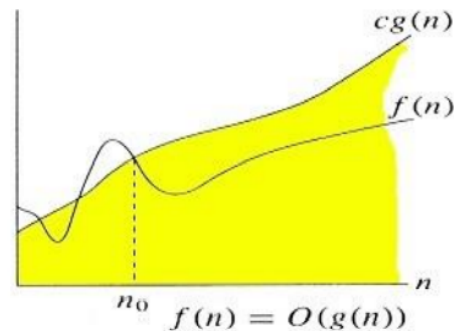


## Asymptotic Notations:

It is often used to describe how the size of the input data affects an algorithm's usage of computational resources. Running time of an algorithm is described as a function of input size  $n$  for large  $n$ .

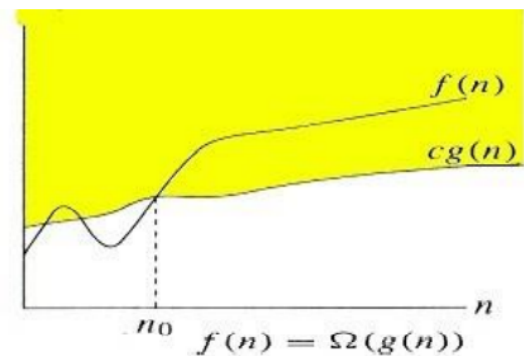
**Big oh(O):** Definition:  $f(n) = O(g(n))$  (read as  $f$  of  $n$  is big oh of  $g$  of  $n$ ) if there exist a positive integer  $n_0$  and a positive number  $c$  such that  $|f(n)| \leq c|g(n)|$  for all  $n \geq n_0$ . Here  $g(n)$  is the upper bound of the function  $f(n)$ .

$f(n)$	$g(n)$	
$16n^3 + 45n^2 + 12n$	$n^3$	$f(n) = O(n^3)$
$34n - 40$	$n$	$f(n) = O(n)$
$50$	$1$	$f(n) = O(1)$



**Omega( $\Omega$ ):** Definition:  $f(n) = \Omega(g(n))$  (read as  $f$  of  $n$  is omega of  $g$  of  $n$ ), if there exists a positive integer  $n_0$  and a positive number  $c$  such that  $|f(n)| \geq c|g(n)|$  for all  $n \geq n_0$ . Here  $g(n)$  is the lower bound of the function  $f(n)$ .

$f(n)$	$g(n)$	
$16n^3 + 8n^2 + 2$	$n^3$	$f(n) = \Omega(n^3)$
$24n + 9$	$n$	$f(n) = \Omega(n)$



**Theta( $\Theta$ ):** Definition:  $f(n) = \Theta(g(n))$  (read as  $f$  of  $n$  is theta of  $g$  of  $n$ ), if there exists a positive integer  $n_0$  and two positive constants  $c_1$  and  $c_2$  such that  $c_1|g(n)| \leq |f(n)| \leq c_2|g(n)|$  for all  $n \geq n_0$ . The function  $g(n)$  is both an upper bound and a lower bound for the function  $f(n)$  for all values of  $n$ ,  $n \geq n_0$ .

$f(n)$	$g(n)$	
$16n^3 + 30n^2 - 90$	$n^2$	$f(n) = \Theta(n^2)$
$7 \cdot 2^n + 30n$	$2^n$	$f(n) = \Theta(2^n)$

