Bell Work: Get a Book and Finish From Last Time...

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PRE-CALC TRIG

Day 25

Review: Properties of Logarithms

$$\log_a 1 = 0 \qquad \Rightarrow a^0 = 1$$

$$\log_a a = 1 \qquad \Rightarrow a^1 = a$$

$$\log_a a^x = x \quad \to a^{\log_a x} = x$$

$$\log_a x = \log_a y = x = y$$

Review: More Properties

Change of Base: (not as important with our calculators)

$$\log_a x = \frac{\log_b x}{\log_b a}$$

Product Property

Quotient Property

 $\log_a(uv) = \log_a(u) + \log_a(v)$ $\log_a(u/v) = \log_a(u) - \log_a(v)$

Power Property

 $\log_a u^n = n \log_a(u)$

Rewrite:

$$\log_{\mathbf{b}} y = x <=> b^x = y$$

3.4 Exponential and Log Equations

Objective:

Solve exponential and log equations

Strategies to Solve:

1.) One to One: rewrite so the bases are the same and compare

2.) Rewrite exponential in log form and apply the Inverse Property

3.) Rewrite log in exponential form and apply the Inverse Property

Examples: Solve

1.)
$$3^x = 81$$

2.)
$$\ln x - \ln 2 = 0$$

3.)
$$2^x = 8$$

4.)
$$\log_6 2x = 4$$

Examples

1.)
$$3^x = 81$$

$$3^{x} = 3^{4}$$

$$x = 4$$

One to One

2.)
$$\ln x - \ln 2 = 0$$

$$ln x = ln 2$$

$$x = 2$$

One to One

3.)
$$2^x = 8$$

$$\log_2 2^x = \log_2 8$$

$$x = 3$$

Inverse

4.)
$$\log_6 2x = 4$$

$$6^{\log_6 2x} = 6^4$$
 $2x = 4$ $x = 2$

$$2x = 4$$

$$x = 2$$

Inverse

Answer the following.

You have deposited \$600 in an account that pays 7.5% interest compounded continuously. Use the $A = Pe^{rt}$, where P is in initial deposit r is the percent (written as decimal) and t is the time in years. How long will it take to double your money? Triple?

Set Up Solution

$$A = Pe^{rt}$$
 $\rightarrow 1800 = 600e^{0.075t} \rightarrow 3 = e^{0.075t} \rightarrow t = ???$

P = 600

r = 0.075

A = 1800 (tripled the P)

t = time

Additional Examples

1.)
$$8(2)^x - 10 = 70$$

5.)
$$3^{5x} = 3^{3x-8}$$

2.)
$$5(3)^{6x-12} + 12 = 32$$

6.)
$$\log_7(4x - 7) = \log_7(x + 8)$$

3.)
$$4e^{x+1} = 12$$

7.) In
$$(6x - 1) = 3$$

4.)
$$4\log_2(2x + 9) - 21 = 3$$

For Next Time

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