

# Two-Qubit Dynamics with Josephson Qubits

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# History

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Topic of this slide

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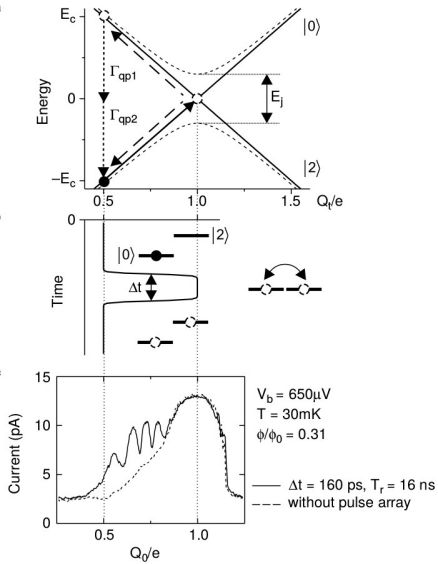


Figure : A simple caption

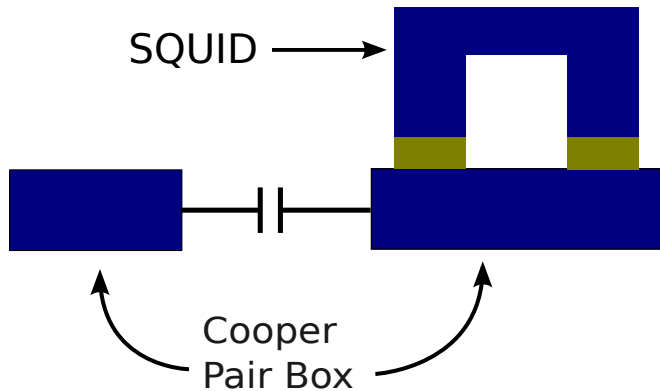
## Coupling of Two Qubits

# Coupling of Two Qubits

## Review

# Coupling of Two Qubits

## Basic Idea





# Coupling of Two Qubits

## The Circuit

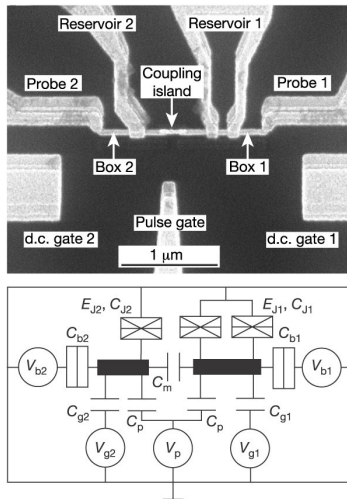


Figure : <http://www.nature.com/nature/journal/v421/n6925/full/nature01365.html>

# Coupling of Two Qubits

## Theory

Hamiltonian

# Coupling of Two Qubits

## Parameter Measurements

# Coupling of Two Qubits

## Charging Diagram of Single-Qubit Case

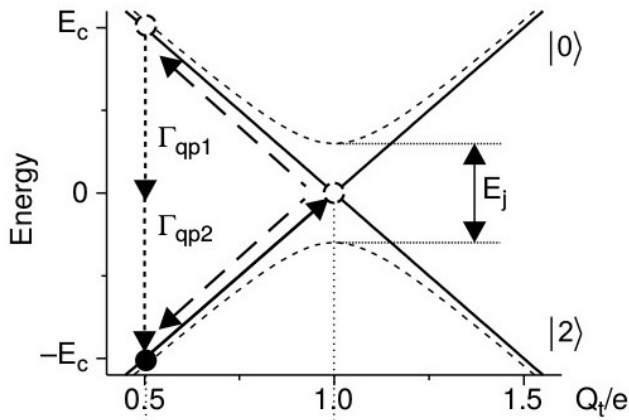


Figure : <http://www.nature.com/nature/journal/v398/n6730/abs/398786a0.html>

# Coupling of Two Qubits

## Charging Diagram Level Curves

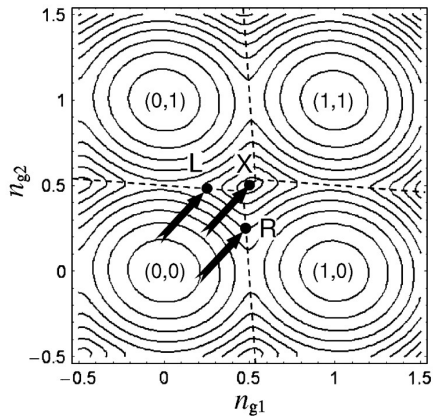


Figure : <http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.193.5098&rep=rep1&type=pdf>

# Coupling of Two Qubits

## Charging Diagram of Two-Qubit Case

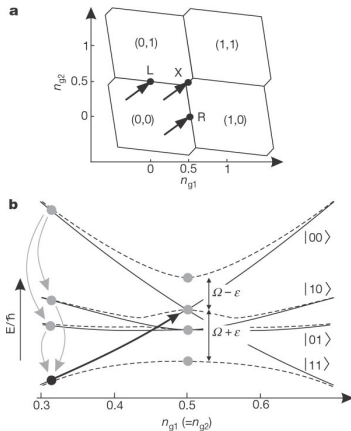


Figure : <http://www.nature.com/nature/journal/v421/n6925/full/nature01365.html>

# Coupling of Two Qubits

## Charging-Energy Diagram

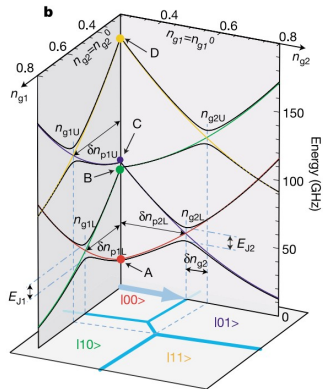
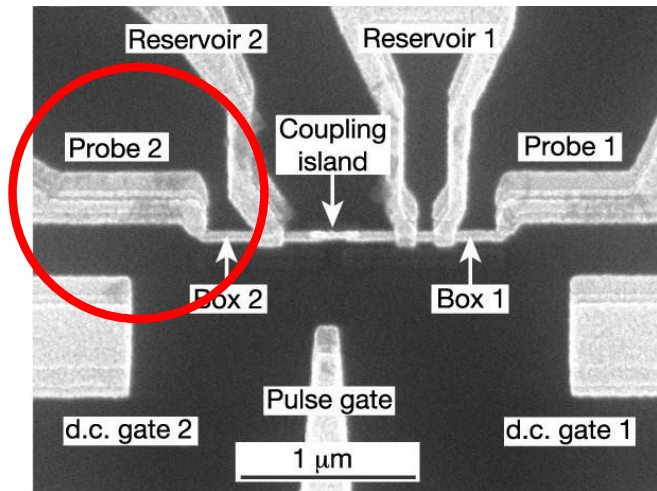


Figure : <http://qudev.ethz.ch/content/courses/QSIT09/pdfs/Yamamoto2003.pdf>

# Coupling of Two Qubits

## State Readout





# Coupling of Two Qubits

## Theory

### Hamiltonian

$$H = \begin{bmatrix} E_{00} & -\frac{1}{2}E_{J1} & -\frac{1}{2}E_{J2} & 0 \\ -\frac{1}{2}E_{J1} & E_{10} & 0 & -\frac{1}{2}E_{J2} \\ -\frac{1}{2}E_{J2} & 0 & E_{01} & -\frac{1}{2}E_{J1} \\ 0 & -\frac{1}{2}E_{J2} & -\frac{1}{2}E_{J1} & E_{11} \end{bmatrix}$$

Where...

- ▶  $E_{n1n2} = E_{c1}(n_{g1} - n_1)^2 + E_{c2}(n_{g2} - n_2)^2 + E_m(n_{g1} - n_1)(n_{g2} - n_2)$
- ▶  $E_{Ji}$  is the Josephson energy of the  $i^{th}$  box
- ▶  $E_{c1,c2} = 4e^2 C_{\Sigma 2, \Sigma 1} / 2(C_{\Sigma 1} C_{\Sigma 2} - C_m^2)$  are the effective Cooper pair charging energies
- ▶  $C_{\Sigma i}$  is the sum of all capacitances connected to the  $i^{th}$  island
- ▶  $n_{g1,g2} = (C_{g1,g2} V_{g1,g2} + C_p V_p) / 2e$  is the charge, indexed by the gate and pulse voltages, on the qubits
- ▶  $E_m = 4e^2 C_m / (C_{\Sigma 1} C_{\Sigma 2} - C_m^2)$

# Coupling of Two Qubits

## Frequency Responses

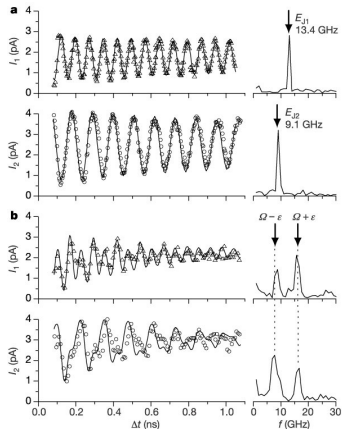


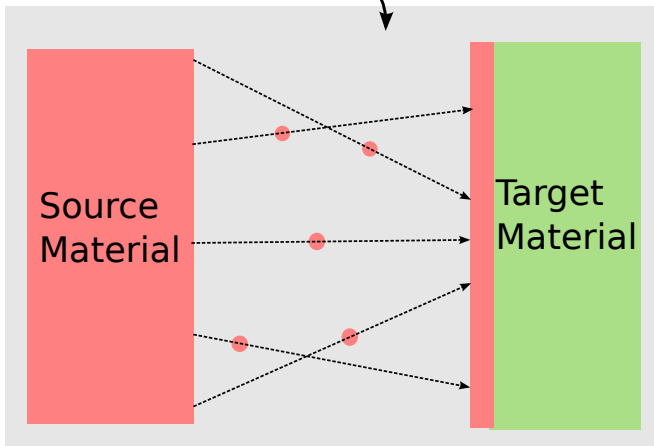
Figure : <http://www.nature.com/nature/journal/v421/n6925/full/nature01365.html>

# Fabrication Techniques

# Fabrication Techniques

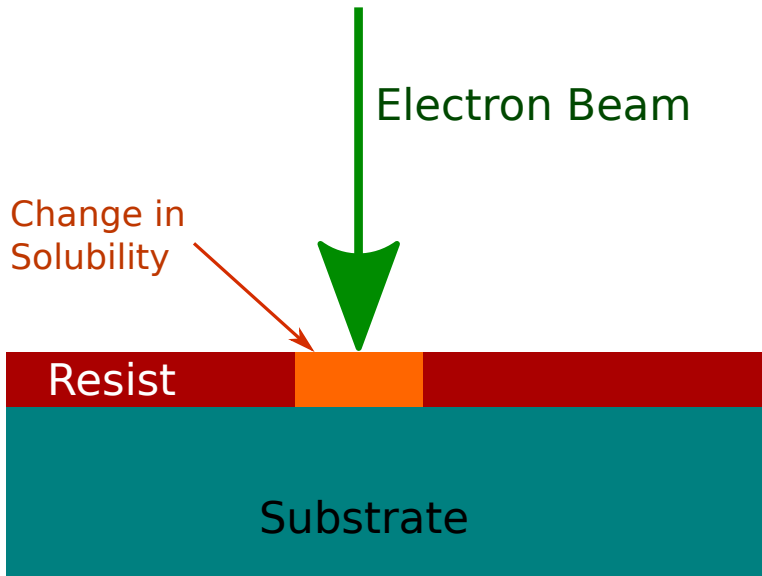
## Evaporation (Deposition)

Vacuum and Heat



# Fabrication Techniques

## Electron Beam Lithography (EBL)



# Fabrication Techniques

## Etching

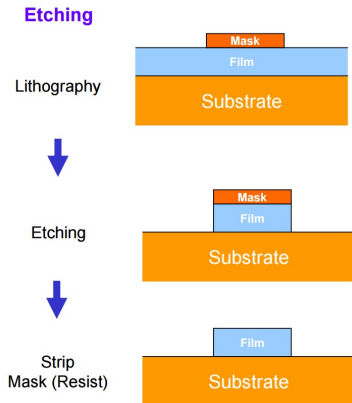


Figure : <http://www.mrsec.harvard.edu/education/ap298r2004/Erli%20chen%20Fabrication%20III%20-%20Etching.pdf>

# Fabrication Techniques

## Lift-off

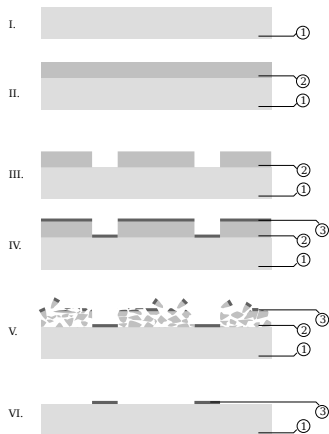


Figure : [http://en.wikipedia.org/wiki/Lift-off\\_%28microtechnology%29](http://en.wikipedia.org/wiki/Lift-off_%28microtechnology%29)

# Fabrication Techniques

SEM image of a SQUID qubit

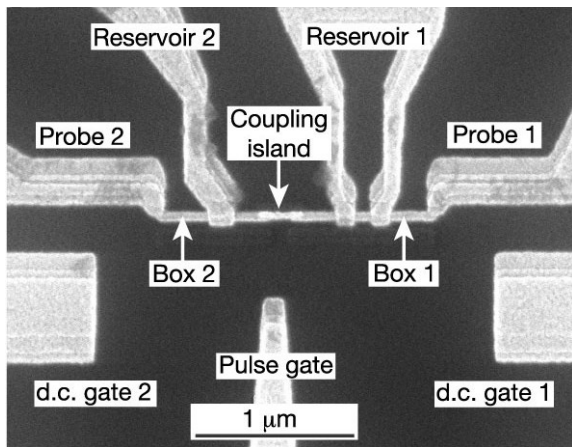


Figure : <http://www.nature.com/nature/journal/v421/n6925/full/nature01365.html>



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## Reference Papers

<http://www.nature.com/nature/journal/v421/n6925/full/nature01365.html>

<http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.193.5098&rep=rep1&type=pdf>

(Figures cited individually)