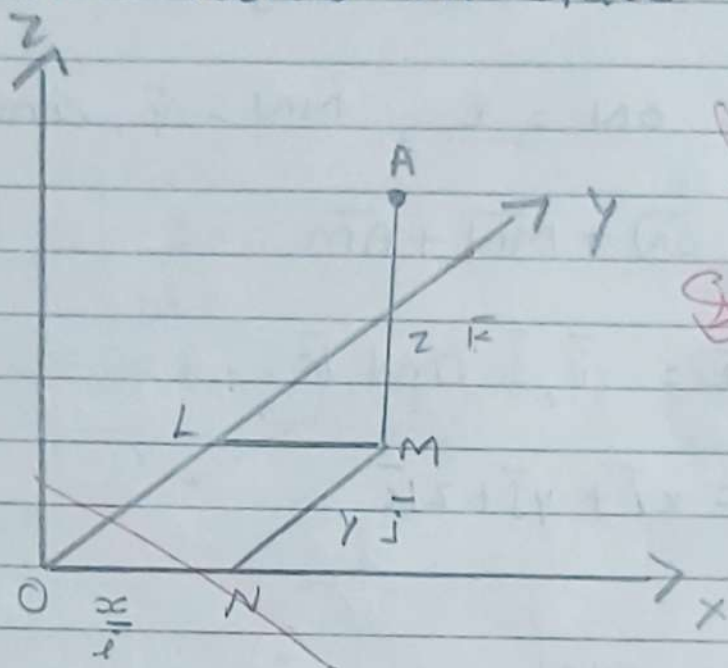


Que: 1. Position vector in space

(10)



→ Position of vector in space is the origin where,

Let A is a one point in space.

A = coordinates of space.

Draw a point in space and take one line and indicate name 'm'.

m, draw ~~the~~ is perpendicular on x and y axes.

Draw MN and ML where MN is perpendicular on x axes and ML is perpendicular on y axes.

We want to find magnitude of  $\vec{OA}$ .

where,  $ON = \vec{x}$ ,  $MN = \vec{y}$ , and  $AM = \vec{z}$ .

$$\vec{OA} = \vec{ON} + \vec{MN} + \vec{AM}$$

$$\vec{OA} = \vec{a} = \vec{i}, \vec{j}, \text{ and } \vec{k}.$$

$$\vec{OA} = x\vec{i} + y\vec{j} + z\vec{k}$$

For example:

1.

$$A = (2, 1, 3).$$

~~$$\vec{a} = (2, 1, 3)$$~~

~~$$\vec{a} = 2\vec{i} + 1\vec{j} + 3\vec{k}$$~~

ue:2  $\vec{a} = \cancel{30} (3, -1, -2)$   $\vec{b} = (7, 1, -1)$   $\vec{c} = (-2, 3, 5)$

$$\vec{a} = 3\vec{i} - 1\vec{j} - 2\vec{k}$$

$$\vec{b} = 7\vec{i} + 1\vec{j} - 1\vec{k}$$

$$\vec{c} = -2\vec{i} + 3\vec{j} + 5\vec{k}$$

1  $\frac{\vec{b}}{|\vec{a} \times \vec{c}|}$

$$\therefore \vec{a} \times \vec{c}$$

$$\begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 3 & -1 & -2 \\ -2 & 3 & 5 \end{vmatrix}$$

$$= ((-1)(5) - (-2)(3))\vec{i} + ((-2)(-2) - (5)(3))\vec{j} + ((3)(3) - (-1)(-2))\vec{k}$$

$$= (-5 + 6)\vec{i} + (4 - 15)\vec{j} + (9 - 2)\vec{k}$$

$$= \vec{i} - 11\vec{j} + 7\vec{k}$$

$$\therefore |\vec{a} \times \vec{c}|$$

$$= \sqrt{(1)^2 + (-11)^2 + (7)^2}$$

$$= \sqrt{1 + 121 + 49}$$

$$= \sqrt{171}$$

$$= 3\sqrt{19}$$



$$= \frac{\vec{b}}{|\vec{a} \times \vec{c}|} \quad (7)$$

$$= \frac{7\vec{i} + 1\vec{j} - 1\vec{k}}{3\sqrt{19}}$$

2  $\frac{\cos \theta}{\sin \theta} \quad (AC)$

$$\vec{a} = 3\vec{i} - \vec{j} - 2\vec{k}$$

$$\vec{c} = -2\vec{i} + 3\vec{j} + 5\vec{k}$$

$$\therefore \cos \theta = \frac{\vec{a} \cdot \vec{c}}{ab \quad ac}$$

$$\bullet \vec{a} \cdot \vec{c}$$

$$= (3)(-2) + (-1)(3) + (-2)(5)$$

$$= -6 - 3 - 10$$

$$= -9 - 10$$

$$= -19$$

$$\bullet ac$$

$$= \sqrt{(3)^2 + (-1)^2 + (-2)^2} \sqrt{(-2)^2 + (3)^2 + (5)^2}$$

$$= \sqrt{9+1+4} \sqrt{4+9+25}$$

$$= \sqrt{14} \sqrt{38}$$

$$= \sqrt{532}$$

$$\cos \theta = \frac{-19}{\sqrt{532}}$$

$$\therefore \sin \theta = \frac{|\vec{a} \times \vec{b}|}{ab}$$

$$\bullet \vec{a} \times \vec{b}$$

$\vec{i}$	$\vec{j}$	$\vec{k}$
3	-1	-2
-2	3	5

$$= ((-1)(5) - (-2)(3))\vec{i} + ((-2)(-2) - (5)(3))\vec{j} + ((3)(3) - (-1)(-2))\vec{k}$$

$$= (-5 + 6)\vec{i} + (4 - 15)\vec{j} + (9 - 2)\vec{k}$$

$$= 1\vec{i} - 11\vec{j} + 7\vec{k}$$

$$\bullet |\vec{a} \times \vec{b}|$$

$$= \sqrt{(1)^2 + (-11)^2 + (7)^2}$$

$$= \sqrt{1 + 121 + 49}$$

$$= \sqrt{171}$$

$$= 3\sqrt{19}$$

$$\bullet ab$$

$$= \sqrt{(3)^2 + (-1)^2 + (-2)^2} \sqrt{(-2)^2 + (3)^2 + (5)^2}$$

$$= \sqrt{9 + 1 + 4} \sqrt{4 + 9 + 25}$$

$$\sqrt{14} \sqrt{38}$$

$$\frac{\cos \theta}{\sin \theta} = \frac{-19}{\sqrt{532}}$$

$$\frac{3\sqrt{19}}{\sqrt{532}}$$

$$\phi = \frac{-19}{3\sqrt{19}}$$

~~2002~~

$$3 \quad \bar{A} \cdot (\bar{B} - \bar{C})$$

$$\therefore \bar{B} - \bar{C}$$

$$= (7 - (-2))\bar{i} + (1 - 3)\bar{j} + (-1 - 5)\bar{k}$$

$$= (7 + 2)\bar{i} + (-2)\bar{j} + (-6)\bar{k}$$

$$= 9\bar{i} - 2\bar{j} - 6\bar{k}$$

~~2002~~

$$\therefore \bar{A} \cdot (\bar{B} - \bar{C})$$

$$= (3\bar{i} - \bar{j} - 2\bar{k}) \cdot (9\bar{i} - 2\bar{j} - 6\bar{k})$$

$$= (3)(9) + (-1)(-2) + (-2)(-6)$$

$$= 27 + 2 + 12$$

$$= 41$$



unit vector of cross product

$$\vec{a} \times \vec{b} \quad \vec{b} \times \vec{c}$$

$$= ((1)(5) - (-1)(3))\hat{i} + ((1)(-2) - (4)(8))\hat{j} + ((7)(3) - (1)(-2))\hat{k}$$

$$= (5+3)\hat{i} + (-2-32)\hat{j} + (21+2)\hat{k}$$

$$= 8\hat{i} - 33\hat{j} + 23\hat{k}$$

$$\therefore |\vec{b} \times \vec{c}|$$

$$= \sqrt{(8)^2 + (-33)^2 + (23)^2}$$

$$= \sqrt{64 + 1089 + 529}$$

$$= \frac{\sqrt{1682}}{29\sqrt{2}} \quad (\text{⚡})$$

$$\frac{\vec{b} \times \vec{c}}{|\vec{b} \times \vec{c}|}$$

$$= \frac{8\hat{i} - 33\hat{j} + 23\hat{k}}{29\sqrt{2}}$$

6  $3\bar{a} \cdot (4\bar{b} - 2\bar{c})$

$$\bar{a} = (3, -1, -2)$$

$$\bar{b} = (7, -1, -1)$$

$$\bar{c} = (-2, 3, 5)$$

→  $\bar{a}$  is scalar multiple with  $\bar{a}$ .  
 $= \bar{a} = 9\bar{i} - 3\bar{j} - 6\bar{k}$

→  $\bar{b}$  is scalar multiple with  $\bar{b}$  4.  
 $= \bar{b} = 28\bar{i} + 4\bar{j} - 4\bar{k}$

→  $\bar{c}$  is scalar multiple with 2  
 $= \bar{c} = -4\bar{i} + 6\bar{j} + 10\bar{k}$

$$\therefore 4\bar{b} - 2\bar{c}$$

$$= (28 - (-4))\bar{i} + (4 - 6)\bar{j} + (-4 - 10)\bar{k}$$

$$= (28 + 4)\bar{i} + (-2)\bar{j} + (-14)\bar{k}$$

$$= 32\bar{i} - 2\bar{j} - 14\bar{k} \quad (2)$$

$$\therefore 3\bar{a} (4\bar{b} - 2\bar{c})$$

$$= (9\bar{i} - 3\bar{j} - 6\bar{k}) (32\bar{i} - 2\bar{j} - 14\bar{k})$$

$$= (9)(32) + (-3)(-2) + (-6)(-14)$$

$$= 288 + 6 + 84$$

$$= \boxed{378}$$