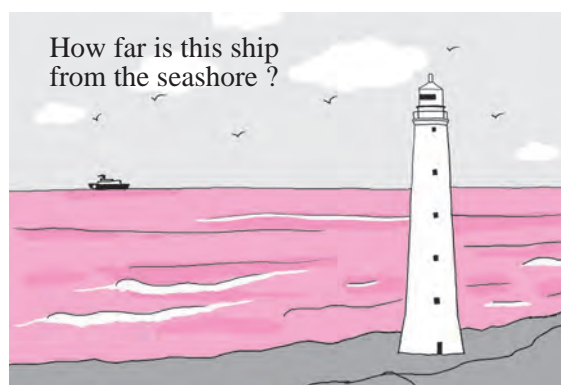
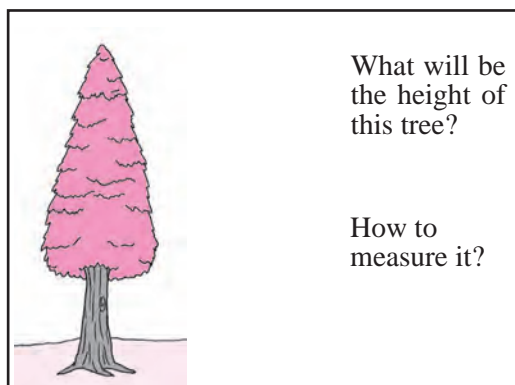




## Let's study.

- Introduction of Trigonometry
- Relations among Trigonometric Ratios
- Trigonometric Ratios
- Trigonometric Ratios of Particular Angles

## Introduction to Trigonometry



We can measure distances by using a rope or by walking on ground, but how to measure the distance between a ship and a light house? How to measure the height of a tall tree?

Observe the above pictures. Questions in the pictures are related to mathematics. Trigonometry, a branch of mathematics, is useful to find answers to such questions. Trigonometry is used in different branches of Engineering, Astronomy, Navigation etc.

The word Trigonometry is derived from three Greek words 'Tri' means three, 'gona' means sides and 'metron' means measurements.



## Let's recall.

We have studied triangle. The subject trigonometry starts with right angled triangle, theorem of Pythagoras and similar triangles, so we will recall these topics.

- In  $\triangle ABC$ ,  $\angle B$  is a right angle and side  $AC$  opposite to  $\angle B$ , is hypotenuse. Side opposite to  $\angle A$  is  $BC$  and side opposite to  $\angle C$  is  $AB$ . Using Pythagoras' theorem, we can write the following statement for this triangle.

$$(AB)^2 + (BC)^2 = (AC)^2$$

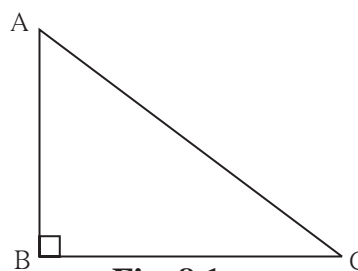
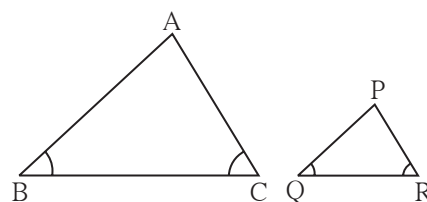


Fig. 8.1



- If  $\triangle ABC \sim \triangle PQR$  then their corresponding sides are in the same proportions.

$$\text{So } \frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$$



**Fig. 8.2**

Let us see how to find the height of a tall tree using properties of similar triangles.

**Activity :** This experiment can be conducted on a clear sunny day.

Look at the figure given alongside.

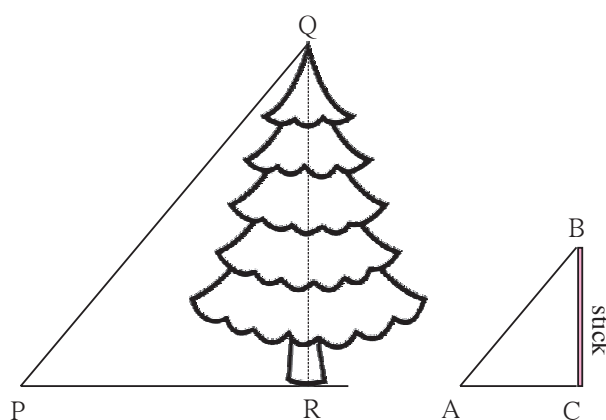
Height of the tree is QR, height of the stick is BC.

Thrust a stick in the ground as shown in the figure. Measure its height and length of its shadow. Also measure the length of the shadow of the tree. Rays of sunlight are parallel. So  $\triangle PQR$  and  $\triangle ABC$  are equiangular, means similar triangles. Sides of similar triangles are proportional.

$$\text{So we get } \frac{QR}{PR} = \frac{BC}{AC}.$$

Therefore, we get an equation,

$$\text{height of the tree} = QR = \frac{BC}{AC} \times PR$$



**Fig.8.3**

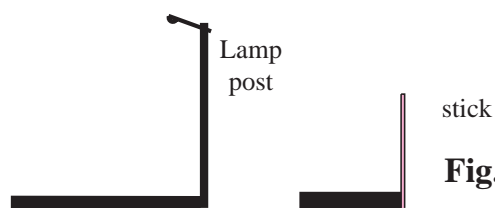
We know the values of PR, BC and AC. Substituting these values in this equation, we get length of QR, means height of the tree.



**Use your brain power !**

It is convenient to do this experiment between 11:30 am and 1:30 pm instead of doing it in the morning at 8'O clock. Can you tell why ?

**Activity :** You can conduct this activity and find the height of a tall tree in your surrounding. If there is no tree in the premises then find the height of a pole.



**Fig. 8.4**



Let's learn.

### Terms related to right angled triangle

In right angled  $\Delta ABC$ ,  $\angle B = 90^\circ$ ,  $\angle A$  and  $\angle C$  are acute angles.

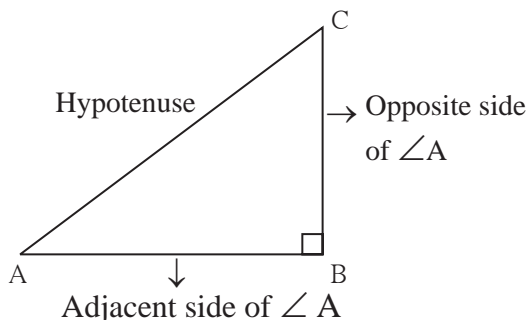


Fig. 8.5

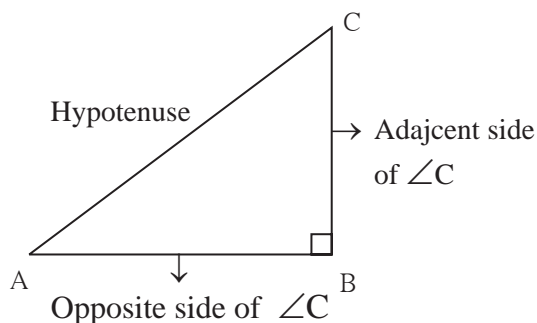


Fig. 8.6

**Ex.** In the figure 8.7,  $\Delta PQR$  is a right angled triangle. Write-

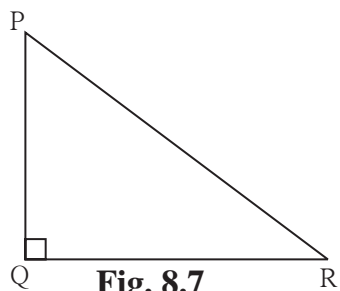


Fig. 8.7

side opposite to  $\angle P = \dots$   
 side opposite to  $\angle R = \dots$   
 side adjacent to  $\angle P = \dots$   
 side adjacent to  $\angle R = \dots$

### Trigonometric ratios

In the adjacent Fig.8.8 some right angled triangles are shown.  $\angle B$  is their common angle. So all right angled triangles are similar.

$$\Delta PQB \sim \Delta ACB$$

$$\therefore \frac{PB}{AB} = \frac{PQ}{AC} = \frac{BQ}{BC}$$

$$\therefore \frac{PQ}{AC} = \frac{PB}{AB} \quad \therefore \frac{PQ}{PB} = \frac{AC}{AB} \quad \dots \text{alternando}$$

$$\frac{QB}{BC} = \frac{PB}{AB} \quad \therefore \frac{QB}{PB} = \frac{BC}{AB} \quad \dots \text{alternando}$$

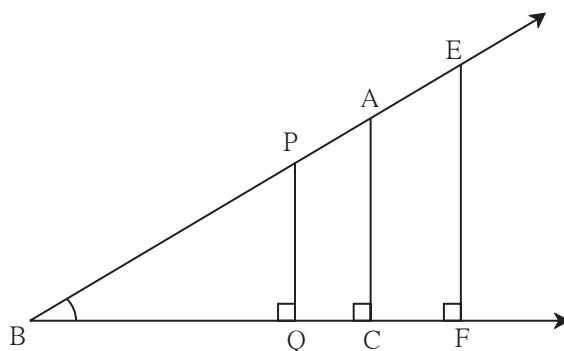
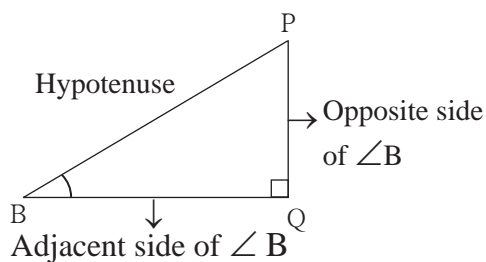
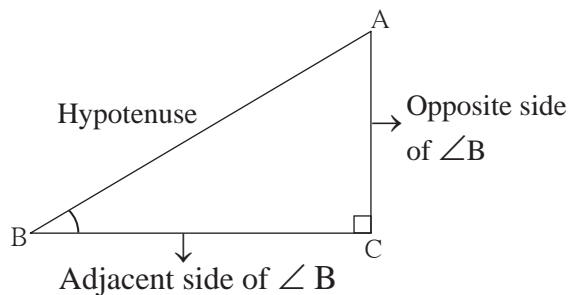


Fig. 8.8

The figures of triangles in 8.9 and 8.10 are of the triangles separated from the figure 8.8



**Fig.8.9**



**Fig.8.10**

(i) In  $\Delta PQB$ ,

$$\frac{PQ}{PB} = \frac{\text{Opposite side of } \angle B}{\text{Hypotenuse}}$$

The ratios  $\frac{PQ}{PB}$  and  $\frac{AC}{AB}$  are equal.

$$\therefore \frac{PQ}{PB} = \frac{AC}{AB} = \frac{\text{Opposite side of } \angle B}{\text{Hypotenuse}}$$

This ratio is called the ‘sine’ ratio of  $\angle B$ , and is written in brief as ‘**sin B**’.

(ii) In  $\triangle PQB$  and  $\triangle ACB$ ,

$$\frac{BQ}{PR} = \frac{\text{Adjacent side of } \angle B}{\text{Hypotenuse}} \quad \text{and} \quad \frac{BC}{AB} = \frac{\text{Adjacent side of } \angle B}{\text{Hypotenuse}}$$

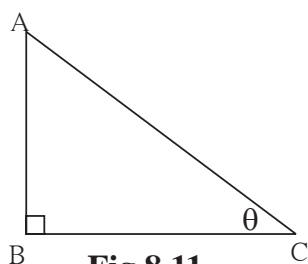
$$\therefore \frac{BQ}{PB} = \frac{BC}{AB} = \frac{\text{Adjacent side of } \angle B}{\text{Hypotenuse}}$$

This ratio is called as the ‘cosine’ ratio of  $\angle B$ , and written in brief as ‘**cos B**’

$$(iii) \frac{PQ}{BO} = \frac{AC}{BC} = \frac{\text{Opposite side of } \angle B}{\text{Adjacent side of } \angle B}$$

This ratio is called as the tangent ratio of  $\angle B$ , and written in brief as **tan B**.

**Ex. :**



**Fig.8.11**

Sometimes we write measures of acute angles of a right angled triangle by using Greek letters  $\theta$  (Theta),  $\alpha$  (Alpha),  $\beta$  (Beta) etc.

In the adjacent figure of  $\Delta ABC$ , measure of acute angle C is denoted by the letter  $\theta$ . So we can write the ratios  $\sin C$ ,  $\cos C$ ,  $\tan C$  as  $\sin \theta$ ,  $\cos \theta$ ,  $\tan \theta$  respectively.

$$\sin C = \sin \theta = \frac{AB}{AC}, \quad \cos C = \cos \theta = \frac{BC}{AC}, \quad \tan C = \tan \theta = \frac{AB}{BC}$$



- $$\sin \text{ ratio} = \frac{\text{opposite side}}{\text{hypotenuse}}$$

- $\cos \text{ ratio} = \frac{\text{adjacent side}}{\text{hypotenuse}}$

- tan ratio =  $\frac{\text{opposite side}}{\text{adjacent side}}$

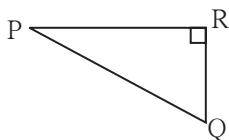
•  $\sin \theta = \frac{\text{opposite side of } \angle \theta}{\text{hypotenuse}}$

- $$\cos \theta = \frac{\text{adjacent side of } \angle \theta}{\text{hypotenuse}}$$

- $$\tan \theta = \frac{\text{opposite side of } \angle \theta}{\text{adjacent side of } \angle \theta}$$

## Practice set 8.1

**1.**

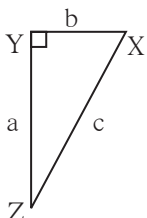


**Fig. 8.12**

In the Fig.8.12,  $\angle R$  is the right angle of  $\triangle PQR$ . Write the following ratios.

(i)  $\sin P$  (ii)  $\cos Q$  (iii)  $\tan P$  (iv)  $\tan Q$

2.

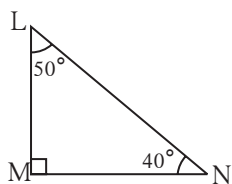


**Fig. 8.13**

In the right angled  $\Delta XYZ$ ,  $\angle XYZ = 90^\circ$  and  $a, b, c$  are the lengths of the sides as shown in the figure. Write the following ratios,

(i)  $\sin X$  (ii)  $\tan Z$  (iii)  $\cos X$  (iv)  $\tan X$ .

3.



**Fig. 8.14**

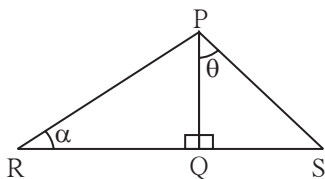
In right angled  $\Delta LMN$ ,  $\angle LMN = 90^\circ$   
 $\angle L = 50^\circ$  and  $\angle N = 40^\circ$ ,

write the following ratios.

(i)  $\sin 50^\circ$                       (ii)  $\cos 50^\circ$

(iii)  $\tan 40^\circ$                       (iv)  $\cos 40^\circ$

4.



**Fig. 8.15**

In the figure 8.15,  $\angle PQR = 90^\circ$ ,

$$\angle PQS = 90^\circ, \angle PRQ = \alpha \text{ and } \angle QPS = \theta$$

Write the following trigonometric ratios.

(i)  $\sin \alpha, \cos \alpha, \tan \alpha$

(ii)  $\sin \theta, \cos \theta, \tan \theta$



**\* For more information**

$$\frac{1}{\sin \theta} = \operatorname{cosec} \theta, \quad \frac{1}{\cos \theta} = \sec \theta, \quad \frac{1}{\tan \theta} = \cot \theta$$

It means cosec  $\theta$ , sec  $\theta$  and cot  $\theta$  are inverse ratios of sin  $\theta$ , cos  $\theta$  and tan  $\theta$  respectively.

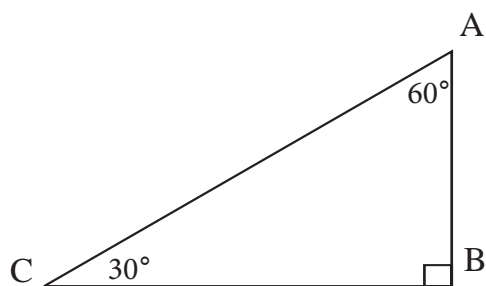
- $\sec \theta = \operatorname{cosec} (90 - \theta)$
- $\operatorname{cosec} \theta = \sec (90 - \theta)$
- $\tan \theta = \cot (90 - \theta)$
- $\cot \theta = \tan (90 - \theta)$



## Lets Recall

### Theorem of $30^\circ$ - $60^\circ$ - $90^\circ$ triangle :

We know that if the measures of angles of a triangle are  $30^\circ, 60^\circ, 90^\circ$  then side opposite to  $30^\circ$  angle is half of the hypotenuse and side opposite to  $60^\circ$  angle is  $\frac{\sqrt{3}}{2}$  of hypotenuse.



**Fig. 8.17**

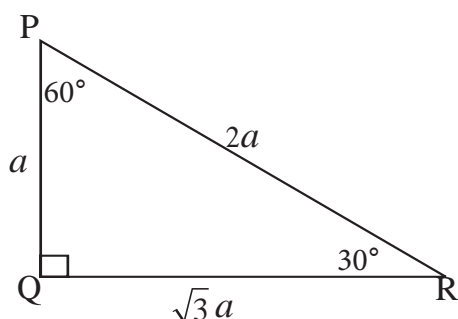
In the Fig. 8.17,  $\triangle ABC$  is a right angled triangle.  $\angle C = 30^\circ$ ,  $\angle A = 60^\circ$ ,  $\angle B = 90^\circ$ .

$$\therefore AB = \frac{1}{2}AC \text{ and } BC = \frac{\sqrt{3}}{2}AC$$



## Let's learn.

### Trigonometric ratios of $30^\circ$ and $60^\circ$ angles



**Fig. 8.18**

In right angled  $\triangle PQR$  if  $\angle R = 30^\circ$ ,  
 $\angle P = 60^\circ$ ,  $\angle Q = 90^\circ$  and  $PQ = a$

then  $PQ = \frac{1}{2} PR$

$$a = \frac{1}{2} \text{ PR}$$

$$\therefore \text{PR} = 2a$$

$$QR = \frac{\sqrt{3}}{2} PR$$

$$QR = \frac{\sqrt{3}}{2} \times 2a$$

$$QR = \sqrt{3} a$$

$\therefore$  If  $PQ = a$ , then  $PR = 2a$  and  $QR = \sqrt{3}a$

(I) Trigonometric ratios of the  $30^\circ$  angle

$$\sin 30^\circ = \frac{PQ}{PR} = \frac{a}{2a} = \frac{1}{2}$$

$$\cos 30^\circ = \frac{QR}{PR} = \frac{\sqrt{3}a}{2a} = \frac{\sqrt{3}}{2}$$

$$\tan 30^\circ = \frac{PQ}{QR} = \frac{a}{\sqrt{3}a} = \frac{1}{\sqrt{3}}$$

(II) Trigonometric ratios of  $60^\circ$  angle

$$\sin 60^\circ = \frac{QR}{PR} = \frac{\sqrt{3}a}{2a} = \frac{\sqrt{3}}{2}$$

$$\cos 60^\circ = \frac{PQ}{PR} = \frac{a}{2a} = \frac{1}{2}$$

$$\tan 60^\circ = \frac{QR}{PQ} = \frac{\sqrt{3}a}{a} = \sqrt{3}$$

In right angled  $\Delta PQR$ ,  $\angle Q = 90^\circ$ . Therefore  $\angle P$  and  $\angle R$  are complimentary angles of each other. Verify the relation between sine and cosine ratios of complimentary angles here also.

$$\sin \theta = \cos (90 - \theta)$$

$$\sin 30^\circ = \cos (90^\circ - 30^\circ) = \cos 60^\circ$$

$$\sin 30^\circ = \cos 60^\circ$$

$$\cos \theta = \sin (90 - \theta)$$

$$\cos 30^\circ = \sin (90^\circ - 30^\circ) = \sin 60^\circ$$

$$\cos 30^\circ = \sin 60^\circ$$



**Remember this !**

$\sin 30^\circ = \frac{1}{2}$	$\cos 30^\circ = \frac{\sqrt{3}}{2}$	$\tan 30^\circ = \frac{1}{\sqrt{3}}$
$\sin 60^\circ = \frac{\sqrt{3}}{2}$	$\cos 60^\circ = \frac{1}{2}$	$\tan 60^\circ = \sqrt{3}$

(III) Trigonometric ratios of the  $45^\circ$  angle

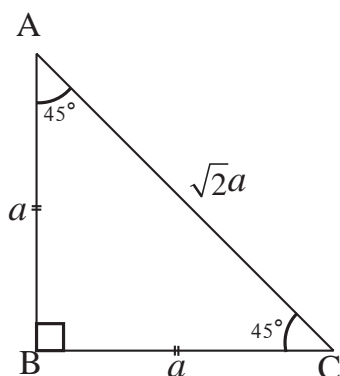


Fig.8.19

In right angled  $\Delta ABC$ ,  $\angle B = 90^\circ$ ,  $\angle A = 45^\circ$ ,  $\angle C = 45^\circ \therefore$  This is an isosceles triangle.

Suppose  $AB = a$  then  $BC = a$ .

Using Pythagoras' theorem, let us find the length of  $AC$ .

$$AC^2 = AB^2 + BC^2$$

$$= a^2 + a^2$$

$$AC^2 = 2a^2$$

$$\therefore AC = \sqrt{2}a$$



In the Fig. 8.19,  $\angle C = 45^\circ$

$$\sin 45^\circ = \frac{AB}{AC} = \frac{a}{\sqrt{2}a} = \frac{1}{\sqrt{2}}$$

$$\cos 45^\circ = \frac{BC}{AC} = \frac{a}{\sqrt{2}a} = \frac{1}{\sqrt{2}}$$

$$\tan 45^\circ = \frac{AB}{BC} = \frac{a}{a} = 1$$



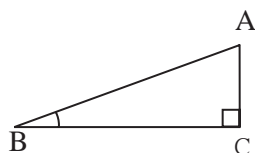
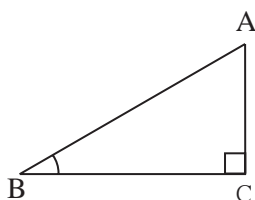
**Remember this !**

$$\sin 45^\circ = \frac{1}{\sqrt{2}},$$

$$\cos 45^\circ = \frac{1}{\sqrt{2}},$$

$$\tan 45^\circ = 1$$

(IV) Trigonometric ratios of the angle  $0^\circ$  and  $90^\circ$

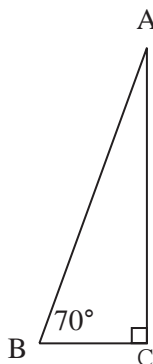
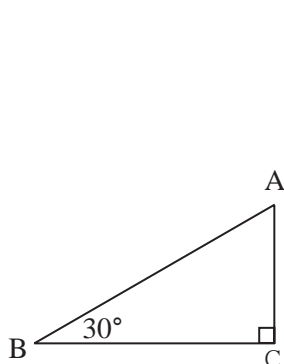


**Fig.8.20**

In the right angled  $\Delta ACB$ ,  $\angle C = 90^\circ$  and  $\angle B = 30^\circ$ . We know that  $\sin 30^\circ = \frac{AC}{AB}$ . Keeping the length of side AB constant, if the measure of  $\angle B$  goes on decreasing the length of AC, which is opposite to  $\angle B$  also goes on decreasing. So as the measure of  $\angle B$  decreases, then value of  $\sin \theta$  also decreases.

$\therefore$  when measure of  $\angle B$  becomes  $0^\circ$ , then length of AC becomes 0.

$$\therefore \sin 0^\circ = \frac{AC}{AB} = \frac{0}{AB} = 0 \quad \therefore \sin 0^\circ = 0$$



**Fig.8.21**

Now look at the Fig. 8.21. In this right angled triangle, as the measure of  $\angle B$  increases the length of AC also increases. When measure of  $\angle B$  becomes  $90^\circ$ , the length of AC become equal to AB

$$\therefore \sin 90^\circ = \frac{AC}{AB} \quad \therefore \sin 90^\circ = 1$$

We know the relations between trigonometric ratios of complimentary angles.

$$\sin \theta = \cos (90 - \theta) \quad \text{and} \quad \cos \theta = \sin (90 - \theta)$$

$$\therefore \cos 0^\circ = \sin (90 - 0)^\circ = \sin 90^\circ = 1$$

$$\text{and } \cos 90^\circ = \sin (90 - 90)^\circ = \sin 0^\circ = 0$$



**Remember this !**

$$\sin 0^\circ = 0,$$

$$\sin 90^\circ = 1,$$

$$\cos 0^\circ = 1,$$

$$\cos 90^\circ = 0$$

We know that,

$$\tan \theta = \frac{\sin \theta}{\cos \theta} \quad \therefore \tan 0 = \frac{\sin 0}{\cos 0} = \frac{0}{1} = 0$$

$$\text{But } \tan 90^\circ = \frac{\sin 90^\circ}{\cos 90^\circ} = \frac{1}{0}$$

But we can not do the division of 1 by 0. Note that  $\theta$  is an acute angle. As it increases and reaches the value of  $90^\circ$ ,  $\tan \theta$  also increases indefinitely. Hence we can not find the definite value of  $\tan 90$ .



**Remember this !**

Trigonometric ratios of particular ratios.

Measures of angles Ratios	$0^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$
sin	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
cos	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
tan	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	Undefined

### Solved Examples :

**Ex. (1)** Find the value of  $2\tan 45^\circ + \cos 30^\circ - \sin 60^\circ$

**Solution :**  $2\tan 45^\circ + \cos 30^\circ - \sin 60^\circ$

$$\begin{aligned} &= 2 \times 1 + \frac{\sqrt{3}}{2} - \frac{\sqrt{3}}{2} \\ &= 2 + 0 \\ &= 2 \end{aligned}$$

**Ex. (2)** Find the value of  $\frac{\cos 56^\circ}{\sin 34^\circ}$

**Solution :**  $56^\circ + 34^\circ = 90^\circ$  means 56 and 34 are the measures of complimentary angles.

$$\sin \theta = \cos (90 - \theta)$$

$$\therefore \sin 34^\circ = \cos (90 - 34)^\circ = \cos 56^\circ$$

$$\therefore \frac{\cos 56^\circ}{\sin 34^\circ} = \frac{\cos 56^\circ}{\cos 56^\circ} = 1$$

**Ex. 3** In right angled  $\triangle ACB$ , If  $\angle C = 90^\circ$ ,  $AC = 3$ ,  $BC = 4$ .

Find the ratios  $\sin A$ ,  $\sin B$ ,  $\cos A$ ,  $\tan B$

**Solution :** In right angled  $\triangle ACB$ , using Pythagoras' theorem,

$$\begin{aligned} AB^2 &= AC^2 + BC^2 \\ &= 3^2 + 4^2 = 5^2 \end{aligned}$$

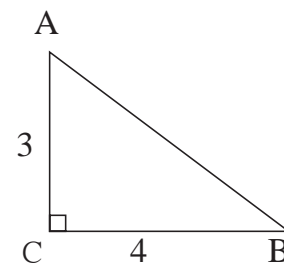
$$\therefore AB = 5$$

$$\sin A = \frac{BC}{AB} = \frac{4}{5}$$

$$\cos A = \frac{AC}{AB} = \frac{3}{5}$$

$$\text{and } \sin B = \frac{AC}{AB} = \frac{3}{5}$$

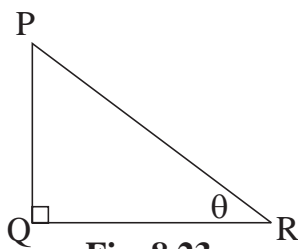
$$\tan B = \frac{AC}{BC} = \frac{3}{4}$$



**Fig. 8.22**

**Ex. 4** In right angled triangle  $\triangle PQR$ ,  $\angle Q = 90^\circ$ ,  $\angle R = \theta$  and if  $\sin \theta = \frac{5}{13}$  then find  $\cos \theta$  and  $\tan \theta$ .

**Solution :**



**Fig. 8.23**

In right angled  $\triangle PQR$ ,  $\angle R = \theta$

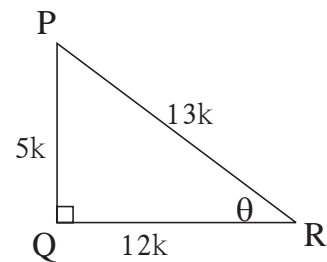
$$\sin \theta = \frac{5}{13}$$

$$\therefore \frac{PQ}{PR} = \frac{5}{13}$$

∴ Let  $PQ = 5k$  and  $PR = 13k$

Let us find  $QR$  by using Pythagoras' theorem,

$$\begin{aligned} PQ^2 + QR^2 &= PR^2 \\ (5k)^2 + QR^2 &= (13k)^2 \\ 25k^2 + QR^2 &= 169k^2 \\ QR^2 &= 169k^2 - 25k^2 \\ QR^2 &= 144k^2 \\ QR &= 12k \end{aligned}$$



**Fig. 8.24**

Now, in right angled  $\Delta PQR$ ,  $PQ = 5k$ ,  $PR = 13k$  and  $QR = 12k$

$$\therefore \cos \theta = \frac{QR}{PR} = \frac{12k}{13k} = \frac{12}{13}, \tan \theta = \frac{PQ}{QR} = \frac{5k}{12k} = \frac{5}{12}$$



**Use your brain power!**

- (1) While solving above example, why the lengths of  $PQ$  and  $PR$  are taken  $5k$  and  $13k$  ?
- (2) Can we take the lengths of  $PQ$  and  $PR$  as  $5$  and  $13$  ? If so then what changes are needed in the writing of the solution.

### Important Equation in Trigonometry

$\Delta PQR$  is a right angled triangle.

$$\angle PQR = 90^\circ, \angle R = \theta$$

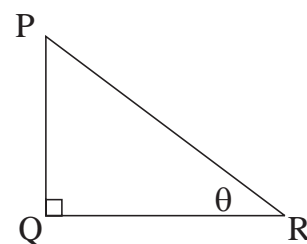
$$\sin \theta = \frac{PQ}{PR} \dots\dots\dots(\text{I})$$

$$\text{and } \cos \theta = \frac{QR}{PR} \dots\dots\dots(\text{II})$$

Using Pythagoras' theorem,

$$PQ^2 + QR^2 = PR^2$$

$$\therefore \frac{PQ^2}{PR^2} + \frac{QR^2}{PR^2} = \frac{PR^2}{PR^2} \dots \text{dividing each term by } PR^2$$



**Fig.8.25**

$$\therefore \left( \frac{PQ}{PR} \right)^2 + \left( \frac{QR}{PR} \right)^2 = 1$$

$$\therefore (\sin \theta)^2 + (\cos \theta)^2 = 1 \text{ ..from (I) \& (II)}$$

**Remember this !**

‘Square of’  $\sin \theta$  means  $(\sin \theta)^2$ . It is written as  $\sin^2 \theta$ .

We have proved the equation  $\sin^2 \theta + \cos^2 \theta = 1$  using Pythagoras’ theorem, where  $\theta$  is an acute angle of a right angled triangle.

Verify that the equation is true even when  $\theta = 0^\circ$  or  $\theta = 90^\circ$

Since the equation  $\sin^2 \theta + \cos^2 \theta = 1$  is true for any value of  $\theta$ . So it is a basic trigonometrical identity.

$$(i) 0 \leq \sin \theta \leq 1, \quad 0 \leq \sin^2 \theta \leq 1 \qquad (ii) 0 \leq \cos \theta \leq 1, \quad 0 \leq \cos^2 \theta \leq 1$$

**Practice set 8.2**

1. In the following table, a ratio is given in each column. Find the remaining two ratios in the column and complete the table.

$\sin \theta$		$\frac{11}{61}$		$\frac{1}{2}$				$\frac{3}{5}$	
$\cos \theta$	$\frac{35}{37}$				$\frac{1}{\sqrt{3}}$				
$\tan \theta$			1			$\frac{21}{20}$	$\frac{8}{15}$		$\frac{1}{2\sqrt{2}}$

2. Find the values of -

(i)  $5 \sin 30^\circ + 3 \tan 45^\circ$

(ii)  $\frac{4}{5} \tan^2 60^\circ + 3 \sin^2 60^\circ$

(iii)  $2 \sin 30^\circ + \cos 0^\circ + 3 \sin 90^\circ$

(iv)  $\frac{\tan 60}{\sin 60 + \cos 60}$

(v)  $\cos^2 45^\circ + \sin^2 30^\circ$

(vi)  $\cos 60^\circ \times \cos 30^\circ + \sin 60^\circ \times \sin 30^\circ$

3. If  $\sin \theta = \frac{4}{5}$  then find  $\cos \theta$

4. If  $\cos \theta = \frac{15}{17}$  then find  $\sin \theta$



## Problem Set 8

1. Choose the correct alternative answer for following multiple choice questions.

(i) Which of the following statements is true ?

- (A)  $\sin \theta = \cos (90 - \theta)$                       (B)  $\cos \theta = \tan (90 - \theta)$   
 (C)  $\sin \theta = \tan (90 - \theta)$                       (D)  $\tan \theta = \tan (90 - \theta)$

(ii) Which of the following is the value of  $\sin 90^\circ$  ?

- (A)  $\frac{\sqrt{3}}{2}$                       (B) 0                      (C)  $\frac{1}{2}$                       (D) 1

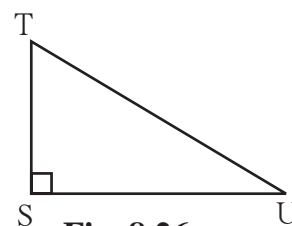
(iii)  $2 \tan 45^\circ + \cos 45^\circ - \sin 45^\circ = ?$

- (A) 0                      (B) 1                      (C) 2                      (D) 3

(iv)  $\frac{\cos 28^\circ}{\sin 62^\circ} = ?$

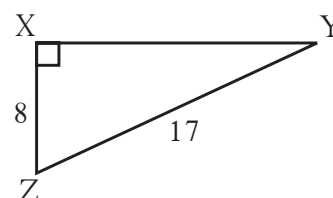
- (A) 2                      (B) -1                      (C) 0                      (D) 1

2. In right angled  $\Delta TSU$ ,  $TS = 5$ ,  $\angle S = 90^\circ$ ,  $SU = 12$  then find  $\sin T$ ,  $\cos T$ ,  $\tan T$ . Similarly find  $\sin U$ ,  $\cos U$ ,  $\tan U$ .



**Fig. 8.26**

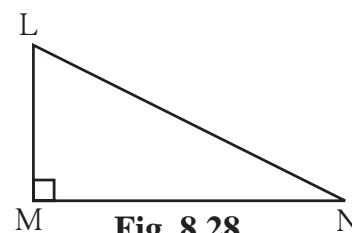
3. In right angled  $\Delta YXZ$ ,  $\angle X = 90^\circ$ ,  $XZ = 8$  cm,  $YZ = 17$  cm, find  $\sin Y$ ,  $\cos Y$ ,  $\tan Y$ ,  $\sin Z$ ,  $\cos Z$ ,  $\tan Z$ .



**Fig. 8.27**

4. In right angled  $\Delta LMN$ , if  $\angle N = \theta$ ,  $\angle M = 90^\circ$ ,  $\cos \theta = \frac{24}{25}$ , find  $\sin \theta$  and  $\tan \theta$

Similarly, find  $(\sin^2 \theta)$  and  $(\cos^2 \theta)$ .



**Fig. 8.28**

5. Fill in the blanks.

(i)  $\sin 20^\circ = \cos \boxed{\phantom{00}}^\circ$

(ii)  $\tan 30^\circ \times \tan \boxed{\phantom{00}}^\circ = 1$

(iii)  $\cos 40^\circ = \sin \boxed{\phantom{00}}^\circ$



## 7. Co - ordinate Geometry

## Practice set 7.1

1. point A : Quadrant II, point B : Quadrant III, point K : Quadrant I, point D : Quadrant I  
point E : Quadrant I, point F : Quadrant IV, point G : Quadrant IV, point H : Y-Axis.  
point M : X-Axis, point N : Y-Axis, point P : Y-Axis, point Q : Quadrant III
2. (i) Quadrant I      (ii) Quadrant III      (iii) Quadrant IV      (iv) Quadrant II

## Practice set 7.2

1. Square                      2.  $x = -7$                       3.  $y = -5$                       4.  $x = -3$                       5. 4  
6. (i) Y-Axis,                      (ii) X-axis,                      (iii) Y-axis,                      (iv) X-axis,  
7. To X-axis (5,0) , To Y-axis (0,5)  
8. (-4,1), (-1.5, 1), (-1.5,5), (-4,5)

## Problem set 7

1. (i) C (ii) A (iii) B (iv) C (v) C (vi) B  
 2. (i) Q (2,2), R(4,-1) (ii) T(0,-1), M(3,0) (iii) point S (iv) point O  
 3. (i) Quadrant IV (ii) Quadrant III  
 (iii) Quadrant II (iv) Quadrant II (v) Y-axis (vi) X-axis  
 5. (i) 3 (ii) P(3,2), Q(3,-1), R (3,0) (iii) 0 6. .  $y = 5$ ,  $y = -5$  7.  $|a|$

## 8. Trigonometry

## Practice set 8.1

1. (i)  $\frac{\underline{QR}}{\underline{PQ}}$  (ii)  $\frac{\underline{QR}}{\underline{PQ}}$  (iii)  $\frac{\underline{QR}}{\underline{PR}}$  (iv)  $\frac{\underline{PR}}{\underline{QR}}$
2. (i)  $\frac{a}{c}$  (ii)  $\frac{b}{a}$  (iii)  $\frac{b}{c}$  (iv)  $\frac{a}{b}$
3. (i)  $\frac{MN}{LN}$  (ii)  $\frac{LM}{LN}$  (iii)  $\frac{LM}{MN}$  (iv)  $\frac{MN}{LN}$
4. (i)  $\frac{PQ}{PR}, \frac{RQ}{PR}, \frac{PQ}{RQ}$  (ii)  $\frac{QS}{PS}, \frac{PQ}{PS}, \frac{QS}{PQ}$

## Practice set 8.2

1.  $\sin \theta : \frac{12}{37}, \frac{1}{\sqrt{2}}, \frac{\sqrt{2}}{\sqrt{3}}, \frac{21}{29}, \frac{8}{17}, \frac{1}{3} ; \cos \theta : \frac{60}{61}, \frac{1}{\sqrt{2}}, \frac{\sqrt{3}}{2}, \frac{20}{29}, \frac{15}{17}, \frac{4}{5}, \frac{2\sqrt{2}}{3}$   
 $\tan \theta : \frac{12}{35}, \frac{11}{60}, \frac{1}{\sqrt{3}}, \sqrt{2}, \frac{3}{4}$

2. (i)  $\frac{11}{2}$  (ii)  $\frac{93}{20}$  (iii) 5 (iv)  $\frac{2\sqrt{3}}{\sqrt{3}+1}$  (v)  $\frac{3}{4}$  (vi)  $\frac{\sqrt{3}}{2}$  3.  $\frac{3}{5}$  4.  $\frac{8}{17}$

### Problem set 8

1. (i) A (ii) D (iii) C (iv) D  
 2.  $\sin T = \frac{12}{13}$ ,  $\cos T = \frac{5}{13}$ ,  $\tan T = \frac{12}{5}$ ,  $\sin U = \frac{5}{13}$ ,  $\cos U = \frac{12}{13}$ ,  $\tan U = \frac{5}{12}$   
 3.  $\sin Y = \frac{8}{17}$ ,  $\cos Y = \frac{15}{17}$ ,  $\tan Y = \frac{8}{15}$ ,  $\sin Z = \frac{15}{17}$ ,  $\cos Z = \frac{8}{17}$ ,  $\tan Z = \frac{15}{8}$   
 4.  $\sin \theta = \frac{7}{25}$ ,  $\tan \theta = \frac{7}{24}$ ,  $\sin^2 \theta = \frac{49}{625}$ ,  $\cos^2 \theta = \frac{576}{625}$   
 5. (i) 70 (ii) 60 (iii) 50

## 9. Surface Area and Volume

### Practice set 9.1

1. 640 sq.cm, 1120 sq.cm. 2. 20 Unit 3. 81 sq.cm, 121.50 sq.cm.  
 4. 3600 sq.cm. 5. 20 m 6. 421.88 cubic cm  
 7. 1632.80 sq.cm, 4144.80 sq.cm. 8. 21 cm

### Practice set 9.2

1. 5 cm 2. 36960 cubic cm. 3. 10 cm, 6 cm 4. ₹ 2640  
 5. 15 cm 6. 8 cm 7. 550 sq.cm 8. 2816 sq.cm, 9856 cubic cm  
 9. 600 cubic metre 10. 28.51 cubic metre, 47.18 sq.m.

### Practice Set 9.3

1. (i) 200.96 sq.cm, 267.95 cubic cm. (ii) 1017.36 sq.cm, 3052.08 cubic cm.  
 (iii) 153.86 sq.m, 179.50 cubic cm.  
 2. 157 sq.cm, 235.5 sq.cm. 3. 14130 cubic cm. 4. 5544 sq.cm. 5. 60 cm

### Problem set 9

1. 1980 sq.m. 2. 96801.6 cubic cm. 3. 12 m, 13 m  
 4. 6 cm 5. 1728 cubic cm. 6. 179.67 cubic cm.  
 7. 21 cm 8. 132 sq.m., ₹ 6864 9. 4620 sq.m, ₹ 32340

