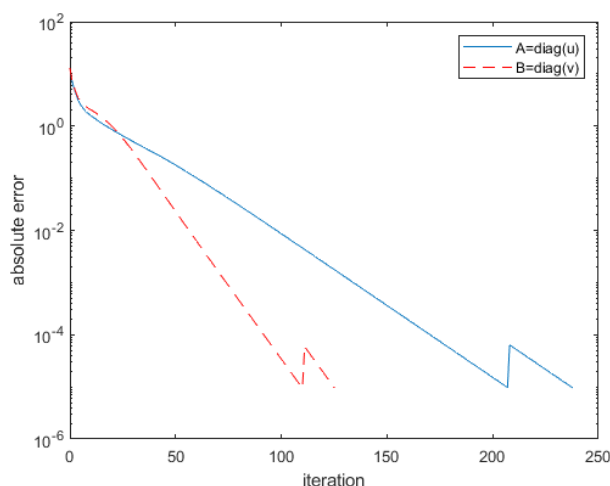Nicholas Garrett

Professor Zhu

MATH 4441

12/1/2021

Homework 10

1. ...

2. Shown below is the returned graph of the absolute errors given when the code is run. As we can

see from the figure, and as was shown repeatedly through testing muliple times, the iterative sequence
is very fast for the first handful of iterations, quickly converging by several orders very quickly. How-
ever, it then hits a bit of a plateau and slows down significantly. Due to this being a power iterative
sequence only and without shifting, if we were to add a shifting parameter, it could be assumed this
deceleration of eigenvalue norm convergence would be less significant.

3. Below is shown the graphical outputs for eigenvalue norms. As the figures show, when $\sigma = 35$, both
matrices converge on their eigenvalues less quickly. So, by this observation, we can be confidently in
saying that λ is closer to 33 than it is to 35. This is because by the closer a shifting parameter is to
the eigenvalue, the faster it converges.
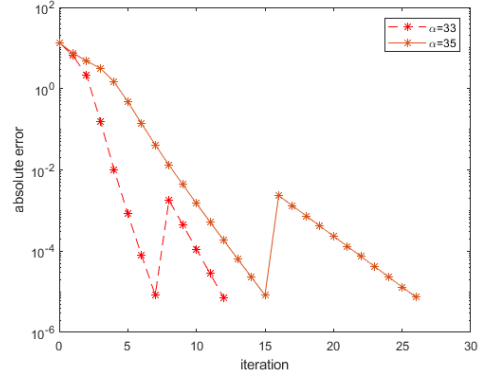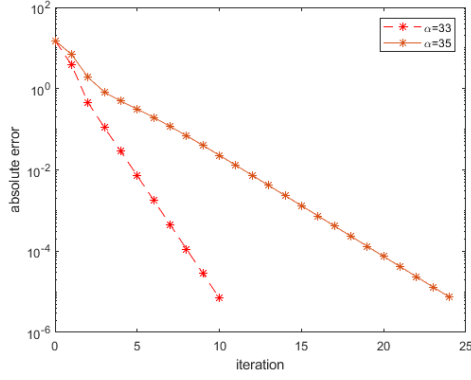
4. The matrix A_1 is defined to be the QR factorization of the initial matrix A. Then, as the iteration sequence defines, each iteration of A_k is the QR factorization of the previous iteration (A_{k-1})

Then, since each iteration is orthogonally similar to the iteration prior to it, as defined by $A_k = R_{k-1}Q_{k-1} = Q_{k-1}^T A_{k-1} Q_{k-1}$, we can know that each iteration must be orthogonally similar to the one imimidiately prior to it, and by the iteration, it is orthogonally similar to each matrix before it–including the original matrix. Therefore, for two matricies in adjacent iterations A_k and A_{k+1} are orthogonally similar.