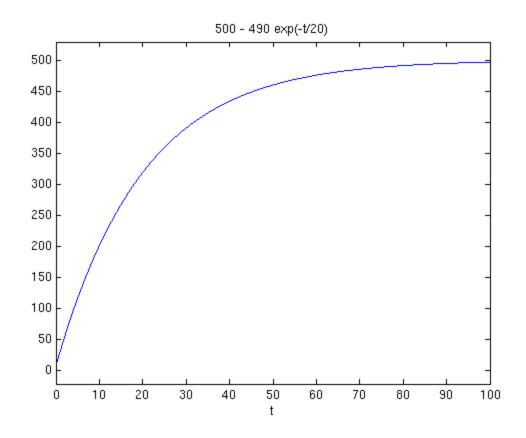
```
dsolve('D2y+Dy=x','y(0)=1,Dy(1)=2','x') ans = \\ 2*exp(1) - x - 2*exp(1)*exp(-x) + x^2/2 + 1
```

Matlab can of course do much more with differential equations as we'll see but for now just appreciate that it can handle most straightfoward examples with no problem at all.

### Plotting a solution.

Plotting a solution is as easy as wrapping dsolve in ezplot:

```
ezplot(dsolve('Dy=0.05*(500-y)','y(0)=10','t'),[0,100])
```



## **Compound Example**

Here's an example of a single Matlab line which will solve the initial value problem y' + 3y + 10 = 0 with y(1) = 2, set the result equal to 0 and solve for x.

```
solve(dsolve('Dy+3*y+10=0','y(1)=2','x'),'x')
ans =
-log((5*exp(-3))/8)/3
```

You can also set the result to a nonzero value with this totally confusing command:

```
solve(strcat(char(dsolve('Dy+3*y+10=0','y(1)=2','x')),'=20000'))
ans =
    -log((30005*exp(-3))/8)/3
```

# **An Example with Variables**

You may notice that if you try the following:

```
a=2;b=3;
dsolve('Dy=a*x+b','x')

ans =
  (a*x^2)/2 + b*x + C2
```

This is annoying. You wanted a and b to be in the answer! The point is that 'Dy=a\*x+b' is treated as a string of characters and therefore a and b as just letters. They're not given their values. To get around this you can solve and then substitute:

Published with MATLAB® 8.0