ALGEBRA 4

Day 74

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7.3 Logarithmic Functions as Inverses 7.4 Properties of Logarithms

Objectives:

To write and evaluate logarithmic expressions

To use the properties of logarithms

7.3 Logarithmic Functions as Inverses Objective: To write and evaluate logarithmic expressions

Logarithmic Function with Base a:

$$f(x) = \log_b(x - h) + k$$

where $x > 0$, $b > 0$, $b \ne 1$

Common Log:

log with a base 10 $log_{10} x = log x$

Rewrite from Exponential to Logarithmic:

$$log_b y = x <=> b^x = y$$

Rewrite: From log to exponential or exponential log

$$\log_2 8 = 3$$

$$5^3 = 125$$

Evaluate

 $log_7 49$

 $\log_{12} 12$

 $log_2 64$

7.4 Properties of Logarithms Objective: To use the properties of logarithms

Properties of Logarithms

$$\log_a 1 = 0 \qquad \Rightarrow a^0 = 1$$

$$\log_a a = 1 \qquad \Rightarrow a^1 = a$$

$$\log_a a^x = x \quad \to a^{\log_a x} = x$$

$$\log_a x = \log_a y = x = y$$

More Properties

Change of Base: (not as important with our calculators)

$$\log_a x = \frac{\log_b x}{\log_b a}$$

Product Property

$$\log_{a}(uv) = \log_{a}(u) + \log_{a}(v)$$

Quotient Property

$$log_a(uv) = log_a(u) + log_a(v)$$
 $log_a(u/v) = log_a(u) - log_a(v)$

Power Property

$$\log_{\mathbf{a}} u^n = n \log_{\mathbf{a}}(\mathbf{u})$$

Rewrite:

$$\log_{\mathbf{b}} y = x <=> b^x = y$$

Examples

Expand:

 $\log_5 25x^3$

Condense:

 $5 \log_6 x + 2 \log_6 7 - 3 \log_6 w$

Simplify:

 log_44

 log_381

 log_81

 $9\log_9 4x$

 $\log_7 49^{3x}$

For Next Time...

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