



Fenwick Tree + Sparse Table

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Fenwick Tree / BIT

$$\text{bit}[i] = \text{sum}(a[f(i)+1; i])$$

$f(i)$ = i with last set bit cleared

$$f(5) = f(101) = 100 = 4$$

$$\text{bit}[5] = \text{sum}(a[5; 5]) = a[5]$$

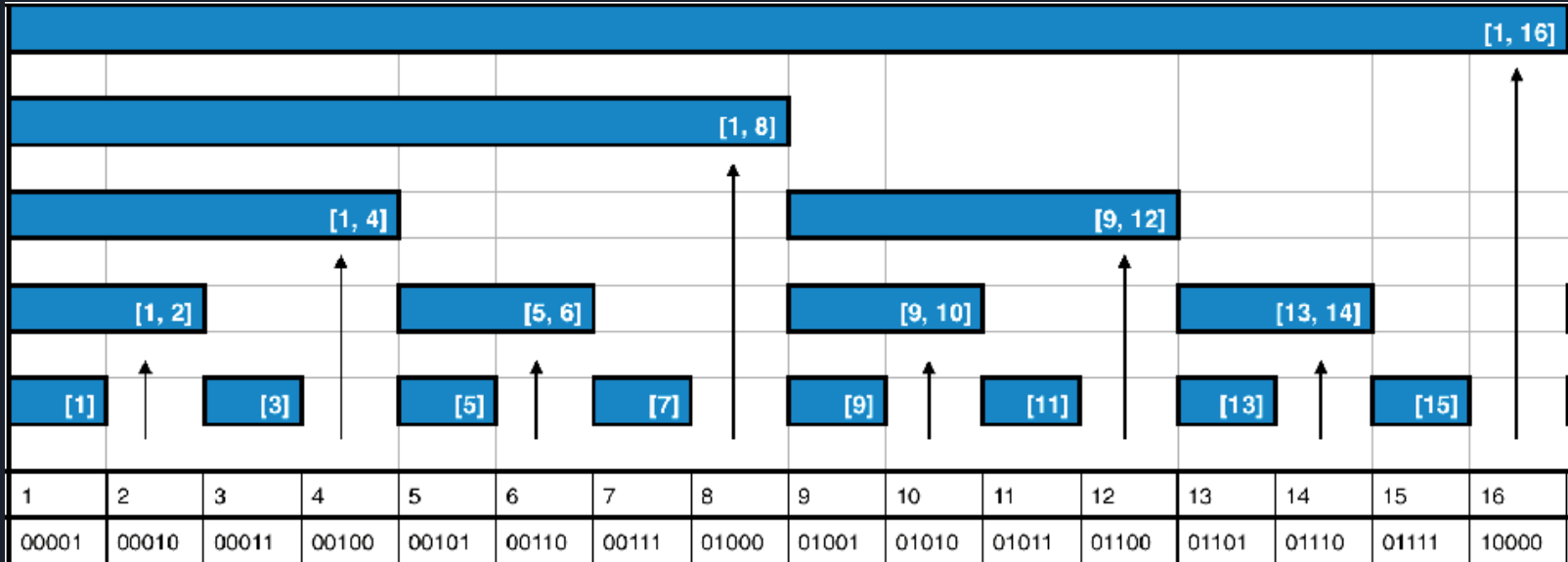
$$\text{bit}[8] = \text{sum}(a[1; 8]) = a[1] + a[2] + \dots + a[8]$$

$$f(i) = i - (i \& -i)$$

Fenwick Tree / BIT

Query : $O(\log n)$

Upd: $O(\log n)$



Sparse Table

$$st[i][j] = \min(a[i; i+2^j])$$

$$st[i][0] = a[i]$$

$$st[i][j] = \min(st[i][j-1], st[i+2^{j-1}][j-1])$$

$$Query = O(1) \quad \checkmark$$

$$\text{Idempotent func: } f(a, a) = a$$

Sparse Table



3	1	5	3	4	7	6	1
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3	1	5	3	4	7	6	1
1	1	3	3	4	6	1	
1	1	3	3	1			
1							