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BSIT 2-2

I. Objective:

$$\text{Minimize } w = 6x_1 + 2x_2 + 3x_3$$

II. Constraints

$$3x_1 + 2x_2 + x_3 \geq 28$$

$$6x_1 + x_3 \geq 24$$

$$3x_1 + x_2 + 2x_3 \geq 40$$

$$x_1, x_2, x_3 \geq 0$$

Matrix

$$\begin{bmatrix} x_1 & x_2 & x_3 & C \\ 3 & 2 & 1 & 28 \\ 6 & 0 & 1 & 24 \\ 3 & 1 & 2 & 40 \\ \hline 6 & 2 & 3 & 0 \end{bmatrix}$$

Transpose matrix

$$\begin{bmatrix} 3 & 6 & 3 & 6 \\ 2 & 0 & 1 & 2 \\ 1 & 1 & 2 & 3 \\ \hline 28 & 24 & 40 & 0 \end{bmatrix}$$

Dual:

I. Objective:

$$\text{Maximize } z = 28y_1 + 24y_2 + 40y_3 \rightarrow -28y_1 - 24y_2 - 40y_3 + z = 0$$

II. Constraints

$$3y_1 + 6y_2 + 3y_3 \leq 6 \rightarrow 3y_1 + 6y_2 + 3y_3 + s_1 = 6$$

$$2y_1 + y_3 \leq 2 \rightarrow 2y_1 + y_3 + s_2 = 2$$

$$y_1 + y_2 + 2y_3 \leq 3 \rightarrow y_1 + y_2 + 2y_3 + s_3 = 3$$

$$\begin{bmatrix} y_1 & y_2 & y_3 & s_1 & s_2 & s_3 & z & C \\ 3 & 6 & 3 & 1 & 0 & 0 & 0 & 6 \\ 2 & 0 & 1 & 0 & 1 & 0 & 0 & 2 \\ 1 & 1 & 2 & 0 & 0 & 1 & 0 & 3 \\ \hline -28 & -24 & -40 & 0 & 0 & 0 & 1 & 0 \end{bmatrix} \begin{matrix} 2 \\ 2 \\ 1.5 \end{matrix} \begin{matrix} R_1 \times \frac{1}{3} \\ R_2 \times \frac{1}{2} \\ R_3 \times \frac{1}{2} \end{matrix}$$

$$\begin{bmatrix} 3 & 6 & 3 & 1 & 0 & 0 & 0 & 6 \\ 2 & 0 & 1 & 0 & 1 & 0 & 0 & 2 \\ \frac{1}{2} & \frac{1}{2} & 1 & 0 & 0 & \frac{1}{2} & 0 & 1.5 \\ \hline -28 & -24 & -40 & 0 & 0 & 0 & 1 & 0 \end{bmatrix} \begin{matrix} R_1: R_1 - 3R_3 \\ R_2: R_2 - R_3 \\ R_4: R_4 + 40R_3 \end{matrix}$$

$$\begin{bmatrix} y_1 & y_2 & y_3 & s_1 & s_2 & s_3 & z & C \\ 3/2 & 9/2 & 0 & 1 & 0 & -1/2 & 0 & 3/2 \\ 3/2 & -1/2 & 0 & 0 & 1 & -1/2 & 0 & 1/2 \\ 1/2 & 1/2 & 1 & 0 & 0 & 1/2 & 0 & 1.5 \\ -8 & -4 & 0 & 0 & 0 & 20 & 1 & 60 \end{bmatrix}$$

$$\begin{bmatrix} 3/2 & 9/2 & 0 & 1 & 0 & -1/2 & 0 & 3/2 \\ 3/2 & -1/2 & 0 & 0 & 1 & -1/2 & 0 & 1/2 \\ 1/2 & 1/2 & 1 & 0 & 0 & 1/2 & 0 & 1.5 \\ -8 & -4 & 0 & 0 & 0 & 20 & 1 & 60 \end{bmatrix} \begin{matrix} 1 \\ 1/3 \\ 3 \end{matrix}$$

$$\begin{bmatrix} 3/2 & 9/2 & 0 & 1 & 0 & -1/2 & 0 & 3/2 \\ 1 & -1/3 & 0 & 0 & 2/3 & -1/3 & 0 & 1/3 \\ 1/2 & 1/2 & 1 & 0 & 0 & 1/2 & 0 & 1.5 \\ -8 & -4 & 0 & 0 & 0 & 20 & 1 & 60 \end{bmatrix} \begin{matrix} R_1: R_1 - 3/2 R_2 \\ R_2: R_2 - 1/2 R_3 \\ R_4: R_4 + 8 R_2 \end{matrix}$$

$$\begin{bmatrix} 0 & 5 & 0 & 1 & -1 & 0 & 0 & 1 \\ 1 & -1/3 & 0 & 0 & 2/3 & -1/3 & 0 & 1/2 \\ 0 & 1/4 & 1 & 0 & -1/3 & 2/3 & 0 & 4/3 \\ 0 & -20/3 & 0 & 0 & 16/3 & 68/3 & 1 & 17/3 \end{bmatrix} \begin{matrix} 1/5 \\ -3/2 \\ 3/16 \end{matrix}$$

$$\begin{bmatrix} 0 & 5 & 0 & 1 & -1 & 0 & 0 & 1 \\ 1 & -1/3 & 0 & 0 & 2/3 & -1/3 & 0 & 1/2 \\ 0 & 1 & 4 & 0 & -4/3 & 8/3 & 0 & 16/3 \\ 0 & -20/3 & 0 & 0 & 16/3 & 68/3 & 1 & 17/3 \end{bmatrix} \begin{matrix} R_1: R_1 - 5 R_3 \\ R_2: R_2 + 1/3 R_3 \\ R_4: R_4 + 20/3 R_3 \end{matrix}$$

$$\begin{bmatrix} 0 & 0 & -5 & 1 & 17/3 & -40/3 & 0 & 0 \end{bmatrix}$$